

## AMS317 HW5 #2

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2a)

```
### ??faraway::seatpos
data = data(seatpos, package = "faraway")

fit1 <- lm(hipcenter ~ Ht, data=seatpos)

summary(fit1)

##
## Call:
## lm(formula = hipcenter ~ Ht, data = seatpos)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -99.956 -27.850   5.656  20.883  72.066
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  556.2553    90.6704   6.135 4.59e-07 ***
## Ht           -4.2650     0.5351  -7.970 1.83e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 36.37 on 36 degrees of freedom
## Multiple R-squared:  0.6383, Adjusted R-squared:  0.6282
## F-statistic: 63.53 on 1 and 36 DF,  p-value: 1.831e-09
```

Yes, it is significant at  $\alpha = 0.01$  (Signif. codes: 0 '\*\*\*')

2b)

```
fit2 <- lm(hipcenter ~ Weight, data=seatpos)
summary(fit2)

##
## Call:
## lm(formula = hipcenter ~ Weight, data = seatpos)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -109.446 -23.179 -2.292 20.171 130.567
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.2422 34.0563 0.036 0.971
## Weight -1.0674 0.2134 -5.002 1.49e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 46.45 on 36 degrees of freedom
## Multiple R-squared: 0.41, Adjusted R-squared: 0.3936
## F-statistic: 25.02 on 1 and 36 DF, p-value: 1.493e-05
```

Yes, it is significant at  $\alpha = 0.01$  (Signif. codes: 0 '\*\*\*')

2c)

```
fit12 <- lm(hipcenter ~ Ht + Weight, data=seatpos)
summary(fit12)
```

```
##
## Call:
## lm(formula = hipcenter ~ Ht + Weight, data = seatpos)
##
## Residuals:
## Min 1Q Median 3Q Max
## -99.061 -27.970 4.611 21.910 70.381
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 589.9006 127.4824 4.627 4.92e-05 ***
## Ht -4.5697 0.9672 -4.725 3.68e-05 ***
## Weight 0.1148 0.3020 0.380 0.706
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 36.81 on 35 degrees of freedom
## Multiple R-squared: 0.6398, Adjusted R-squared: 0.6192
## F-statistic: 31.08 on 2 and 35 DF, p-value: 1.738e-08
```

It is no longer significant.

2d)

```
cor(seatpos$Ht, seatpos$Weight)
```

```
## [1] 0.8285257
```

Ht is considered to be the “impactful” variable instead since weight and height might be correlated. Height is “credited” as the more impactful variable as a result. Since they are highly correlated, weight does not appear to explain as much of the data.

2e)  $H_0: \beta_{Ht} = 0$   $H_1: \beta_{Ht} \neq 0$

nested model:  $Y \sim x\_Ht$  larger model:  $Y \sim x\_Ht + x\_Weight$

2f)  $H\_0$ :  $\beta\_Ht = 0$  and  $\beta\_Weight = 0$   $H\_1$ : at least one of  $\beta\_Ht$  or  $\beta\_Weight \neq 0$

nested model:  $Y \sim 1$  larger model:  $Y \sim 1 + x\_Ht + x\_Weight$

2g)

```
anova(fit2,fit12)
```

```
## Analysis of Variance Table
##
## Model 1: hipcenter ~ Weight
## Model 2: hipcenter ~ Ht + Weight
##   Res.Df    RSS Df Sum of Sq    F    Pr(>F)
## 1      36 77664
## 2      35 47420   1    30244 22.322 3.675e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

i)  $H\_0$ :  $\beta\_Ht = 0$   $H\_1$ :  $\beta\_Ht \neq 0$

ii) The F statistic for `anova(fit2,fit12)` is the square of that t test and have the same p value since they have the same nested and larger models.

iii) Even though they are testing the same thing, the `anova(fit1,fit2)` has models:  $h\_0$ :  $Y \sim 1 + \beta\_weight$   
 $h\_1$ :  $Y \sim 1 + \beta\_weight + \beta\_Ht$

and `fit1` had models:  $h\_0$ :  $Y \sim 1$   $h\_1$ :  $Y \sim 1 + \beta\_Ht$

The models are not the same.