

ECGR 2254 – Project 1

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Problem 1 A

A: Find the Amplitude of the steady state current.

$$R1 = 0.1$$

$$VS = (480*\sqrt{2})$$

$$EQ = R1 + (\Omega * L * j)$$

$$Amp = VS / \text{abs}(EQ);$$

$$Amp = 480*\sqrt{2} / \text{abs}(0.1 + (\Omega * L * j))$$

$$Amp = 480\sqrt{2} / (\text{abs}(0.1 + 1.6965j))$$

$$Amp = 399.4472$$

The formula, EQ, comes from turning the resistors into phasor domain and multiply the inductor L by Ω and j as well as adding it the whole thing by R1. The magnitude of the steady state is found by multiplying 480 and the square root of 2 together, and dividing the whole thing by the magnitude of the impedance, which is the absolute value of the formula EQ.

B: Differential Equation

Using KVL, the differential equation for the RL circuit would be in this form:

$$Vs(t) = (R * I) + L \frac{di}{dt}$$

C: Determine an appropriate time step

$$\Omega = 2 * \pi * 60$$

$$\tau = L / R1;$$

$$T = 2 * \pi / \Omega;$$

%Time Step

$$\Delta t = T / 100;$$

$$t = [0 : \Delta t : 35 * \tau];$$

R2 was not included because, when the switch is open R1 is the only resistor that is connected to the circuit at the time. I choose this as my time step, since the period is much smaller than the τ in this problem.

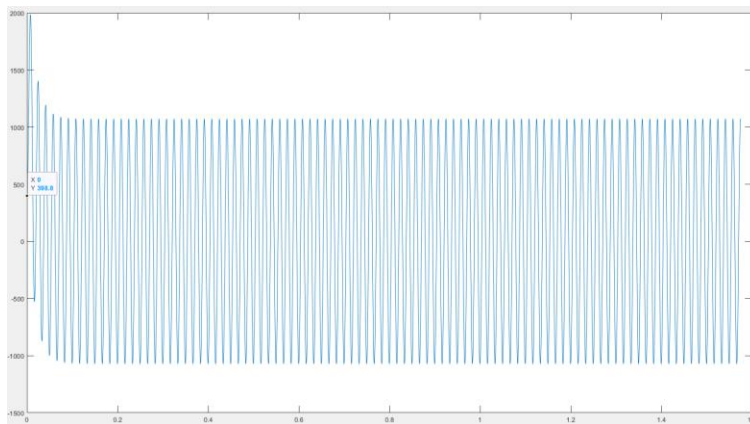
D: Find $I(s)$ with a MATLAB script

```
Phi = 90;
A = T/Delta;
IS= zeros(size(t));
x = (VS*cos(Omega*t-Phi*pi/180))/R1;
Y0 = abs(Amp)*cos((Omega*t) + (deg2rad(Phi - 86.626)));
for U = 1:length(t)-1;
    if U==1
        IS(1) = Y0(1);
        IS(U+1) = (x(U) - IS(U) + A*IS(U))/A;
    else
        IS(U+1) = (x(U) - IS(U) + A*IS(U))/A;
    end
end
```

The loop was needed to evaluate the differential equation in section B. After testing different values of Φ with the evaluated differential equation, the current had its maximum peak when Φ was equal to 90 degrees.

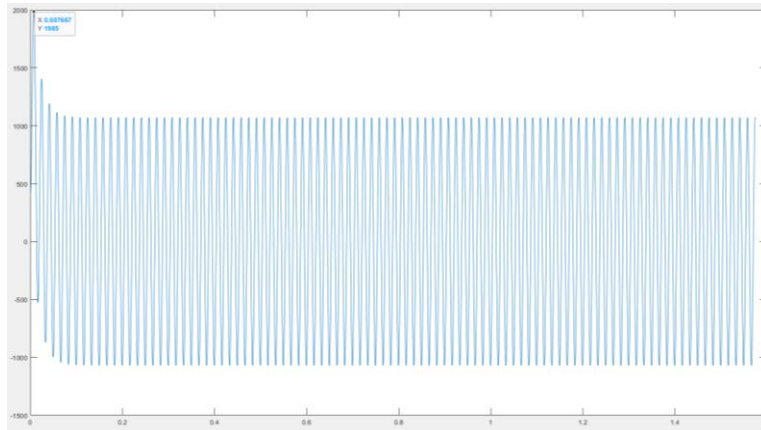
E: Using Φ , find the true value of $I_s(0)$

Using MATLAB, the true value of $I_s(0)$ is at 398.8 Amps.



