Taller - Series de Tiempo y Python IIE - UNAM

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Abstract Este Notebook incluye una introduccion al manejo de Series de Tiempo con Python

Librerías y Configuración de entorno

```
import numpy as np # Libreria Matematica basica
import pandas as pd # Libreria para manejo, manipulacion y visualizacion de
datos
from pandas import read_excel # funcion para leer archivos de excel

import matplotlib as mpl # Libreria para visualizacion de datos y graficas
import matplotlib.pyplot as plt # Funcion para graficar
import seaborn as sns # Libreria para visualizacion de datos
```

Introducción - Manejo de Datos (Básico)

En esta parte vamos introducir el manejo básico de archivos de texto que pueden contener información asociada a una serie de tiempos, para ello primero instalamos los requerimientos de software.

```
path = 'AirPassengers.csv' # Directorio en el que se encuentra el documento

df = pd.read_csv(path)

df.tail()
```

	Month	#Passengers
139	1960-08	606
140	1960-09	508
141	1960-10	461
142	1960-11	390

```
Month #Passengers

143 1960-12 432
```

De manera similar podemos abrir un archivo tipo .xls y con ello tenemos los 2 archivos mas comunes y básicos de los cuales podemos obtener datos

Nota: En entornos más avanzados es necesario gestionar provenientes de bases de datos, lo cual escapa de las fronteras abarcadas por este curso.

```
# !conda install xlrd -y # Libreria necesaria para poder abrir xls.
#!pip install xlrd -y # Libreria necesaria para poder abrir xls.

dfl = read_excel('AirlineSales.xls')
dfl.head()
```

Dates Observations 0 1971-01-01 112 1 1971-02-01 118 2 1971-03-01 132 3 1971-04-01 129 4 1971-05-01 121

```
#! conda install openpyxl -y
ejemplo2 = read_excel('ClayBricks.xls')
ejemplo3 = read_excel('Electricity.xls')
ejemplo4 = read_excel('MilkProduction.xls')
ejemplo5 = read_excel('JapaneseCars.xls')
ejemplo6 = read_excel('HouseSales.xls')
```

Edicion de datos y Graficas con Pandas

Ahora editemos un par datos de nuestros "Data Frames"

```
df.columns = ['Fechas','Numero de Pasajeros']

df.head()
```

	Fechas	Numero de Pasajeros
0	1949-01	112
1	1949-02	118
2	1949-03	132

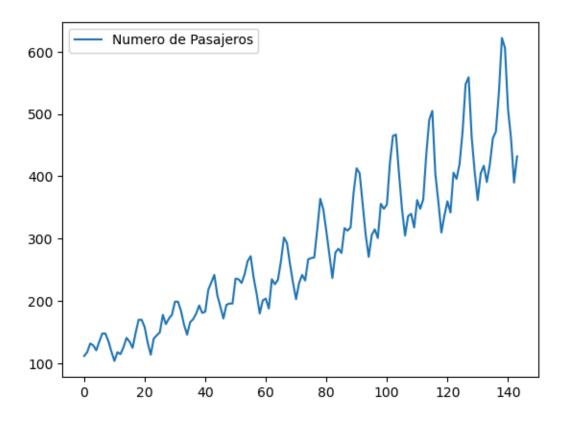
Fechas Numero de Pasajeros 3 1949-04 129 4 1949-05 121

```
dfl.columns = ['Fechas','Numero de Pasajeros']
dfl.tail()
```

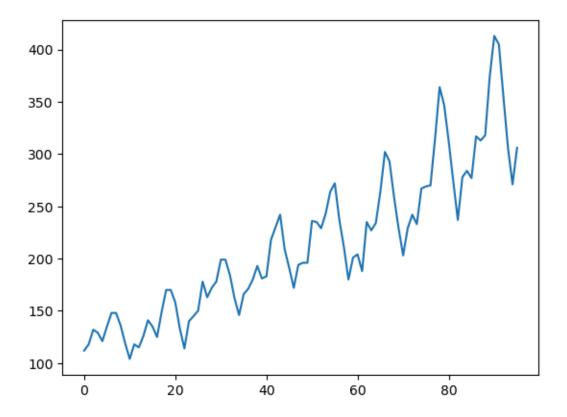
	Fechas	Numero de Pasajeros
91	1978-08-01	405
92	1978-09-01	355
93	1978-10-01	306
94	1978-11-01	271
95	1978-12-01	306

A continuacion vemos que de manera muy sencilla podemos graficar nuestras series de tiempo solamente usando la libreria de Pandas y MatPlotLib cuyo resultado a constinuacion es simple y con poco formato.

```
df.plot()
plt.show()
```



df1["Numero de Pasajeros"].plot()
plt.show()



Para tener una mejor presentacion de los datos vamos a definimos una funcion para graficar nuestros Data Frames/ Series de tiempo.

```
def plot_df(df, x, y, title="", xlabel='Fecha', ylabel='Numero de Pasajeros',
colores="", dpi=100):
   plt.figure(figsize=(15,4), dpi=dpi)
   plt.plot(x, y, color=colores)
   plt.gca().set(title=title, xlabel=xlabel, ylabel=ylabel)
   plt.show()
```

```
plot_df(df, x=df['Fechas'], y=df['Numero de Pasajeros'], title='Tendencia y
Temporalidad', colores="blue")
```



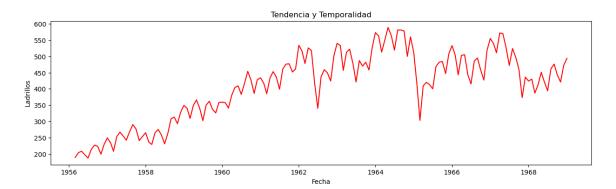
Para el segundo Data Frame

```
plot_df(df1, x=df1['Fechas'], y=df1['Numero de Pasajeros'], title='Tendencia y
Temporalidad', colores="green")
```

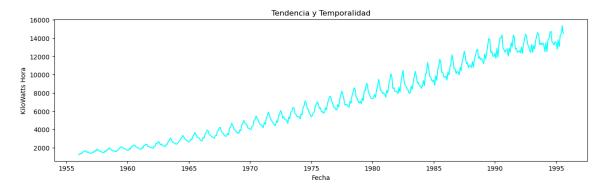


Graficas de Ejemplos

```
plot_df(ejemplo2, x=ejemplo2['Dates'],
y=ejemplo2['Bricks'],ylabel="Ladrillos", title='Tendencia y Temporalidad',
colores="red")
```



```
plot_df(ejemplo3, x=ejemplo3['Month and year'],
y=ejemplo3['Kwh'],ylabel="KiloWatts Hora" ,title='Tendencia y Temporalidad',
colores="cyan")
```



