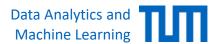
### **Machine Learning for Graphs and Sequential Data**

#### **Robustness of Machine Learning Models**

Lecturer: Prof. Dr. Stephan Günnemann

cs.cit.tum.de/daml

Summer Term 2023



#### Roadmap

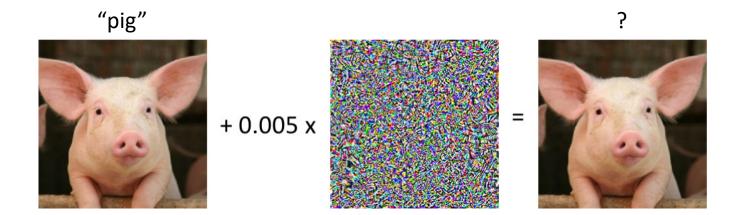
- 1. Introduction
- 2. Construction of adversarial examples
- 3. Improving robustness
- 4. Certifiable robustness
  - Exact certification
  - Convex relaxations
  - Lipschitz-continuity
  - Randomized smoothing

#### Introduction

- Often ML models and algorithms are optimized w.r.t. simple metrics
  - e.g. misclassification rate, reconstruction error, etc.
- As ML/AI is becoming more widespread and is used in critical applications (e.g. autonomous driving, algorithmic decision-making involving humans) we must consider further aspects
- As ML models get deployed in the real-world they create feedback loops which can have potentially unintended consequences
- One important aspect: Are the ML models reliable?
  - How do they behave in the wild? When your data might, e.g., be corrupted?

## **What Are Adversarial Examples?**

# Predicted class:

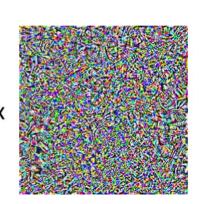


## **What Are Adversarial Examples?**

# Predicted class:



+ 0.005 x

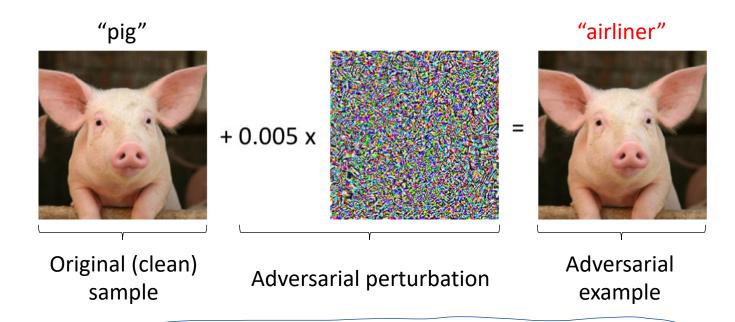


"airliner"



### What Are Adversarial Examples?

# Predicted class:



**Small** (imperceptible) but **specifically crafted perturbations** lead to **false predictions** in machine learning models.

- Why should we care about adversarial examples?
- What does "small" mean?
- How are adversarial examples created?
- How to protect against adversarial examples?

Image from <a href="http://gradientscience.org/intro">http://gradientscience.org/intro</a> adversarial/

### Why We (Should) Care About Adversarial Examples

#### **Real-world risks**

- Adversarial examples are an obvious security threat for many real-world applications, e.g. self-driving cars.
- Adversarial examples also exist in the real world, e.g. 2D / 3D prints, special glasses to disturb face recognition, etc.

对许多现实世界的应用来说,对抗性的例子是一个明显的安全威胁,例如自动驾驶汽车。现实世界中也存在对抗性的例子,例如二维/三维打印,干扰人脸识别的特殊眼镜、等等。

#### 概念上的差距

#### **Conceptual gaps**

假设神经网络能够学习有意义的表征,捕捉对领域和任务的语义理解。

- 对抗性的例子是这个假设的反例: 样本的语义内容没有改变, 但网络被愚弄了。

自然界是一个对抗者:即使在我们的用例中没有对手,我们也应该对最坏情况下的噪音的鲁棒性进行量化

- Neural networks are hypothesized to learn meaningful representations that capture semantic understanding of the domain and task.
  - Adversarial examples are counterexamples to this hypothesis: the semantic content of the samples is unchanged but the network is fooled.
- Nature as an adversary: Even if there is no adversary in our use-case, we should quantify robustness to worst-case noise

#### **Adversarial Examples**



**Adversarial glasses** fool facial recognition systems into classifying the wearer as someone else, [Sharif 2016]



ML systems classify the adversarially modified STOP sign as a speed limit sign, [Eykholt 2018]

Mahmood Sharif et al. "Accessorize to a crime: Real and stealthy attacks on state-of-the-art face recognition." *SIGSAC* 2016. Kevin Eykholt, et al. "Robust physical-world attacks on deep learning visual classification." *CVPR* 2018.

