$$BA = \frac{3PL}{16} = \frac{3(16)(14)}{16} = \frac{39,375}{16}$$

$$BC = \frac{-11 \text{ W L}^2}{192} = -\frac{11(3)(12)^2}{192} = -24,75$$

$$CB = \frac{5 \text{ W L}^2}{192} = \frac{5(3)(12)^2}{192} = \frac{11,25}{192}$$

$$CD = -\frac{\text{W L}^2}{30} = \frac{-1.5(14)^2}{30} = -9.8$$

$$EI_1 = \frac{29000(800)}{12^2} = \frac{161 \text{ HI}}{12^2}$$

$$EI_2 = \frac{2900(1600)}{12^2} = \frac{322 \text{ 222}}{122}$$

$$EI_3 = \frac{2900(1600)}{12^2} = \frac{322 \text{ 222}}{12^2}$$



EI = 29000 (300)= 161 H1,111

EI<sub>2</sub> = 2900 (1600) = 322 222.

## MOMENTOS

MBA = 34 523,809 (AB) + 39,375 = 34 523,809 BB + 39,375 MBA = 157,52 K. FE

Mgc = 53 703,704 (208 + Oc - 0,010416) -24,75

MBC = 107 407, 4080B + 53 703,7040c - 584, 128 = - 157,56 K. Ft

McB = 53 703,704 (20c + 08 -0,010416) +11,25

MCB = 107 407, 408 02 + 53 703, 704 08 - 548, 128 = -246, 313 K. FE

MED = 23015,873 (20c + 0,0089 28) -9,8

McD = 46 031,746 Ac + 195,686 = 246,275 K. St

MDC = 23015,873 (Oc + 0,008928) + 14,7

MDC = 23015,8730 C + 220,186 = 245,48 K. Ft

## ECUACIONES

MBA + MBC = 0

 $34523.809 \theta_{B} + 39.375 + 107407.408 \theta_{B} + 53703.7048$ -584.128 = 0

141 931,217 AB + 53 703,704 Ac = 544,753

McB + McD = 0

107 407, 408 0c + 53 703, 704 0B - 548, 128 + 46 031, 746 0c + 195, 686 = 0

53 703, 704 AB + 153 439, 154 De = 352, 442

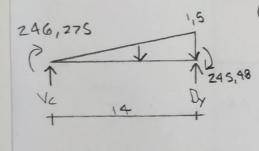
08 = 0,003422

0 = 0,001099

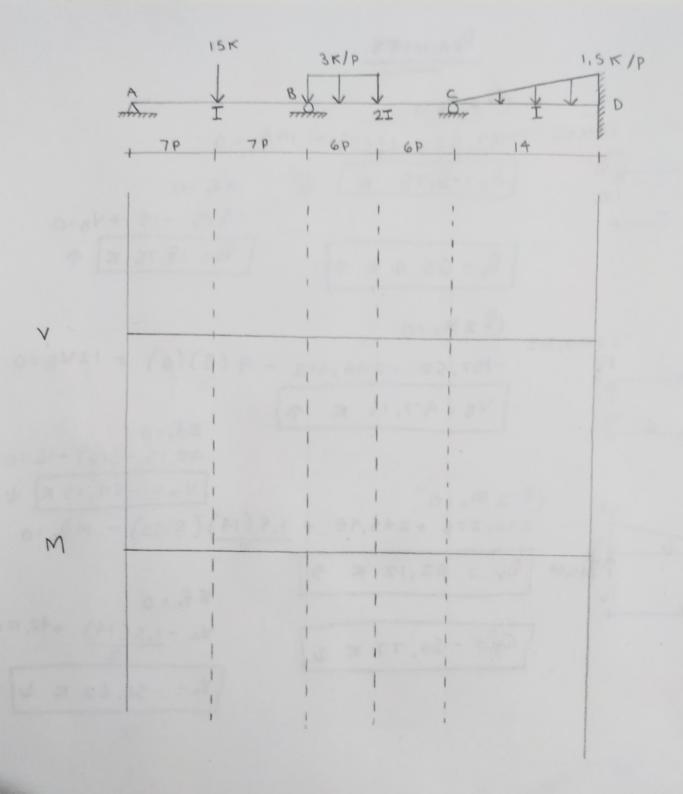
# REACIONES

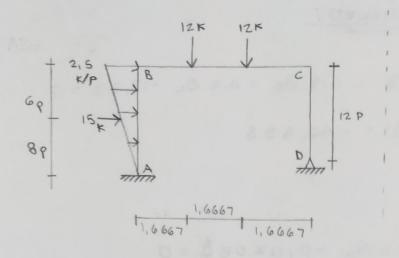
$$-157.52 - 246.313 - 9(3)(6) + 12V_8 = 0$$

