

# RNA structure characterization from chemical mapping experiments

Sharon Aviran, Julius B. Lucks, and Lior Pachter

**Abstract**—Despite great interest in solving RNA secondary structures due to their impact on function, it remains an open problem to determine structure from sequence. Among experimental approaches, a promising candidate is the “chemical modification strategy”, which involves application of chemicals to RNA that are sensitive to structure and that result in modifications that can be assayed via sequencing technologies. One approach that can reveal paired nucleotides via chemical modification followed by sequencing is SHAPE, and it has been used in conjunction with capillary electrophoresis (SHAPE-CE) and high-throughput sequencing (SHAPE-Seq). The solution of mathematical inverse problems is needed to relate the sequence data to the modified sites, and a number of approaches have been previously suggested for SHAPE-CE, and separately for SHAPE-Seq analysis.

Here we introduce a new model for inference of chemical modification experiments, whose formulation results in closed-form maximum likelihood estimates that can be easily applied to data. The model can be specialized to both SHAPE-CE and SHAPE-Seq, and therefore allows for a direct comparison of the two technologies. We then show that the extra information obtained with SHAPE-Seq but not with SHAPE-CE is valuable with respect to ML estimation.

## I. INTRODUCTION

RNA dynamics are increasingly recognized as central components of cellular function, controlling key processes such as gene regulation, antiviral defense, and environmental sensing [1], [2], [3]. Strong links between RNA structure and function underlie the importance of structural analysis, which greatly benefits from the wealth of information provided by existing and emerging chemical mapping techniques [4]. In chemical mapping experiments, a chemical reagent modifies RNA molecules in a structure-dependent fashion. Depending on the reagent used, four distinct types of information can be gleaned, including spatial nucleotide contact information, solvent accessibility of the backbone, the local electrostatic environment adjacent to each nucleotide, and local nucleotide flexibility [4], [5]. This information is then used to infer RNA structural dynamics, either independently or in conjunction with structure prediction algorithms [6], [7]. The modification

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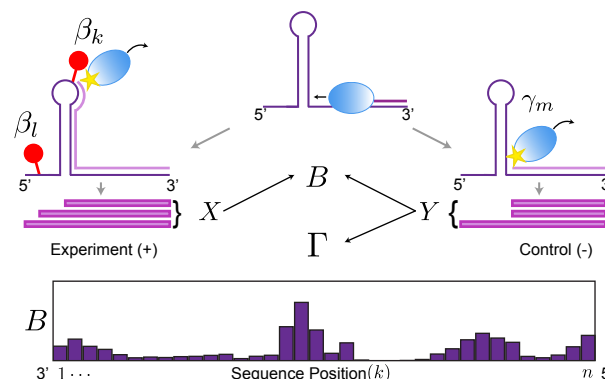


Fig. 1. Overview of a SHAPE-Seq chemical mapping experiment, model, and statistical analysis.

location is detected by means of conversion to cDNA using reverse transcriptase (RT), whereby transcription is blocked at the sites of modification (see illustration in Fig. 1). This generates a pool of cDNA fragments that begin at the 3' end of the molecule and terminate at the modified sites, or possibly at sites where there was natural RT dropoff [8]. Traditionally, the cDNA fragments have been resolved and quantified with capillary electrophoresis (CE) [8], although recently next-generation sequencing (NGS) technologies with much higher throughput have been used instead [9].

There are several challenges in interpreting chemical mapping data obtained from reverse transcription, irrespectively of the fragment quantification method that follows it. Primarily, in molecules with multiple modifications, only the first one (i.e., the closest to the 3' end) is revealed (see Fig. 1), and thus less information is available about the 5' region of the molecule. Second, RT's natural propensity to terminate at any site needs to be decoupled from modification-based termination, and this effect is controlled for in a separate control experiment. Finally, experimental variations need to be controlled for when combining measurements.

In previous work, we introduced a stochastic model for a specific next-gen sequencing based chemical modification experiment called SHAPE-Seq (selective 2'-hydroxyl acylation analyzed by primer extension followed by sequencing) [10]. Here we extend that work by presenting a more general model that entails fewer assumptions. In addition to capturing our previous SHAPE-Seq model as a special case, it is suitable for other experimental protocols, such as SHAPE-CE (SHAPE followed by capillary electrophoresis). The new model has the

added advantage that the generalization reveals a simplified maximum likelihood estimation scheme that leads to an elegant and fast approach for recovering chemical modification signal. Finally, we show how the general framework can be used to directly compare the power of SHAPE-CE to SHAPE-Seq. A key result is that SHAPE-Seq improves on SHAPE-CE not only by allowing for multiplexing but also by measuring extra information that can be utilized in the statistical inference framework we propose.

## II. MODELING SEQUENCING-BASED CHEMICAL MAPPING

We consider an RNA molecule that contains  $n$  sites, numbered 1 to  $n$  according to their sequence-position with respect to the molecule's 3' end (see Fig. 1), where the 3' end is excluded from analysis and assumes position 0. A cDNA fragment of length  $k$  that maps to the sequence between sites 0 and  $k-1$  ( $1 \leq k \leq n$ ) is called a *k-fragment*, and a full transcript of length  $n+1$  is called a *complete fragment*. In a SHAPE experiment, often called the (+) channel, the RNA is treated with an electrophile that reacts with conformationally flexible nucleotides to form 2'-O-adducts. We define the *relative reactivity* of a site,  $\beta_k$ , to be the probability of adduct formation at that site. In the control experiment, called the (−) channel, the primary source of incomplete fragments is RT's natural dropoff while transcribing the molecule. Because its propensity to drop may vary along sites, we define the *dropoff propensity at site k*,  $\gamma_k$ , to be the conditional probability that transcription terminates at site  $k$ , given that RT has reached this site. Therefore, associated with the RNA molecule are  $2n$  probabilities:  $B = (\beta_1, \dots, \beta_n)$ ,  $0 \leq \beta_k \leq 1 \forall k$ , and  $\Gamma = (\gamma_1, \dots, \gamma_n)$ ,  $0 \leq \gamma_k \leq 1 \forall k$ , which we wish to estimate from sequencing data.