### **Adversarial Examples – Definition**

#### Classification task:

- Dataset:  $(\mathbf{x}_i, y_i) \sim \mathbb{P}_{\text{data}}, \quad (\mathbf{x}_i, y_i) \in \mathbb{R}^d \times \mathcal{Y}$
- Classifier:  $f: \mathbb{R}^d \to \mathcal{Y}$
- Specify a perturbation set  $\mathcal{P}(\mathbf{x})$ , i.e. a set of perturbations which when applied to  $\mathbf{x}$  do not change its semantic
  - and, thus, should also not change its classification
- We say that a point  $\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})$  is an adversarial example for f at  $(\mathbf{x}, y)$ 
  - if  $f(\mathbf{x}) = y$ , i.e., f correctly classifies  $\mathbf{x}$
  - but  $f(\tilde{\mathbf{x}}) \neq y$ , i.e. fails to correctly classify  $\tilde{\mathbf{x}}$

#### On "small" Perturbations

- Perturbations should not change the semantic content of a sample.
- This is often translated into  $L_p$  constraints with some small  $\epsilon$   $L_p \text{ norm: } \mathcal{P}_{\epsilon,p}(\mathbf{x}) = \big\{ \widetilde{\mathbf{x}} \colon \|\widetilde{\mathbf{x}} \mathbf{x}\|_p < \epsilon \big\}, \text{ typically } p \in \{1,2,\infty\}$
- While mathematically convenient,  $L_p$  norms with small  $\epsilon$  do not contain **all** semantically meaningless perturbations.
- For example, a small rotation does typically not change the meaning of a picture but often corresponds to large changes in  $L_p$  norm.

#### **Attack Variants**

- **Evasion attacks**: given a **fixed**, trained classifier f, the attacker aims to find an adversarial perturbation (at test time)
- Poisoning attacks: the adversary aims to modify the training dataset such that a classifier trained on the dataset has properties desired by the attacker.
  - i.e. the manipulation/corruption is done **before** training
  - → Not covered in this course.
- **Targeted attacks**: the attacker aims to have a certain sample classified as a specific class (e.g. speed limit 100 km/h sign).
- Untargeted attacks: the attacker aims to have a <u>sample misclassified as</u> any class different than the correct one.

逃避攻击: 给定一个固定的、经过训练的分类器f,攻击者的目的是找到一个对抗性的扰动(在测试时间)。

中毒攻击:对抗者的目的是修改训练数据集,使在该数据集上训练的分类器具有攻击者所期望的属性。 - 即操纵/破坏是在训练前完成的 è 本课程不涉及。

有针对性的攻击:攻击者的目的是让某个样本被分类为特定的类别(如限速100公里/小时的标志)。

非目标攻击:攻击者的目的是将一个样本错误地分类为与正确类别不同的任何类别。

### Roadmap

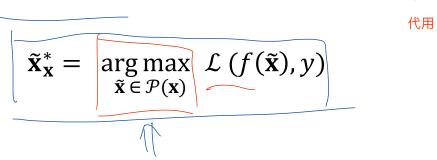
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#### **Adversarial Attacks: Objective Function**

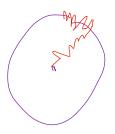
Construction of adversarial examples can be phrased as an optimization problem. For example:

$$\tilde{\mathbf{x}}_{\mathbf{x}}^* = \left| \underset{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})}{\operatorname{arg max}} \ell_{0/1}(f(\tilde{\mathbf{x}}), y) \right|$$

- **Recall:**  $\ell_{0/1}$  is the zero/one loss (0 if correct, 1 if incorrect).
- **However**:  $\ell_{0/1}$  has either zero or undefined gradient.
- Therefore, the **cross-entropy loss**  $\mathcal{L}$  is often used as a surrogate:



