mathematically correct

analysis matches the question