



Bornes de Latence dans les Réseaux Temps-Réel

Présentation visite École des Mines

Ludovic Thomas ludovic.thomas@loria.fr



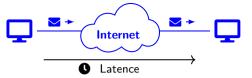




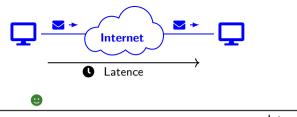


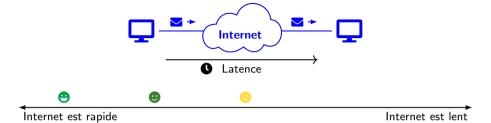


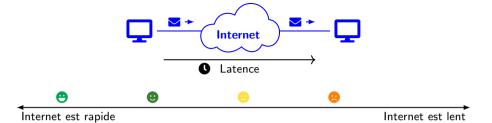
Internet est rapide Internet est lent

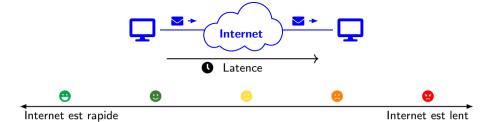




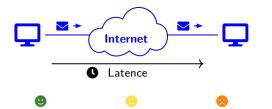




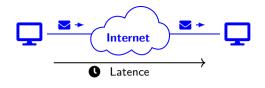






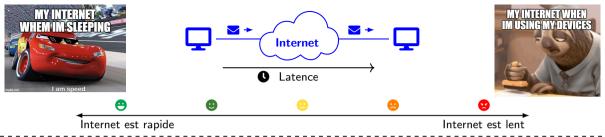




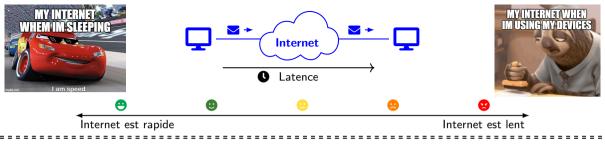


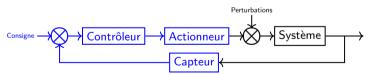


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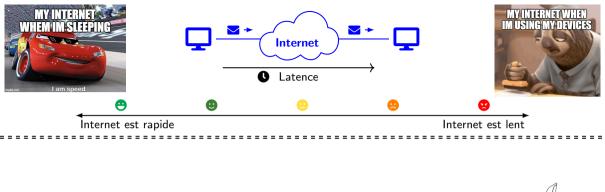


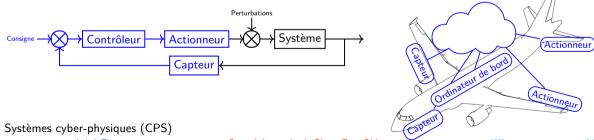
2023

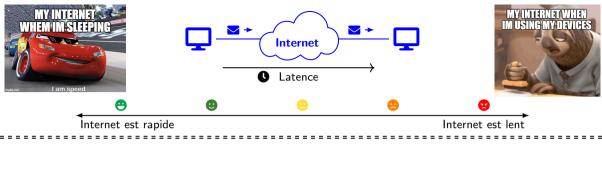


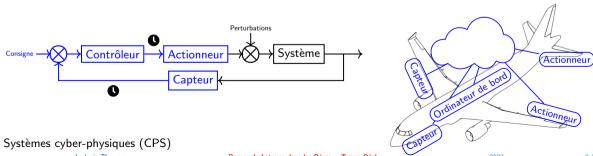


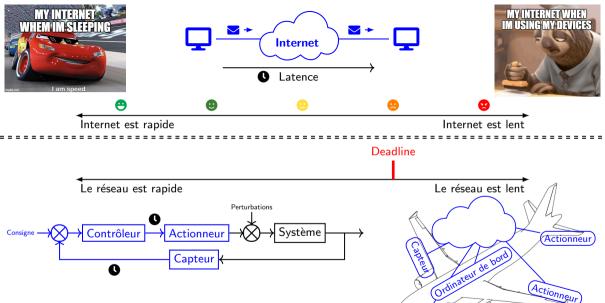
Systèmes cyber-physiques (CPS)