## **Projected Gradient Descent**

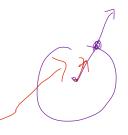


$$\tilde{\mathbf{x}}_{\mathbf{x}}^* = \underset{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})}{\operatorname{arg max}} \mathcal{L}(f(\tilde{\mathbf{x}}), y)$$

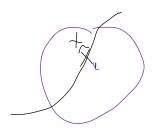
- One common method is **Projected gradient descent** (PGD): after each gradient step on the objective, project onto the valid domain.
- $\mathbf{x}_{t+1} = \Pi(\mathbf{x}_t + \eta_t \nabla_{\mathbf{x}} \mathcal{L}(f(\mathbf{x}_t), y)) \subseteq$
- Like training the model but updating the data instead of the weights.
- Note: since  $f(\tilde{\mathbf{x}})$  is **not convex**, in general we cannot find the global optimum.

#### Fast Gradient-Sign Method (FGSM):

- $\tilde{\mathbf{x}} = \Pi(\mathbf{x} + \eta \cdot \operatorname{sign}(\nabla_{\mathbf{x}} \mathcal{L}(f(\mathbf{x}), y)))$
- When  $\mathcal{P}(\mathbf{x})$  is a ball with radius  $\epsilon$  measured by the  $L_{\infty}$  norm, setting  $\eta = \epsilon$  yields valid perturbations with only a single step and without projection.



## **Alternative Optimization Problem**



An alternative formulation is to optimize:

$$\min_{\tilde{\mathbf{x}}} \ \mathcal{D}(\mathbf{x}, \tilde{\mathbf{x}}) \ \text{ subject to } \ell_{0/1}(f(\tilde{\mathbf{x}}), \mathbf{y}) > 0$$

- Here,  $\mathcal{D}$  is a term that is large when  $\tilde{\mathbf{x}}$  is far from  $\mathbf{x}$  (e.g., an  $L_p$  distance)
- [Carlini and Wagner, 2017] convert this constrained into an unconstrained optimization problem:

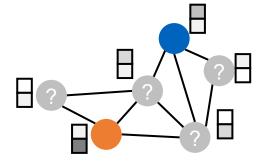
$$\min_{\widetilde{\mathbf{x}}} \ \mathcal{D}(\mathbf{x},\widetilde{\mathbf{x}}) + \lambda \cdot L(\widetilde{\mathbf{x}},\mathbf{y}),$$
 A very effective loss function is

$$L(\tilde{\mathbf{x}}, \mathbf{y}) = \left[ Z(\tilde{\mathbf{x}})_y - \max_{i \neq y} (Z(\tilde{\mathbf{x}})_i) \right]_{+}$$

- y is the original class we want  $\tilde{\mathbf{x}}$  to deviate from
- $[x]_{+} = \max(x, 0)$
- $Z(\tilde{\mathbf{x}})_i = \log f(\tilde{\mathbf{x}})_i$  (log probability of class i)
- The loss L is positive if  $\tilde{\mathbf{x}}$  is classified as y and 0 otherwise.

Carlini, Nicholas, and David Wagner. "Towards evaluating the robustness of neural networks." *IEEE symposium on security and privacy (sp).* 2017.

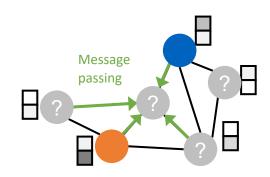
#### **Adversarial Attacks on GNNs**



- Graph Neural Networks are also not robust under adversarial perturbations
- In contrast to e.g. image classifiers, GNNs use **both** the **node's attributes** as well as their **connections** to make a prediction.
  - Therefore, adversarial attacks can happen through both the **node attributes** as well as the **graph structure** we have
  - Structural attacks are indeed quite common in the real world (e.g. adding fake connections in a social network)
- Structure attacks are specifically challenging since they change the flow of messages passed through the GNN

#### **Adversarial Attacks on GNNs**

Example: two-layer GCN in matrix form:



node attributes

$$m{Z} \in \mathbb{R}^{N imes C} = f_{ heta}(m{A}, m{X}) = \operatorname{softmax} ig( m{\widehat{A}} \operatorname{ReLU} ig( m{\widehat{A}} m{X} m{W}^{(1)} + m{b}^{(1)} ig) m{W}^{(2)} + m{b}^{(2)} ig)$$
message passing

- $\theta = \{ W^{(1)}, b^{(1)}, W^{(2)}, b^{(2)} \}$  are learnable model weights.
- Adversarial attack: Modify node attributes X and/or adjacency matrix A in order to maximize classification loss
  - of an individual target node or
  - on the whole dataset/test set (global attack).

