

## **Worst-case Delay Bounds in Time-Sensitive Networks with Packet Replication and Elimination**

Published in *IEEE/ACM Transactions on Networking*

**Ludovic Thomas, Ahlem Mifdaoui, Jean-Yves Le Boudec**

WoNeCa-6  
September 8th, 2022

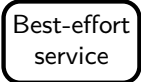
# Time-Sensitive Networks

**IEEE time-sensitive networking (TSN):** the Ethernet for safety-critical applications (layer 2)

## Time-Sensitive Networks

**IEEE time-sensitive networking (TSN)**: the Ethernet for safety-critical applications (layer 2)

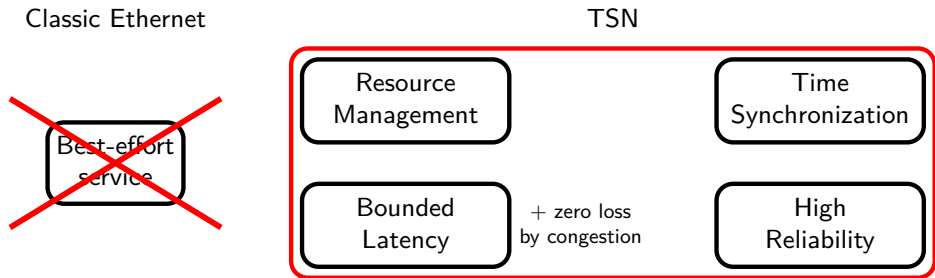
Classic Ethernet



Best-effort  
service

## Time-Sensitive Networks

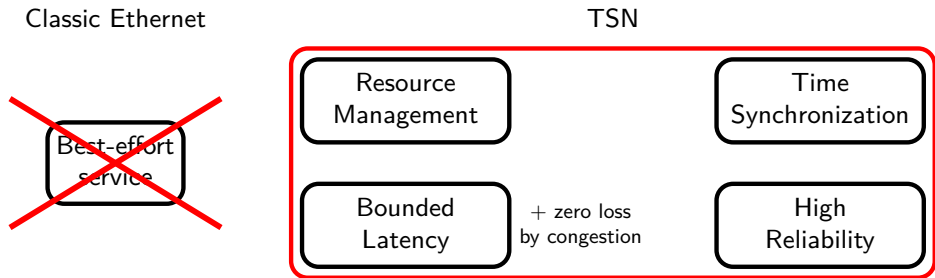
**IEEE time-sensitive networking (TSN):** the Ethernet for safety-critical applications (layer 2)



The four “key components” of TSN [Farkas 2018]

## Time-Sensitive Networks

**IEEE time-sensitive networking (TSN):** the Ethernet for safety-critical applications (layer 2)

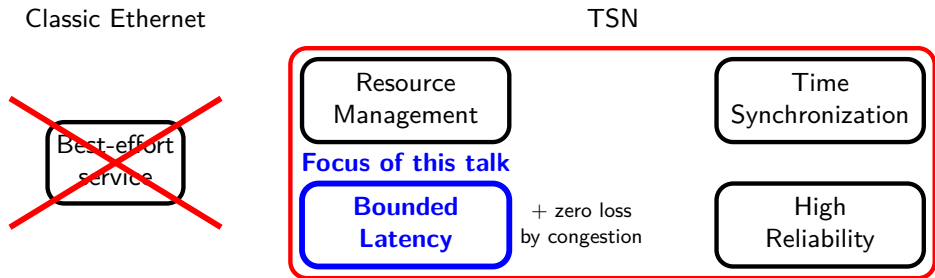


The four “key components” of TSN [Farkas 2018]

Similar ideas in **IETF deterministic networking (DetNet)** for IP and MPLS networks (layer 3) [RFC 8655]

## Time-Sensitive Networks

**IEEE time-sensitive networking (TSN):** the Ethernet for safety-critical applications (layer 2)



The four “key components” of TSN [Farkas 2018]

Similar ideas in **IETF deterministic networking (DetNet)** for IP and MPLS networks (layer 3) [RFC 8655]

## Class-Based Queuing Mechanisms improve the Classic Ethernet Output Port

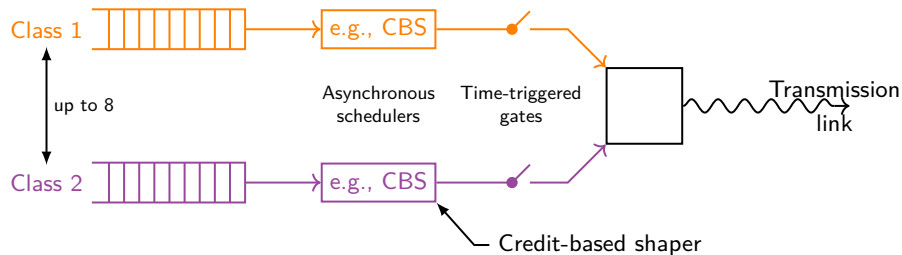


## Class-Based Queuing Mechanisms improve the Classic Ethernet Output Port

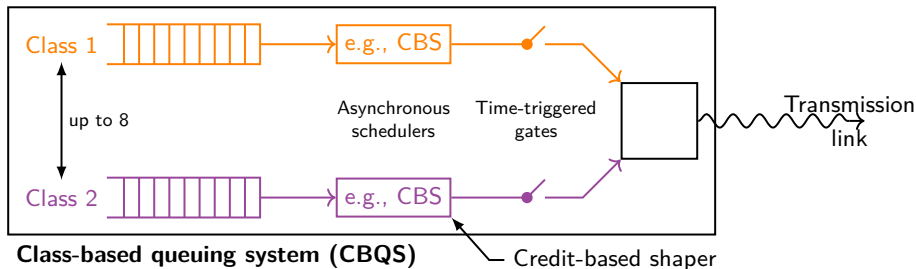




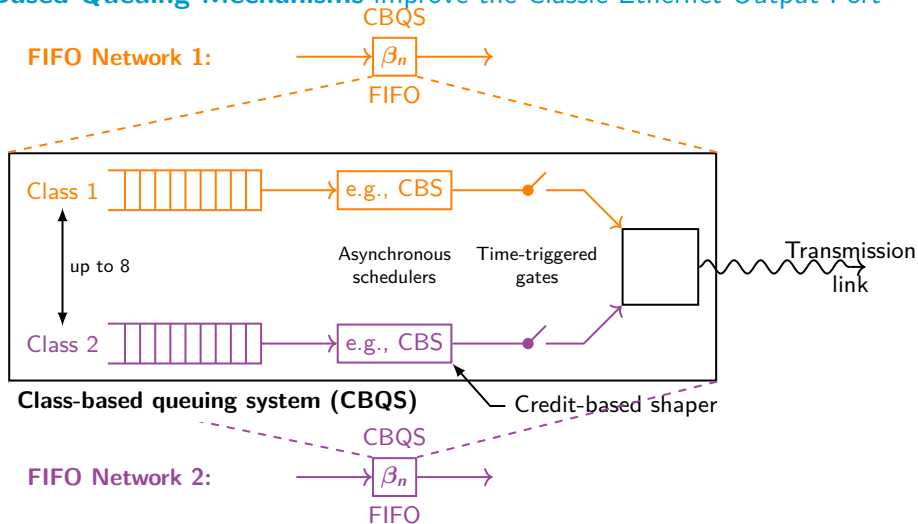
## Class-Based Queuing Mechanisms improve the Classic Ethernet Output Port



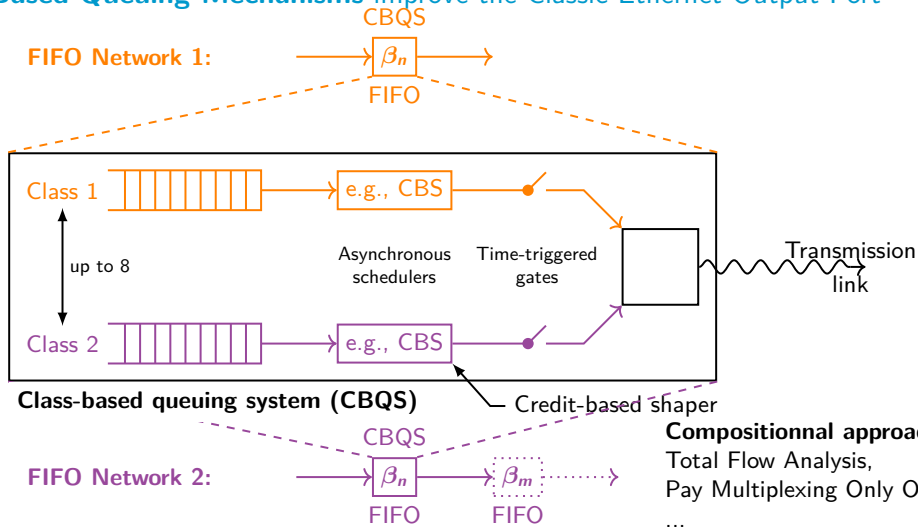
## Class-Based Queuing Mechanisms improve the Classic Ethernet Output Port



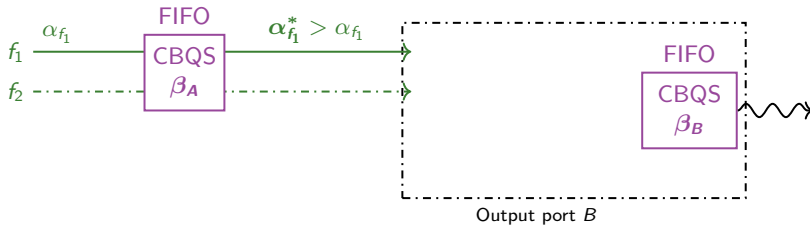
## Class-Based Queuing Mechanisms improve the Classic Ethernet Output Port



## Class-Based Queuing Mechanisms improve the Classic Ethernet Output Port

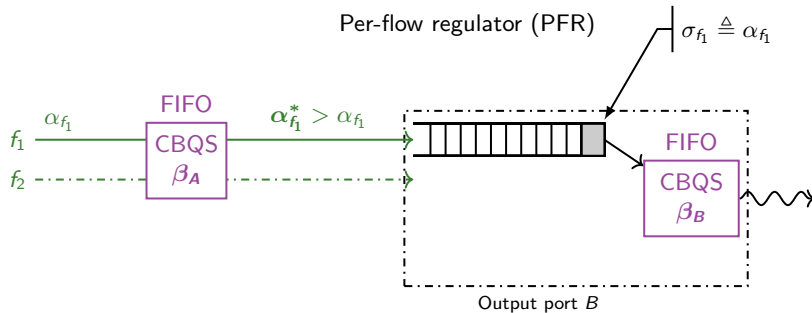


## Within One Class, **Traffic Regulators** Allow for a Per-Flow Control



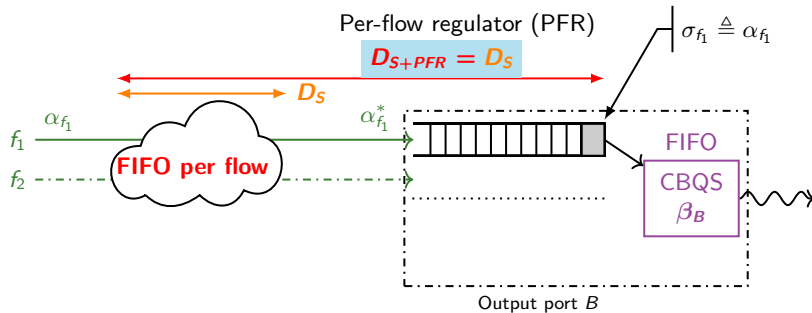
CBQS: Class-based queuing system (FIFO for the class aggregate)

