# Applied Linear Algebra for

# 1 COLLECTIONS/CONTAINERS

### List/Vector

Create a new vector/list as follows

```
import numpy as np
all import numpy as np
all all = [0, 2, 4, 6, 8]
all all = np.arange(0,10)
all all = np.linspace(0,8,5)
all = np.random.randint(0,7, size)
= 5)
```

Add item

```
import numpy as np

lst = [0, 2, 4, 6, 8]

seq = [1, 4]

lst.append(-4) ## add item at
   end: [0, 2, 4, 6, 8, -4]

lst.insert(3, 7) ## insert a
   item at specific index: [0,
        2, 4, 7, 6, 8]

lst.extend(seq) ## add sequence
   of items at end: [0, 2, 4, 6,
        8, 1, 4]
```

Remove item(s)

```
import numpy as np

lst = [0, 2, 4, 6, 8, 4]

lst.remove(4) ## remove first
   item with value 4: [0, 2, 6,
      8, 4]

lst.pop(2) ## remove item at
   specific index: [0, 2, 6, 8,
   4]

del lst[1] ## remove item at
   specific index: [0, 4, 6, 8,
   4]

lst.clear() ## remove all items:
   []
```

To get value in a list: Ist[index]

# Set

· Do not allow duplicate values

- Set elements are unchangable (only remove/ insert new elements)
- Set elements are unordered (present in a different order every time when you run)
- Can not access items in a set by specific index

Add new item(s)

```
import numpy as np

s = {0, 2, 4, 6, 8}

s.add(5) ## add item: {0, 2, 4,
    5, 6, 8}

s.update({3,9})## add sequence
    of items: {0, 2, 3, 4, 5, 6,
        8, 9}

## unordered

ss = {'xa','ka'}

ss.add('nkk') ## {'ka','xa','nkk
    '}
```

Remove item

```
import numpy as np

s = {0, 2, 4, 6, 8}

s.remove(4) ## remove item: {0,
        2, 5, 6, 8}

s.discard(6) ## remove item: {0,
        2, 5, 8}

s.pop() ## remove first item:
        {2, 5, 8}

s.clear() ## remove all items:
        {}
}
```

### **Dictionary**

A dictionary is used to store data as key-value pairs.

- · A collection is ordered
- Set elements are changable
- · Do not allow duplicate values

Add new item

```
import numpy as np

d = {1:'banana', 2:'monkey', 3:'
    apple', 4:'dog', 5:'cat'}
```

```
4 d.update({8:'tiger', 7: 'pig'})
    ## {1:'banana', 2:'monkey',
    3:'apple', 4:'dog', 5:'cat',
    7:'pig', 8:'tiger'}
5 d[6] = 'snake' ## {1:'banana',
    2:'monkey', 3:'apple', 4:'dog
    ', 5:'cat', 6:'snake', 7:'pig
    '}
```

Update item

```
import numpy as np

d = {1:'banana', 2:'monkey', 3:'
    apple', 4:'dog', 5:'cat'}

d.update({5:'tiger', 4: 'pig'})
    ## {1:'banana', 2:'monkey',
    3:'apple', 4:'pig', 5:'tiger
    '}

d[3] = 'orange' ## {1:'banana',
    2:'monkey', 3:'orange', 4:'
    pig', 5:'tiger'}
```

Remove item

```
import numpy as np

d = {1:'banana', 2:'monkey', 3:'
    apple', 4:'dog', 5:'cat', 6:'
    pig'}

d.pop(5) ## remove key = 5: {1:'
    banana', 2:'monkey', 3:'apple
    ', 4:'dog', 6:'pig'}

del d[1] ## remove key = 1:{2:'
    monkey', 3:'apple', 4:'dog',
    6:'pig'}

d.popitem() ## remove last item:
    {2:'monkey', 3:'apple', 4:'
    dog'}

d.clear() ## remove all items
```

To get value in a dictionary: d.get(key), d[key]

## Tuple

This type data is utilized to store multiple items in a single variable. Tuple is **ordered and unchangeable**.

```
import numpy as np

## create a new tuple

t1 = tuple((1, "k", 7.4))

t2 = (1, "k", 7.4)

t3 = 1, "k", 7.4
```

## 2 LINEAR ALGEBRA IN PYTHON

### **Vector**

Access elements in a vector

```
import numpy as np

limport numpy as np

limpo
```

Reverse vector

Combine two vectors

Find specific elements in vector with **np.where** or logic operations

```
Find and replace
```

Vector operations: +, -, \*\*, /, \*, dot product, inner product

```
1 import numpy as np
2
3 u = np.array([[1, 3, 5, 1, 2]])
4 v = np.array([[1, 3, 5, 7, 2]])
6 # [[ 2 6 10 8 4
                        3]]
7 va = u + v
8 ## [[ 0 0 0 -6 0
                          3]]
9 vs = u - v
10 # [[1, 9, 15, 1, 4]]
11 ve = u * * 2
12 # [[0.5 1.5 2.5 3.5 1. 0.]]
13 vd = v/2
14 # [[ 1 9 25 7
                         0]]
15 \text{ vm} = \text{u} * \text{v}
16 np.inner(u,v) # [[46]]
17 np.dot(u,v.T) # [[46]]
18 vdt = u@v.T # [[46]]
```

In addition, some functions are provided such as: **np.sum**, **np.max**, **np.min**, **np.mean**, **np.argmax**, **np.argmin**, **np.unique** 

### **Matrix**

Reshape vector/matrix

Matrix analysis

Solving the system of equations Ax = b

### Norm

· Norm-vector

```
import numpy as np

k = [1, 0, 2, -1]

# Eclidean norm (12)

12 = np.linalg.norm(k)# 2.449

# 11

11 = np.linalg.norm(k, 1) # 4

# 1-inf (max)

l_inf_max = np.linalg.norm(k, np.inf)

# 1-inf (min)

1 l_inf_min = np.linalg.norm(k, -np.inf)
```

Norm-matrix

Matrix factorization:

• Eigen decomposition

```
1 import numpy as np
```

```
2
3 A = np.array([[2, 1, -2],[3,
          0, 1], [1, 1, -1]])
4
5 # Find the eigen values of A
6 evalue = np.linalg.eigvals(A)
7 # Find the eigen values and
        eigen vectors
8 evalue, evector = np.
        linalg.eig(A)
```

· Singular value decomposition

# 20.0 - \* 17.5 15.0 12.5 10.0 - \* 7.5 -

7 plt.scatter(x, y, c = 'c', alpha

=0.5, marker = '\*')

8 plt.show()

5.0

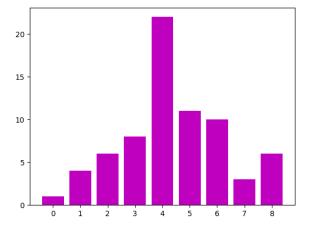
2.5

# 3 GRAPH

Draw a histogram of the following vector:

```
import matplotlib.pyplot as plt

1 import matplotlib.pyplot as plt
2
3 l = [1, 4, 6, 8, 22, 11, 10, 3, 6]
4 x = [str(i) for i in np.arange(len(l))]
5 plt.bar(np.arange(len(l)),l, color='m')
6 plt.xticks(np.arange(len(l)),x)
7 plt.show()
```



Draw scatter plot:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 x = [1, 4, 6, 8, 22, 11, 10, 3, 6]
5 y = [11, 2, 10, 6, 7, 20, 4, 4, 6]
```