Manejo de Archivos R y Graficas

Ahora vamos a ver como abrir archivos con datos asociados a ST en R, para ello instalamos la siguente libreria en Python o en su defecto trabajar directamente con R Studio o agun FrameWork para R.

```
#!pip install rpy2
%load_ext rpy2.ipython
```

Instalamos e importamos liberias de R que necesitaremos

```
from rpy2.robjects.packages import importr, data
utils = importr('utils')
base = importr('base')
#utils.install packages('stats')
#utils.install_packages('lme4')
#utils.install packages("ggplot2")
#utils.install packages("tseries")
#utils.install packages("fable")
#utils.install_packages("tsibble")
#utils.install packages("dplyr")
#utils.install packages("lubridate")
#utils.install_packages("feasts")
# library(fable) # en un entorno nativo de R se cargan las liberias asi.
#feasts = importr("feasts")
lubridate = importr("lubridate")
dplyr = importr("dplyr")
#tsibble = importr("tsibble")
```

```
#fable = importr("fable")
#tseries= importr("tseries")
stats = importr('stats')
#lme4 = importr('lme4')
#ggplot2 = importr("ggplot2")
```

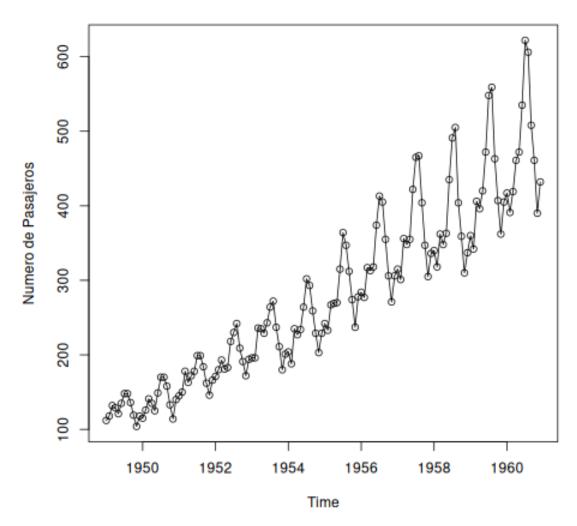
```
%R
airline <- read.csv('AirPassengers.csv')
head(airline)</pre>
```

```
%%R
airline_TS <- ts(airline$X.Passengers,frequency = 12, start = c(1949, 1))
airline_TS
```

```
Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
1949 112 118 132 129 121 135 148 148 136 119 104 118
1950 115 126 141 135 125 149 170 170 158 133 114 140
1951 145 150 178 163 172 178 199 199 184 162 146 166
1952 171 180 193 181 183 218 230 242 209 191 172 194
1953 196 196 236 235 229 243 264 272 237 211 180 201
1954 204 188 235 227 234 264 302 293 259 229 203 229
1955 242 233 267 269 270 315 364 347 312 274 237 278
1956 284 277 317 313 318 374 413 405 355 306 271 306
1957 315 301 356 348 355 422 465 467 404 347 305 336
1958 340 318 362 348 363 435 491 505 404 359 310 337
1959 360 342 406 396 420 472 548 559 463 407 362 405
1960 417 391 419 461 472 535 622 606 508 461 390 432
```

```
%R
plot(airline_TS,type='o',ylab='Numero de Pasajeros',main='Serie de Tiempos
Aerolinea')
```

Serie de Tiempos Aerolinea



Descomposición de Series de Tiempo

En esta parte vamos a ver código que nos genera automáticamente una descomposición de las series temporales que tengamos a nuestra disposición. Lo primero que vamos a hacer es importar la librería statsmodels cuyas rutinas nos serán útiles para modelar ST.

```
#! conda install statsmodels -y
from statsmodels.tsa.seasonal import seasonal_decompose
```

Sabemos que una serie temporal se puede descomponer considerando lo siguiente $X_t=f(T_t,S_t,N_t)$. Los modelos más sencillos consisten en consideran una función aditiva $X_t=$

 $T_t + S_t + N_t$ o multiplicativa $S_t = T_t S_t N_t$, cuyos ejemplos prácticos e implementados automáticamente los encontramos en los siguientes códigos.

Tendencias

existen multiples estrategias para estimar la tendencia de una serie de tiempo, cada una es adaptable dependiendop del tipo de serie que se tenga y el fenomeno que se intenta modelar. Las estrategias mas comunes son las siguientes:

- Calcular la media de los datos.
- Usar algun modelo de regresion.
- Calcular medias moviles dependiendo de patrones estacionales.

A continuación vemos como hacer estos calculos para la TS del ejemplo 2 y 3.

```
ejemplo2["Bricks"].mean()

np.float64(408.7935483870968)

ejemplo3["Kwh"].mean()

np.float64(6903.0672268907565)
```

Medias Moviles

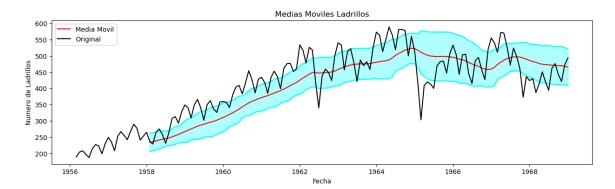
Para calcular medias moviles con Pandas

```
ma_eje1 = ejemplo2["Bricks"].rolling(6).mean()
std_ma_eje1 = ejemplo2["Bricks"].rolling(6).std()
```

Definimos una funcion para graficar la media movil

```
def plot_ts2(df, x, y, title="", xlabel='Fecha', ylabel='Numero de Pasajeros',
    colores="", dpi=100,MA=6):
        ma= y.rolling(MA).mean()
        std_ma=y.rolling(MA).std()
        plt.figure(figsize=(15,4), dpi=dpi)
        plt.plot(x, ma+std_ma, color="cyan")
        plt.plot(x, ma-std_ma, color="cyan")
        plt.fill_between(x, yl=ma+std_ma, y2=ma-std_ma, alpha=0.3, linewidth=2,
    color='cyan')
        plt.plot(x, ma, color="red", label="Media Movil")
        plt.plot(x, y, color=colores, label="Original")
        plt.gca().set(title=title, xlabel=xlabel, ylabel=ylabel)
        plt.legend(loc="best")
        plt.show()
```

```
plot_ts2(ejemplo2, ejemplo2["Dates"], ejemplo2["Bricks"], title="Medias Moviles
Ladrillos", xlabel='Fecha', ylabel='Numero de Ladrillos',
colores="black", MA=24)
```