While we can readily infer the natural dropoff propensities from the (−) channel data alone [10], the fragments observed in the (+) channel reflect the combined effects of natural dropoff and chemical modification. A point that is key to interpreting chemical mapping data is that a *k-fragment* is assumed to be generated when site  $k$  is the site that is *first* encountered by RT, regardless of the number of adducts that formed upstream of  $k$ . Assuming that adduct formations at the various nucleotides are statistically independent, the probability that a molecule is modified at site  $k$  (and possibly also at subsequent sites) is

$$Prob(\text{first adduct at site } k) = \beta_k \prod_{i=1}^{k-1} (1 - \beta_i) \quad (1)$$

for all  $1 \leq k \leq n$ . Incorporating the natural degradation in the elongating pool of modified molecules, we have

$$Prob\left(\begin{array}{c} k\text{-fragment} \\ \text{from} \\ \text{modification} \end{array}\right) = \prod_{i=1}^{k-1} (1 - \gamma_i) \times \beta_k \prod_{i=1}^{k-1} (1 - \beta_i). \quad (2)$$

We assume all other fragments originate from natural dropoff, either from unmodified or modified molecules, thus accounting

for the following probability:

$$\begin{aligned} & Prob(k\text{-fragment from natural dropoff}) \quad (3) \\ &= Prob\left(\begin{array}{c} \text{dropoff} \\ \text{at site } k \end{array} \middle| \begin{array}{c} \text{no adduct} \\ \text{at any site} \\ l \leq k \end{array}\right) \times Prob\left(\begin{array}{c} \text{no adduct} \\ \text{at any site} \\ l \leq k \end{array}\right) \\ &= \gamma_k \prod_{i=1}^{k-1} (1 - \gamma_i) \prod_{i=1}^k (1 - \beta_i). \end{aligned}$$

Taken together, Eqs. 2 and 3 imply

$$\begin{aligned} & Prob(k\text{-fragment in (+) channel}) \quad (4) \\ &= \left[1 - (1 - \gamma_k)(1 - \beta_k)\right] \prod_{i=1}^{k-1} (1 - \gamma_i)(1 - \beta_i) \end{aligned}$$

for all  $1 \leq k \leq n$ . Finally, because complete fragments can only arise from natural dropoff, we have

$$\begin{aligned} & Prob(\text{complete fragment in (+) channel}) \quad (5) \\ &= \prod_{i=1}^n (1 - \gamma_i) \prod_{i=1}^n (1 - \beta_i) = \prod_{i=1}^n (1 - \gamma_i)(1 - \beta_i). \end{aligned}$$

Assuming we observe  $(X_1, \dots, X_{n+1})$  *k-fragment* and complete-fragment counts in the (+) channel, and similarly,  $(Y_1, \dots, Y_{n+1})$  fragment counts in the (−) channel, the likelihood of observing the entire sequencing data is given by

$$\begin{aligned} \mathcal{L}(B, \Gamma) &= \prod_{k=1}^n \left[ \gamma_k \prod_{i=1}^{k-1} (1 - \gamma_i) \right]^{Y_k} \quad (6) \\ &\quad \prod_{k=1}^n \left[ \left(1 - (1 - \gamma_k)(1 - \beta_k)\right) \right. \\ &\quad \left. \prod_{i=1}^{k-1} (1 - \gamma_i)(1 - \beta_i) \right]^{X_k} \\ &\quad \left[ \prod_{i=1}^n (1 - \gamma_i) \right]^{Y_{n+1}} \left[ \prod_{i=1}^n (1 - \gamma_i)(1 - \beta_i) \right]^{X_{n+1}}. \end{aligned}$$

## III. MAXIMUM-LIKELIHOOD ESTIMATION

In this section, we use the likelihood formulation in Eq. 6 to show that *the ML estimates are given by*

$$\beta_k^* = \max \left\{ 0, \frac{\frac{X_k}{\sum_{i=k}^{n+1} X_i} - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}}{1 - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}} \right\}, \quad 1 \leq k \leq n. \quad (7)$$

Moreover, as will become clear from the derivation below, the likelihood formulation in Eq. 6 and its optimization can be readily extended to accommodate data from multiple replicates. One can then estimate the reactivities from multiple sources of data simultaneously and in a straightforward manner, and without any further assumptions or estimation of the statistical inter-experiment variation.

We start by rearranging terms in the log-likelihood function and writing it as the following sum of  $n$  terms:

$$\begin{aligned} \log \mathcal{L}(B, \Gamma) = & \sum_{k=1}^n \left[ \sum_{i=k+1}^{n+1} (X_i + Y_i) \log(1 - \gamma_k) \right. \\ & + \sum_{i=k+1}^{n+1} X_i \log(1 - \beta_k) + Y_k \log \gamma_k \\ & \left. + X_k \log(1 - (1 - \gamma_k)(1 - \beta_k)) \right]. \end{aligned} \quad (8)$$

Eq. 8 suggests that  $\log \mathcal{L}(B, \Gamma)$  is separable in the pairwise variables  $(\beta_k, \gamma_k)$ , hence each of the  $n$  two-dimensional functions can be optimized separately. To simplify notation, we introduce the constants  $S_k = \sum_{i=k+1}^{n+1} (X_i + Y_i)$ ,  $R_k = \sum_{i=k+1}^{n+1} X_i$ , and the functions

$$\begin{aligned} l_k(\beta_k, \gamma_k) = & S_k \log(1 - \gamma_k) + R_k \log(1 - \beta_k) \\ & + Y_k \log \gamma_k + X_k \log(1 - (1 - \gamma_k)(1 - \beta_k)) \end{aligned} \quad (9)$$

for  $1 \leq k \leq n$ , such that  $\log \mathcal{L}(B, \Gamma) = \sum_{k=1}^n l_k(\beta_k, \gamma_k)$ .