## Within One Class, Traffic Regulators Allow for a Per-Flow Control



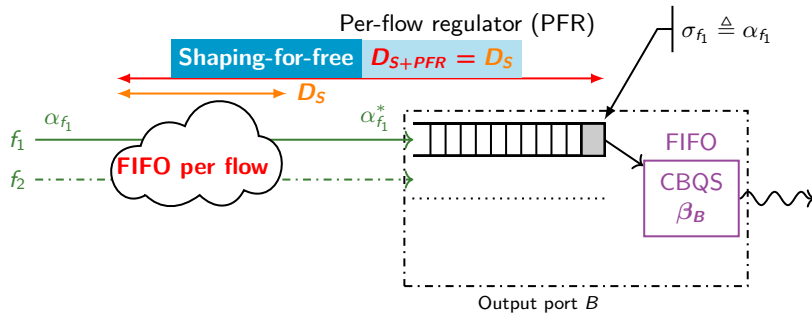
CBQS: Class-based queuing system (FIFO for the class aggregate)

## Within One Class, Traffic Regulators Allow for a Per-Flow Control



CBQS: Class-based queuing system (FIFO for the class aggregate)

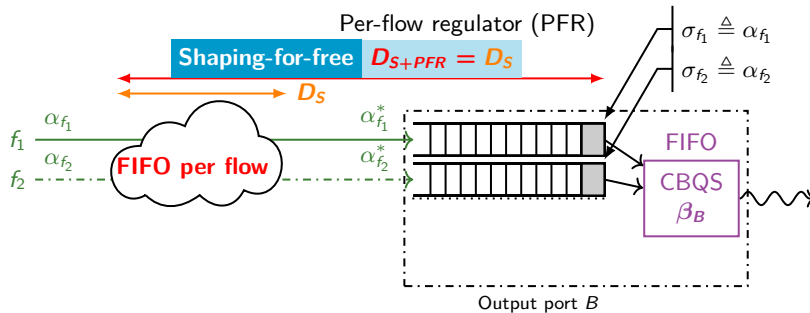
## Within One Class, Traffic Regulators Allow for a Per-Flow Control



CBQS: Class-based queuing system (FIFO for the class aggregate)

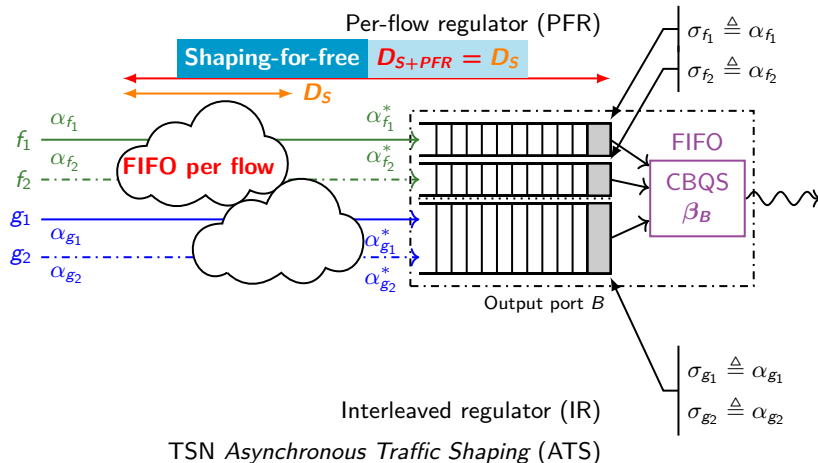


## Within One Class, Traffic Regulators Allow for a Per-Flow Control



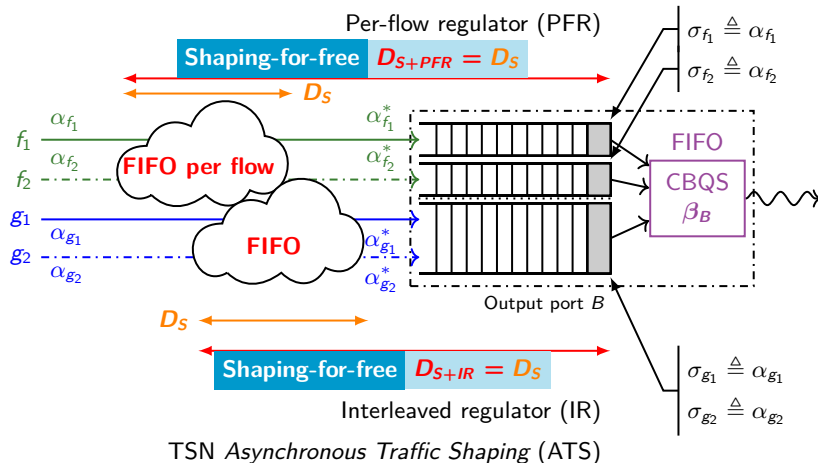
CBQS: Class-based queuing system (FIFO for the class aggregate)

## Within One Class, Traffic Regulators Allow for a Per-Flow Control



CBQS: Class-based queuing system (FIFO for the class aggregate)

## Within One Class, Traffic Regulators Allow for a Per-Flow Control



CBQS: Class-based queuing system (FIFO for the class aggregate)

Focus of  
this talk

Bounded  
Latency

**Class-based queuing mechanisms:**

- Asynchronous schedulers
- Time-triggered gates

**Traffic regulators (*shapers*):**

- Asynchronous Traffic Shaping (ATS)

Focus of  
this talk

Bounded  
Latency

Network Calculus

**Class-based queuing mechanisms:**

- Asynchronous schedulers
- Time-triggered gates

**Traffic regulators (*shapers*):**

- Asynchronous Traffic Shaping (ATS)

Focus of  
this talk

Bounded  
Latency

Network Calculus

**Class-based queuing mechanisms:**

- Asynchronous schedulers
- Time-triggered gates

**Traffic regulators (*shapers*):**

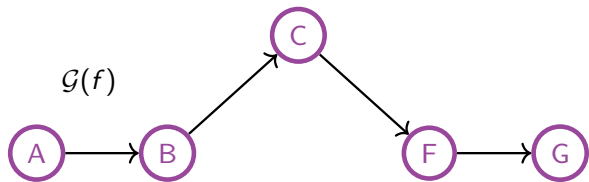
- Asynchronous Traffic Shaping (ATS)

High  
Reliability

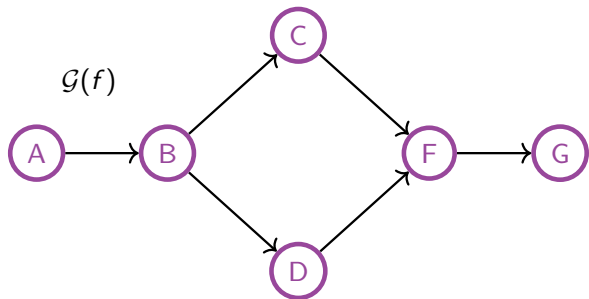
- Frame Replication and Elimination for Redundancy (FRER) [IEEE 802.1CB]
- Packet Replication, Elimination and Ordering Functions (**PREOF**) [RFC 8655]

Redundancy mechanisms

## Redundancy Relies on **Packet Replication (PRF)** and **Packet Elimination (PEF)** Functions

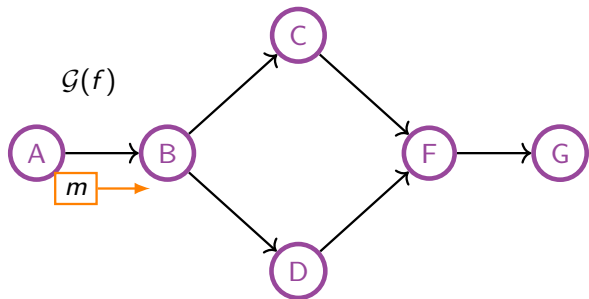


## Redundancy Relies on **Packet Replication (PRF)** and **Packet Elimination (PEF)** Functions

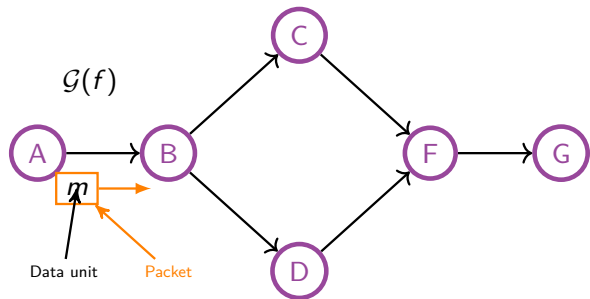




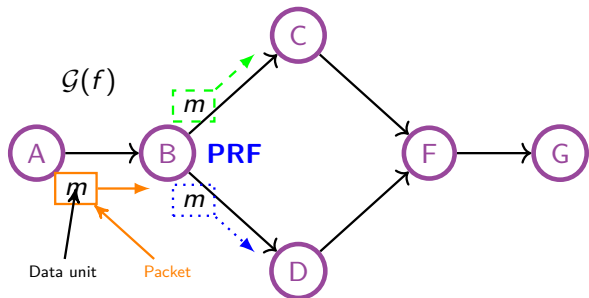
## Redundancy Relies on **Packet Replication (PRF)** and **Packet Elimination (PEF)** Functions



## Redundancy Relies on **Packet Replication (PRF)** and **Packet Elimination (PEF)** Functions

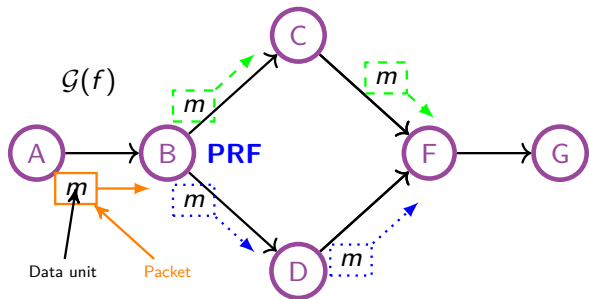


## Redundancy Relies on Packet Replication (PRF) and Packet Elimination (PEF) Functions



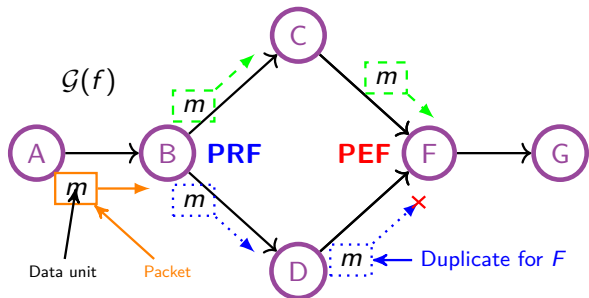
**PRF** Packet Replication Function (DetNet)  
Stream splitting function (TSN)

## Redundancy Relies on Packet Replication (PRF) and Packet Elimination (PEF) Functions



**PRF** Packet Replication Function (DetNet)  
Stream splitting function (TSN)

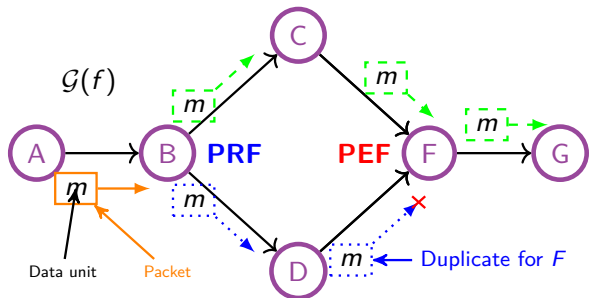
## Redundancy Relies on Packet Replication (PRF) and Packet Elimination (PEF) Functions