Creamos una grafica interactiva variando la ventana para el calculo de la media movil

```
import ipywidgets as widgets
def graf_ma(l):
    w=plot_ts2(ejemplo2, ejemplo2["Dates"],ejemplo2["Bricks"], title="Medias
Moviles Ladrillos", xlabel='Fecha', ylabel='Numero de Ladrillos',
colores="black",MA=1)
```

```
widgets.interact(graf_ma, l=(2,24))
```

```
interactive(children=(IntSlider(value=13, description='l', max=24, min=2),
Output()), _dom_classes=('widget-in...
```

```
<function __main__.graf_ma(l)>
```

Usando R

```
%R
BricksTS
```

```
1953 540 533 457 513 522 478 421 487 470 482 458 526

1954 573 563 513 551 589 564 519 581 581 578 500 560

1955 512 412 303 409 420 413 400 469 482 484 447 507

1956 533 503 443 503 505 443 415 485 495 458 427 519

1957 555 539 511 572 570 526 472 524 497 460 373 436

1958 424 430 387 413 451 420 394 462 476 443 421 472

1959 494
```

Descomposicion con Paquetes de Software

Hacemos la descomposicion de la serie de tiempos de pasajeros de aerolinea.

```
# Multiplicative Decomposition
multiplicative_decomposition = seasonal_decompose(df['Numero de Pasajeros'],
model='multiplicative', period=12)

# Additive Decomposition
additive_decomposition = seasonal_decompose(df['Numero de Pasajeros'],
model='additive', period=12)

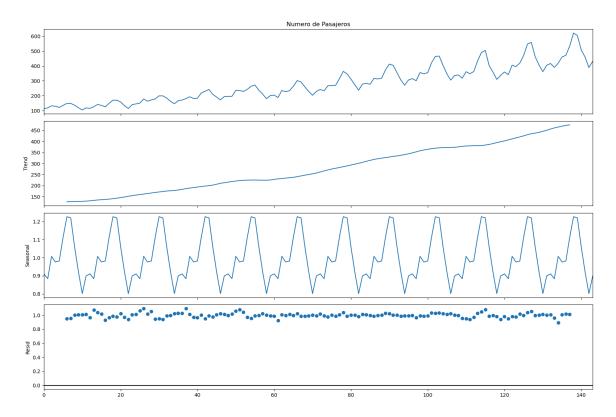
# Plot
plt.rcParams.update({'figure.figsize': (16,12)})

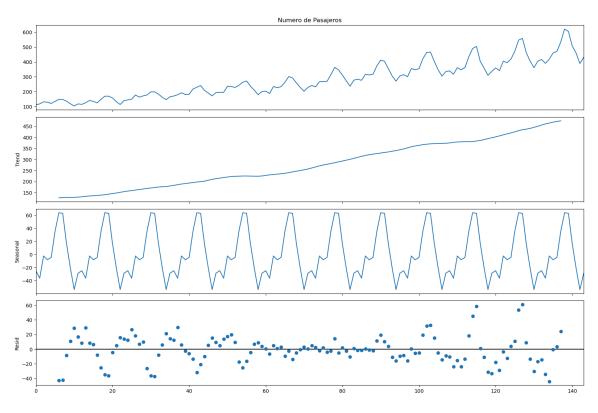
multiplicative_decomposition.plot().suptitle('Descomposición Multiplicativa',
fontsize=16)
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

additive_decomposition.plot().suptitle('Descomposición Aditiva', fontsize=16)
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

plt.show()
```

Descomposición Multiplicativa





Hacemos descomposicion de la serie de tiempo de ladrillos

```
# Multiplicative Decomposition
multiplicative_decomposition2 = seasonal_decompose(ejemplo2['Bricks'],
model='multiplicative', period=12)

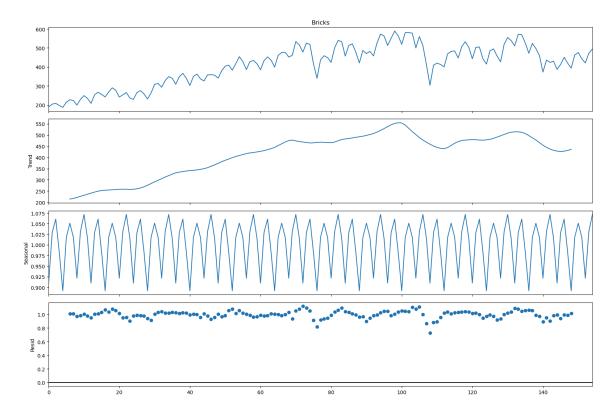
# Additive Decomposition
additive_decomposition2 = seasonal_decompose(ejemplo2['Bricks'],
model='additive', period=12)

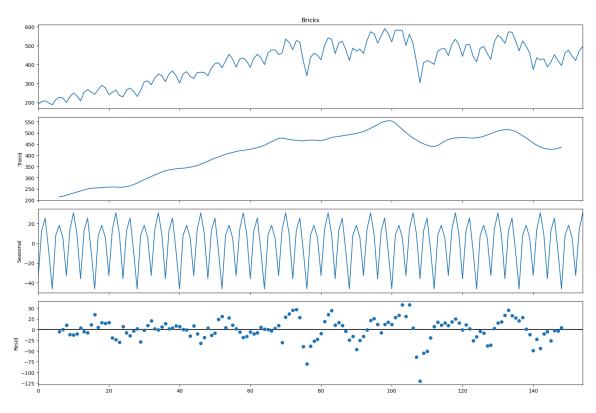
# Plot
plt.rcParams.update({'figure.figsize': (16,12)})
multiplicative_decomposition2.plot().suptitle('Descomposición Multiplicativa',
fontsize=16)
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

additive_decomposition2.plot().suptitle('Descomposición Aditiva', fontsize=16)
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

plt.show()
```