F: What is the peak current?

The peak current is reached at $t = 7.667\text{ms}$ with a value of 1985 Amps.



Problem 1A Code:

```
clear all;

%Known Variables

L = 4.5*10^-3

R1 = 0.1;

R2 = 23.04;

%Needed Variables

Omega = 2*pi*60;

Tau = L/R1;

T = 2*pi/Omega;

%Time Step

Delta = T/100;

t = [0:Delta:35*Tau];

% VS,EQ and B is used to find the Amplitude of the Steady State

VS = (480*sqrt(2))

EQ = R1+(Omega*L*j);

Amp = VS/abs(EQ);

% Phi, A, IS, x, Y0, and the loop is needed in order to find I(s)

Phi = 90;

A = T/Delta;
```

```

IS= zeros(size(t));
x = (VS*cos(Omega*t-Phi*pi/180))/R1;
Y0 = abs(Amp)*cos((Omega*t) + (deg2rad(Phi - 86.626)));
%Loop
for U = 1:1:length(t)-1;
    if U==1
        IS(1) = Y0(1);
        IS(U+1) = (x(U) - IS(U) + A*IS(U))/A;
    else
        IS(U+1) = (x(U) - IS(U) + A*IS(U))/A;
    end
end
figure(1);
plot(t,IS)

```

Problem 1 B

A: Find the function of the current for $I_s(0)$

$$I_s(0) = \frac{V_s * \cos\left(\Omega * t - \Phi * \frac{\pi}{180}\right)}{R_1}$$

B: Differential Equation

Using KVL, the differential equation for the RL circuit would be in this form:

$$I_s(t) = (R * I) + L \frac{di}{dt}$$

C: Determine an appropriate time step

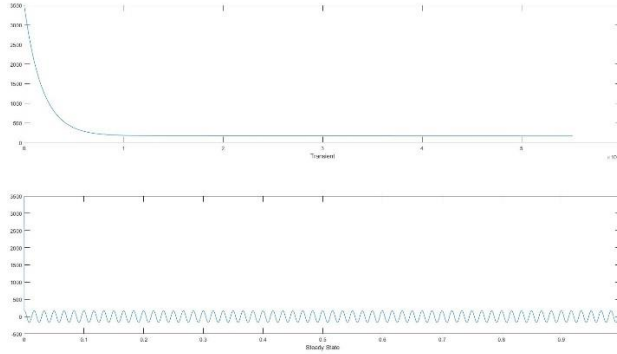
```

Omega = 2*pi*60
Tau = L/R1
T = 2*pi/Omega
%Time Step
Delta = 5*Tau/100
t = [0:Delta:60*T]

```

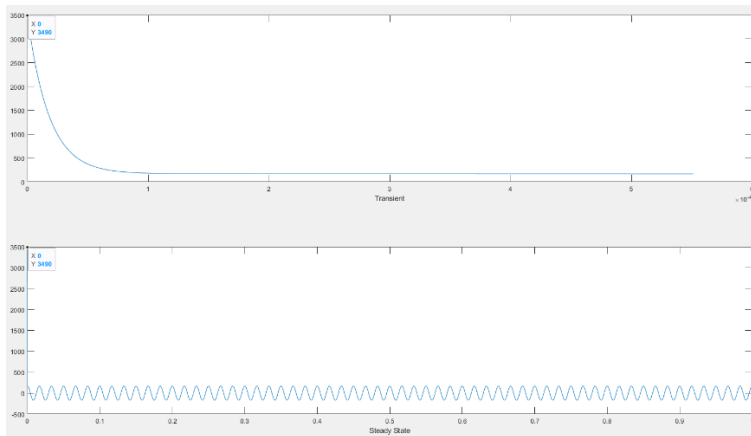
I choose this as my time step, since the tau is much smaller than the period in this problem, and $5\tau/100$ for the Delta is about how long it takes for the initial value to go down to 0.