**PRF** Packet Replication Function (DetNet)  
Stream splitting function (TSN)

**PEF** Packet Elimination Function (DetNet)  
Sequence recovery function (TSN)

## Redundancy Relies on Packet Replication (PRF) and Packet Elimination (PEF) Functions



**PRF** Packet Replication Function (DetNet)  
Stream splitting function (TSN)

**PEF** Packet Elimination Function (DetNet)  
Sequence recovery function (TSN)

## Our Main Concern

Focus of  
this talk

Bounded  
Latency

Network Calculus

**Class-based queuing:**

- Asynchronous schedulers
- Time-Triggered Gates

**Traffic regulators (*shapers*):**

- Asynchronous Traffic Shaping (ATS)

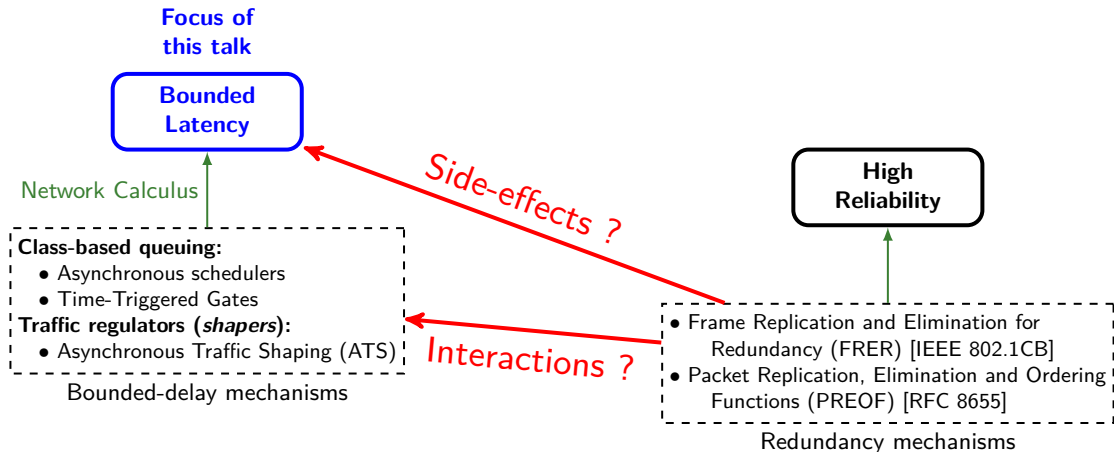
Bounded-delay mechanisms

High  
Reliability

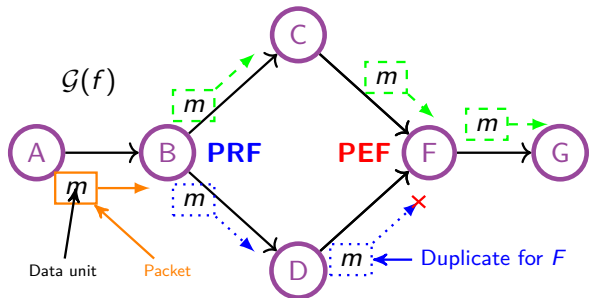
- Frame Replication and Elimination for Redundancy (FRER) [IEEE 802.1CB]
- Packet Replication, Elimination and Ordering Functions (PREOF) [RFC 8655]

Redundancy mechanisms

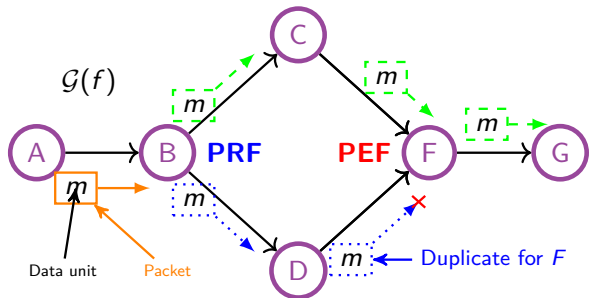
## Our Main Concern





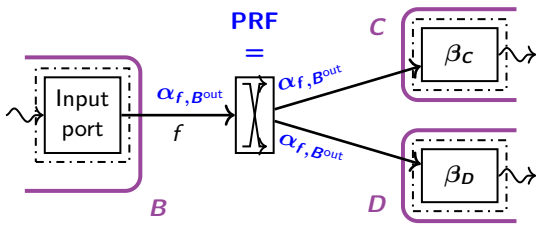


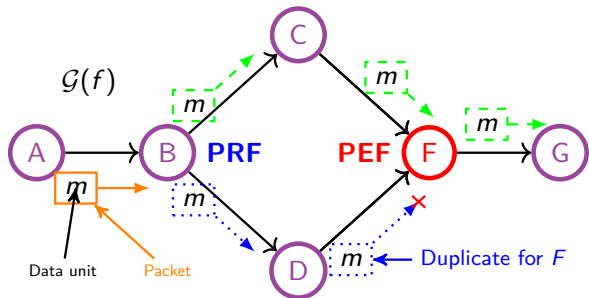
**PRF** Packet Replication Function  
**PEF** Packet Elimination Function



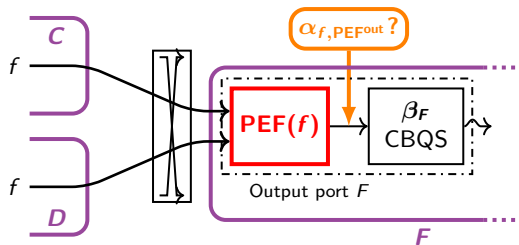
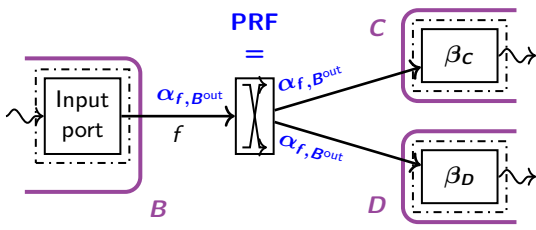
PRF Packet Replication Function

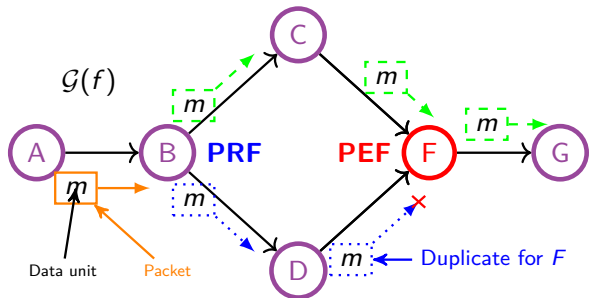
PEF Packet Elimination Function





**PRF** Packet Replication Function  
**PEF** Packet Elimination Function



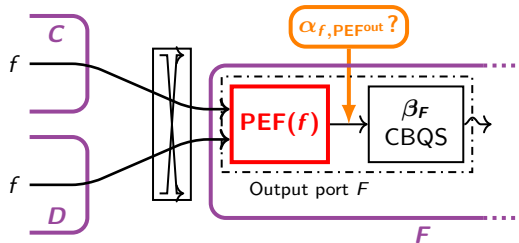
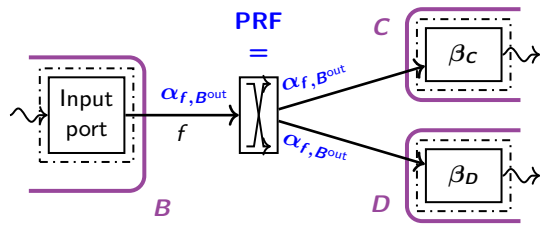


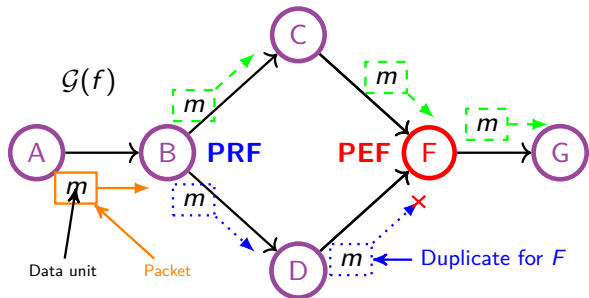
**PRF** Packet Replication Function

**PEF** Packet Elimination Function

### Assumption

The **PEF** is correctly configured: it drops all duplicates and only them



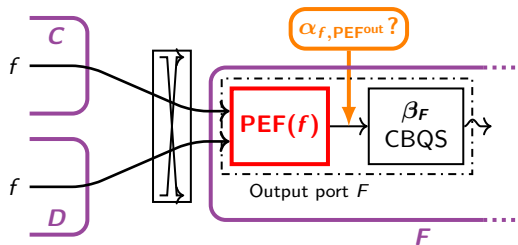
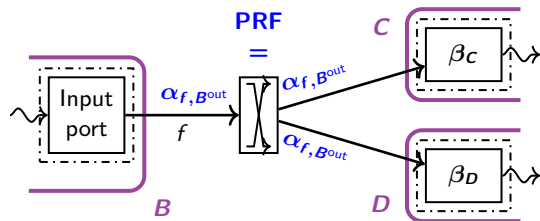


**PRF** Packet Replication Function

**PEF** Packet Elimination Function

### Assumption

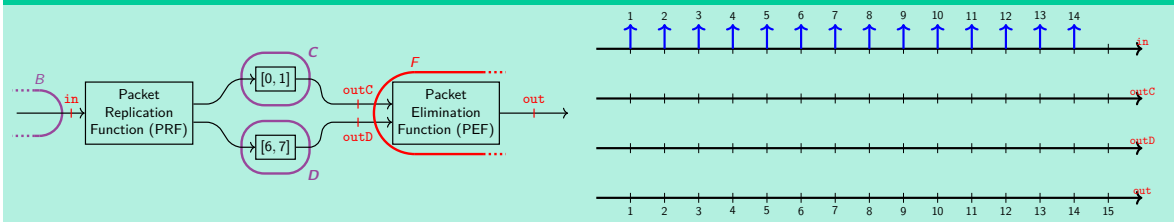
The **PEF** is correctly configured: it drops all duplicates and only them [Maile, *et al.* 2022]



– [Maile, *et al.* 2022] Lisa Maile, Dominik Voitlein, Kai-Steffen Hielscher, and Reinhard German [May 2022]. “Ensuring Reliable and Predictable Behavior of IEEE 802.1CB Frame Replication and Elimination”. In: *ICC 2022 - IEEE International Conference on Communications*. DOI: 10.1109/ICC45855.2022.9838905

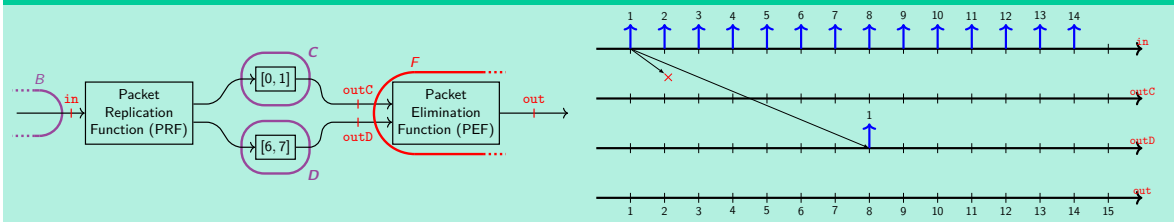
## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



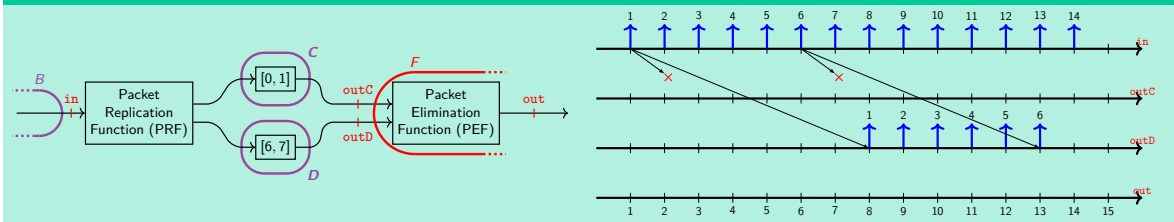
## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