## **GNN Adversarial Attacks: Challenges**

- 1. Optimization over **discrete variables** (the graph structure). Perturbations are measured via non-convex  $L_0$  norm.
- 2. Relational dependencies between the nodes: cannot view samples in isolation.
- 3.  $(A', X') \approx (A, X)$ : What is a sensible measure of perturbations that do not change the semantics for (attributed) graphs?

对于(归属)图来说,不改变语义的扰动的合理措施是什么?

4. Transductive setting: unlabeled data is used during training; most realistic scenario is a poisoning attack, where the attacker modifies the training data, which corresponds to a challenging bilevel optimization problem:

传导式设置:在训练过程中使用未标记的数据;最现实的情况是中毒攻击,攻击者修改训练数据,这相当于一个具有挑战性的二层优化问题:

$$\max_{\boldsymbol{A},\boldsymbol{X}} \mathcal{L}_{test}(f_{\boldsymbol{\theta}^*}(\boldsymbol{A},\boldsymbol{X})) \quad s.t. \quad \boldsymbol{\theta}^* = \arg\min_{\boldsymbol{\theta}} \mathcal{L}_{train}(f_{\boldsymbol{\theta}}(\boldsymbol{A},\boldsymbol{X}))$$

$$\text{good wode}$$

#### **GNN Adversarial Attack: Nettack**

- One of the earliest GNN attack algorithms [Zügner, 2018].
- Targets a single node's prediction.

$$Z = f_{\theta}(A, X) = sof max(\widehat{A} RXLU(\widehat{A}XW^{(1)})W^{(2)})$$
 Linearize classifier

$$\log \mathbf{Z}' = \widehat{A}^2 \mathbf{X} \mathbf{W}'$$

Structure perturbations: 
$$\max_{\widehat{A}} \mathcal{L}'(\log \mathbf{Z}'_v)$$
 where  $\log Z'_v = [\widehat{A}^2 \mathbf{C}]_v$  Constants  $\max_{\mathbf{X}} \mathcal{L}'(\log \mathbf{Z}'_v)$  where  $\log Z'_v = [\mathbf{C}_1 \mathbf{X} \mathbf{C}_2]_v$ 

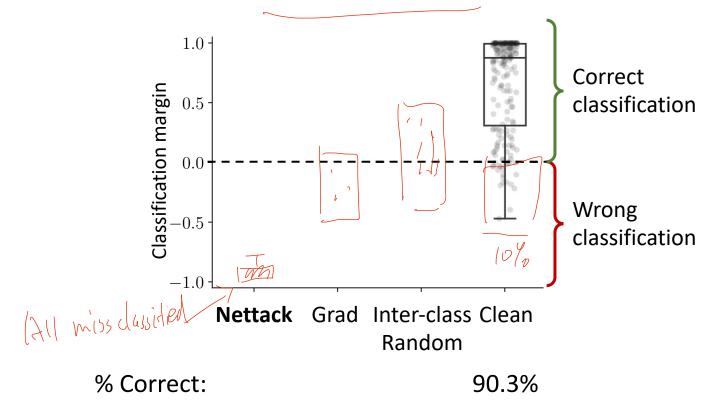
$$\max_{\mathbf{X}} \mathcal{L}'(\log \mathbf{Z}'_v) \text{ where } \log Z'_v = [\mathbf{C}_1 \mathbf{X} \mathbf{C}_2]_v$$

- → **Greedily** pick the **optimal perturbation** at each step.
- → Uses closed-form solutions for the **optimal perturbation** at each step

Daniel Zügner, Amir Akbarnejad, and Stephan Günnemann. Adversarial attacks on neural networks for graph data. KDD 2018.

