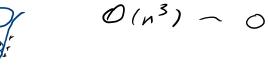
Support vector machines - Grundidé hyperplan for att separera klasser





design mutyions stylet

. Stulle kunna gora feature expansion

· Kerneltrick

· Hyperplan har viredan soft men internamgivit. β, + p, x, -1 ... + p, xp = 0 (Spay(5,75) (P=3) ax + by + (2 + d = 0) $\Pi = (\alpha, 6, c) \quad \text{om } P > 3 \quad \Pi = (\beta, \dots, \beta_p)$ Bo= 0 sa ingas origo, annays inte

Aust and punkt/plan
$$P_{0} = (x_{0}, y_{0}, Z_{0})$$

$$A = (p, q, 1)$$

$$I = \frac{1(x_{0} - p)\alpha + (y_{0} - q)6 + (Z_{0} - r)c!}{\sqrt{\alpha^{2} + 6^{2} + c^{2}}}$$

$$I = \frac{|u| \cdot m}{m \cdot n} |v| ||k_{0}|| \cdot |m| = 1 = \sqrt{p_{0}^{2} + c^{2}}$$

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## Maximal margin

Om marginalen måste vara tom blir metoden könslig för blus -> Soft Mappin

sidantatt  $ZB^{3}=1$ (i - varie rad i indutar)  $\beta_0 + \beta_1 \times 11 + \dots + \beta_p \times 1p > M(1 - \epsilon_i)$   $\epsilon_i \ge 0$ ,  $\epsilon_i \le C$  (budget)

·Keyne/ -Matris med "vikter"  $u_{1}\cdot v_{1}=\sum_{j=1}^{N}u_{1}v_{j}$ < 41, 1/2 - M·V (euclidisher) Klassificeringen kan skrivas som funktion (svor hörledning):  $f(x) = \beta_0 + \sum_{i=1}^{N} \alpha_i \langle x_i x_i \rangle$ S = Support set Stodvektorerna vi valt ⇒ Bo + E Q; (x,x;)

Kernel funktioner

 $K(U, y) \in \left(1 + \sum_{j=1}^{p} u_j v_j\right)^d \longrightarrow \left(1 + U \cdot y\right)^d$ 



RBF (Radial basis function)

 $K(u, y) = e^{-y \sum_{j=1}^{2} (u_j - y_j)^2}$ 

berätuar inje produtter for d-limensionella polynom.

y >> 0, litau 0<sup>2</sup>
y << 1, stay o<sup>2</sup>
(mjuka linjay)

> > hyperparameter

(p+d) has, motsvarar polynom expansion



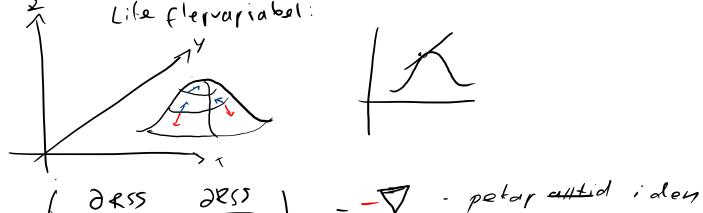
Multingmiella klasser Ova: ONe-versus-all

Kau bli dyrt for stord datamangden

(drs gigabyte +)

040 : one-veysus-one

Grundidé tou et litet steg i en "bja" riletning for att na Gradient descent Iterativa funktioner minimum  $X_{n+1} = X_n$ Logistisk exvation (iterativ)  $\frac{x_{n+1}=r(1-x_n)}{\sqrt{2}} \approx 12$ Basfall to= a · Differens exvation. iterer or over tid · Differential exvation over kontinuerlig tid "iteration" (integration)



titting som har storst f Spändring shustighet

$$OLS:$$
 $C(\beta) = MSE$ 
 $Ridge$ 

 $C(\beta) = MSF + \sum_{i=1}^{p} \beta_{i}^{2}$ 

 $C(\theta) = \frac{1}{n-k-1} \sum_{i=1}^{\infty} (y_i - \hat{y}_i)^2$ 

som iterativ (rekurent) funktion:

 $= \frac{1}{n-k-1} \sum_{i=1}^{N} (q_i - \theta \cdot x_i)^2$ 

$$C(\beta) = MSE$$
Ridge

som iterative funktion:  $\theta_{i+1} - \theta_i - \eta \mathcal{O}(.(0))$  $\theta_{j+1} = \theta_{j} - \eta \left( \frac{z}{n-k-1} \times^{T} \left( \times \theta_{j} - y \right) \right)$ Batch (> Stickprov (Stal. Sample) sample () datapunt (data point) Batch Gradient Descent tonderay att fatha i Istalamin.

Stochastic Gradient Descent Välj en slumpmässig datapunkt.

Raba P på den punkten.

uppepa givet antal garger.

- ger en EPOL (EPOCH)

n = hor storg

konvergerar ej!



Minibatey Vilj delmängd av punkter och räbna gradient annars som SCO.

Kk+1 = xk- SZk

ZK = Df + BZK-1

x = x = 7. Dfk

\* t+1 \*\* \* \* t /- \* t -1