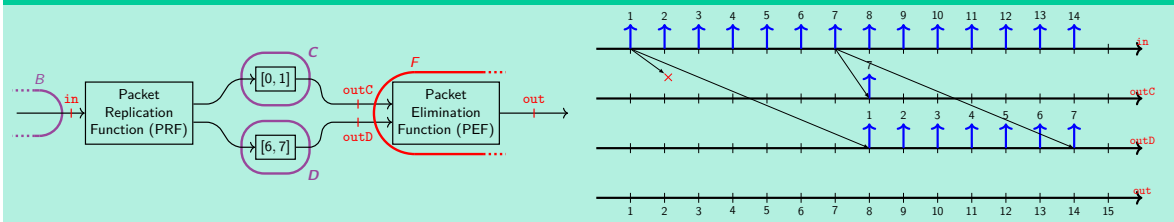
### A Possible Trajectory on a Toy Example





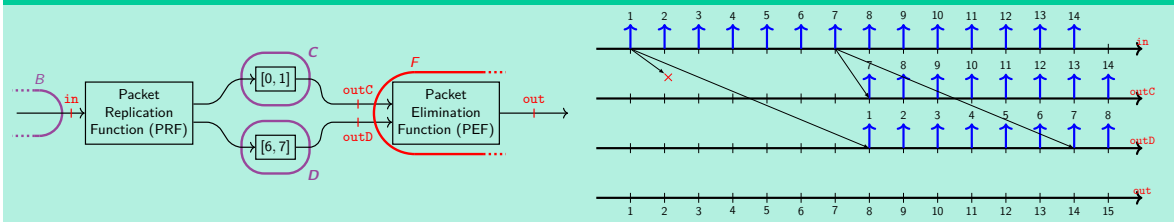
## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



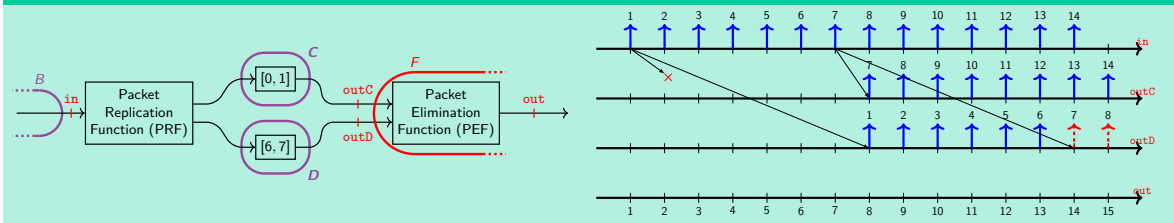
## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



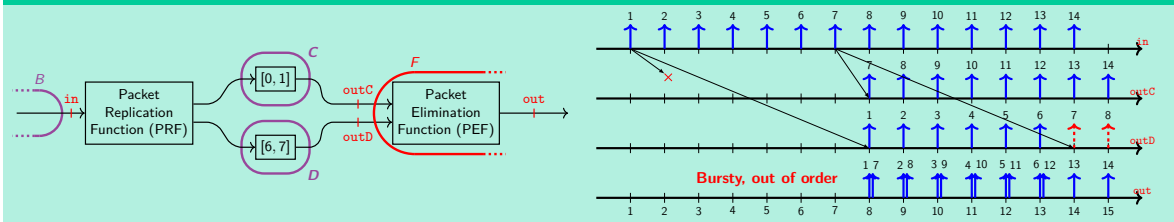
## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



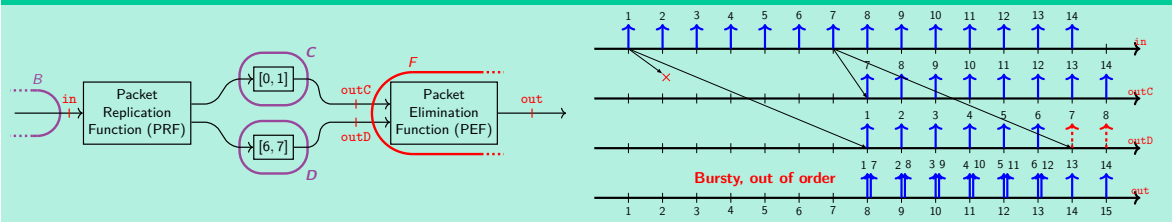
## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

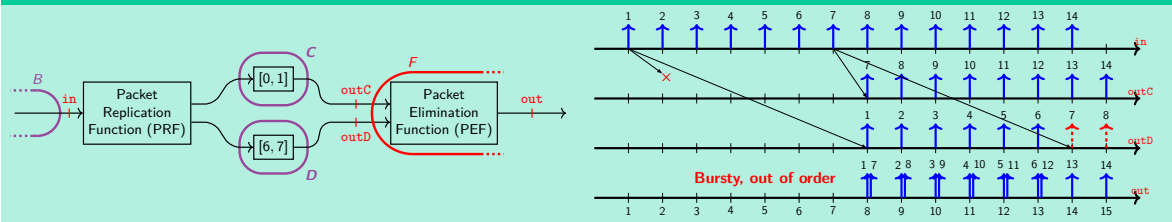
### A Possible Trajectory on a Toy Example



- Output of PEF bursty, mis-ordered  $\Rightarrow$  Can we bound the burstiness and mis-ordering at the PEF's output?

## What is the **Traffic at the Output of the PEF** ? (Packet Elimination Function)

### A Possible Trajectory on a Toy Example



- Output of PEF bursty, mis-ordered  $\Rightarrow$  Can we bound the burstiness and mis-ordering at the PEF's output?
- Output bursty  $\rightarrow$  leads to high delay in downstream  $\Rightarrow$  Place a traffic regulator after the PEF ?

## An **Arrival Curve** at The Output of The PEF (Packet Elimination Function)

### **Theorem: PEF Output Arrival Curve**

## An Arrival Curve at The Output of The PEF (Packet Elimination Function)

### Theorem: PEF Output Arrival Curve

- $\alpha_{f, PEF^{in}}$  is an arrival curve at  $PEF^{out}$

Intuitive approach



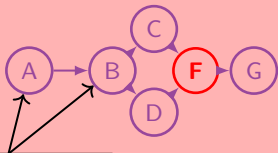


## An Arrival Curve at The Output of The PEF (Packet Elimination Function)

### Theorem: PEF Output Arrival Curve

- $\alpha_{f, PEF^{in}}$  is an arrival curve at  $PEF^{out}$

Intuitive approach



- $\forall a$ , diamond ancestor,

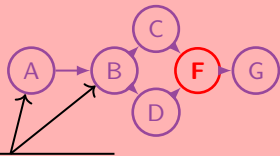


## An Arrival Curve at The Output of The PEF (Packet Elimination Function)

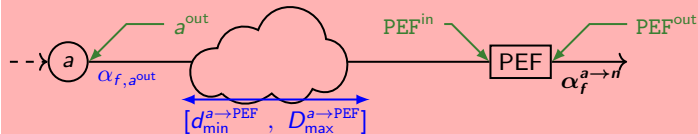
### Theorem: PEF Output Arrival Curve

- $\alpha_{f, \text{PEF}^{\text{in}}}$  is an arrival curve at  $\text{PEF}^{\text{out}}$

Intuitive approach



- $\forall a$ , diamond ancestor,

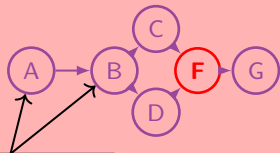


## An Arrival Curve at The Output of The PEF (Packet Elimination Function)

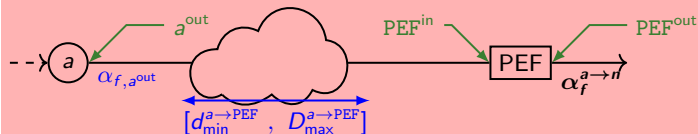
### Theorem: PEF Output Arrival Curve

- $\alpha_{f,PEF^{in}}$  is an arrival curve at  $PEF^{out}$

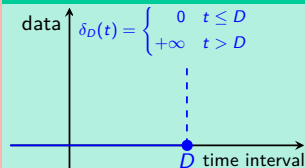
Intuitive approach



- $\forall a$ , diamond ancestor,  $\alpha_f^{a \rightarrow PEF} \triangleq \left( \alpha_{f,a^{out}} \otimes \delta_{(D_{\max}^{a \rightarrow PEF} - d_{\min}^{a \rightarrow PEF})} \right)$  is an arrival curve at  $PEF^{out}$



### Bounded-Delay $\delta_D$

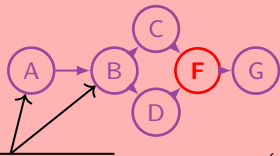


## An Arrival Curve at The Output of The PEF (Packet Elimination Function)

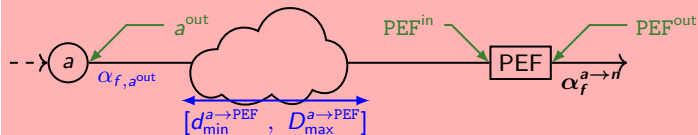
### Theorem: PEF Output Arrival Curve

- $\alpha_{f, \text{PEF}^{\text{in}}}$  is an arrival curve at  $\text{PEF}^{\text{out}}$

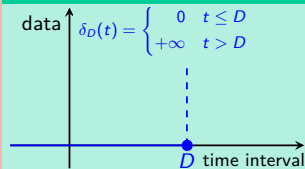
Intuitive approach



- $\forall a, \text{diamond ancestor}, \alpha_f^{a \rightarrow \text{PEF}} \triangleq \left( \alpha_{f, a^{\text{out}}} \otimes \delta_{(D_{\max}^{a \rightarrow \text{PEF}} - d_{\min}^{a \rightarrow \text{PEF}})} \right)$  is an arrival curve at  $\text{PEF}^{\text{out}}$



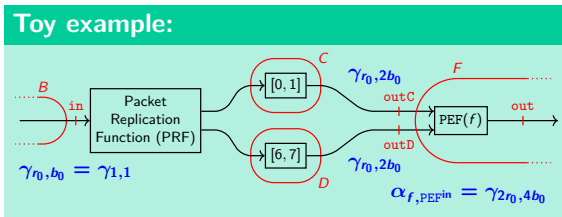
### Bounded-Delay $\delta_D$



$\Rightarrow$  **Tight Model:**

The min-plus convolution of all above arrival curves is an arrival curve at  $\text{PEF}^{\text{out}}$ .