$$V_8 = 47.15 \times \Lambda$$



By =





## FEM

$$AB = -\frac{WL^{2}}{30} - \frac{Pb^{2}a}{L^{2}} = -\frac{2.5(14)^{2}}{30} - \frac{15(6)^{2}(8)}{14^{2}} = -38,374$$

$$BA = \frac{WL^{2}}{20} + \frac{Pa^{2}b}{L^{2}} = \frac{2.5(14)^{2}}{20} + \frac{15(8)^{2}(6)}{14^{2}} = 53,888$$

$$BC = -\frac{2PL}{9} = -\frac{2(12)(5)}{9} = -13,33$$

CB = 13,33

## MOMENTOS

MAB = 0,1429 EI (OB - 0,21429A)-38,374 = 0,1429 OB - 0,0306 A - 38,37

MAB = -215,13 K. Ft

MBA = 0,1429 EI (20B - 0,21429A) +53,888 = 0,2858 AB - 0,0306 A + 53,888

MBA = -106,37 K. Ft

MBC = 0,4 EI (20B + Oc) - 13,33 = 0,80B + 0,40c - 13,33

MBC = [106,37 K. Ft]

MCB = 0,4 EI (20c + 0B) + 13,33 = 0,80c + 0,40B + 13,33

MCB = 114, 25 K. Ft

Mco = 0,25 EI(0c - 0,08333A) = 0,250c - 0,02 08A

McD= - 114,25 K. Ft

## ECUACIONES

MBA + MBK = 0

 $0.2868 \, \theta_8 - 0.0306 \, \Delta + 53.888 + 0.8 \, \theta_8 + 0.4 \, \theta_c - 13.33 = 0$   $1.0858 \, \theta_8 + 0.40 \, c - 0.0306 \, \Delta = -40.558$ 

 $M_{CB} + M_{CD} = 0$   $0.8\theta_{c} + 0.4\theta_{B} + 13.33 + 0.25\theta_{c} - 0.0208\Delta = 0$   $0.4\theta_{B} + 1.05\theta_{c} - 0.0208\Delta = -13.33$ 

$$\begin{array}{c}
M_{RA} \\
M_{AR} \\
M_{AB} \\
M_{A$$

 $52F_{x} = 0$  17.5 + 15 - Ax - Dx = 0 32.5 + MAB + MBA + MCB = 0 14

 $455 + 0,142998 - 0,0306\Delta - 38,374 + 0,285898 - 0,0306\Delta + 53,888 + 0,29179c - 0,0243\Delta = 0$ 

0,4287 08 + 0,2917 Bc - 0,0855 A =-470,514

$$RBC = \frac{4EI}{L} = \frac{4}{16} = 0.25$$

$$R_{CD} = \frac{4 \, \text{EI}}{L} = \frac{4}{12} = 0.3333$$

$$D_{BA} = \frac{R_{AB}}{R_{AB} + R_{BC}} = \frac{0.2308}{0.2308 + 0.25} = 0.48$$

$$D_{CD} = \frac{R_{CD}}{R_{BC} + R_{CD}} = \frac{0.33333}{0.25 + 0.3333} = 0.57$$

$$AB = -\frac{Pb^{2}a}{L^{2}} - \frac{6EIA}{L^{2}} = \frac{-8(7)^{2}(6)}{13^{2}} - \frac{6(29000)(800)(0.4)}{13^{2}(12)^{3}}$$

$$BA = \frac{Pa^{2}b}{L^{2}} - \frac{6EIA}{L^{2}} = \frac{8(6)^{2}(7)}{13^{2}} - \frac{6(29000)(800)(0.4)}{13^{2}}$$