D: Plot the voltage for $V_L(0)$



E: What is the maximum voltage?

The maximum voltage of the circuit is 3490V when $t = 0$.



Problem 1B Code:

```
clear all;
```

```
%Known Variables
```

```
L = 2.65*10^-3
```

```
R1 = 144;
```

```
R2 = 7.2;
```

```
%Needed Variables
```

```
VS = (480*sqrt(2))
```

```
Omega = 2*pi*60;
```

```
Tau = L/R1;
```

```

T = 2*pi/Omega;
%Time Step
Delta = 5*Tau/100;
t = [0:Delta:60*T];
% Phi, A, VL, x, Y0,xt, and the loop is needed in order to find VL
Phi = 0;
A =Tau/Delta;
V1 = zeros(size(t));
IS = (VS*cos(Omega*t-Phi*pi/180))/R1;
Y0 = 24.49*cos(Omega*t-8.289*pi/180);
xt = (120*sqrt(2))*cos(Omega*t+Phi*pi/180))/R1;
%Loop
for U = 1:1:length(t)-1;
    if U==1
        V1(1) = Y0(1);
        V1(U+1) = (xt(U) - V1(U) + A*V1(U))/A;
    else
        V1(U+1) = (xt(U) - V1(U) + A*V1(U))/A;
    end
end
VL = R1*V1
figure(1);
subplot (2,1,1)
plot(t(1:600),VL(1:600));
xlabel ('Transient');
subplot (2,1,2 )
plot(t,VL);
xlabel('Steady State');

```

Problem 2

A: What is V_{out1} when V_{in_1} is equal to 0V and 5V?

When V_{in1} is equal to 0V, V_{out} is equal 5V and when V_{in1} is equal to 5V, V_{out} is equal to 0V. This is due to the inverter gate causing V_{out} to always have an inverse relationship with V_{in} . When V_{in} is low, V_{out} is high and vice versa.

B: What is the value of the following?

- $V_{th} = 5V$. When the current is high, V_{out} and the Thevenin voltage are equal.
- $R_{th} = 900 \text{ Ohms}$. The Thevenin resistance is the same as Resistor 1 when V_{in} is at 0V.
- $V_{out1} = 5V$. The inverter gate will cause the output to be high when the input is low and vice versa.
- $V_{in2} = 5V$. V_{in2} and V_{out1} are equal.
- $I_L = 5.56 \times 10^{-3} \text{ Amps}$. You need to divide the Thevenin voltage by the Thevenin resistance to get the value of the current.

C: What is the value of the following when V_{in1} is high?

- Differential Equation: $V = \frac{Dv^2}{Dt^2} + \frac{R_{TH}}{L_l} * \frac{Dv}{dt} + \frac{v_{TH}}{L_l C_{GS2}}$
- $V_{in2} = 5V$. Since V_{in1} is high, it will cause V_{out1} to be low. V_{out1} is also inversely proportional to V_{in2} which means V_{in2} will also be high, which is 5V.
- $\frac{Dv_{in2}(0)}{dt} = 0$. The current is currently zero, which means that this formula is also equal to zero.
- $V_{th} = 5$. Voltage cannot change when a capacitor has been charged, which means that the Thevenin voltage stays at 5V.
- $R_{TH} = 90$. The resistors in the circuit become parallel whenever the switch is flipped. The value of Thevenin resistance becomes the inverse of $(1/R_1 + 1/R_2)$.