We now optimize  $l_k(\beta_k, \gamma_k)$  under the assumption that all fragment counts are positive. In that case,  $\gamma_k$  is bound to lie in  $(0, 1)$  and  $\beta_k$  cannot exceed 1, but the constraint  $\beta_k \geq 0$  is not inherent in the function and needs to be imposed during optimization. If we relax it, we find the optimal solution by setting the partial derivatives to zero, as follows

$$\begin{aligned} -\frac{R_k}{1 - \beta_k} + \frac{X_k(1 - \gamma_k)}{1 - (1 - \gamma_k)(1 - \beta_k)} &= 0 \\ -\frac{S_k}{1 - \gamma_k} + \frac{Y_k}{\gamma_k} + \frac{X_k(1 - \beta_k)}{1 - (1 - \gamma_k)(1 - \beta_k)} &= 0, \end{aligned} \quad (10)$$

yielding the solution

$$\hat{\beta}_k = \frac{\frac{X_k}{\sum_{i=k}^{n+1} X_i} - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}}{1 - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}}, \quad \hat{\gamma}_k = \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}. \quad (11)$$

One can verify local maximality of  $(\hat{\beta}_k, \hat{\gamma}_k)$  from  $l_k$ 's Hessian. Its global optimality then follows from  $l_k(\beta_k, \gamma_k)$ 's continuity and from the fact that it approaches  $-\infty$  near the boundary of its domain's closure. Eq. 11 clearly results in  $\hat{\beta}_k < 1$ , but there is no guarantee that  $\hat{\beta}_k \geq 0$ , as its numerator consists of two terms, each comprising of data from either the (+) or the (−) channels. As such, they are not constrained to yield a positive difference, and might result in infeasible estimates. We then wish to find a *feasible* ML solution, and we argue that whenever  $\hat{\beta}_k < 0$ , this solution is attained at

$$(\beta_k^*, \gamma_k^*) = (0, \frac{X_k + Y_k}{\sum_{i=k}^{n+1} (X_i + Y_i)}) \quad (12)$$

(see Appendix for justification). This means that whenever we observe a site  $k$  for which  $\frac{X_k}{\sum_{i=k}^{n+1} X_i} < \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}$ , the best explanation of the observed data is that no modification occurred at that site and that all  $k$ -fragments arose from natural dropoff. Remarkably, this result supports existing approaches to analyzing SHAPE-CE data, whereby sites whose recovered signal is negative are assigned zero reactivity [7].

We now allow zero counts when  $k \leq n$ , while assuming that  $X_{n+1}, Y_{n+1} > 0$ . The latter assumption is justified by the fact that  $Y_{n+1} = 0$  is indicative of severe dropoff that could stem from strong transcription termination at select sites or reflect a cumulative effect of imperfect transcription elongation over a long RNA strand. Both situations are avoided by truncating the analyzed sequence at  $n' < n$ , such that  $Y_{n'+1} > 0$ . On the other hand,  $X_{n+1} = 0$  (while  $Y_{n+1} > 0$ ) suggests a “too high” average modification rate, leading to strong signal decay in the (+) channel. One should then decrease the reagent's concentration. Nevertheless, zero counts at intermediate sites are commonly observed in practice. When  $X_k = 0$  but  $Y_k \neq 0$ , it is straightforward to show that the optimum is determined by Eq. 12, whereas the case where  $Y_k = 0$  and  $X_k \neq 0$  is optimized by the initial solution in Eq. 11.

#### A. Poisson-distributed chemical modification

In this subsection, we revisit a chemical mapping model that we have previously developed and used for structure characterization [10]. The model incorporates an assumption on the stochastic nature of the underlying chemistry, and we discuss its implications on ML estimation from SHAPE-Seq data. By casting the model as a special case of the framework we presented above we are able to simplify our previous estimation scheme to obtain **closed-form ML estimates of relative reactivities for the Poisson model in [10]**:

$$r_k^* = \max \left\{ 0, \log \left( 1 - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i} \right) - \log \left( 1 - \frac{X_k}{\sum_{i=k}^{n+1} X_i} \right) \right\}. \quad (13)$$

The work in [10] makes an assumption that is widely used in models of biochemical reactions, whereby the reaction with the modifying reagent follows a Poisson process. Specifically, during modification, an RNA may be exposed to varying numbers of electrophile molecules, and we model the number of times it is exposed to these molecules as a Poisson process of an unknown rate  $c > 0$ , i.e., we assume that  $\text{Prob}(i \text{ exposures}) = \frac{c^i e^{-c}}{i!}$ . It is worth noting that the Poisson framework is especially suitable for low-incidence settings [11], and that mapping experiments are particularly calibrated to yield single-hit kinetics, that is, they aim to achieve an average modification rate of  $c \approx 1$ . Now, each exposure may result in the modification of a site, where the site is determined according to a probability distribution  $\Theta = (\theta_1, \dots, \theta_n)$ ,  $\sum_{k=1}^n \theta_k = 1$ , where  $\theta_k$  represents the *relative reactivity* of site  $k$ . It is easy to show that the number of modifications at site  $k$  also obeys a Poisson distribution, with an unknown rate  $r_k = c\theta_k$ , that is,  $\text{Prob}(i \text{ modifications at site } k) = \frac{(c\theta_k)^i e^{-c\theta_k}}{i!}$ . It then follows that  $\text{Prob}(\text{site } k \text{ is not modified}) = e^{-c\theta_k}$ . Setting

$$\beta_k := 1 - \text{Prob}(\text{site } k \text{ is not modified}) = 1 - e^{-c\theta_k}, \quad (14)$$

we can write

$$\begin{aligned}
& \text{Prob}(\text{first adduct at site } k) \\
&= \beta_k \prod_{i=1}^{k-1} (1 - \beta_i) = (1 - e^{-c\theta_k}) e^{-c \sum_{i=1}^{k-1} \theta_i} \\
&= (1 - e^{-c\theta_k}) e^{c(\sum_{i=k}^n \theta_i - 1)} \\
&= e^{c(\sum_{i=k}^n \theta_i - 1)} - e^{c(\sum_{i=k+1}^n \theta_i - 1)},
\end{aligned} \tag{15}$$

$$\text{Prob}(\text{no modification}) = \prod_{i=1}^n (1 - \beta_i) = e^{-c}. \tag{16}$$

When plugging these expressions into Eq. 6, the likelihood function reduces to that in [10]. We can therefore use the initial estimates in Eq. 11 along with Eq. 14 to estimate the distribution  $\Theta$  as follows:

$$\hat{\theta}_k = \frac{1}{\hat{c}} \left[ \log \left( 1 - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i} \right) - \log \left( 1 - \frac{X_k}{\sum_{i=k}^{n+1} X_i} \right) \right], \tag{17}$$

where the scaling constant  $\hat{c}$  is the estimate of the average modification rate, which is recovered from Eq. 16 to equal

$$\hat{c} = - \sum_{i=1}^n \log(1 - \hat{\beta}_i) = \log \left( \frac{Y_{n+1}}{\sum_{i=1}^{n+1} Y_i} \right) - \log \left( \frac{X_{n+1}}{\sum_{i=1}^{n+1} X_i} \right). \tag{18}$$

It is now apparent that Eqs. 17 and 18 are the outputs of Algorithm 1 in [10].