$$BA = 11.93 - 190.44 - \sqrt{13^{2}}$$

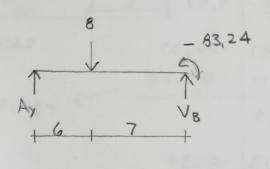
$$BC = -\frac{5WL^2}{192} + \frac{6EIA}{L^2} = -\frac{5(1.5)(16)^2}{192} + \frac{6(29000)(800)(0.4)}{162(12)^3}$$

$$CB = \frac{11 \text{ WL}^2}{192} + \frac{6 \text{ EIA}}{L^2} = \frac{11(1.5)(16)^2}{192} + \frac{6(29000)(300)(0.4)}{16^2(12)^3}$$

$$CD = -\frac{2PL}{9} = -\frac{2(10)(12)}{9} = [-26,67]$$

A	3	
0,48	0,52 ( 2 ) 0,43	0,57 = 2
-204,58 -178,73	115,87 147,87	-26,67 26,67
204,58 30,17	32,69 -52,12	-69.03
102,29	-26,06 16,34	-34,54
-36,59	-39,64 -7,03	-9,31
1,68	-3,51 1,82 -19,82	> -4,65
100	3,32	
-2,04	4,26	5,65
Bullet of Property	-0,19	-0,52
0,09	0,1	0.63
Va 30.3- (2)211	0,23 = > 0,05	> 0,31
-0,11	-0,12 -0,02	-0,03
MAB = 0	MBC = 83,24 K. Ft	Mco = -93,68 K. FE
MBA = -83,24 K.FE	Mc8 = 93,68 K.FE	Moc = -6,82 K. Ft

## REACCIONES



$$-83,24 \quad (\mp E M_{B=0})$$

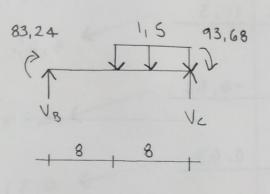
$$-83,24 - 8(7) + 13A_{Y} = 0$$

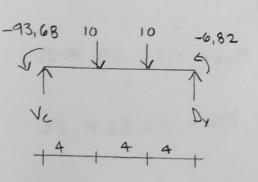
$$A_{Y} = 10,71 \text{ K}$$

$$+$$

$$E F_{Y} = 0$$

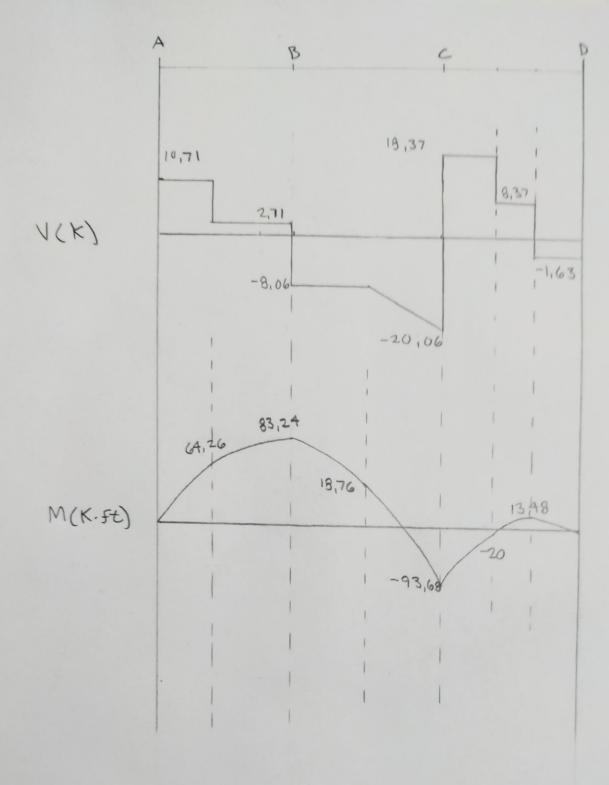
$$B_{V} = -2.71 - 8.06 = 10.71 + V_8 - 8 = 0$$
 $B_{V} = -10.77 \times V$ 
 $V_{B} = -2.71 V$ 