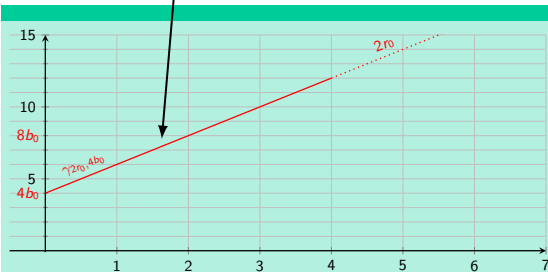
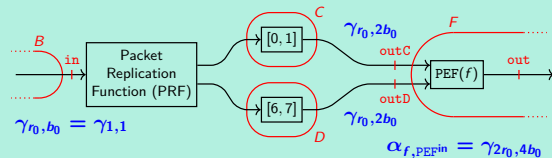
## Applying our Result to the Toy Example Provides a **Tight Output Arrival Curve**



## Applying our Result to the Toy Example Provides a **Tight Output Arrival Curve**

$$\blacksquare \alpha_{f, \text{PEF}^{\text{in}}} = \gamma_{2r_0, 4b_0}$$

Toy example:



## Applying our Result to the Toy Example Provides a Tight Output Arrival Curve

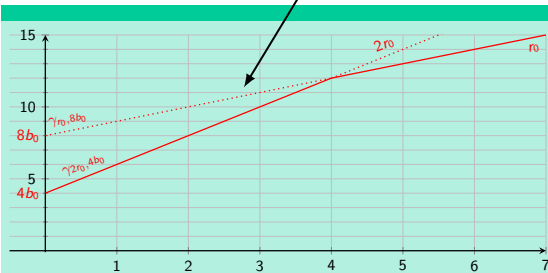
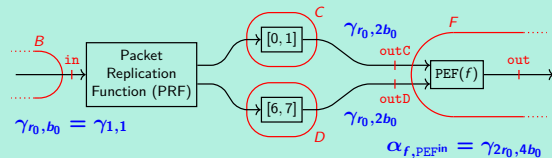
■  $\alpha_{f, \text{PEF}^{\text{in}}} = \gamma_{2r_0, 4b_0}$

■  $B$  is diamond ancestor

$$\alpha_f^{B \rightarrow \text{PEF}} = \left( \alpha_{f, a^{\text{out}}} \oslash \delta \left( D_{\max}^{a \rightarrow \text{PEF}} - d_{\min}^{a \rightarrow \text{PEF}} \right) \right)$$

$$= \gamma_{r_0, b_0} \oslash \delta_7 = \gamma_{r_0, 8b_0}$$

Toy example:







## Applying our Result to the Toy Example Provides a Tight Output Arrival Curve

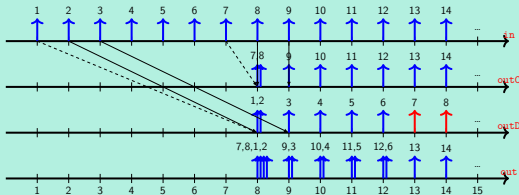
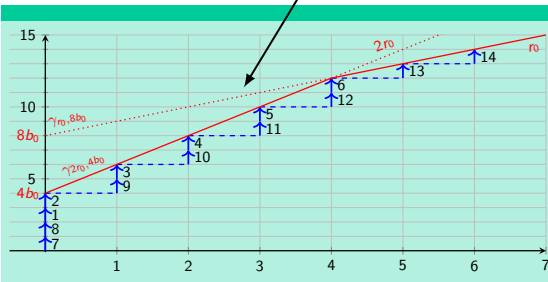
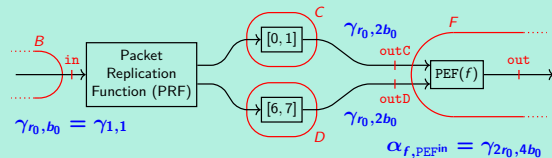
■  $\alpha_{f, \text{PEF}^{\text{in}}} = \gamma_{2r_0, 4b_0}$

■  $B$  is diamond ancestor

$$\alpha_f^{B \rightarrow \text{PEF}} = \left( \alpha_{f, a^{\text{out}}} \oslash \delta_{(D_{\max}^{a \rightarrow \text{PEF}} - d_{\min}^{a \rightarrow \text{PEF}})} \right)$$

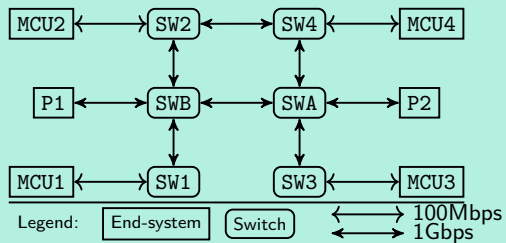
$$= \gamma_{r_0, b_0} \oslash \delta_7 = \gamma_{r_0, 8b_0}$$

### Toy example:

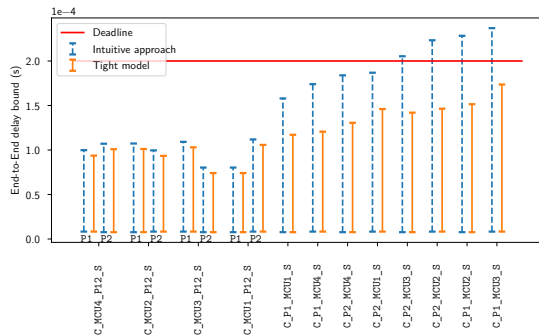


**Tight Model**, better bounds than the **Intuitive approach**

## An industrial use-case: The Volvo Core TSN Network



48 flows, 40 are redounded.



## Question 1

Output of PEF bursty, mis-ordered  $\Rightarrow$  Can we bound the burstiness and mis-ordering at the PEF's output?

## Question 1

Output of PEF bursty, mis-ordered  $\Rightarrow$  Can we bound the burstiness and mis-ordering at the PEF's output?

- Yes! Using novel network-calculus results.
- Mis-ordering: Bound based on the metrics from [Mohammadpour, Le Boudec 2021]

---

– [Mohammadpour, Le Boudec 2021] [Ehsan Mohammadpour and Jean-Yves Le Boudec \[2021\]](#). “On Packet Reordering in Time-Sensitive Networks”. In: *IEEE/ACM Transactions on Networking*. DOI: [10.1109/TNET.2021.3129590](#)

## Question 1

Output of PEF bursty, mis-ordered  $\Rightarrow$  Can we bound the burstiness and mis-ordering at the PEF's output?

- Yes! Using novel network-calculus results.
- Mis-ordering: Bound based on the metrics from [Mohammadpour, Le Boudec 2021]

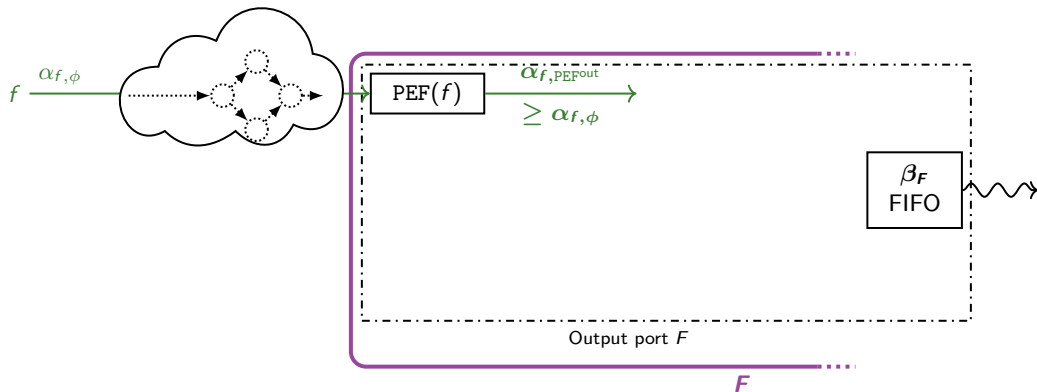
## Question 2

Output bursty  $\rightarrow$  leads to high delay in downstream  $\Rightarrow$  Place a traffic regulator after the PEF ?

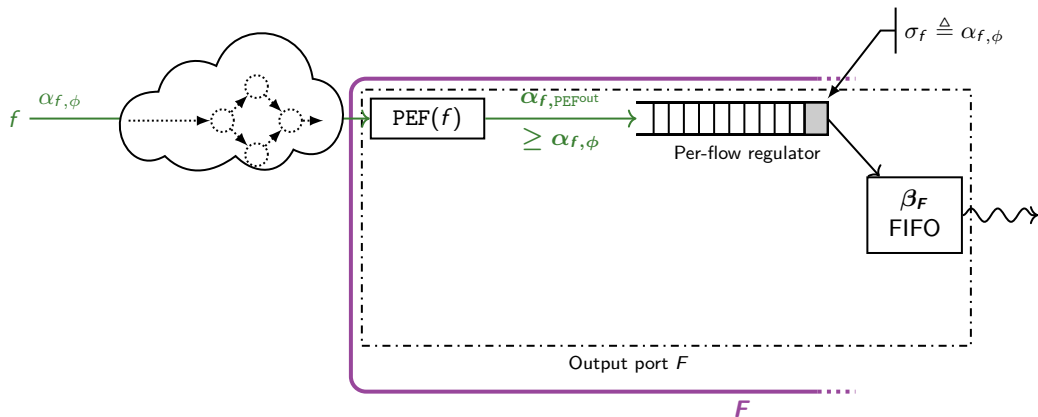
---

– [Mohammadpour, Le Boudec 2021] [Ehsan Mohammadpour and Jean-Yves Le Boudec \[2021\]](#). “On Packet Reordering in Time-Sensitive Networks”. In: *IEEE/ACM Transactions on Networking*. DOI: [10.1109/TNET.2021.3129590](#)

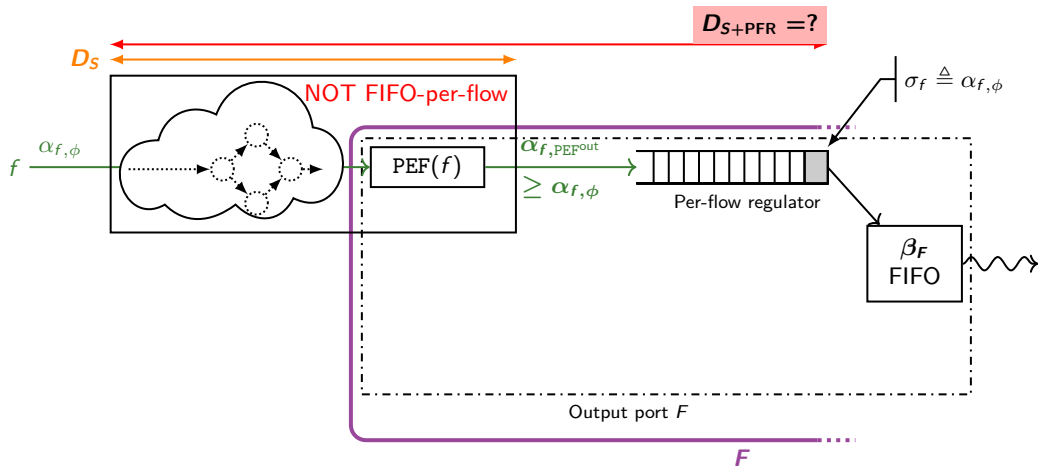
## Combination of Traffic Regulators with Redundancy Functions: **FIFO** assumption is lost!