Descomposición Multiplicativa





Descomposicion de la serie de consumo de energia

```
# Multiplicative Decomposition
multiplicative_decomposition3 = seasonal_decompose(ejemplo3['Kwh'],
model='multiplicative', period=12)

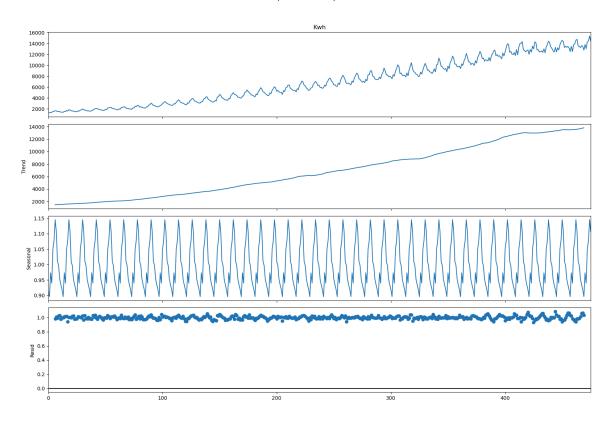
# Additive Decomposition
additive_decomposition3 = seasonal_decompose(ejemplo3['Kwh'],
model='additive', period=12)

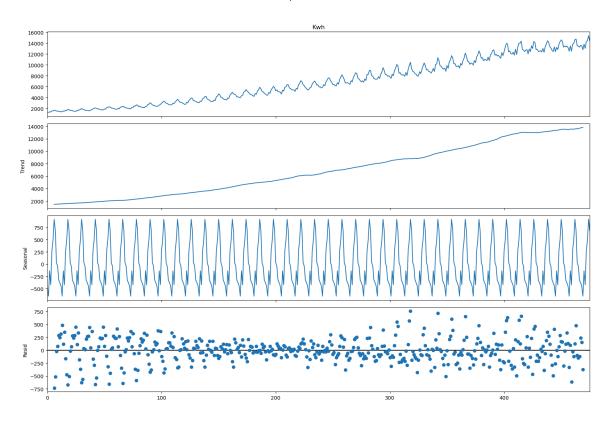
# Plot
plt.rcParams.update({'figure.figsize': (16,12)})
multiplicative_decomposition3.plot().suptitle('Descomposición Multiplicativa',
fontsize=16)
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

additive_decomposition3.plot().suptitle('Descomposición Aditiva', fontsize=16)
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

plt.show()
```

Descomposición Multiplicativa





Descomposicion en R

```
#utils.install_packages("readxl")
#utils.install_packages("TSstudio")

#TSstudio = importr("TSstudio")
readxl = importr("readxl")
```

```
%%R
# Abrimos los archivos .xls
Bricks <- read_excel('ClayBricks.xls')
Electricity <- read_excel('Electricity.xls')

# Construimos la TS

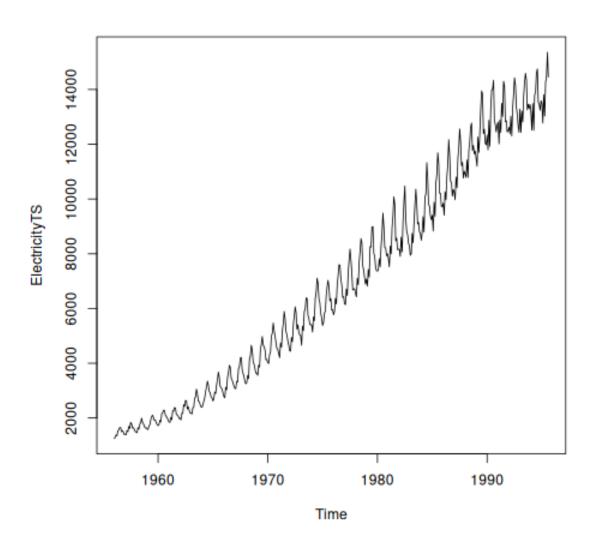
BricksTS <- ts(Bricks$Bricks,frequency = 12, start = c(1946, 3))
ElectricityTS <- ts(Electricity$Kwh,frequency = 12, start = c(1956, 1))

#plot.ts(BricksTS)
plot.ts(ElectricityTS)</pre>
```

```
#ts_decompose(BricksTS, type = "both")
Bricks
```

```
# A tibble: 155 × 2
  Dates
                     Bricks
  <dttm>
                      <dbl>
1 1956-03-01 00:00:00
                      189
2 1956-04-01 00:00:00
                        204
                      208
3 1956-05-01 00:00:00
4 1956-06-01 00:00:00
                      197
5 1956-07-01 00:00:00
                      187
6 1956-08-01 00:00:00
                      214
7 1956-09-01 00:00:00
                      227
8 1956-10-01 00:00:00
                      223
9 1956-11-01 00:00:00 199
10 1956-12-01 00:00:00 229
# i 145 more rows
# i Use `print(n = ...)` to see more rows
```