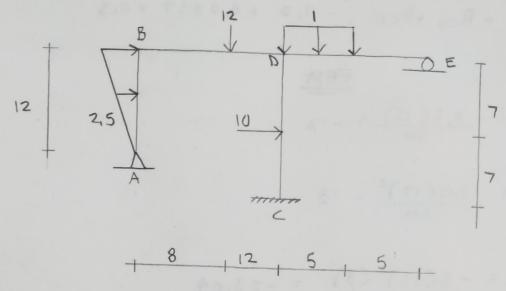




$$(72M_{D=0})$$
 $-6.82-93.68-10(4)-10(8)+12V_{C=0}$ 
 $V_{C=18.37}$ 
 $\Sigma F_{r=0}$ 

$$24y = 0$$
 $18.37 - 20 + D_v = 0$ 
 $D_v = 1.63 KT$ 





$$R_{AB} = 3EI = \frac{3}{12} = 0.25$$

$$R_{BD} = \frac{4EI}{L} = \frac{4}{20} = 0.2$$

$$R_{CD} = \frac{4EI}{14} = \frac{4}{14} = 0.2857$$

$$ROE = \frac{3EI}{L} = \frac{3}{10} = 0.3$$

$$D_{BA} = \frac{R_{AB}}{R_{AB} + R_{BD}} = \frac{0.25}{0.25 + 0.2} = 0.56$$

$$D_{BD} = \frac{R_{BD}}{R_{AB} + R_{BD}} = \frac{0.2}{0.25 + 0.2} = 0.44$$

$$D_{08} = \frac{R_{80}}{R_{80} + R_{c0} + R_{0E}} = \frac{0.2}{0.2 + 0.2857 + 0.3} = 0.26$$

$$D_{DC} = \frac{R_{CD}}{R_{8D} + R_{CO} + R_{DE}} = \frac{0.2857}{0.2 + 0.2857 + 0.3} = 0.36$$

$$D_{DE} = \frac{R_{DE}}{R_{BD} + R_{CD} + R_{CE}} = \frac{0.3}{0.2 + 0.2857 + 0.3} = 0.38$$

$$AB = -WL^2 = -2.5(12)^2 = -12$$

$$BA = \frac{WL^2}{20} = \frac{2.5(12)^2}{20} = 18$$

$$BD = -Pb^{2}a = -8(12)^{2}(8) = -23.04$$

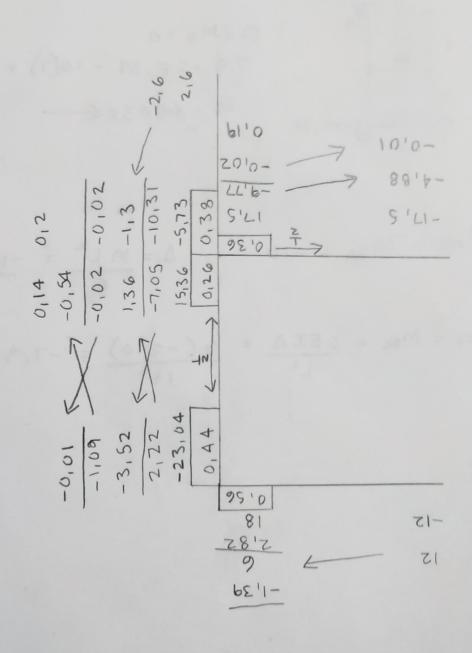
$$DB = \frac{Pa^2b}{L^2} = \frac{8(8)^2(12)}{20^2} = 15,36$$