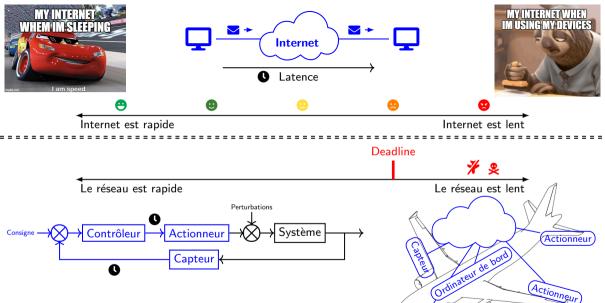




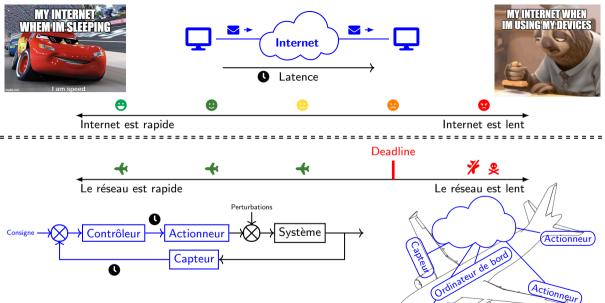




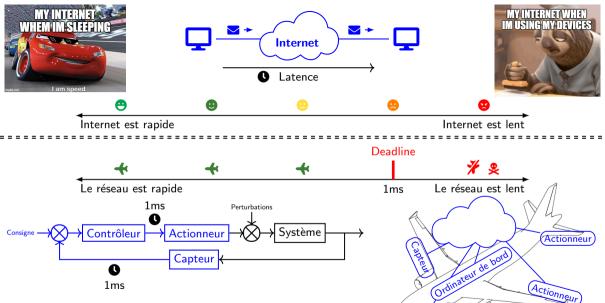
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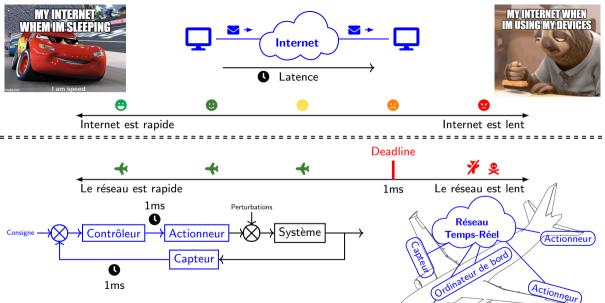


Actionne



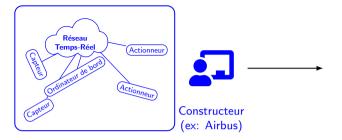
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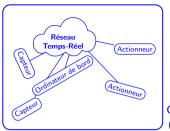
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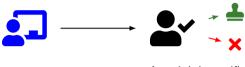


1ms

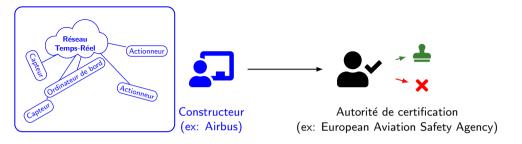
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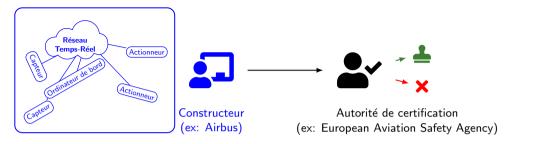




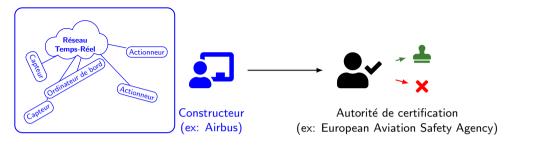
Autorité de certification (ex: European Aviation Safety Agency)