When optimization yields negative  $\hat{\beta}_k$ 's, they correspond to negative  $\hat{\theta}_k$ 's (see Eq. 14). However, when imposing non-negativity, these are projected onto  $\beta_k^* = 0$ , and  $\theta_k^* \propto \log(1 - \beta_k^*) = 0$  accordingly. The revised modification rate estimate now amounts to  $c^* = - \sum_{i: \hat{\beta}_i > 0} \log(1 - \hat{\beta}_i)$ , which is larger than the initial  $\hat{c}$ . Consequently, the distribution  $\hat{\Theta}$  is updated such that all negative entries are set to zero, while the others are effectively scaled down due to the increase from  $\hat{c}$  to  $c^*$ . In other words, one merely needs to compute the relative reactivity estimate in Eq. 13 and then normalize it by  $c^*$  to generate a proper probability distribution  $\Theta^*$ . Alternatively, one could apply any other normalization method to the outputs of Eq. 13, such as the ones currently used for interpreting SHAPE reactivities [12], [7]. This would retain the relativity between reactivities, while adjusting the dynamic range to a scale that is in line with current settings of subsequent structure prediction modules [7], [13].

In practice, the formulation of site-specific modifications via  $n$  independent Poisson processes, as opposed to the multinomially-distributed choice of a site via  $\Theta$ , vastly simplifies the likelihood function's derivation and optimization. In particular, it removes the need for the iterative likelihood optimization routine that follows Algorithm 1 in [10]. The equivalence between the two formulations is an instance of general equivalence between multinomial and Poisson log-linear models with respect to ML estimation [11], [14].

It is interesting to compare the estimates obtained under a Poisson assumption with those obtained without it. To qualitatively compare them, consider the relations  $\theta_k^* \propto -\log(1 - \beta_k^*)$ , and note that  $-\log(1 - x) \approx x$  when  $x \approx 0$ . This

means that a Poisson assumption is not expected to affect sites with small reactivity, but on the other hand, it amplifies the estimated *relative* reactivities at more reactive sites, and more intensely as the reactivity increases (i.e., as  $1 - \beta_k^* \rightarrow 0$ ). It thus exerts its effect by stretching the dynamic range of reactivities, and thereby might confer more sensitivity to outliers. Because the effect's intensity depends on  $\beta_k^*$ 's magnitude, it is likely to be more pronounced under high modification rate conditions, where either the reagent concentration is high or the RNA entails many highly reactive sites.

A quantitative comparison between the two models using experimental data for the *Staphylococcus aureus* plasmid pT181 sense RNA is shown in Fig. 2. To allow for a fair comparison between  $B^*$  and  $\Theta^*$ , we scaled  $B^*$  such that its entries sum to 1. Note that the scaling factor is larger in the Poisson case, and thus the Poisson-based reactivities are smaller than their general-model counterparts at relatively unreactive sites. The data in Fig. 2 reveal very mild differences between the estimates and consequently, minor increase in the dynamic range. Similar results were observed for a number of other molecules that we have probed [9]. It is worth noting that the modification rate in this experiment was estimated at  $c^* = 1.94$  adducts per molecule, which is relatively high and clearly diverts from single-hit kinetics. This suggests that the Poisson assumption may not be critical even in the presence of high modification rate, and that the two model-based schemes may generally be used interchangeably.

Finally, we stress that the Poisson-based correction aligns more closely with current CE-based analysis methodology [7], [15], in the sense that the signals are in fact corrected separately for each channel and then subtracted, along the lines of Eq. 13. In contrast, ML estimation under the general framework is not amenable to such decoupling (see Eq. 11). Alongside this seemingly Poisson-based correction, current analysis guidelines also recommend using one of two outlier filters [7], and these may remedy the increased sensitivity to outliers that we highlighted earlier.

#### IV. ADAPTATION TO QUANTIFICATION BY CAPILLARY ELECTROPHORESIS

Traditional chemical mapping techniques have used electrophoresis to identify the cDNA fragments and to quantify their abundances [4]. Most recently, capillary electrophoresis (CE) has been used to detect fluorescently labeled cDNAs from experiments. CE systems output an electropherogram, consisting of analog traces that report fluorescence intensity as a function of time. These traces must be extensively processed to extract quantitative nucleotide information, and while steady progress is being made with the development of computer-aided analysis tools [12], [16], [17], there is still a need for more statistically-robust and automated analysis methods.

Despite the challenges in analyzing CE-based data and the advances offered by NGS platforms, the conventional approach is still valuable for two reasons. First, it is currently cheaper and faster to apply when the multiplexing and sensitivity advantages of the newer platforms are not needed, and second,

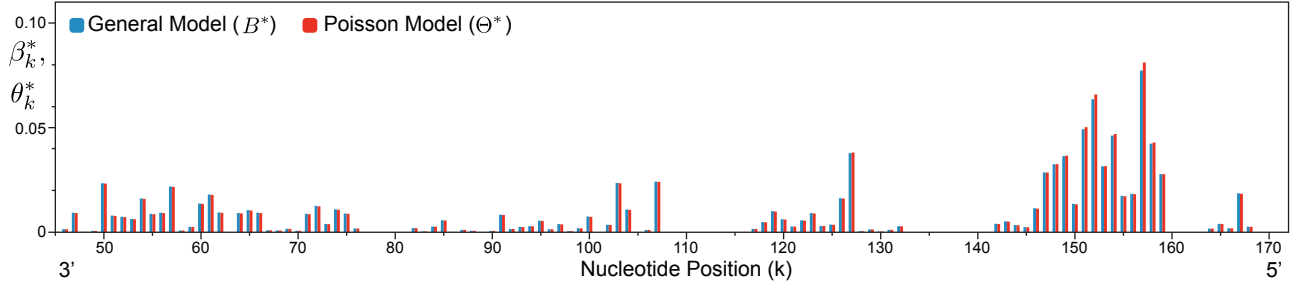


Fig. 2. Relative reactivity estimates for *S. aureus* plasmid pT181 sense RNA under the general-model and the Poisson-model maximum-likelihood frameworks. Sites 1-45 showed negligible probabilities and were omitted from display.

it can be used for probing a few pilot RNAs prior to conducting a larger-scale NGS-based experiment. These considerations have motivated us to adapt our SHAPE-Seq ML framework to the case of SHAPE-CE. While the differences in analog versus digital signal processing are apparent, an essential difference between SHAPE-Seq and SHAPE-CE data has to do with the lack of information about complete fragments in CE settings. This is due to large amounts of long fragments under single-hit-kinetics conditions, causing detector saturation. Notably, a strong full-length signal also poses difficulty in accurately quantifying the last stretch of 10-20 nucleotides [18], but in this work, we only address the first issue and assume that all other peaks are quantifiable.