Además: Hubo 22 avisos (use warnings() para verlos)



```
%R
BricksTS
```

```
Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec

1946 - 189 204 208 197 187 214 227 223 199 229

1947 249 234 208 253 267 255 242 268 290 277 241 253

1948 265 236 229 265 275 258 231 263 308 313 293 328

1949 349 340 309 349 366 340 302 350 362 337 326 358

1950 359 357 341 380 404 409 383 417 454 428 386 428

1951 434 417 385 433 453 436 399 461 476 477 452 461

1952 534 516 478 526 518 417 340 437 459 449 424 501
```

```
1953 540 533 457 513 522 478 421 487 470 482 458 526

1954 573 563 513 551 589 564 519 581 581 578 500 560

1955 512 412 303 409 420 413 400 469 482 484 447 507

1956 533 503 443 503 505 443 415 485 495 458 427 519

1957 555 539 511 572 570 526 472 524 497 460 373 436

1958 424 430 387 413 451 420 394 462 476 443 421 472

1959 494
```

```
%R
BricksTS_Da <- decompose(BricksTS)
BricksTS_Da</pre>
```

```
$x
    Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
1946
            189 204 208 197 187 214 227 223 199 229
1947 249 234 208 253 267 255 242 268 290 277 241 253
1948 265 236 229 265 275 258 231 263 308 313 293 328
1949 349 340 309 349 366 340 302 350 362 337 326 358
1950 359 357 341 380 404 409 383 417 454 428 386 428
1951 434 417 385 433 453 436 399 461 476 477 452 461
1952 534 516 478 526 518 417 340 437 459 449 424 501
1953 540 533 457 513 522 478 421 487 470 482 458 526
1954 573 563 513 551 589 564 519 581 581 578 500 560
1955 512 412 303 409 420 413 400 469 482 484 447 507
1956 533 503 443 503 505 443 415 485 495 458 427 519
1957 555 539 511 572 570 526 472 524 497 460 373 436
1958 424 430 387 413 451 420 394 462 476 443 421 472
1959 494
$seasonal
           Jan
                      Feb
                                 Mar
                                            Apr
                                                       May
                                                                  Jun
1946
                          -36.037800 12.583728 25.465672 -7.898911
1947
     30.851089
                 8.687895 -36.037800 12.583728
                                                 25.465672 -7.898911
1948
     30.851089
                 8.687895 -36.037800
                                      12.583728
                                                 25.465672
                                                            -7.898911
1949
     30.851089
                 8.687895 -36.037800
                                     12.583728 25.465672 -7.898911
1950
     30.851089
                 8.687895 -36.037800 12.583728 25.465672
                                                           -7.898911
1951
     30.851089
                 8.687895 -36.037800
                                      12.583728
                                                 25.465672
                                                            -7.898911
1952
     30.851089
                 8.687895 -36.037800 12.583728 25.465672 -7.898911
1953
     30.851089
                 8.687895 -36.037800 12.583728
                                                 25.465672 -7.898911
1954
     30.851089
                 8.687895 -36.037800 12.583728
                                                 25.465672
                                                            -7.898911
1955
     30.851089
                 8.687895 -36.037800
                                     12.583728
                                                 25.465672
                                                           -7.898911
1956
     30.851089
                 8.687895 -36.037800
                                      12.583728
                                                 25.465672
                                                            -7.898911
1957
     30.851089
                 8.687895 -36.037800
                                     12.583728 25.465672
                                                           -7.898911
1958
     30.851089
                 8.687895 -36.037800
                                     12.583728 25.465672 -7.898911
1959 30.851089
           Jul
                      Aug
                                 Sep
                                            0ct
                                                       Nov
                                                                  Dec
```

```
1946 - 46.343355
                 7.992188
                           18.111506
                                        5.448311 -32.787800 13.927478
1947 -46.343355
                 7.992188
                           18.111506
                                        5.448311 -32.787800 13.927478
1948 - 46.343355
                 7.992188
                            18.111506
                                        5.448311 -32.787800
                                                             13.927478
1949 -46.343355
                7.992188
                                        5.448311 -32.787800 13.927478
                            18.111506
1950 -46.343355
                 7.992188
                            18.111506
                                        5.448311 -32.787800 13.927478
1951 -46.343355
                 7.992188
                            18.111506
                                        5.448311 -32.787800
                                                             13.927478
1952 -46.343355
                 7.992188
                                        5.448311 -32.787800 13.927478
                            18.111506
1953 -46.343355
                 7.992188
                            18.111506
                                        5.448311 -32.787800
                                                             13.927478
1954 - 46.343355
                 7.992188
                            18.111506
                                        5.448311 -32.787800
                                                             13.927478
1955 - 46.343355
                 7.992188
                            18.111506
                                        5.448311 -32.787800
                                                            13.927478
1956 -46.343355
                                        5.448311 -32.787800
                 7.992188
                            18.111506
                                                             13.927478
1957 -46.343355
                 7.992188
                           18.111506
                                        5.448311 -32.787800 13.927478
1958 -46.343355
                7.992188 18.111506
                                        5.448311 -32.787800 13.927478
1959
$trend
                   Feb
                            Mar
                                     Apr
                                              May
                                                       Jun
          Jan
                                                                Jul
                                                                         Aug
1946
                                               NA
                             NA
                                      NA
                                                        NA
                                                                 NA
                                                                           NA
1947 231.0417 235.5833 240.4583 245.3333 249.3333 252.0833 253.7500 254.5000
1948 257.7917 257.1250 257.6667 259.9167 263.5833 268.8750 275.5000 283.3333
1949 318.7083 325.2917 331.1667 334.4167 336.7917 339.4167 341.0833 342.2083
1950 360.4583 366.6250 373.2500 380.8750 387.1667 392.5833 398.6250 404.2500
1951 421.8333 424.3333 427.0833 430.0417 434.8333 438.9583 444.5000 452.7917
1952 473.7917 470.3333 468.6250 466.7500 464.4167 464.9167 466.8333 467.7917
1953 474.4583 479.9167 482.4583 484.2917 487.0833 489.5417 491.9583 494.5833
1954 520.5000 528.5000 537.0417 545.6667 551.4167 554.5833 553.4583 544.6250
1955 477.3750 467.7500 458.9583 450.9167 444.7917 440.3750 439.0417 443.7083
1956 477.2083 478.5000 479.7083 479.1667 477.2500 476.9167 478.3333 480.7500
1957 508.3750 512.3750 514.0833 514.2500 512.0833 506.3750 497.4583 487.4583
1958 437.3333 431.5000 428.0417 426.4583 427.7500 431.2500 435.6667
1959
           NA
                            Nov
          Sep
                   0ct
                                     Dec
1946 214.1250 216.9583 221.4583 226.3333
1947 255.4583 256.8333 257.6667 258.1250
1948 291.0000 297.8333 305.1250 312.3333
1949 344.2500 346.8750 349.7500 354.2083
1950 408.5833 412.6250 416.8750 420.0417
1951 460.7917 468.5417 475.1250 477.0417
1952 467.6250 466.2083 465.8333 468.5417
1953 498.1667 502.0833 506.4583 512.8333
1954 529.5833 514.9167 501.9583 488.6250
1955 453.3333 463.0833 470.5417 475.3333
1956 485.0833 490.7917 496.3750 502.5417
1957 477.7500 465.9583 454.3750 445.0000
1958
           NA
                    NA
                             NA
                                      NA
1959
$random
```

```
Feb
               Jan
                                           Mar
                                                         Apr
                                                                       May
1946
                                            NA
                                                          NA
                                                                        NA
1947
      -12.8927557
                    -10.2712279
                                    3.5794665
                                                  -4.9170612
                                                                -7.7990057
1948
      -23.6427557
                    -29.8128946
                                    7.3711332
                                                  -7.5003946
                                                               -14.0490057
1949
       -0.5594223
                      6.0204388
                                                  1.9996054
                                                                3.7426610
                                   13.8711332
1950
      -32.3094223
                    -18.3128946
                                    3.7877999
                                                -13.4587279
                                                                -8.6323390
1951
      -18.6844223
                    -16.0212279
                                   -6.0455335
                                                  -9.6253946
                                                                -7.2990057
1952
       29.3572443
                     36.9787721
                                   45.4127999
                                                 46.6662721
                                                                28.1176610
1953
       34.6905777
                     44.3954388
                                   10.5794665
                                                 16.1246054
                                                                9.4509943
1954
       21.6489110
                     25.8121054
                                   11.9961332
                                                  -7.2503946
                                                                12.1176610
1955
                    -64.4378946 -119.9205335
        3.7739110
                                                -54.5003946
                                                               -50.2573390
1956
       24.9405777
                     15.8121054
                                   -0.6705335
                                                 11.2496054
                                                                2.2843277
1957
       15.7739110
                     17.9371054
                                   32.9544665
                                                 45.1662721
                                                                32.4509943
1958
      -44.1844223
                    -10.1878946
                                   -5.0038668
                                                -26.0420612
                                                                -2.2156723
1959
                NA
               Jun
                             Jul
                                           Aug
                                                         Sep
                                                                       0ct
1946
                NA
                              NA
                                            NA
                                                  -5.2365057
                                                                 0.5933554
1947
                     34.5933554
                                    5.5078125
                                                 16.4301610
                                                                14.7183554
       10.8155777
1948
       -2.9760890
                      1.8433554
                                   -28.3255208
                                                  -1.1115057
                                                                9.7183554
1949
        8.4822443
                      7.2600221
                                   -0.2005208
                                                  -0.3615057
                                                              -15.3233112
                     30.7183554
1950
       24.3155777
                                    4.7578125
                                                 27.3051610
                                                                9.9266888
1951
        4.9405777
                      0.8433554
                                    0.2161458
                                                  -2.9031723
                                                                3.0100221
1952
      -40.0177557
                    -80.4899779
                                  -38.7838542
                                                -26.7365057
                                                              -22.6566446
1953
       -3.6427557
                    -24.6149779
                                  -15.5755208
                                                -46.2781723
                                                              -25.5316446
                     11.8850221
1954
                                                 33.3051610
                                                                57.6350221
       17.3155777
                                   28.3828125
1955
      -19.4760890
                      7.3016888
                                   17.2994792
                                                 10.5551610
                                                                15.4683554
                    -16.9899779
                                   -3.7421875
                                                  -8.1948390
1956
      -26.0177557
                                                              -38.2399779
                                   28.5494792
                                                  1.1384943
                                                               -11.4066446
1957
       27.5239110
                     20.8850221
1958
       -3.3510890
                      4.6766888
                                            NA
                                                          NA
                                                                        NA
1959
               Nov
                             Dec
1946
       10.3294665
                    -11.2608112
1947
       16.1211332
                    -19.0524779
       20.6627999
                      1.7391888
1948
1949
        9.0377999
                    -10.1358112
1950
        1.9127999
                     -5.9691446
1951
        9.6627999
                    -29.9691446
1952
       -9.0455335
                     18.5308554
1953
      -15.6705335
                     -0.7608112
1954
       30.8294665
                     57.4475221
1955
        9.2461332
                     17.7391888
1956
      -36.5872001
                      2.5308554
1957
      -48.5872001
                    -22.9274779
1958
                NA
                              NA
1959
$figure
 [1] -36.037800 12.583728 25.465672 -7.898911 -46.343355
                                                                   7.992188
```