## Combination of Traffic Regulators with Redundancy Functions: **FIFO** assumption is lost!

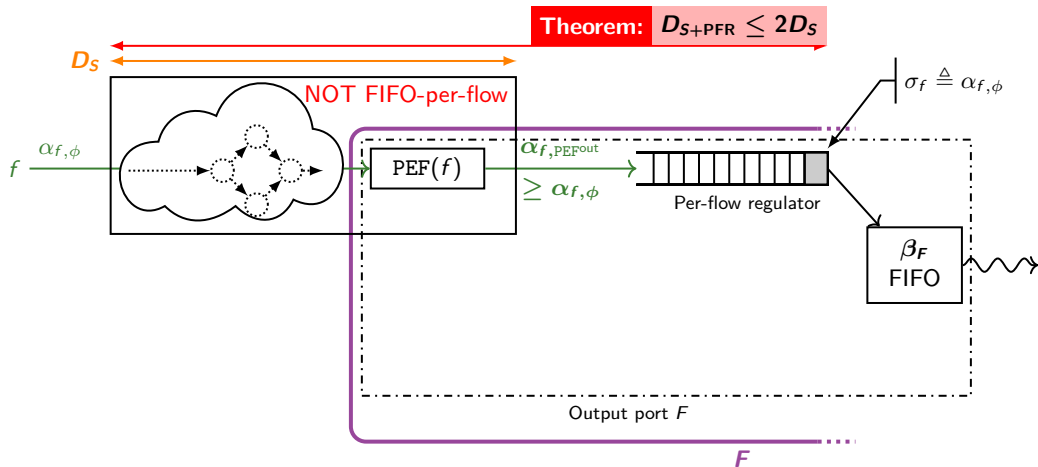


## Combination of Traffic Regulators with Redundancy Functions: **FIFO** assumption is lost!

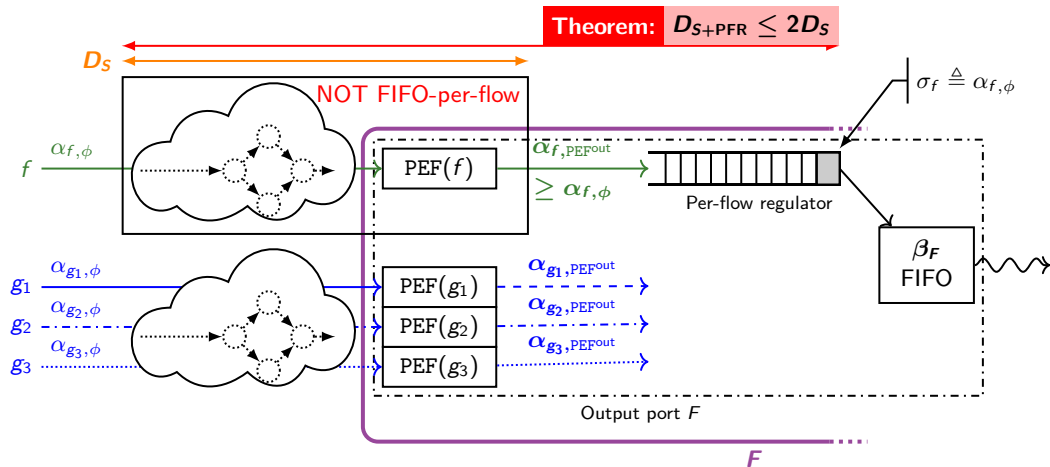




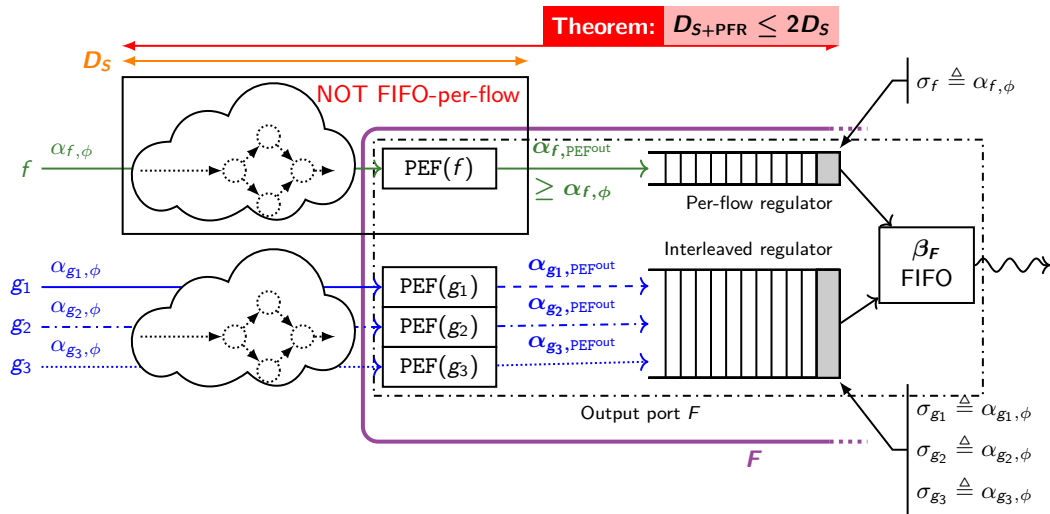
## Combination of Traffic Regulators with Redundancy Functions: **FIFO assumption is lost!**



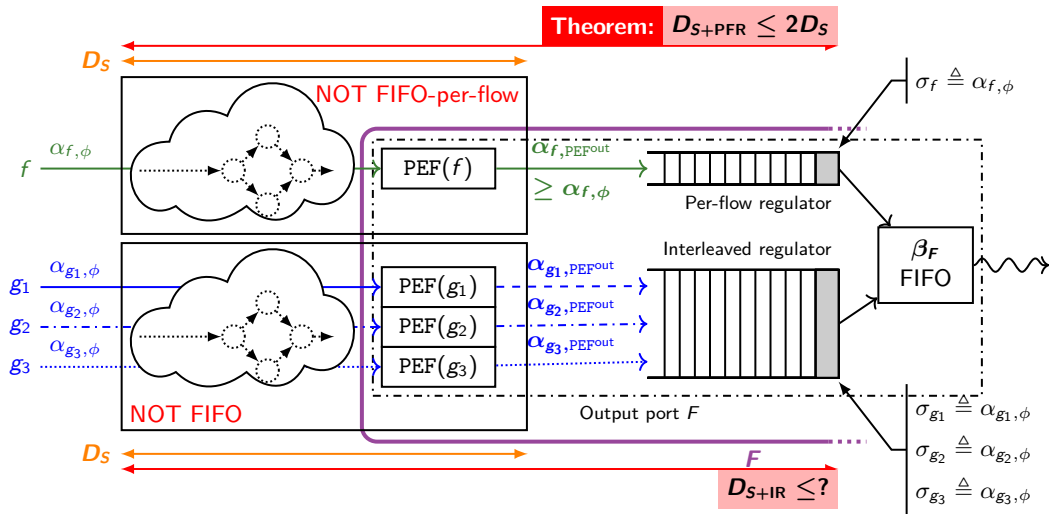
## Combination of Traffic Regulators with Redundancy Functions: **FIFO assumption is lost!**



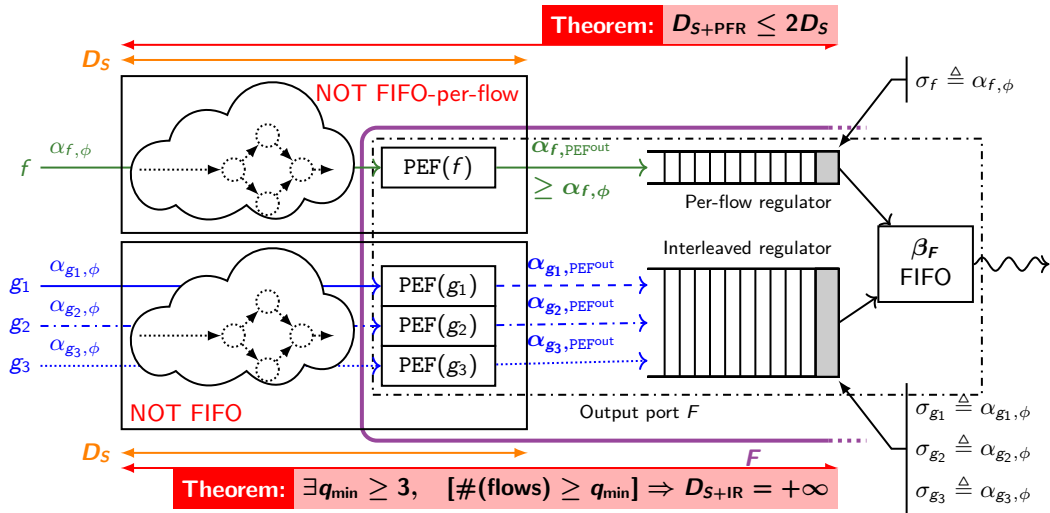
## Combination of Traffic Regulators with Redundancy Functions: **FIFO** assumption is lost!



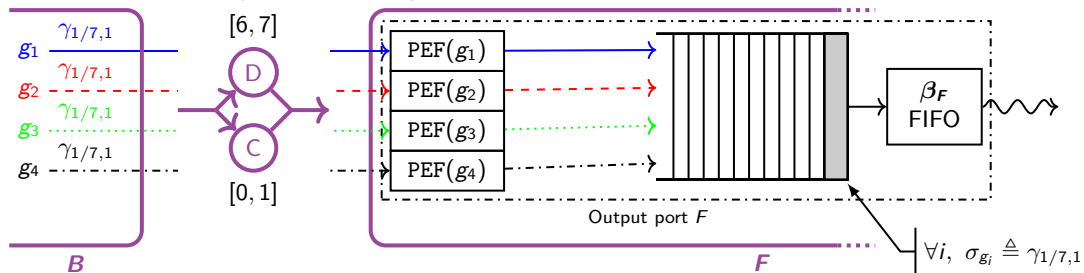
# Combination of Traffic Regulators with Redundancy Functions: **FIFO** assumption is lost!



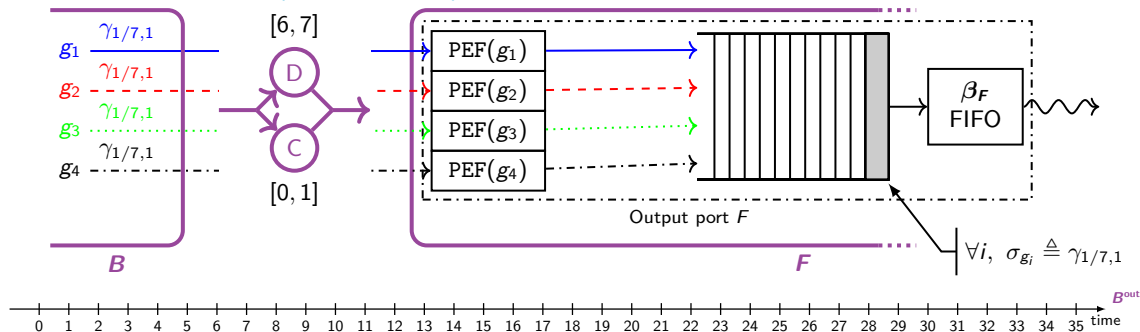
# Combination of Traffic Regulators with Redundancy Functions: **FIFO** assumption is lost!



