第十六章 二端口网络

- 二端口网络
- 二端口的方程和参数
- 二端口的等效电路

§ 16-1 二端口网络



如果在任何时间,从端子1流入的电流等于从端子1流出的电流,从端子2流入的电流等于从端子2流出的电流,这种电路称为二端口电路。

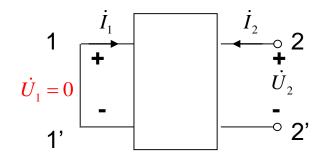
$$\dot{I}_{1} = Y_{11}\dot{U}_{1} + Y_{12}\dot{U}_{2}
\dot{I}_{2} = Y_{21}\dot{U}_{1} + Y_{22}\dot{U}_{2}
\begin{bmatrix} \dot{I}_{1} \\ \dot{I}_{2} \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} \dot{U}_{1} \\ \dot{U}_{2} \end{bmatrix}$$

$$Y_{11} = \frac{\dot{I}_1}{\dot{U}_1} \bigg|_{\dot{U}_2 = 0} \qquad Y_{21} = \frac{\dot{I}_2}{\dot{U}_1} \bigg|_{\dot{U}_2 = 0}$$

$$\begin{array}{c|c}
 & \dot{I}_1 \\
 & \dot{U}_1 \\
 & \vdots \\
 & 1, \\
\end{array}$$

$$\begin{array}{c|c}
 & \dot{I}_2 \\
 & \vdots \\
 & \dot{U}_2 = 0 \\
 & 2, \\
\end{array}$$

$$Y_{12} = \frac{\dot{I}_1}{\dot{U}_2} \Big|_{\dot{U}_1 = 0} \qquad Y_{22} = \frac{\dot{I}_2}{\dot{U}_2} \Big|_{\dot{U}_1 = 0} \qquad 1$$



Y: 短路导纳参数

$$\dot{U}_{1} = Z_{11}\dot{I}_{1} + Z_{12}\dot{I}_{2}$$

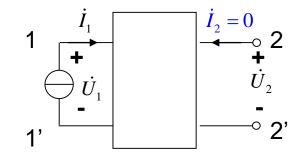
$$\dot{U}_{2} = Z_{21}\dot{I}_{1} + Z_{22}\dot{I}_{2}$$

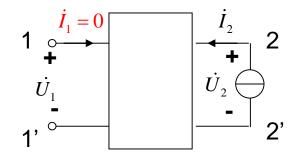
$$\begin{bmatrix} \dot{U}_1 \\ \dot{U}_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} \dot{I}_1 \\ \dot{I}_2 \end{bmatrix}$$

$$Z_{11} = \frac{\dot{U}_1}{\dot{I}_1} \bigg|_{\dot{I}_2 = 0} \qquad Z_{21} = \frac{\dot{U}_2}{\dot{I}_1} \bigg|_{\dot{I}_2 = 0}$$

$$Z_{12} = \frac{\dot{U}_1}{\dot{I}_2} \bigg|_{\dot{I}_1 = 0}$$
 $Z_{22} = \frac{\dot{U}_2}{\dot{I}_2} \bigg|_{\dot{I}_1 = 0}$

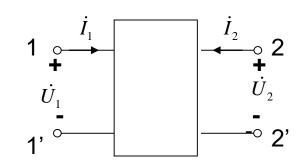
Z: 开路阻抗矩阵





Y参数方程:
$$\dot{I}_1 = Y_{11}\dot{U}_1 + Y_{12}\dot{U}_2$$
 $\dot{I}_2 = Y_{21}\dot{U}_1 + Y_{22}\dot{U}_2$

Y: 短路导纳矩阵 $\begin{vmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{vmatrix}$



Z参数方程:
$$\dot{U}_1 = Z_{11}\dot{I}_1 + Z_{12}\dot{I}_2$$
 $\dot{U}_2 = Z_{21}\dot{I}_1 + Z_{22}\dot{I}_2$

$$Z$$
: 开路阻抗矩阵 $\begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix}$

$$Z = Y^{-1} \qquad Y = Z^{-1}$$

二端口方程和参数 § 16-2

A参数方程:
$$\dot{U}_1 = A_{11}\dot{U}_2 + A_{12}(-\dot{I}_2)$$

$$\dot{I}_1 = A_{21}\dot{U}_2 + A_{22}(-\dot{I}_2)$$

$$A_{11} = \frac{\dot{U}_1}{\dot{U}_2}\Big|_{\dot{I}_2=0}$$

$$A_{21} = \frac{\dot{I}_1}{\dot{U}_2}\Big|_{\dot{I}_2=0}$$

$$A_{22} = \frac{\dot{I}_1}{-\dot{I}_2}\Big|_{\dot{U}_2=0}$$

$$\left[\begin{array}{c} \dot{U}_1 \\ \dot{I}_1 \end{array}\right] = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} \dot{U}_2 \\ -\dot{I}_2 \end{bmatrix}$$

$$\begin{bmatrix} \dot{U}_1 \\ \dot{I}_1 \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} \dot{U}_2 \\ -\dot{I}_2 \end{bmatrix}$$