#### **GNN Adversarial Attack: Nettack results**

- Poisoning attack scenario (model is trained on perturbed data)
- Each point represents one attacked node
- Attack budget per node:  $\Delta(i) = \deg(i) + 2$



#### **Adversarial Attacks for Model Evaluation**

Adversarial attacks can be used to evaluate a model's robustness

- I.e., evaluating the performance of models under worst-case noise

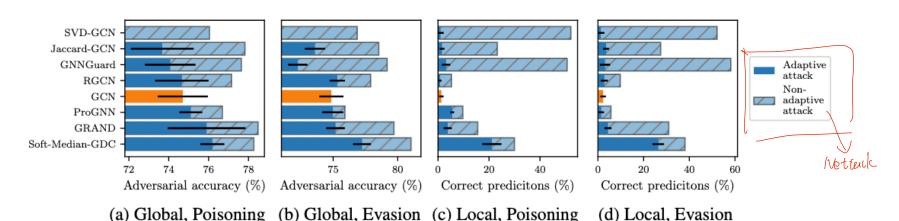
(adversarial accuracy)

「以用对抗性攻击来评估模型的稳健性
- 即评价模型在最坏情况下的噪音(对抗性准确性)的性

But adversarial attacks should be model-specific

但是对抗性攻击应该是针对模型的

- 一个攻击对一个架构的成功并不意味着该攻击对其他架构的成功
- 对抗性攻击必须适应架构的变化(适应性对抗性攻击)。
- Just because an attack is successful against one architecture does not mean the attack is successful for other architectures
- Adversarial attacks must be adapted to architectural changes (adaptive adversarial attacks)



Felix Mujkanovic, Simon Geisler, Stephan Günnemann, Aleksandar Bojchevski. Are Defenses for Graph Neural Networks Robust? NeurIPS 2022

#### Roadmap

- 1. Introduction
- 2. Construction of adversarial examples
- 3. Improving robustness
- 4. Certifiable robustness
  - Exact certification
  - Convex relaxations
  - Lipschitz-continuity
  - Randomized smoothing

#### Introduction

- Most ML models (trained and/or applied in the traditional way) are vulnerable to adversarial examples
- How to defend against adversarial examples?
- Can we prevent them?
- Can we improve the robustness of our models?

#### What does <u>not</u> seem to work

攻击的事后预防 例如,梯度混淆,即随机化或粉碎模型的梯度,以防 止基于梯度的攻击。到目前为止,这些防御措施都被更强的攻击所打 破。

检测对抗性例子 如分布外的转变:由于对抗性例子来自与自然图像不同的分布,我们可以尝试区分这两个分布或进行离群者/异常检测。虽 然这些方法中的一些对 "普通的 "PGD攻击有效,但有针对性的攻击对 这些防御措施非常成功。

修复一个 "坏 "的模型似乎并不是解决办法

**E.g. gradient obfuscation**, i.e. randomizing or shattering gradients of the model in order to prevent gradient-based attacks. So far, these defenses have all been broken by stronger attacks.

Detection of adversarial examples

Post-hoc prevention of attacks

- **E.g. out-of-distribution shift**: since the adversarial examples come from a different distribution than the natural images, we could try to distinguish the two distributions or perform outlier / anomaly detection. While some of these methods work against "vanilla" PGD attacks, targeted attacks are very successful against these defenses.
- Fixing a "bad" model seems not to be the solution

Athalye, Anish, Nicholas Carlini, and David Wagner. "Obfuscated gradients give a false sense of security: Circumventing defenses to adversarial examples." ICML 2018.

Nicholas Carlini and David Wagner. "Adversarial examples are not easily detected: Bypassing ten detection methods." AlSec 2017.

#### **Robust Training**

健壮训练指的是旨在产生对对抗性(和/或其他)扰动具有健壮性的模型的训练程序。

一个共同的主题是优化 "最坏情况 "的损失(也称为稳健损失),即在最坏情况的扰动下实现的损失。

Robust training refers to training procedures aimed at producing models that are robust to adversarial (and/or other) perturbations.

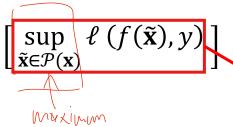
A common theme is to optimize a 'worst-case' loss (also called robust loss), i.e. the loss achieved under the worst-case perturbation.