D: Determine an appropriate time step

$$B = R_{th}/L$$

$$C = V_{th}/(L * Cap);$$

$$s = \text{roots}([1 \ B \ C]);$$

$$\Omega = \text{imag}(s(1));$$

$$\tau = R_{th} * Cap;$$

$$T = 2 * \pi / \Omega$$

$$\% \text{Time Step}$$

$$\Delta = \tau / 1000;$$

$$t = [0:\Delta:50 * T];$$

B and C come from the differential equation stated in Part C. A quadratic equation based on the coefficients of the differential equations can be used to find the roots. Omega is found by taking the imaginary part of the roots. I choose this as my time step, since the period is much smaller than the Tau in this problem.

E: Find Vin2(t) with a MATLAB script

% y1, y2, and x used to solve Voltage

```
y1 = zeros(size(t));
```

```
y2 = zeros(size(t));
```

```
x = ones(size(t));
```

```
%Loop
```

```
for U = 1:length(t)-1;
```

```
    if U==1
```

```
        y1(1) = Y0(1);
```

```
        y2(1) = YPrime(1);
```

```
    else
```

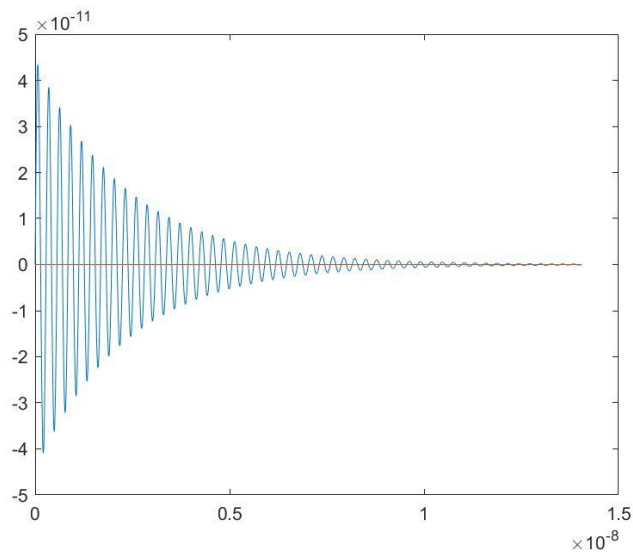
```
        y1(U+1) = y1(U) + Delta*y2(U);
```

```
        y2(U+1) = Delta*(x(U) - B*y2(U) - C*y1(U)) + y2(U);
```

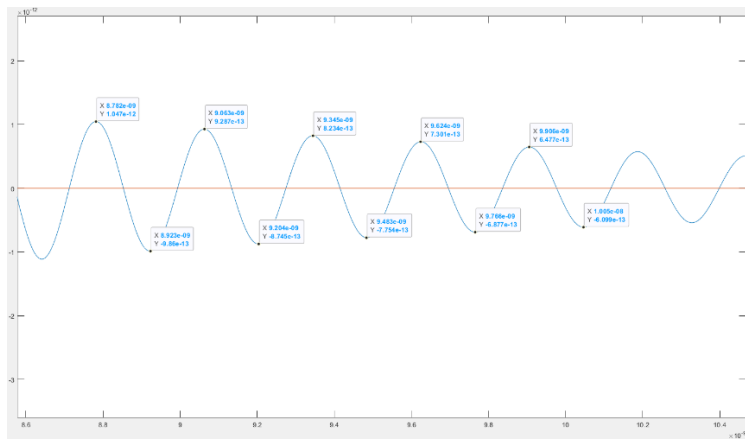
```
    end
```

```
end
```

The loop was needed to evaluate the differential equation in section C.



F: How long does it take for the voltage to remain below 1V?



Based on the peak values at each interval, the waveform stays below 1 volt at around $t = 8.923 \times 10^{-9}$.