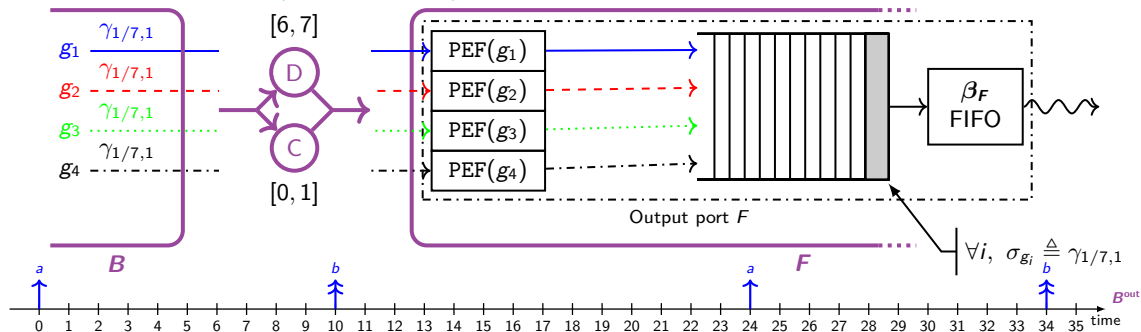
## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof



## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof

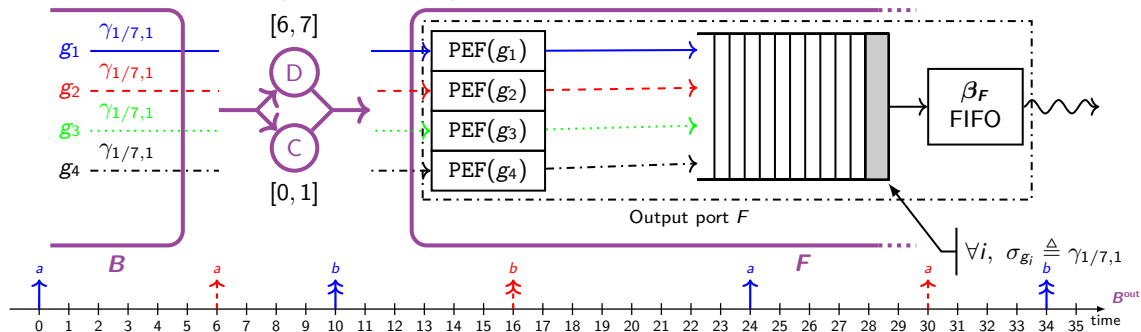


## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof

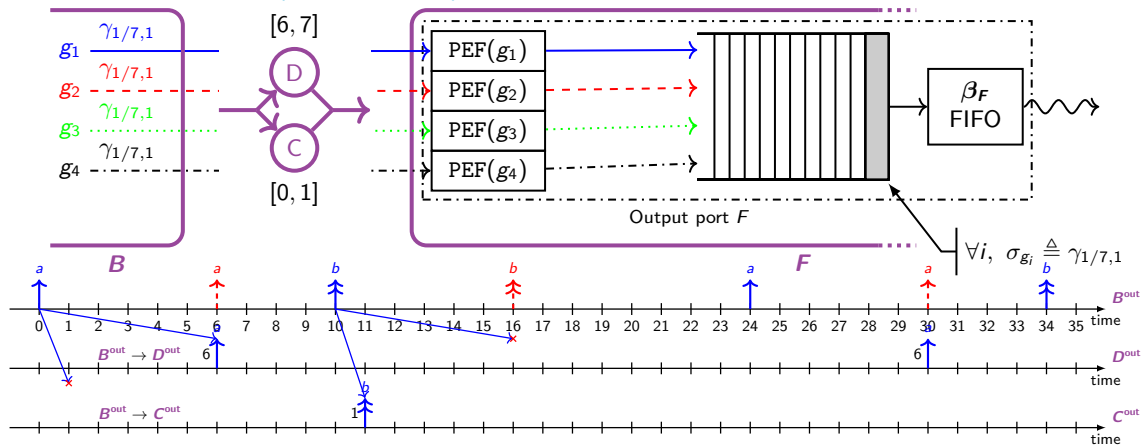




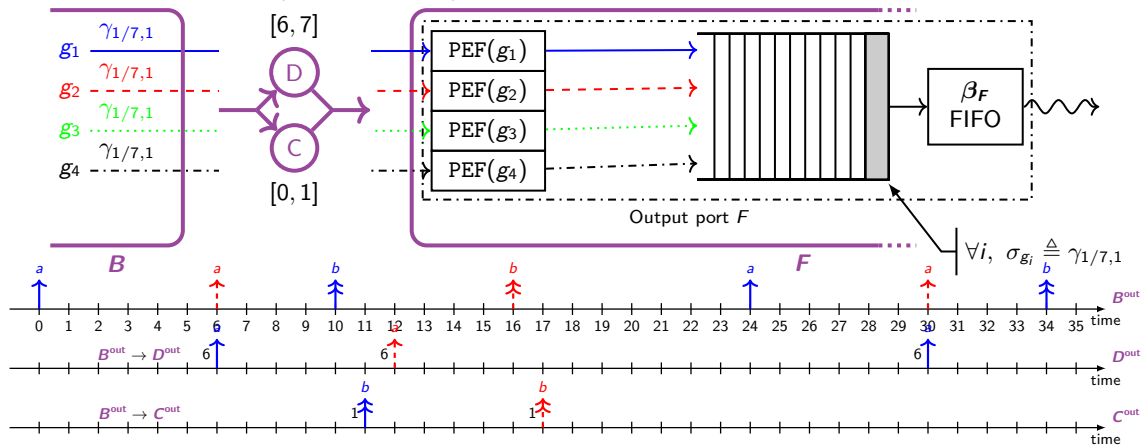
## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof



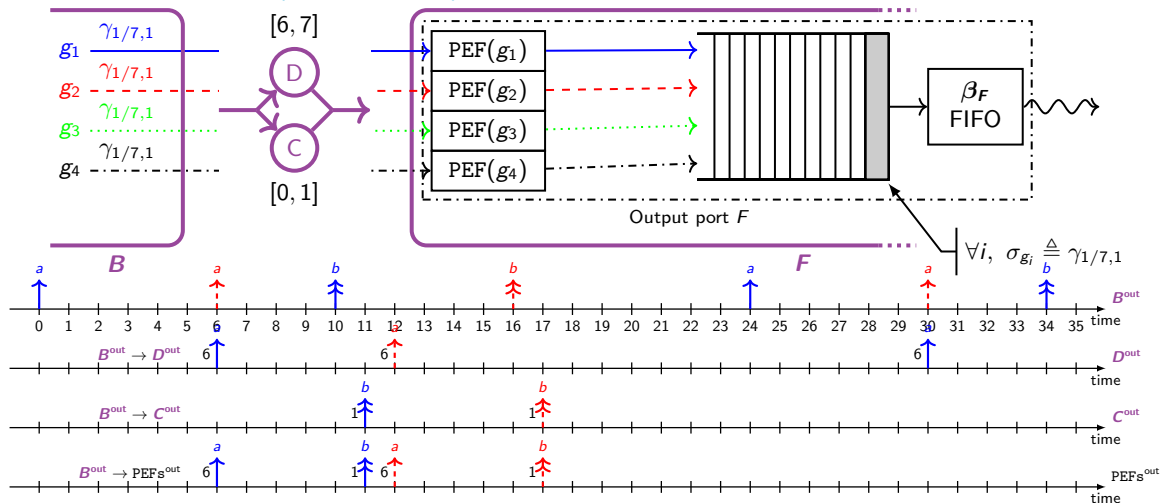
## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof



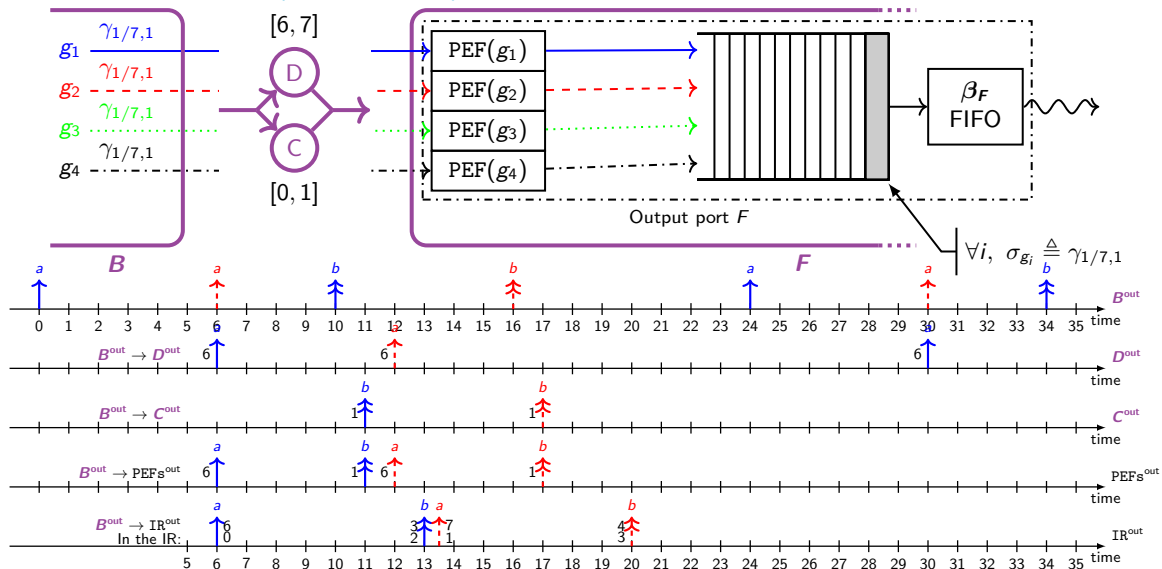
## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof



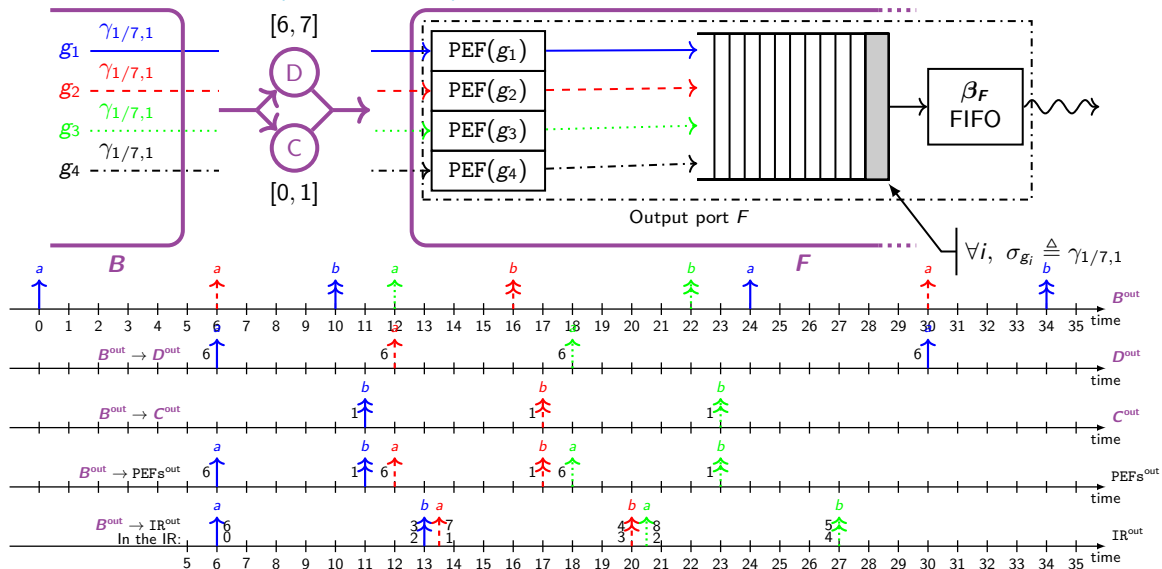
## Interleaved Regulator (IR, TSN ATS) **Unstable after PEF**: Intuition of the Proof



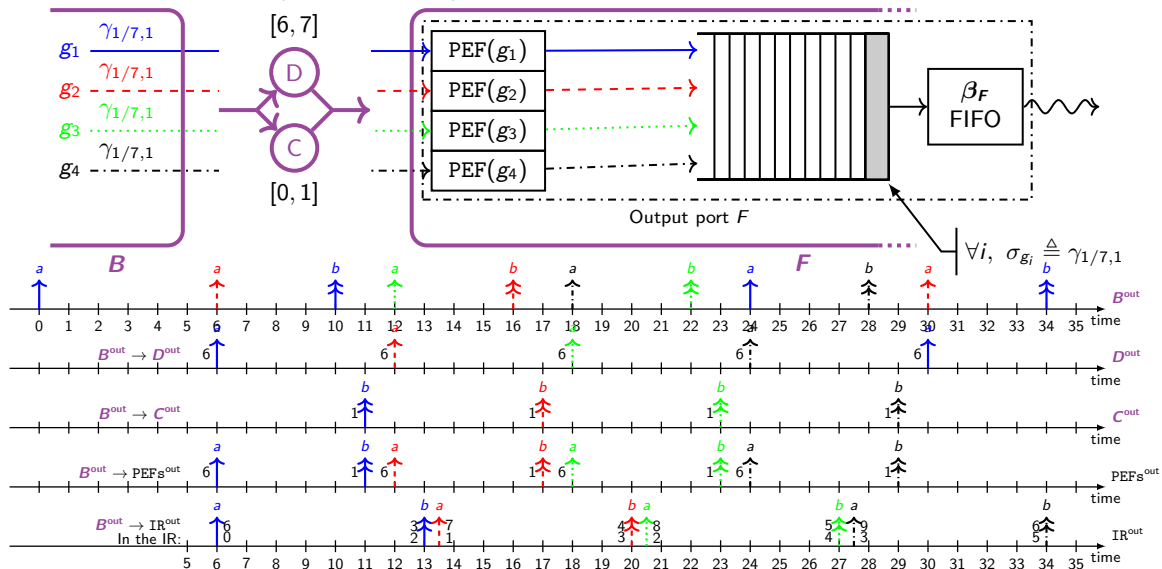
## Interleaved Regulator (IR, TSN ATS) Unstable after PEF: Intuition of the Proof