- Let  $\ell(\hat{y}, y)$  be some loss, e.g. cross-entropy loss
- The (non-robust) training tries to find an f that minimizes the expected loss

$$R = \underset{(\mathbf{x}, y) \in \mathbb{P}_{\text{data}}}{\mathbb{E}} [\ell(f(\mathbf{x}), y)]$$

The robust version of this problem is

$$R_{\text{rob}} = \mathbb{E}_{(\mathbf{x}, y) \in \mathbb{P}_{\text{data}}} \left[ \sup_{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})} \ell(f(\tilde{\mathbf{x}}), y) \right]$$



Loss achieved by the worst-case perturbation in  $\mathcal{P}(\mathbf{x})$ 

### **Robust Training**

**Robust training** refers to training procedures aimed at producing models that are robust to adversarial (and/or other) perturbations.

A **common theme** is to optimize a 'worst-case' loss (also called robust loss), i.e. the loss achieved under the worst-case perturbation.

- Adversarial training is an easy-to-implement robust training procedure that uses adversarial examples as a proxy for the 'worst-case' perturbation.
- In the next chapter, we will cover **robustness certification** techniques. Some of these can also be used for robust training.

对抗性训练是一种易于实施的稳健训练程序,它使用对抗性例子作为 "最坏情况 "扰动的代理。

在下一章,我们将介绍鲁棒性认证技术。其中一些也可以用于鲁棒性训练。

### **Adversarial Training**

**Idea**: perform stochastic gradient descent (SGD) on the **robust loss**  $R_{\rm rob}$ :

$$R_{\text{rob}} = \underset{(\mathbf{x}, y) \in \mathbb{P}_{\text{data}}}{\mathbb{E}} \left[ \sup_{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})} \ell \left( f(\tilde{\mathbf{x}}), y \right) \right]$$

For  $f = f_{\theta}$  being a **neural network** parameterized by weights  $\theta$ , we can write

$$\nabla_{\theta} R_{\text{rob}} = \nabla_{\theta} \left( \underset{(\mathbf{x}, y) \in \mathbb{P}_{\text{data}}}{\mathbb{E}} \left[ \underset{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})}{\sup} \ell \left( f_{\theta}(\tilde{\mathbf{x}}), y \right) \right] \right)$$

$$= \underset{(\mathbf{x}, y) \in \mathbb{P}_{\text{data}}}{\mathbb{E}} \left[ \nabla_{\theta} \left( \underset{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})}{\sup} \ell \left( f_{\theta}(\tilde{\mathbf{x}}), y \right) \right) \right]$$

How to take the gradient of the worst-case loss w.r.t. the weights  $\theta$ ?

### **Adversarial Training: Danskin's Theorem**

- How to obtain  $\nabla_{\theta} L = \nabla_{\theta} \left( \sup_{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})} \ell \left( f_{\theta}(\tilde{\mathbf{x}}), y \right) \right)$ ?
- That is, the **gradient** of the **worst-case loss** w.r.t. the model parameters.
- MaxImm **Danskin's Theorem\***: Let  $\Delta(\theta)$  be the set of  $\tilde{\mathbf{x}}$  for which the supremum is obtained. If  $\Delta(\theta)$  contains only a single element, i.e.  $\Delta(\theta) = \{\tilde{\mathbf{x}}_{\theta}^*\}$ , then the sup is differentiable at  $\theta$  and

$$\nabla_{\theta} \left( \sup_{\tilde{\mathbf{x}} \in \mathcal{P}(\mathbf{x})} \ell \left( f_{\theta}(\tilde{\mathbf{x}}), y \right) \right) = \nabla_{\theta} \ell \left( f_{\theta}(\tilde{\mathbf{x}}_{\theta}^{*}), y \right)$$
The requires some conditions which might the [Madry et al., 2017]

Madry, Aleksander, et al. "Towards Deep Learning Models Resitant to Adversarial Attacks", ICLR 2018.

<sup>\*</sup> Technically, the theorem requires some conditions which might not hold in our case, see [Madry et al., 2017]