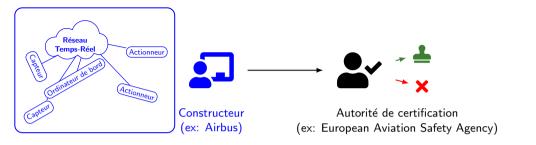
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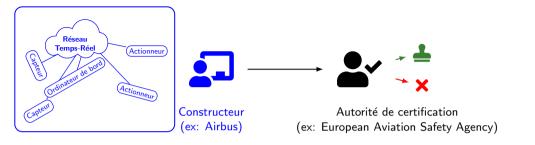


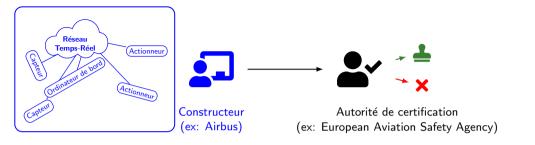
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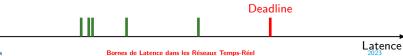


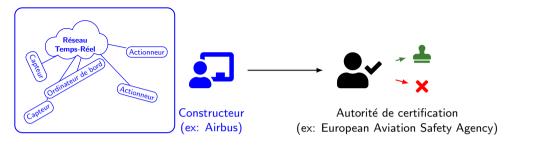
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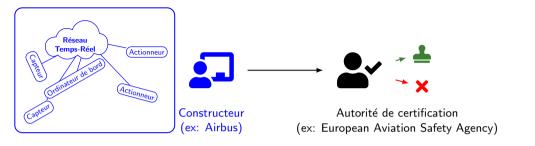


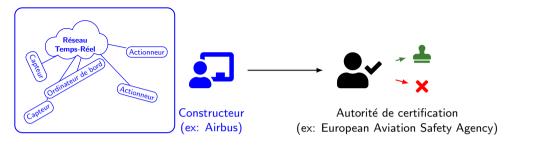






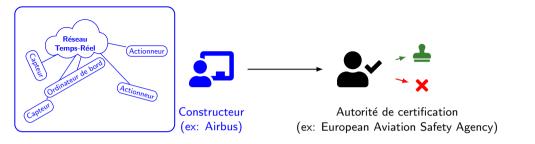






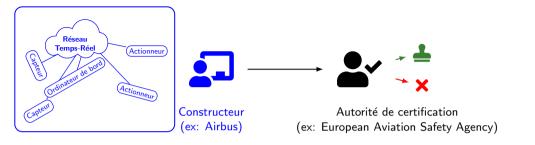


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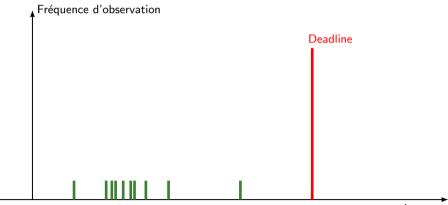


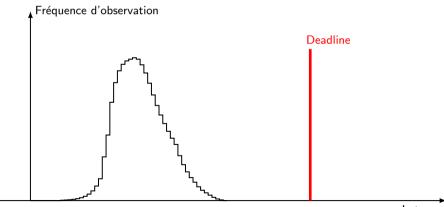
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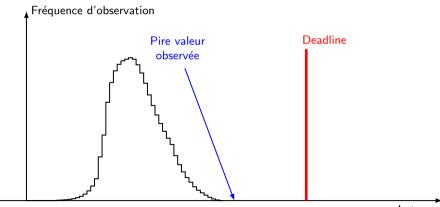


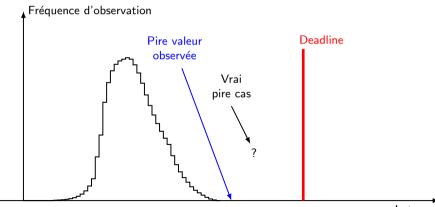


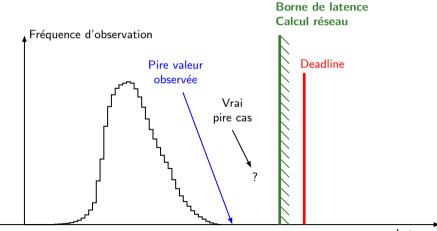
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Algèbre "classique"