Problem 2 Code:

```
clear all

% Known Variables
L = 100*10^-9;
Cap = 0.1*10^-12;
R1 = 100;
R2 = 900;
Rth = (1/R1 + 1/R2)^-1
Y0 = 5;
YPrime = 0;
Vth = 5;

% Needed Variables
B = Rth/L
C = Vth/(L*Cap);
s = roots([ 1 B C]);
Omega = imag(s(1));
Tau = Rth*Cap;
T = 2*pi/Omega
% Time Step
```

```

Delta = Tau/100;
t = [0:Delta:100*T];
% y1, y2, and x used to solve Voltage
y1 = zeros(size(t));
y2 = zeros(size(t));
x = ones(size(t));
%Loop
for U = 1:1:length(t)-1;
    if U==1
        y1(1) = Y0(1);
        y2(1) = YPrime(1);
    else
        y1(U+1) = y1(U) + Delta*y2(U);
        y2(U+1) = Delta*(x(U) - B*y2(U) - C*y1(U)) + y2(U);
    end
end
figure(1);
plot(t,y2,t,x/C)

```

Problem 3

A: Simplify X(t)

Using the double angle formula. X(t) can be rewritten as:

$$X(t) = \frac{X_{audio}}{2 * \cos(4\pi ft)}$$

B: Create vectors

%Time Step

```
t = [0:Delta:Delta*(length(x)-1)];
```

```
Row = transpose(x);
```

```
Out = Row.*(cos(2*pi*frequency*t));
```

```
for U = 1:1:length(t)-1
```

```
    if U==1
```

```
        W(1) = Y0;
```

```
        Z(1) = YPrime;
```

```
    end
```

```
        W(U+1)= W(U) + Delta*Z(U);
```

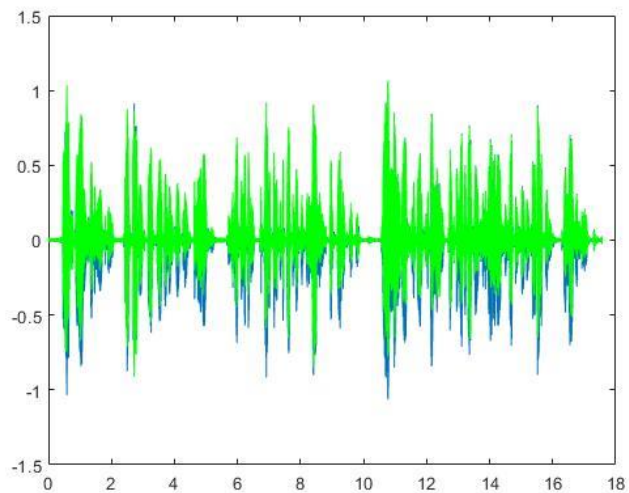
```
        Z(U+1) = Delta*(x(U))+A*W(U)+B*Z(U)+Z(U);
```

```
end
```

C: Differential Equation

The circuit requires a second order differential equation for voltage. The form for this would be:

$$V = \frac{Dv^2}{Dt^2} + \frac{1}{RC} * \frac{Dv}{dt} + \frac{X_{Out}}{LC}, Y(0) = 0, Y'(0) = 0$$



D: Audio Samples

The sound that is played is the Gettysburg address. Xout is a lot louder compared to Xaudio since Xout is being played at a higher frequency as can be seen in the graph above. When changing the frequency around the audio starts to sound very staticky and at some point, distorted. If you change the frequency too much than the audio will sound nothing like the original audio that is expected to play.

Problem 3 Code:

```
clear all;

clear sound;

%Code from project file to play the sound

fileID = fopen('problem3.bin','r');

x=fread(fileID,'single');

fclose(fileID);

%Known Variables

frequency = 50e3;

Amp = 2.205e6;

L = 253.3*10^-6;

R = 11.254;

C = 1*10^-6;

Delta = 1/Amp;

%Needed Variables

Y0 = 0;

YPrime=0;

A = 1/(R*C);%Diff Eq

B = 1/(L*C);%Diff Eq

%Time Step

t = [0:Delta:Delta*(length(x)-1)];

Row = transpose(x);
```

```

Out = Row.*(cos(2*pi*frequency*t));

%Loop
for U = 1:1:length(t)-1
    if U==1
        W(1) = Y0;
        Z(1) = YPrime;
    end
    W(U+1)= W(U) + Delta*Z(U);
    Z(U+1) = Delta*(x(U))+A*W(U)+B*Z(U)+Z(U);
end
x_audio = downsample(Out,100);
sound (x_audio, 22.053e3);
plot(t,x, t,Out, 'g');

```

Problem 4

A: What is X3?