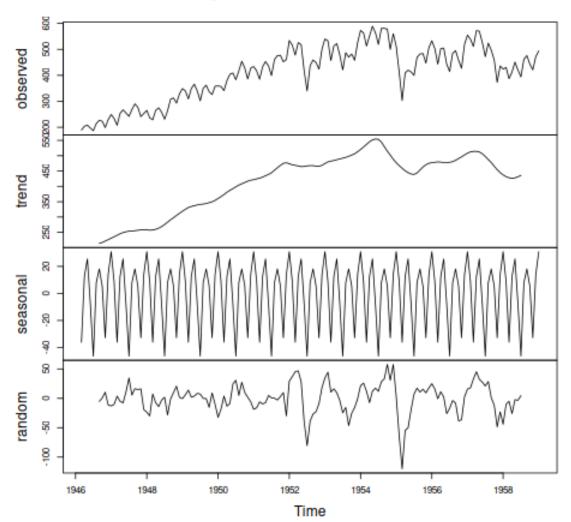
```
[7] 18.111506 5.448311 -32.787800 13.927478 30.851089 8.687895

$type
[1] "additive"

attr(,"class")
[1] "decomposed.ts"
```

```
%%R
plot(BricksTS_Da)
```

Decomposition of additive time series



```
%%R
BricksTS_Dm <- decompose(BricksTS, type = "multiplicative")
BricksTS_Dm</pre>
```