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4 + 2 = 6	
$5 \times 3 = 15$	

Algèbre "classique"	Algèbre min-plus
4 + 2 = 6	4 + 2 = 2
5 × 3 = 15	5 × 3 = 8

Algèbre "classique" $(\mathbb{R},+,\times)$	Algèbre min-plus $(\mathbb{R}^+, \min, +)$
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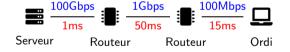
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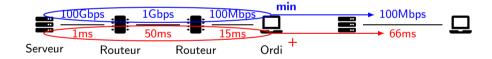




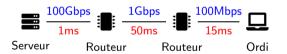
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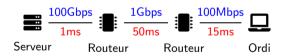


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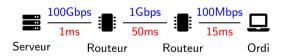
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$$\beta_1$$
 Service curve (dur!) β_3

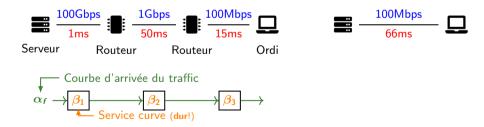
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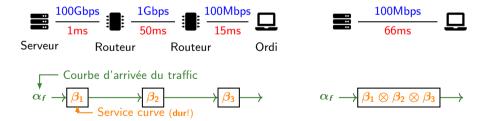
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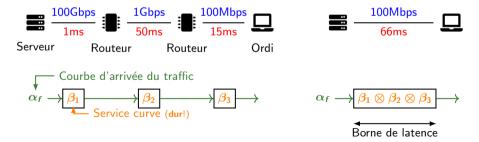
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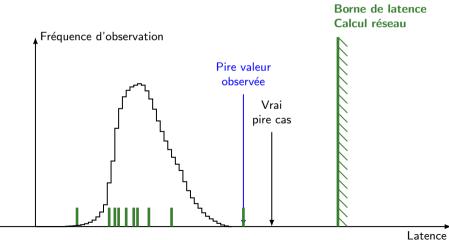
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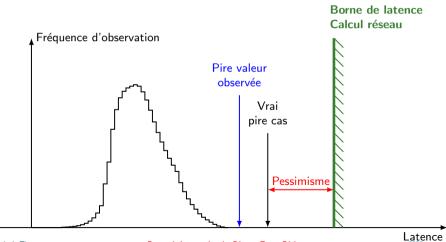
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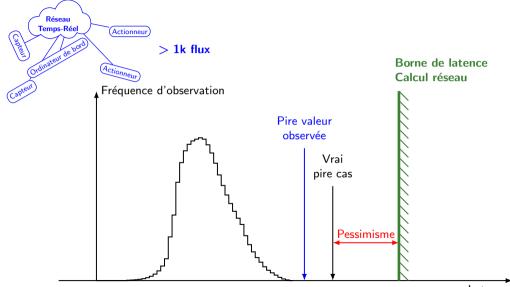
Challenge récurrent: Complexité vs Pessimisme



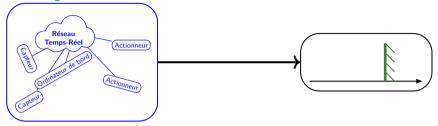
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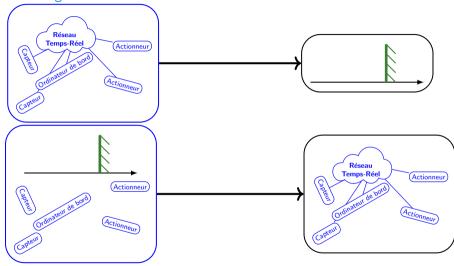
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Les Challenges à Venir



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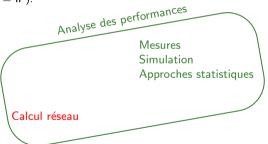
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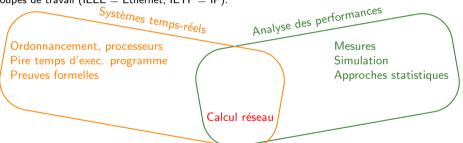
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Calcul réseau

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