p(vaccinated | infected)

vaccinated & infected

total infected in the population

mathematically correct analysis matches the question