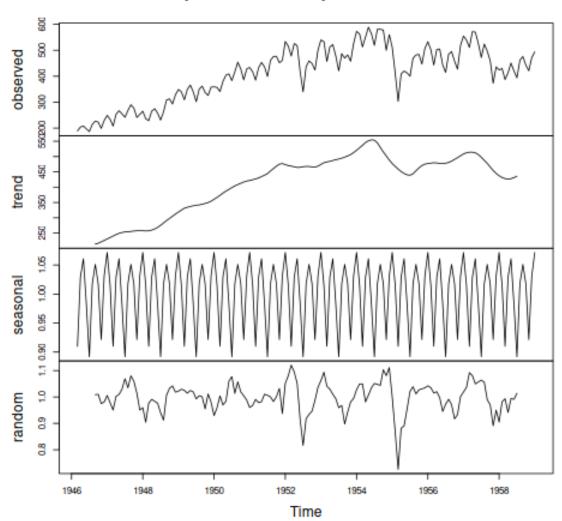
```
$x
     Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
1946
             189 204 208 197 187 214 227 223 199 229
1947 249 234 208 253 267 255 242 268 290 277 241 253
1948 265 236 229 265 275 258 231 263 308 313 293 328
1949 349 340 309 349 366 340 302 350 362 337 326 358
1950 359 357 341 380 404 409 383 417 454 428 386 428
1951 434 417 385 433 453 436 399 461 476 477 452 461
1952 534 516 478 526 518 417 340 437 459 449 424 501
1953 540 533 457 513 522 478 421 487 470 482 458 526
1954 573 563 513 551 589 564 519 581 581 578 500 560
1955 512 412 303 409 420 413 400 469 482 484 447 507
1956 533 503 443 503 505 443 415 485 495 458 427 519
1957 555 539 511 572 570 526 472 524 497 460 373 436
1958 424 430 387 413 451 420 394 462 476 443 421 472
1959 494
$seasonal
           Jan
                     Feb
                               Mar
                                         Apr
                                                   May
                                                             Jun
                                                                        Jul
1946
                         0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1947 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1948 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1949 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1950 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1951 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1952 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1953 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1954 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1955 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1956 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1957 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1958 1.0715541 1.0151491 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431
1959 1.0715541
           Aug
                     Sep
                               0ct
                                         Nov
                                                   Dec
1946 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1947 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1948 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1949 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1950 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1951 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1952 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1953 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1954 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
```

```
1955 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1956 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1957 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1958 1.0176729 1.0509676 1.0175704 0.9216109 1.0311689
1959
$trend
                   Feb
                            Mar
                                                                 Jul
          Jan
                                     Apr
                                              May
                                                        Jun
                                                                          Aug
1946
                             NA
                                      NA
                                               NA
                                                        NA
                                                                  NA
                                                                           NA
1947 231.0417 235.5833 240.4583 245.3333 249.3333 252.0833 253.7500 254.5000
1948 257.7917 257.1250 257.6667 259.9167 263.5833 268.8750 275.5000 283.3333
1949 318.7083 325.2917 331.1667 334.4167 336.7917 339.4167 341.0833 342.2083
1950 360.4583 366.6250 373.2500 380.8750 387.1667 392.5833 398.6250 404.2500
1951 421.8333 424.3333 427.0833 430.0417 434.8333 438.9583 444.5000 452.7917
1952 473.7917 470.3333 468.6250 466.7500 464.4167 464.9167 466.8333 467.7917
1953 474.4583 479.9167 482.4583 484.2917 487.0833 489.5417 491.9583 494.5833
1954 520.5000 528.5000 537.0417 545.6667 551.4167 554.5833 553.4583 544.6250
1955 477.3750 467.7500 458.9583 450.9167 444.7917 440.3750 439.0417 443.7083
1956 477.2083 478.5000 479.7083 479.1667 477.2500 476.9167 478.3333 480.7500
1957 508.3750 512.3750 514.0833 514.2500 512.0833 506.3750 497.4583 487.4583
1958 437.3333 431.5000 428.0417 426.4583 427.7500 431.2500 435.6667
1959
           NA
          Sep
                   0ct
                            Nov
1946 214.1250 216.9583 221.4583 226.3333
1947 255.4583 256.8333 257.6667 258.1250
1948 291.0000 297.8333 305.1250 312.3333
1949 344.2500 346.8750 349.7500 354.2083
1950 408.5833 412.6250 416.8750 420.0417
1951 460.7917 468.5417 475.1250 477.0417
1952 467.6250 466.2083 465.8333 468.5417
1953 498.1667 502.0833 506.4583 512.8333
1954 529.5833 514.9167 501.9583 488.6250
1955 453.3333 463.0833 470.5417 475.3333
1956 485.0833 490.7917 496.3750 502.5417
1957 477.7500 465.9583 454.3750 445.0000
1958
           NA
                    NA
                             NA
1959
$random
                               Mar
                                                                        Jul
           Jan
                     Feb
                                         Apr
                                                   May
                                                              Jun
1946
                                NA
                                          NA
                                                    NA
                                                               NA
                                                                         NA
1947 1.0057614 0.9784564 0.9505620 1.0021680 1.0096513 1.0293562 1.0692326
1948 0.9593187 0.9041445 0.9766393 0.9908053 0.9836831 0.9764250 0.9400550
1949 1.0219224 1.0296180 1.0253422 1.0141778 1.0246139 1.0193313 0.9926801
1950 0.9294484 0.9592158 1.0039487 0.9695667 0.9838387 1.0601348 1.0772019
1951 0.9601404 0.9680529 0.9906154 0.9784845 0.9822360 1.0107245 1.0063846
1952 1.0518159 1.0807223 1.1208807 1.0951611 1.0516287 0.9127053 0.8165446
1953 1.0621396 1.0940358 1.0409104 1.0294066 1.0104334 0.9935915 0.9594374
```

```
1954 1.0273533 1.0493819 1.0497028 0.9812976 1.0071076 1.0348607 1.0513451
1955 1.0009127 0.8676680 0.7254815 0.8814620 0.8902933 0.9543266 1.0214500
1956 1.0423297 1.0355145 1.0148069 1.0201357 0.9976677 0.9452155 0.9727031
1957 1.0188135 1.0362654 1.0923060 1.0809318 1.0494813 1.0570198 1.0637710
1958 0.9047721 0.9816526 0.9935320 0.9411309 0.9940930 0.9910369 1.0139225
1959
           Aug
                     Sep
                               0ct
                                         Nov
                                                   Dec
1946
            NA 1.0087166 1.0100993 0.9750198 0.9811991
1947 1.0347580 1.0801613 1.0598977 1.0148718 0.9505186
1948 0.9121156 1.0070903 1.0327771 1.0419388 1.0184171
1949 1.0050074 1.0005650 0.9547561 1.0113751 0.9801543
1950 1.0136262 1.0572700 1.0193511 1.0046941 0.9881470
1951 1.0004475 0.9829084 1.0004738 1.0322454 0.9371623
1952 0.9179537 0.9339544 0.9464591 0.9876150 1.0369545
1953 0.9675675 0.8977055 0.9434237 0.9812375 0.9946715
1954 1.0482632 1.0438847 1.1031294 1.0808234 1.1114310
1955 1.0386448 1.0116728 1.0271214 1.0307701 1.0343794
1956 0.9913209 0.9709560 0.9170729 0.9334055 1.0015335
1957 1.0562959 0.9898432 0.9701666 0.8907315 0.9501598
1958
                      NA
                                NA
                                          NA
            NA
                                                    NA
1959
$figure
 [1] 0.9100034 1.0290191 1.0606193 0.9827213 0.8919431 1.0176729 1.0509676
 [8] 1.0175704 0.9216109 1.0311689 1.0715541 1.0151491
$type
[1] "multiplicative"
attr(, "class")
[1] "decomposed.ts"
```

```
%%R
plot(BricksTS_Dm)
```

Decomposition of multiplicative time series



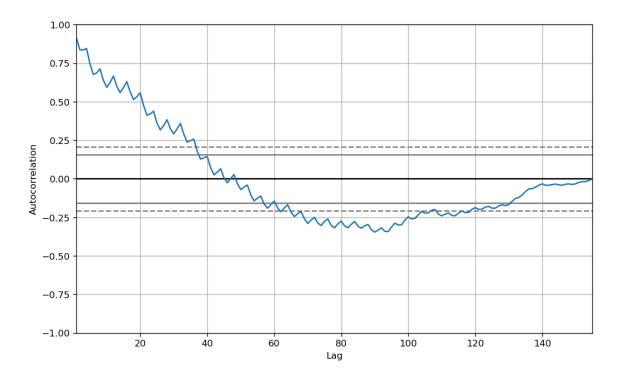
Referencias

- https://rpubs.com/davoodastaraky/TSA1
- $\bullet \ https://www.kaggle.com/code/prashant111/complete-guide-on-time-series-analysis-in-python/notebook \\$
- https://link.springer.com/article/10.1007/s43069-022-00179-z

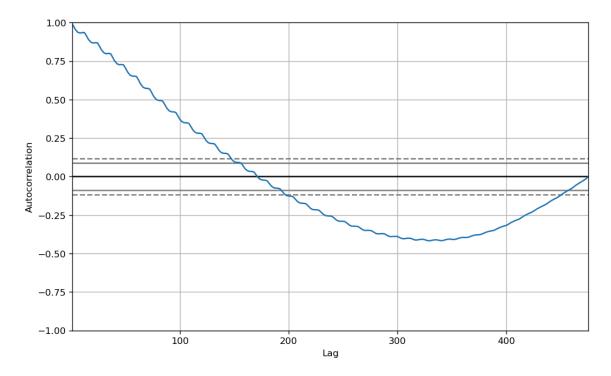
Segunda Parte ACF y PACF

from pandas.plotting import autocorrelation_plot

```
plt.rcParams.update({'figure.figsize':(10,6), 'figure.dpi':120})
autocorrelation_plot(ejemplo2["Bricks"].tolist())
```