The form needed for this problem is, $X(t) = X_audio * X_3$, however the exponent in $X(t)$ needs to be rid of. By making $X3$ equal the equation below, it will get rid of exponent and allow $Xout = X_audio$.

$$X_3 = \frac{1}{e^{(j * 2 * pi * f * t)}}$$

B: Create Vectors

```

%Code from project file to play the sound
fileID = fopen('problem4.bin','r');
XIN=fread(fileID,'single');
fclose(fileID);

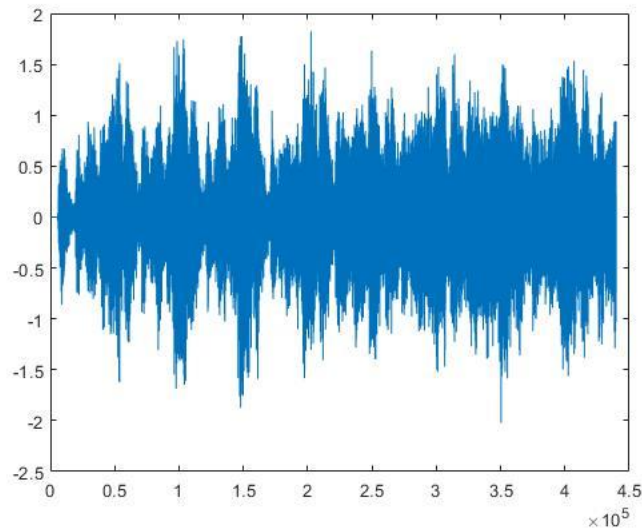
% Vectors
x = (XIN(1:2:length(XIN))+j*XIN(2:2:length(XIN)));
t = [0:Delta:Delta*(length(x)-1)];
x_3 = (1./exp(j*2*pi*frequency*t));
Row = transpose(x);

```

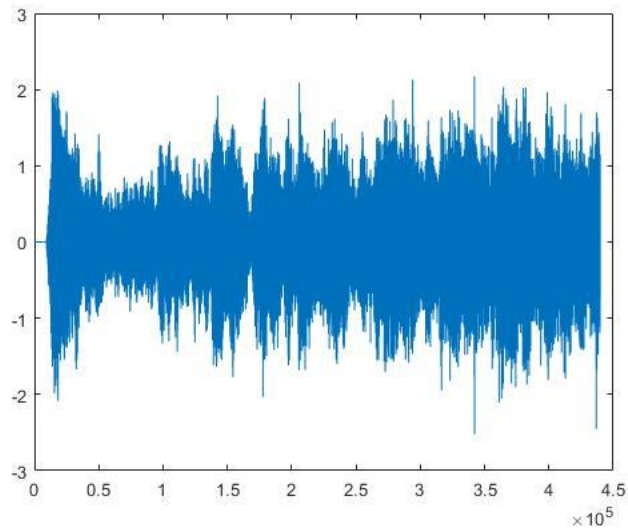
```
Out = Row .*x_3;
```

C: Audio Samples

The imaginary sound sample plays the Imperial March.



The real sound sample plays the Star Wars Theme.



Problem 4 Code:

```
clear all;  
clear sound  
%Code from project file to play the sound  
fileID = fopen('problem4.bin','r');
```

```

XIN=fread(fileID,'single');
fclose(fileID);

%Known Variables
frequency = 50e3;
amp = 2.205e6;
Delta = 1/amp;

% Vectors
x = (XIN(1:2:length(XIN))+j*XIN(2:2:length(XIN)));
t = [0:Delta:Delta*(length(x)-1)];

x_3 = (1./exp(j*2*pi*frequency*t));

Row = transpose(x);

Out = Row .*x_3;

x_audio = downsample(imag(Out),100);
sound (x_audio, 22.053e3);

plot(x_audio);

```