H参数方程:
$$\dot{U}_1 = H_{11}\dot{I}_1 + H_{12}\dot{U}_2$$
 $\dot{I}_2 = H_{21}\dot{I}_1 + H_{22}\dot{U}_2$
 $H_{11} = \frac{\dot{U}_1}{\dot{I}_1}\bigg|_{\dot{U}_2=0}$
 $H_{21} = \frac{\dot{I}_2}{\dot{I}_1}\bigg|_{\dot{U}_2=0}$
 $H_{12} = \frac{\dot{U}_1}{\dot{U}_2}\bigg|_{\dot{I}_1=0}$
 $H_{22} = \frac{\dot{I}_2}{\dot{U}_2}\bigg|_{\dot{I}_1=0}$

$$H_{11} = \frac{\dot{U}_{1}}{\dot{I}_{1}}\Big|_{\dot{U}_{2}=0} H_{21} = \frac{\dot{I}_{2}}{\dot{I}_{1}}\Big|_{\dot{U}_{2}=0} \left[\begin{array}{c} \dot{U}_{1} \\ \dot{I}_{2} \end{array} \right] = \begin{bmatrix} H_{11} & H_{12} \\ H_{21} & H_{22} \end{bmatrix} \begin{bmatrix} \dot{I}_{1} \\ \dot{U}_{2} \end{bmatrix}$$

$$\dot{U}_{1} = \frac{\dot{U}_{1}}{\dot{I}_{2}} H_{21} H_{22} = \frac{\dot{I}_{2}}{\dot{I}_{2}} H_{22} = \frac{\dot{I}_{2}}{\dot{I}_{2}} H_{21} H_{22} H_{22} = \frac{\dot{I}_{2}}{\dot{I}_{2}} H_{22} H_{22} H_{22} H_{22} = \frac{\dot{I}_{2}}{\dot{I}_{2}} H_{21} H_{22} H_{22} = \frac{\dot{I}_{2}}{\dot{I}_{2}} H_{21} H_{22} H$$

互易条件

对称条件

Y参数:
$$Y_{12} = Y_{21}$$

$$Y_{12} = Y_{21}$$
 $Y_{11} = Y_{22}$

$$Y_{11} = Y_{22}$$

Z参数:
$$Z_{12} = Z_{21}$$

$$Z_{12} = Z_{21}$$
 $Z_{11} = Z_{22}$

A参数:
$$A_{11}A_{22} - A_{12}A_{21} = 1$$

$$A_{11}A_{22} - A_{12}A_{21} = 1$$

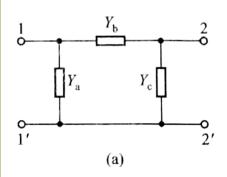
$$A_{11} = A_{22}$$

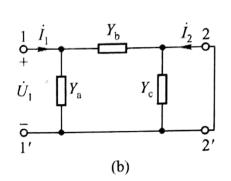
$$H_{12} = -H_{21}$$

$$H_{11}H_{22} - H_{12}H_{21} = 1$$

$$H_{12} = -H_{21}$$

例16-1 求二端口的Y参数





$$\dot{I}_{1} = \dot{U}_{1} (Y_{a} + Y_{b})$$

$$- \dot{I}_{2} = \dot{U}_{1} Y_{b}$$

$$Y_{11} = \frac{\dot{I}_{1}}{\dot{U}_{1}} \Big|_{\dot{U}_{2}=0} = Y_{a} + Y_{b}$$

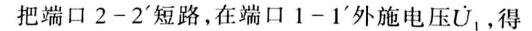
$$Y_{21} = \frac{\dot{I}_{2}}{\dot{U}_{1}} \Big|_{\dot{U}_{2}=0} = -Y_{b}$$

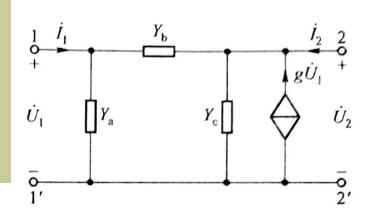
$$Y_{12} = -Y_b$$

$$Y_{22} = Y_b + Y_c$$

对R、L、C构成的任何无源二端口,总有: $Y_{12} = Y_{21}$

例16-2 求二端口的Y参数





$$\dot{I}_{1} = \dot{U}_{1} (Y_{a} + Y_{b})$$

$$\dot{I}_{2} = -\dot{U}_{1} Y_{b} - g \dot{U}_{1}$$

$$Y_{11} = \frac{\dot{I}_{1}}{\dot{U}_{1}} = Y_{a} + Y_{b}$$

$$Y_{21} = \frac{\dot{I}_{2}}{\dot{U}_{1}} = -Y_{b} - g$$

同理,为了求 Y_{12} 、 Y_{22} ,把端口 1-1′ 短路,即令 $U_1=0$,这时受控源的电流也等于零,故得

$$Y_{12} = \frac{\dot{U}_1}{\dot{U}_2} = -Y_b$$
 $Y_{22} = \frac{\dot{I}_2}{\dot{U}_2} = Y_b + Y_c$