#### A. Maximum likelihood framework

Here, we show that in the absence of complete-fragment information, the relative reactivities at sites 1 to  $n - 1$  are estimated using the following formula ( $1 \leq k \leq n - 1$ ):

$$\beta_k^{(CE)*} = \max \left\{ 0, \frac{\frac{\tilde{X}_k}{\sum_{i=k}^n \tilde{X}_i} - \frac{\tilde{Y}_k}{\sum_{i=k}^n \tilde{Y}_i}}{1 - \frac{\tilde{Y}_k}{\sum_{i=k}^n \tilde{Y}_i}} \right\}, \quad (19)$$

where  $(\tilde{X}_1, \dots, \tilde{X}_n)$  and  $(\tilde{Y}_1, \dots, \tilde{Y}_n)$  are the areas under the detected peaks in the (+) and (-) channel traces, respectively. We also show that  $\beta_n^{(CE)*}$  cannot be determined from the available information.

Our result is possible due to the very recent automation of the trace-alignment and peak-fitting steps with the HiTRACE software [17]. This, in turn, generates quantifiable nucleotide reactivity data, in the form of integrated peak areas, prior to signal correction and scaling. The peak areas can then be used in place of the digital sequence-counts to deconvolve the effects of over-modification and natural dropoff on the observed (+) channel signal, as was recently done in [15] by means of an optimization routine. This is in contrast to previous analysis tools, where signal correction and scaling were needed prior to the application of semi-manual alignment, fitting, and integration routines [12].

We assume that the peak areas from the (+) and (-) channels are proportional to the fragment counts as follows:  $\tilde{X}_k = \delta X_k$  and  $\tilde{Y}_k = \epsilon Y_k$  for all  $1 \leq k \leq n$  where  $\delta$  and  $\epsilon$  are unknown positive constants. The two potentially different

constants reflect experimental variation between the channels, including differences in such factors as molecular concentrations and dye intensities [12]. Currently, these are corrected for by scaling the (-) channel signal by a constant factor that is set either manually following visual inspection [12] or automatically via an optimization routine [15]. We will see that in our ML scheme there is no benefit in applying such a “correction”.

The likelihood of observing the peak areas is given by

$$\mathcal{L}^{CE}(B, \Gamma) = \prod_{k=1}^n \left[ \gamma_k \prod_{i=1}^{k-1} (1 - \gamma_i) \right]^{\frac{\tilde{Y}_k}{\epsilon}} \prod_{k=1}^n \left[ \left( 1 - (1 - \gamma_k)(1 - \beta_k) \right) \prod_{i=1}^{k-1} (1 - \gamma_i)(1 - \beta_i) \right]^{\frac{\tilde{X}_k}{\delta}}, \quad (20)$$

and the log-likelihood function is then written as

$$\log \mathcal{L}^{CE}(B, \Gamma) = \sum_{k=1}^{n-1} l_k^{CE}(\beta_k, \gamma_k) + \frac{1}{\epsilon} \tilde{Y}_n \log \gamma_n + \frac{1}{\delta} \tilde{X}_n \log (1 - (1 - \gamma_n)(1 - \beta_n)), \quad (21)$$

where

$$l_k^{CE}(\beta_k, \gamma_k) = U_k \log(1 - \gamma_k) + V_k \log(1 - \beta_k) + \frac{1}{\epsilon} \tilde{Y}_k \log \gamma_k + \frac{1}{\delta} \tilde{X}_k \log (1 - (1 - \gamma_k)(1 - \beta_k)), \quad (22)$$

and  $U_k = \sum_{i=k+1}^n (\frac{1}{\delta} \tilde{X}_i + \frac{1}{\epsilon} \tilde{Y}_i)$ ,  $V_k = \frac{1}{\delta} \sum_{i=k+1}^n \tilde{X}_i$ .

Assuming all peak areas are nonzero, we can repeat the derivation in the previous section, while noting two differences: first, different coefficients appear in the equations and second, the last equation (when  $k = n$ ) is different. Whereas the first difference is minor when all observables are positive, the second one leads to an important difference in the ML solution. Therefore, we start by optimizing  $l_k^{CE}(\beta_k, \gamma_k)$  when  $1 \leq k \leq n - 1$  to obtain

$$\hat{\beta}_k^{CE} = \frac{\frac{\tilde{X}_k}{\sum_{i=k}^n \tilde{X}_i} - \frac{\tilde{Y}_k}{\sum_{i=k}^n \tilde{Y}_i}}{1 - \frac{\tilde{Y}_k}{\sum_{i=k}^n \tilde{Y}_i}}, \quad \hat{\gamma}_k^{CE} = \frac{\tilde{Y}_k}{\sum_{i=k}^n \tilde{Y}_i}. \quad (23)$$

In the special cases where  $\tilde{X}_k$  or  $\tilde{Y}_k$  are zero, but  $U_k$  and  $V_k$  are positive and  $U_k > V_k$ , we obtain  $(\hat{\beta}_k^{CE}, \hat{\gamma}_k^{CE}) = (0, \frac{\tilde{Y}_k}{\sum_{i=k}^n \tilde{Y}_i})$  and  $(\hat{\beta}_k^{CE}, \hat{\gamma}_k^{CE}) = (\frac{\tilde{X}_k}{\sum_{i=k}^n \tilde{X}_i}, 0)$ , respectively. It can also be verified that these points correspond to a global maximum, independently of the  $\delta$  and  $\epsilon$  values. When  $\hat{\beta}_k^{CE} < 0$ , one can repeat previous arguments to show that the constrained maximum is attained at  $(\beta_k^{(CE)*}, \gamma_k^{(CE)*}) = (0, \frac{\frac{1}{\delta}\tilde{X}_k + \frac{1}{\epsilon}\tilde{Y}_k}{U_k + V_k})$ . Taken together, these results lead to the formulation in Eq. 19. Importantly, one cannot evaluate  $\gamma_k^{(CE)*}$  without knowledge of the relative scaling factor  $\frac{\delta}{\epsilon}$ , however, our goal is to estimate the relative reactivities, and these are independent of  $\frac{\delta}{\epsilon}$ .