$$CD = -\frac{PL}{8} = -\frac{10(14)}{8} = -17.5$$

$$DE = -11 WL^{2} = -11(1)(10)^{2} = -5.73$$

$$ED = \frac{5WL^2}{192} = \frac{5(1)(10)^2}{192} = 2.6$$

MOC = 7,9 Mco =



$$\frac{25,43}{25,43} \quad \text{(FEMB=0)}$$

$$\frac{25,43}{25,43} + \frac{2,5(12)}{2}(4) + 12A \times = 0$$

$$Ax = 2,88 \times 4$$

$$7 = 10$$

$$7,9 = 0$$

$$7,9 = 22,39 = 10(7) + 14 Cx = 0$$

$$Cx = 64.03K$$

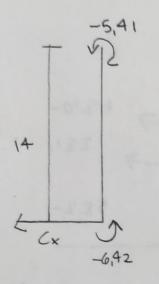
$$Cx = 64.03K$$

$$M_{AB} = M_{BA} = -10$$
  $\Delta = M_{C}^{2} = -10(12)^{2} = -240$ 

$$M_{cD} = M_{DC} = \frac{GEIA}{L^2} = \frac{G(-240)}{14^2} = -7.35$$

		~	P8.0					
3		4 4					1	
2,03	0	-5,41						
							he was	
1,	0	0						
N DE	MEDI	30 c -					80'0	101-
2	_						14110	7 6210-
							p L'0-	1135 6
				00	1	,	5912	7
				80'0	-0.84	2,79	5E'L-	9214-
				0	1	100	98'0 =	
				5 -	12 2	1,91		State .
	~			0,05	15'0-	- 0		
MB0 = 4,77	3,38			0 1	1, 1	1/1		
4					V	-In		
0	MOB			V	/\ v			
NB	8				14	1 4	702001 -	
_	_			0,12	-0,42	4,4		
				0 0	10	4 0	2010	
				3 000			95.0	
							9'5	VI-
							29'0-	
	11						91'0	
	The second second							

$$-4.77$$
 ( $\pm 2M_{B=0}$ )
 $-4.77 + 12A \times = 0$ 
 $A \times = 0.3975 \leftarrow$ 
 $A \times = 0.3975 \leftarrow$ 



$$-5.41$$

$$-5.41 - 6.42 + 14 Cx = 0$$

$$Cx = 0.845 \leftarrow$$

# MOMENTO FINALES

MAB = MED = 0

MBA = 25,43 + 12,9497 (-4,77) = -36,34 K. Ft

MBD = -25,44 + 12,9497 (4,77) = 36,34 K. Ft

MOB = 9,25 + 12,9497 (3,38) = 53,02 K. Ft

MDE = -17,16 + 12,9497 (2,03) = 9,13 K. FE

MOC = 7,9 + 12,9497 (-5,41) = -62,16 K. Ft

McD = -22,39 + 12,94 97 (-6,42) = -105,53 K. Ft

$$\begin{array}{c} 3 \\ 7 \\ \hline \end{array}$$

$$\begin{array}{c} 3 \\ \hline \end{array}$$

$$\begin{array}{c} 5 \\ \hline \end{array}$$

## ELEMENTO 1

$$K_{1} = \begin{bmatrix} 0.045 & -0.089 & -0.045 & 0.089 \\ -0.089 & 0.179 & 0.089 & -0.179 & 2 \\ -0.045 & 0.089 & 0.045 & -0.089 & 3 \\ 0.089 & -0.179 & -0.089 & 0.179 & 4 \end{bmatrix}$$

$$\lambda_{X} = \frac{-2}{2} = -1$$

$$\lambda_{Y} = 0$$

$$\lambda_{X} = \frac{-2}{2} = -1$$

$$\lambda_{X$$

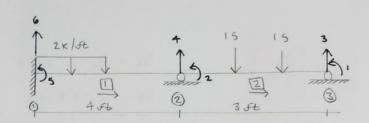
## ELEMENTO 4

### ELEMENTO S

$$\lambda_{x} = \frac{A}{6,4031} = 0.6247 \qquad \lambda_{y} = \frac{-6}{6,4031} = -0.7809 \qquad \frac{L}{AE} = 6.403$$

$$\begin{cases} 5 & 6 & 7 & 8 \\ 0.061 & -0.076 & -0.861 & 0.076 \\ -0.076 & 0.095 & 0.076 & -0.095 & 6 \\ -0.061 & 0.076 & 0.061 & -0.076 & 7 \\ 0.076 & -0.095 & -0.076 & 0.095 & 8 \end{cases}$$