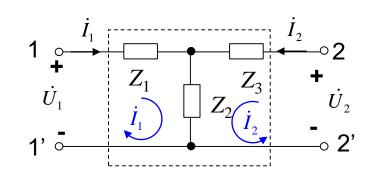
含受控源时, $Y_{12} \neq Y_{21}$

T形电路

网孔电流方程:

$$\dot{U}_1 = (Z_1 + Z_2)\dot{I}_1 + Z_2\dot{I}_2$$

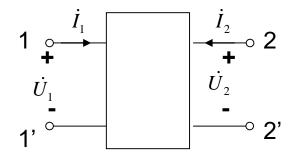
$$\dot{U}_2 = Z_2\dot{I}_1 + (Z_2 + Z_3)\dot{I}_2$$



前面已知:

$$\dot{U}_{1} = Z_{11}\dot{I}_{1} + Z_{12}\dot{I}_{2}$$

$$\dot{U}_{2} = Z_{21}\dot{I}_{1} + Z_{22}\dot{I}_{2}$$



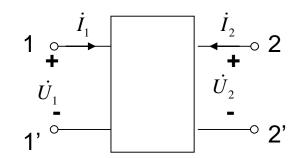
则有:

$$Z_1 = Z_{11} - Z_{12}$$
 $Z_2 = Z_{12}$
 $Z_3 = Z_{22} - Z_{12}$

若二端口内部含有受控源 $Z_{12} \neq Z_{21}$

$$\dot{U}_{1} = Z_{11}\dot{I}_{1} + Z_{12}\dot{I}_{2}$$

$$\dot{U}_{2} = Z_{21}\dot{I}_{1} + Z_{22}\dot{I}_{2}$$

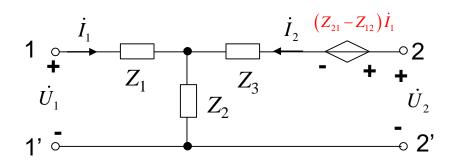


先构建一个不含受控源的电路,再加上受控源

$$\dot{U}_{2} = \mathbf{Z}_{12}\dot{I}_{1} + \mathbf{Z}_{22}\dot{I}_{2} + (\mathbf{Z}_{21} - \mathbf{Z}_{12})\dot{I}_{1}$$

$$\dot{U}_{2} - (Z_{21} - Z_{12})\dot{I}_{1} = Z_{12}\dot{I}_{1} + Z_{22}\dot{I}_{2}$$

$$Z_1 = Z_{11} - Z_{12}$$
 $Z_2 = Z_{12}$
 $Z_3 = Z_{22} - Z_{12}$



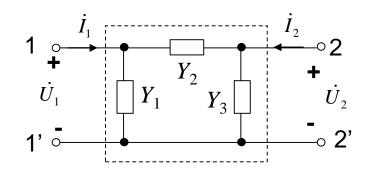
π形电路

由例16-1,

$$Y_{11} = Y_1 + Y_2$$

$$Y_{21} = -Y_2$$

$$Y_{22} = Y_2 + Y_3$$



则有:

$$Y_1 = Y_{11} + Y_{12}$$

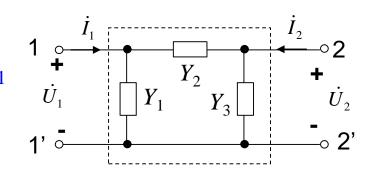
 $Y_2 = -Y_{12} = -Y_{21}$
 $Y_3 = Y_{22} + Y_{21}$

π形电路

若二端口内部含有受控源 $Y_{12} \neq Y_{21}$

$$\dot{I}_1 = Y_{11}\dot{U}_1 + Y_{12}\dot{U}_2$$

$$\dot{I}_2 = Y_{21}\dot{U}_1 + Y_{22}\dot{U}_2$$



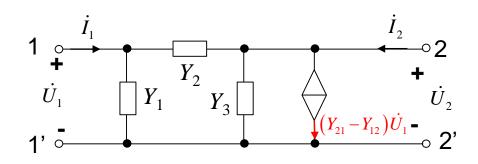
先构建一个不含受控源的电路,再加上受控源

$$\dot{I}_2 = Y_{12}\dot{U}_1 + Y_{22}\dot{U}_2 + (Y_{21} - Y_{12})\dot{U}_1$$

$$\dot{I}_2 - (Y_{21} - Y_{12})\dot{U}_1 = Y_{12}\dot{U}_1 + Y_{22}\dot{U}_2$$

$$Y_1 = Y_{11} + Y_{12}$$

 $Y_2 = -Y_{12} = -Y_{21}$
 $Y_3 = Y_{22} + Y_{12}$



作业

P439

16-9

16-10

下周是最后一节课,答疑。因此本次作业不用交,自行练习、参考书上的答案。