While the estimates in Eq. 19 bear great similarity to the NGS-based estimates, the case where  $k = n$  reveals a different scenario, as the missing  $\tilde{X}_{n+1}$  and  $\tilde{Y}_{n+1}$  hamper  $\beta_n$ 's estimation. In this case, we optimize the function  $l_n^{CE}(\beta_n, \gamma_n) = \frac{1}{\epsilon}\tilde{Y}_n \log \gamma_n + \frac{1}{\delta}\tilde{X}_n \log(1 - (1 - \gamma_n)(1 - \beta_n))$ , which is maximized at  $\hat{\gamma}_n = 1$ , where its value is independent of  $\hat{\beta}_n$ 's value. Consequently, one cannot determine  $\hat{\beta}_n$ . Moreover, one cannot recover the exact fraction of modified molecules, as it depends on all  $n$  reactivities as follows:

$$f_{mod} = \text{Prob}(\text{molecule is modified}) = 1 - \prod_{i=1}^n (1 - \beta_i). \quad (24)$$

A possible way to circumvent this limitation is by excluding site  $n$  from analysis and evaluating only  $\beta_1^{(CE)*}, \dots, \beta_{n-1}^{(CE)*}$  based on all available peak areas, including  $\tilde{X}_n$  and  $\tilde{Y}_n$ . In practice, the effect of such omission is likely to be minor, since the studied RNA sequence is typically embedded in between auxiliary RNA constructs, called structure cassettes [8], and site  $n$  is therefore included in one of these cassettes [9]. We can then approximate the modification fraction by  $\hat{f}_{mod}^{CE} \approx 1 - \prod_{i=1}^{n-1} (1 - \beta_i^{(CE)*})$ , where the goodness of this approximation depends on how large  $\tilde{X}_n$  is in comparison to the missing  $\tilde{X}_{n+1}$ . This is because the approximation implicitly assumes that  $\beta_n^{(CE)*} = 0$ , whereas in the presence of a full-length signal we would have  $\beta_n^{(CE)*} = 1 - \frac{\tilde{X}_{n+1}}{\tilde{X}_n + \tilde{X}_{n+1}} \times \frac{\tilde{Y}_n + \tilde{Y}_{n+1}}{\tilde{Y}_{n+1}}$ , which might diverge from zero whenever  $\frac{\tilde{X}_{n+1}}{\tilde{X}_n + \tilde{X}_{n+1}}$  diverges from 1. The reasoning behind setting  $\hat{\beta}_n = 0$  is twofold: first, our past experience with analyzing SHAPE-Seq data shows that the structure cassettes tend to display negligible reactivities, and second, the observed counts  $X_{n+1}$  and  $Y_{n+1}$  were very large compared to *any* other count. For example, in mapping experiments we conducted,  $X_{n+1}$  amounted to approximately 10% of the total (+)-channel reads and  $Y_{n+1}$  amounted to 15% – 20% of the total (–)-channel reads [10], [9], whereas the rest of the reads were associated with a total of 100 – 200 nucleotides. Based on these observations and on the premise that SHAPE-CE statistics should follow similar patterns, we believe that this approximation is fairly accurate in general. Nonetheless, one must keep in mind that this may not always be the case, especially when studying long RNAs, where cumulative dropoff effects result in severe signal attenuation and consequently relatively weak full-length signal. In

addition, we point out another subtle difference between the scheme's implementations under the two platforms. Specifically, we may not assume that the CE-based  $U_k$  and  $V_k$  are always positive, whereas we made a similar assumption when we derived NGS-based estimates. That assumption was based on the fact that probing experiments can be designed such that a strong full-length signal arises. While this also applies to CE-based protocols, the absence of a full-length signal might complicate analysis whenever  $\tilde{X}_n = 0$  or  $\tilde{Y}_n = 0$ . However, this can be easily remedied by converting these zeros into very small constants, such that the resulting approximations are negligible.

To summarize, building on recent contributions to the automation of CE-based analog signal processing [17], our method facilitates a simple and completely automated data analysis pipeline for CE-based chemical mapping probes, and in particular, for SHAPE-CE. Another interesting point arising from our derivation is that our ML scheme is invariant under background-signal scaling.

### B. Effects of full-length signal information on ML estimation

Our analysis highlights the fact that the difference in ML estimation between the two platforms lies essentially in the presence or absence of a full-length signal (compare Eqs. 7 and 19). In this subsection, we first use our derivation to qualitatively explore the potential impact of this difference. We then quantify its effects by deleting the full-length signal information from SHAPE-Seq data to mimic SHAPE-CE data, such that the estimates under both platforms can be compared.

Before we start, we stress that this difference between platforms pertains only to RNAs that are no longer than 400–600 nucleotides [4], a limitation imposed by RT's imperfect processivity, as well as to RNAs that do not contain major transcription barriers that result in severe dropoff. RNAs of these two types are probed by annealing multiple primers at various sites [13], [19], [20], in which case a full-length signal is not obtained from most primer locations even when the fragments are sequenced. In such settings, NGS and CE platforms generate similar information, and analysis should follow the lines of the CE framework. In what follows, we simplify the exposition by using the same notation for  $X_k$  and  $\tilde{X}_k$ , and similarly for  $Y_k$  and  $\tilde{Y}_k$ .

To better understand the implications of not recording the full-length information, we rewrite the initial estimates as

$$1 - \hat{\beta}_k^{SEQ} = \frac{1 - \frac{X_k}{\sum_{i=k}^{n+1} X_i}}{1 - \frac{Y_k}{\sum_{i=k}^{n+1} Y_i}}, \quad 1 - \hat{\beta}_k^{CE} = \frac{1 - \frac{X_k}{\sum_{i=k}^n X_i}}{1 - \frac{Y_k}{\sum_{i=k}^n Y_i}}, \quad (25)$$

and consider the following two examples.