			1	2	3	4	5	6	7	00	
	57		0,545	-0,089	-0,045	0,089	-0,5	0	0	07	[D, ]
7	3		-0.089	0,179	0,089	-0,179	٥	0	0	0	02
0	3		-0.045	0,689	0,245	-0,089	Ó	0	-0,2	0	D3
1	)	11	0,089	-0,179	-0,089	0,429	۵	-0,25	0	0	D <sub>4</sub>
16	SS		-0,5	0	0	0	0,561	-0,076	-0,061	0.076	0
6	26		0	0	0	-0,25	-0.076	0,345	0.076	-0,095	0
0	7		0	0	-0,2	0	-0,061	0,076	0,261	-0.076	0
La	8		0	0	0	0	0,076	-0.095	-0,076	0,095	0



ELEMENTO Z

6 5 4 2

$$K_1 = \begin{bmatrix} 0.19 & 0.38 & -0.19 & 0.38 & 0.5 \\ 0.19 & 0.38 & 1 & -0.38 & 0.5 \\ -0.38 & 1 & -0.38 & 0.5 \\ 0.38 & 0.49 & -0.38 & 1 \\ 0.38 & 0.6 & -0.38 & 1 \end{bmatrix} = \begin{bmatrix} 0.44 & 0.67 & -0.44 & 0.67 \\ 0.67 & 1.33 & -0.67 & 0.67 \\ -0.44 & -0.67 & 0.44 & -0.67 \\ 0.167 & 0.167 & -0.67 & 1.33 \\ 0.167 & 0.167 & -0.67 & 1.33 \\ 0.167 & 0.167 & -0.67 & 1.33 \\ 0.167 & 0.167 & 0.067 & 0.067 \\ 0.1667 & 0.1292 & 0.15 & 0.375 \\ 0.167 & 0.1292 & -0.1444 & 0.632 & -0.1375 & -0.188 \\ 0.167 & 0.1375 & 0 & -0.138 & 0.375 & 0.188 \\ 0.187 & 0.1375 & 0 & -0.188 & 0.375 & 0.188 \\ 0.188 & 0.375 & 0.188 & 0.375 & 0.188 \\ 0.188 & 0.375 & 0.188 & 0.375 & 0.188 \\ 0.188 & 0.375 & 0.188 & 0.375 & 0.188 \\ 0.188 & 0.$$

$$f_{12} = \frac{-11 \text{ WL}^2}{192} = \frac{-11(2)(4)^2}{192} = -1.8333$$
  $f_{21} = \frac{5 \text{ WL}^2}{192} = \frac{5(2)(4)^2}{192} = 0.8333$ 

$$f_{23} = -PL = -15(3) = -15$$

(2)

$$\begin{array}{c} 0,8333\\ -15 \end{array}$$

$$\begin{array}{c} 0,8333\\ -15 \end{array}$$

$$\begin{array}{c} -14,1667\\ \hline 0 \end{array}$$

$$\begin{array}{c} 0\\ 12,394 \end{array}$$

$$\begin{array}{c} -2,606\\ 15 \end{array}$$

$$\begin{bmatrix} 0 \\ -14,1667 \end{bmatrix} = \begin{bmatrix} 1,333 & 0,667 \\ 0,667 & 2,333 \end{bmatrix} \begin{bmatrix} D_1 \\ D_2 \end{bmatrix}$$

$$D_1 = 3.541675$$
 $D_2 = -7.08335$ 

$$\begin{bmatrix} 0_3 \\ Q_4 \\ 0_5 \\ Q_6 \end{bmatrix} = \begin{bmatrix} -0.667 & -0.667 \\ 0.292 \\ 0.375 \end{bmatrix} \begin{bmatrix} 3.54.675 \\ -7.08335 \\ 0_6 \end{bmatrix} \begin{bmatrix} Q_3 = 2.361 \\ -7.08335 \\ Q_6 = -3.545 \\ Q_6 = -2.65 \end{bmatrix}$$

$$Q_3 = 2.361$$

$$Q_4 = 0.1295$$

$$Q_5 = -3.542$$

$$Q_6 = -2.656$$

R3 = 2,361 + 15 = 17,361 K1

R4 = 0,295 + 12,394 = 12,689 KA

Rs = 3,542 -1,8333 = 1,7087 K. Ft (7

R6 = 63,95 R11 = 6,000