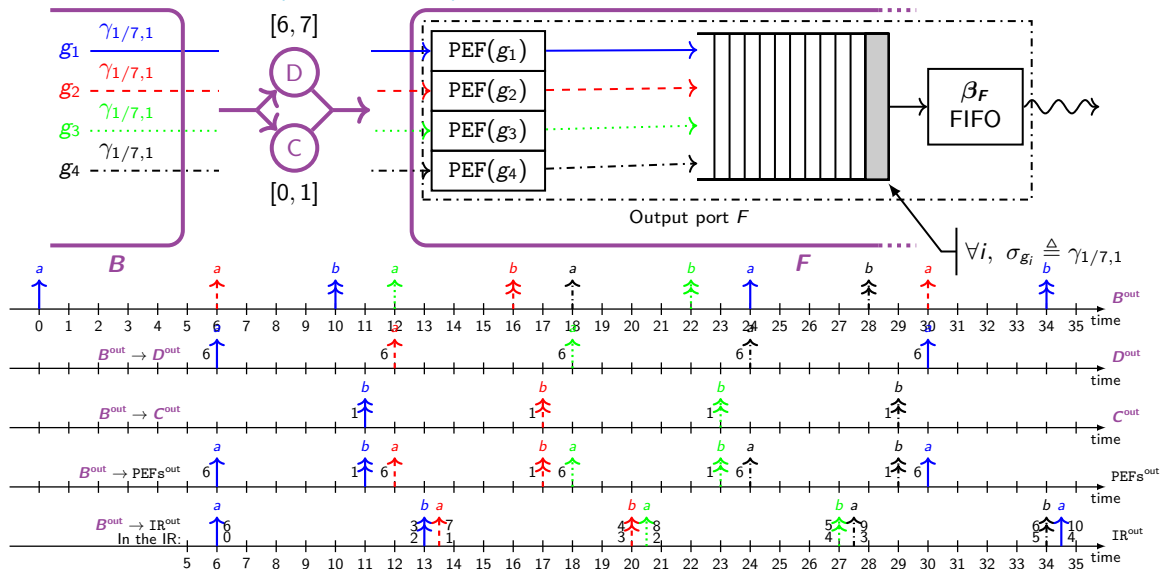
## Interleaved Regulator (IR, TSN ATS) Unstable after PEF: Intuition of the Proof



# Interleaved Regulator (IR, TSN ATS) Unstable after PEF: Intuition of the Proof



# Interleaved Regulator (IR, TSN ATS) Unstable after PEF: Intuition of the Proof





## Summary of our **Contributions**

### Toolbox for Modeling Redundancy in the Network-Calculus Framework

- Output arrival curve, bound on the mis-ordering.

## Summary of our **Contributions**

### Toolbox for Modeling Redundancy in the Network-Calculus Framework

- Output arrival curve, bound on the mis-ordering.

### Analysis of the Interactions Redundancy/Interleaved Regulator, *i.e.*, FRER/ATS

- Interleaved regulator placed immediately after a PEF yields **unbounded latencies**.
- *i.e.*, **TSN ATS** placed immediately after a **TSN sequence recovery function** yields **unbounded latency**.

## Summary of our **Contributions**

### Toolbox for Modeling Redundancy in the Network-Calculus Framework

- Output arrival curve, bound on the mis-ordering.

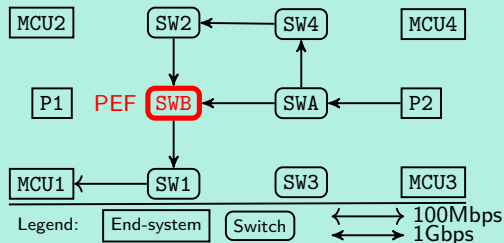
### Analysis of the Interactions Redundancy/Interleaved Regulator, *i.e.*, FRER/ATS

- Interleaved regulator placed immediately after a PEF yields **unbounded latencies**.
- *i.e.*, **TSN ATS** placed immediately after a **TSN sequence recovery function** yields **unbounded latency**.
- Reordering prior to the regulator solves the issue (but only available in DetNet!)

Ludovic Thomas, Ahlem Mifdaoui, and Jean-Yves Le Boudec [2022]. “Worst-Case Delay Bounds in Time-Sensitive Networks With Packet Replication and Elimination”. In: *IEEE/ACM Transactions on Networking*. DOI: [10.1109/TNET.2022.3180763](https://doi.org/10.1109/TNET.2022.3180763)

## Effect of IR (TSN ATS) On a Industrial Use-case with Redundancy Mechanisms

### On the industrial use-case: focus on one path

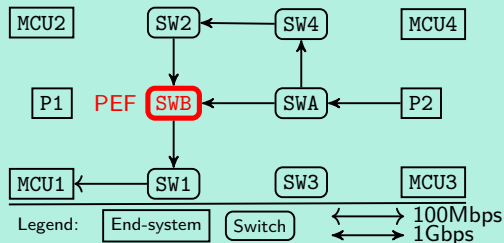


PEF: Packet Elimination Function  
PFR: Per-flow Regulator

POF: Packet Ordering Function  
IR: Interleaved Regulator (=TSN ATS)

## Effect of IR (TSN ATS) On a Industrial Use-case with Redundancy Mechanisms

### On the industrial use-case: focus on one path

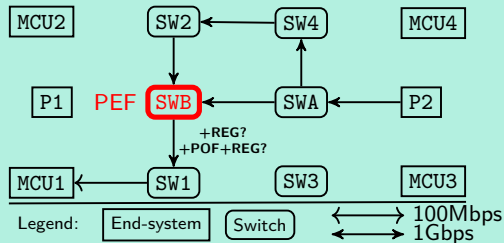


PEF: Packet Elimination Function  
PFR: Per-flow Regulator

POF: Packet Ordering Function  
IR: Interleaved Regulator (=TSN ATS)

## Effect of IR (TSN ATS) On a Industrial Use-case with Redundancy Mechanisms

### On the industrial use-case: focus on one path

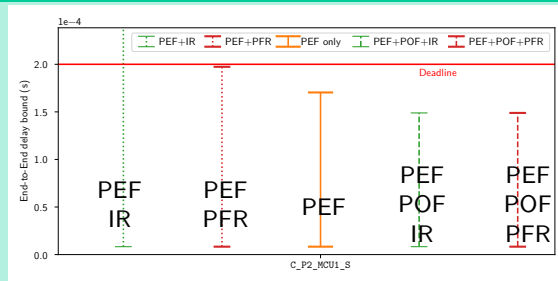
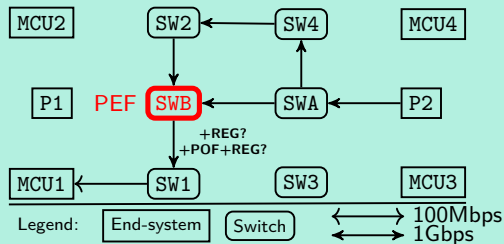


PEF: Packet Elimination Function  
PFR: Per-flow Regulator

POF: Packet Ordering Function  
IR: Interleaved Regulator (=TSN ATS)

# Effect of IR (TSN ATS) On a Industrial Use-case with Redundancy Mechanisms

## On the industrial use-case: focus on one path



PEF: Packet Elimination Function  
PFR: Per-flow Regulator

POF: Packet Ordering Function  
IR: Interleaved Regulator (=TSN ATS)

## Bibliography I

- [Farkas 2018] Farkas, János (Nov. 11, 2018). “TSN Basic Concepts”. URL: <https://www.ieee802.org/1/files/public/docs2018/detnet-tsn-farkas-tsn-basic-concepts-1118-v01.pdf> (visited on 01/25/2022).
- [Maile, et al. 2022] Maile, Lisa et al. (May 2022). “Ensuring Reliable and Predictable Behavior of IEEE 802.1CB Frame Replication and Elimination”. In: *ICC 2022 - IEEE International Conference on Communications*. ICC 2022 - IEEE International Conference on Communications, pp. 2706–2712. DOI: 10.1109/ICC45855.2022.9838905.
- [Mohammadpour, Le Boudec 2021] Mohammadpour, Ehsan and Jean-Yves Le Boudec (2021). “On Packet Reordering in Time-Sensitive Networks”. In: *IEEE/ACM Transactions on Networking*, pp. 1–13. ISSN: 1558-2566. DOI: 10.1109/TNET.2021.3129590.
- [RFC 8655] Finn, Norman et al. (2019). “Deterministic Networking Architecture”. In: RFC 8655. ISSN: 2070-1721. DOI: 10.17487/RFC8655. URL: <https://www.rfc-editor.org/info/rfc8655> (visited on 06/07/2021).



## Bibliography II

- [IEEE 802.1Qcr] “IEEE Standard for Local and Metropolitan Area Networks—Bridges and Bridged Networks - Amendment 34” (Nov. 2020). “IEEE Standard for Local and Metropolitan Area Networks—Bridges and Bridged Networks - Amendment 34:Asynchronous Traffic Shaping”. In: *IEEE Std 802.1Qcr-2020 (Amendment to IEEE Std 802.1Q-2018 as amended by IEEE Std 802.1Qcp-2018, IEEE Std 802.1Qcc-2018, IEEE Std 802.1Qcy-2019, and IEEE Std 802.1Qcx-2020)*, pp. 1–151. DOI: 10.1109/IEEESTD.2020.9253013.
- [IEEE 802.1CB] “IEEE Standard for Local and Metropolitan Area Networks—Frame Replication and Elimination for Reliability” (Oct. 2017). In: *IEEE Std 802.1CB-2017*, pp. 1–102. DOI: 10.1109/IEEESTD.2017.8091139.

## Where is **TSN ATS** wrt to **TSN FRER** ?

The place of the Interleaved Regulator (IR) with respect to the PEF is not clear in TSN.

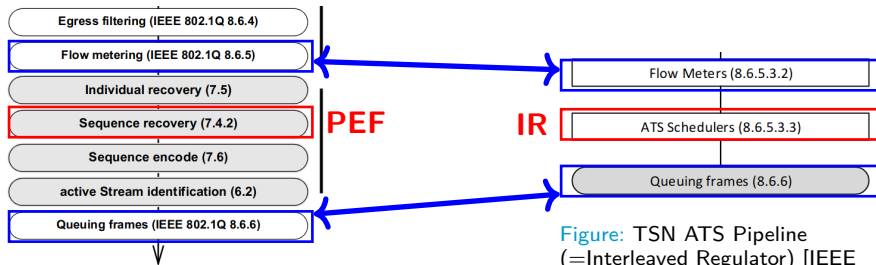


Figure: TSN FRER Pipeline [IEEE 802.1CB]

Figure: TSN ATS Pipeline  
(=Interleaved Regulator) [IEEE 802.1Qcr]