- 1) Assume for simplicity that the (+) and (–) RNA pools are the same size, i.e.,  $\sum_{i=1}^{n+1} X_i = \sum_{i=1}^{n+1} Y_i$ , and suppose we probe a highly reactive molecule, or alternatively, use high reagent concentration. Both scenarios divert from single-hit kinetics toward higher modification rates, resulting in large dropoff in the (+) channel. As an extreme case, assume that the proportion of complete



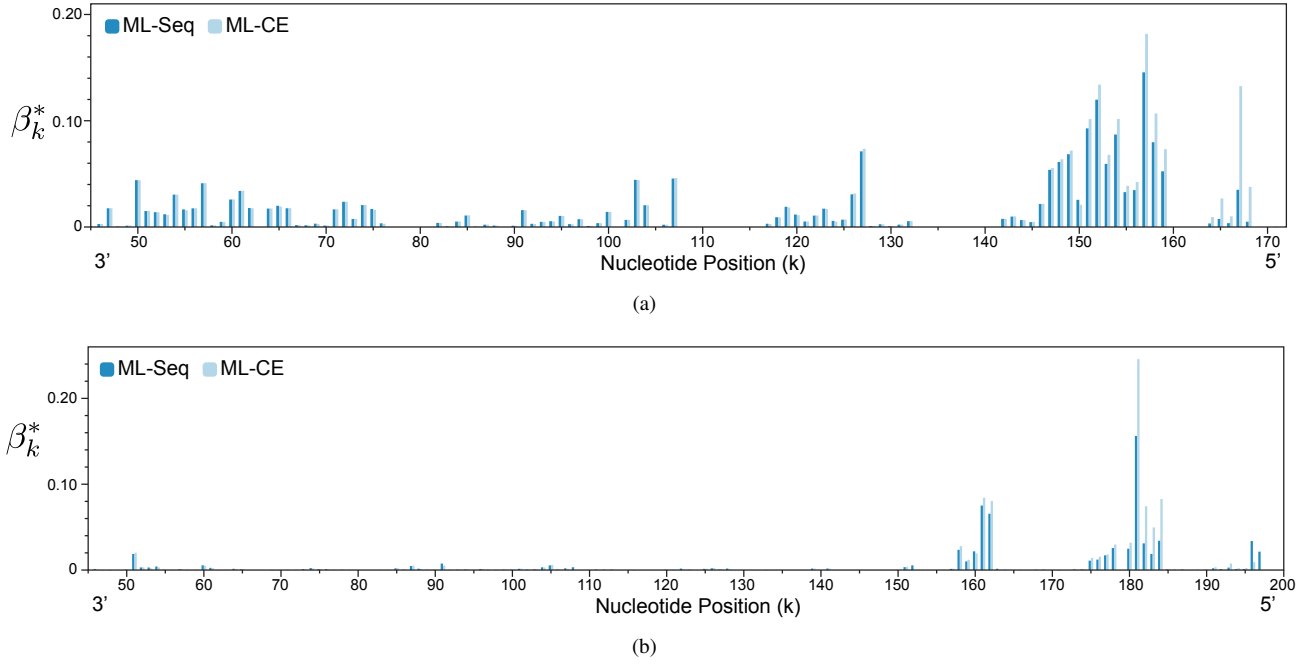


Fig. 3. Reactivity estimates in the presence and absence of complete-fragment information for *S. aureus* plasmid pT181 sense RNA (a) and *B. subtilis* RNase P RNA (b). Sites at the 3' end that showed negligible reactivities were omitted from display.

fragments in the (+) channel is negligible, such that  $\sum_{i=1}^n X_i \approx \sum_{i=1}^{n+1} X_i$ , while it is significant in the (-) channel. In this case, the difference between  $1 - \hat{\beta}_k^{SEQ}$  and  $1 - \hat{\beta}_k^{CE}$  amounts to the difference between  $\frac{Y_k}{\sum_{i=k}^{n+1} Y_i}$  and  $\frac{Y_k}{\sum_{i=k}^n Y_i}$ . Because  $Y_{n+1}$  occupies a major fraction of the (-) channel pool, the denominator of the right-hand expression is larger than the left-hand one, and consequently  $\hat{\beta}_k^{SEQ} > \hat{\beta}_k^{CE}$ . This example illustrates that the missing information might lead to different estimates, and that under some scenarios, it results in under-estimation of all reactivities. Furthermore, the effect becomes more pronounced as we progress toward site  $n$ , since  $Y_{n+1}$  occupies increasingly larger fractions of  $\sum_{i=k}^{n+1} Y_i$ . For this reason, the *relative* reactivities are distorted as well, even when all the  $\beta_k$ 's are under-estimated.

- 2) In this example, we still assume that  $\sum_{i=1}^{n+1} X_i = \sum_{i=1}^{n+1} Y_i$ , but we now require both  $X_{n+1}$  and  $Y_{n+1}$  to represent significant fractions of the overall pools. We further assume that at the last two sites we observe  $Y_n = Y_{n-1} = 3$ ,  $X_{n-1} = 30$ , and  $X_n = 6$ . Then, for site  $k = n - 1$  we obtain  $\hat{\beta}_{n-1}^{CE} = 1 - (1 - \frac{30}{36}) / (1 - \frac{3}{6}) = \frac{2}{3}$ , but on the other hand, when  $X_{n+1}, Y_{n+1}$  are large enough (e.g., on the order of thousands), we have  $\hat{\beta}_{n-1}^{SEQ} \approx 0$ . Here, unknown large end-signals lead to the misinterpretation of minor (+) channel signals (or merely system noise) as indicative of high reactivity. This stems from misrepresentation of the molecular pool composition by  $X_1, \dots, X_n$ , and as before, the effect tends to intensify as we get closer to site  $n$ .