#### 利用Danskin定理,我们可以计算出给定相应扰动的最坏情况下的损失梯度。

#### **Adversarial Training: Algorithm**

问题:找到最坏情况下的扰动例子x .是难以实现的;如果我们能有效地找到它,我们就解决了精确验证问题。

这个想法:创建任何对抗性例子作为最坏情况下的扰动的代理, 例如通过快速梯度符号法(FGSM)。

- Using **Danskin's theorem** we can compute the gradient of the worst-case loss given the corresponding perturbation.
- **Problem**: finding the **worst-case** perturbed example  $\tilde{\mathbf{x}}$  is **intractable**; if we could find it efficiently, we would have solved the **exact verification** problem.
- Idea: Create any adversarial example as a proxy of the worst-case perturbation, e.g. via the fast gradient-sign method (FGSM).
- Adversarial training algorithm outline:
  - 1. Sample  $(\mathbf{x}_i, y_i) \sim \mathbb{P}_{\text{data}}$
  - 2. Using an adversarial attack procedure, find an  $\tilde{\mathbf{x}}_i$  with high loss  $\ell(f_{\theta}(\tilde{\mathbf{x}}_i), y_i)$
  - 3. Update weights via gradient descent:  $\theta \leftarrow \theta \eta \nabla_{\theta} \ell(f_{\theta}(\tilde{\mathbf{x}}_{i}), y_{i})$

In step 2, we must trade off the strength of the attack with its computational cost.

#### **Adversarial Training: Summary**

#### Pro:

- It empirically increases robustness of the resulting models.
- It is easy to implement.

#### Con:

- If we want to use a powerful attack on the inner optimization, the slowdown is about 10x compared to standard training.
- The resulting models typically have lower accuracy on clean data.
- We don't get any theoretical guarantees of the model's robustness

#### GNN的稳健性是一个非常活跃的研究领域 - 到目前为止,还没有针对结构攻击的防御措施能够持续改善结

- 到目前为止,还没有针对结构攻击的防御措施能够持续改善结 果;标准方法,如对抗性训练,似乎并不奏效

#### **Improving Robustness for GNNs**

#### 自发式防御措施

例如,通过截断的奇异值分解进行相邻的低秩近似[Entezari

2020];通过属性相似性过滤恶意边缘[Wu 2019]

- 然而: CNN的等效/类似防御措施已被证明对最坏情况下的扰动是不健全的(见之前: 关于自适应攻击的幻灯片)。

#### GNN robustness is a highly active research area

- To date there exists **no defense** against **structure attacks** that consistently improves results; standard methods such as **adversarial training** do not seem to work well

#### Heuristic defenses

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- 以对抗性训练的形式,例如,通过投影梯度下降[Xu 2019]。
- 或者与认证技术一起提出(即将到来的主题)。
- E.g. adjacency low-rank approximation via truncated Singular Value Decomposition [Entezari 2020]; filtering of malicious edges via attribute similarity [Wu 2019]
- However: equivalent/similar defenses for CNNs have been proven to be non-robust against worst-case perturbations (see before: slide on adaptive attacks)

#### **Robust Training**

- In form of Adversarial Training, e.g., via Projected Gradient Descent [Xu 2019]
  - Or proposed together with a certification technique (upcoming topic)

Negin Entezari, Saba A. Al-Sayouri, Amirali Darvishzadeh, and Evangelos E. Papalexakis. All you need is Low (rank): Defending against adversarial attacks on graphs. WSDM 2020.

Huijun Wu, Chen Wang, Yuriy Tyshetskiy, Andrew Docherty, Kai Lu, and Liming Zhu.

Adversarial examples for graph data: Deep insights into attack and defense. IJCAI 2019.

Kaidi Xu, Hongge Chen, Sijia Liu, Pin Yu Chen, Tsui Wei Weng, Mingyi Hong, and Xue Lin.

Topology attack and defense for graph neural networks: An optimization perspective. IJCAI 2019.

#### **Questions – Robustness**

1. Given an arbitrary binary classifier f for an input domain  $\mathbb{R}^d$  and the perturbation set  $\mathcal{P}_{\epsilon,p}(\mathbf{x})$  as defined before. Is it possible that every  $\mathbf{x} \in \mathbb{R}^d$  is "robust", i.e. no adversarial example exists?

- 2. Will the fast gradient-sign method (FGSM) always find an adversarial example (assuming there exist some in the set of perturbations  $\mathcal{P}_{\epsilon,\infty}(\mathbf{x})$ )?
- 3. Is a projected-gradient-descent (PGD) attack on a GNN via the graph structure a good idea? Why or why not?

#### **Recommended Reading**

 Lecture 09: Introduction to adversarial examples and Lecture 10: Empirical defenses for adversarial examples of Jerry Li's course on Robustness in Machine Learning (CSE 599-M), <a href="https://jerryzli.github.io/robust-ml-fall19.html">https://jerryzli.github.io/robust-ml-fall19.html</a>