These examples describe very specific and perhaps extreme scenarios, and clearly, it is difficult to predict the effect of a given pair  $X_{n+1}, Y_{n+1}$  on the estimates of the entire RNA sequence, as these also depend on the underlying fragment-length distributions. While distortion may certainly be small at many sites, such differences accumulate when all estimates are jointly aggregated into an estimate of the modification fraction  $f_{mod}$ . To demonstrate this cumulative effect, we first assume that the initial estimate  $\hat{B}$  consists entirely of nonnegative  $\hat{\beta}_k$ 's under both platforms, and so no zeroing is applied. It is then easy to see that

$$\begin{aligned} \hat{f}_{mod}^{CE} &\approx 1 - \frac{X_n}{Y_n} \times \frac{\sum_{i=1}^n Y_i}{\sum_{i=1}^n X_i} \\ \hat{f}_{mod}^{SEQ} &= 1 - \frac{X_{n+1}}{Y_{n+1}} \times \frac{\sum_{i=1}^{n+1} Y_i}{\sum_{i=1}^{n+1} X_i}, \end{aligned} \quad (26)$$

where the inequality is due to an unknown  $\hat{\beta}_n$  under CE settings (see discussion following Eq. 24). For simplicity, we again assume equally sized (+) and (-) RNA pools, in which case  $\frac{X_{n+1}}{Y_{n+1}}$  completely determines  $\hat{f}_{mod}^{SEQ}$ , whereas  $\hat{f}_{mod}^{CE}$  is affected by site  $n$ 's data ratio,  $\frac{X_n}{Y_n}$ , as well as by  $X_{n+1}$  and  $Y_{n+1}$ 's portions of the entire RNA pools (rather than by their ratio). It thus appears that the CE-based estimate is more susceptible to the actual experimental conditions and to noise toward the signal's end. Yet, in practice, many of the point estimates are zeroed out and so the formulation above may not accurately capture the true estimates.

We conclude with two examples computed from SHAPE-Seq data, where we compare the NGS- and CE-based ML frameworks for the *Staphylococcus aureus* pT181 RNA and

for the *Bacillus subtilis* RNase P RNA specificity domain. The CE case was analyzed by deleting the (+) and (−) end signals, thus reflecting our assumption that SHAPE-CE data closely resembles SHAPE-Seq data, as we have previously observed for these two RNAs [9]. The estimated reactivities shown in Fig. 3 support our observations, and a clear trend of divergence between the estimates under the two frameworks is apparent toward the 5′ end, where in these two cases the CE data result in over-estimation. Interestingly, the divergence in the fraction of modified molecules was minor in the pT181 case ( $\hat{f}_{mod}^{CE} \approx 0.9$  vs.  $\hat{f}_{mod}^{SEQ} \approx 0.86$ ) and amounted to approximately 20% for RNase P ( $\hat{f}_{mod}^{CE} \approx 0.62$  vs.  $\hat{f}_{mod}^{SEQ} \approx 0.52$ ). Our results thus point out to a potential shortcoming of likelihood-based signal recovery schemes, when used in conjunction with CE systems. It is important to stress, however, that the previous and less automated method developed by the Weeks and Giddings labs [12] does not suffer from this shortcoming. This is because it relies on visual assessment of the signal’s decay and its subsequent correction, whereas likelihood-based methods such as ours and the one reported in [15] explicitly utilize the observed frequencies to correct the signal. At the same time, relying on user feedback poses challenges to the reproducibility and accuracy of analysis, as discussed in [10].

## V. CONCLUSION

In this work, we presented a model and a maximum-likelihood framework, which lead to simple closed-form reactivity estimates, and which are applicable to chemical probes that use either CE or NGS for transcript quantification. We used this general framework to directly compare the estimates obtained with the two detection platforms, and concluded that lack of full-length signal information in CE settings degrades the estimates quality, and hence SHAPE-Seq is a more informative, and potentially more accurate, technique. Yet, it remains to determine the effects of this missing information on structure prediction’s accuracy in order to clearly characterize the benefits of using new protocols such as SHAPE-Seq.

## APPENDIX

To justify our claim that Eq. 12 pertains to the feasible ML solution, we first assume that  $\beta_k = 0$  and then optimize  $l_k(0, \gamma_k) = S_k \log(1 - \gamma_k) + (X_k + Y_k) \log \gamma_k$  to obtain  $\gamma_k^*$  as its maximizing argument. Hence, this point represents the maximum over all points on one edge of the constrained optimization domain  $\mathcal{D} = \{(\beta_k, \gamma_k) : 0 \leq \beta_k \leq 1, 0 \leq \gamma_k \leq 1\}$ . Now, assume that our claim is not correct, i.e., the maximum over  $\mathcal{D}$  is not attained at a point where  $\beta_k = 0$ . Then, there exists a point  $(\tilde{\beta}_k, \tilde{\gamma}_k)$  such that  $l_k(\tilde{\beta}_k, \tilde{\gamma}_k) > l_k(\beta_k^*, \gamma_k^*) \geq l_k(0, \gamma_k)$  for any  $0 < \gamma_k < 1$ . Clearly,  $(\tilde{\beta}_k, \tilde{\gamma}_k)$  must lie in  $\mathcal{D}$ ’s interior since  $l_k$  approaches  $-\infty$  near all other three edges of  $\mathcal{D}$ . Next, we construct a rectangular compact set  $\mathcal{E} = \{(\beta_k, \gamma_k) : 0 \leq \beta_k \leq a < 1, 0 < b \leq \gamma_k \leq c < 1\} \subset \mathcal{D}$  around  $(\tilde{\beta}_k, \tilde{\gamma}_k)$ , where we choose  $a, b$  and  $c$  such that  $l_k(\tilde{\beta}_k, \tilde{\gamma}_k)$  exceeds  $l_k$ ’s values over  $\mathcal{E}$ ’s boundary. This is possible due to the function’s decline to  $-\infty$  as  $\beta_k$  approaches 1 and as  $\gamma_k$  approaches  $\{0, 1\}$  and because  $l_k(\tilde{\beta}_k, \tilde{\gamma}_k)$  is greater than  $l_k$ ’s values at the fourth

edge (where  $\beta_k = 0$ ). Since  $\mathcal{E}$  is compact,  $l_k$  must attain a global maximum over it, but it follows from the construction that the maximum must lie in its interior. This, in turn, means that this maximum must also be a stationary point (since  $l_k$  is differentiable over  $\mathcal{E}$ ), which contradicts the fact that the only stationary point is  $(\hat{\beta}_k, \hat{\gamma}_k)$ , which lies outside of  $\mathcal{D}$ .

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