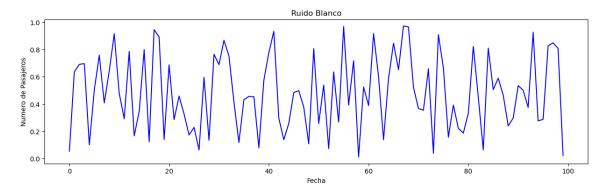


```
plt.rcParams.update({'figure.figsize':(10,6), 'figure.dpi':120})
autocorrelation_plot(ejemplo3["Kwh"].tolist())
```

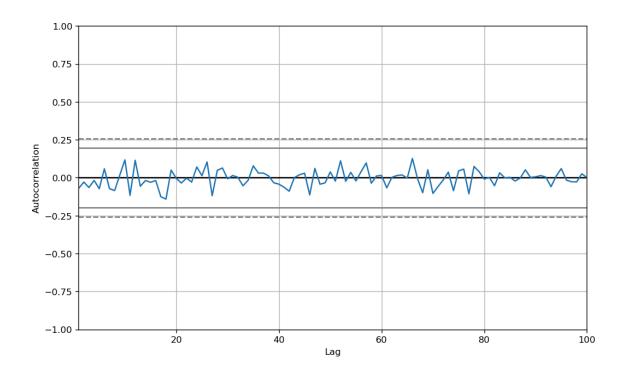


Simulemos un Ruido blanco para poder graficar son ACF

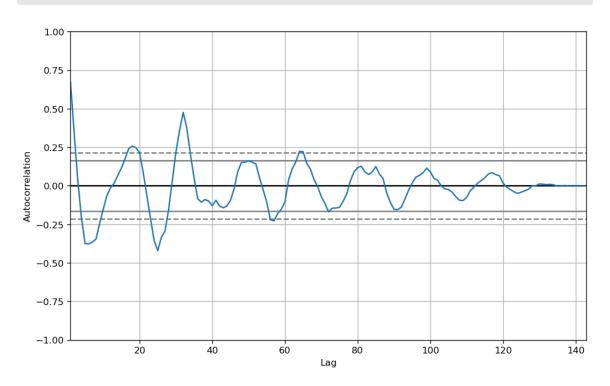
```
n=100
ruido = np.random.rand(n)
ruido_df=pd.Series(ruido)
plot_df(ruido_df, x=range(n), y=ruido_df, title='Ruido Blanco',
colores="blue")
```



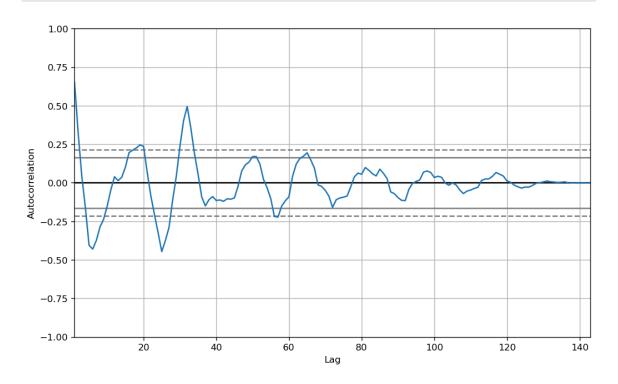
```
autocorrelation_plot(ruido_df)
```



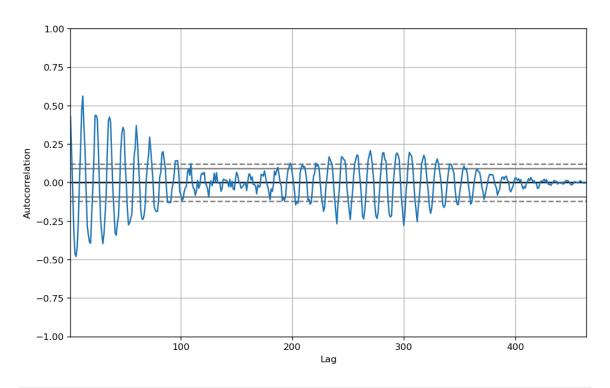
residuos2_1= multiplicative_decomposition2.resid
autocorrelation_plot(residuos2_1.dropna())

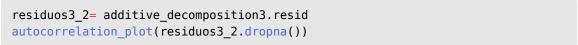


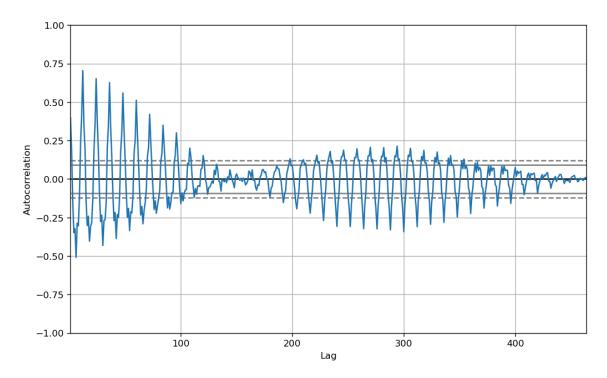
residuos2_2= additive_decomposition2.resid autocorrelation_plot(residuos2_2.dropna())



residuos3_1= multiplicative_decomposition3.resid
autocorrelation_plot(residuos3_1.dropna())



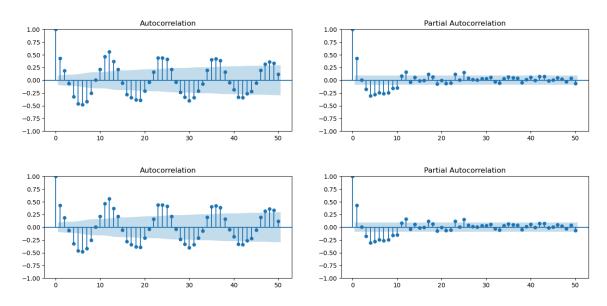




Otro paquete que nos permite graficar la ACF y PACF es statsmodels

```
from statsmodels.tsa.stattools import acf, pacf
 from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
 # Graficas
 fig, axes = plt.subplots(1,2,figsize=(16,3), dpi= 100)
 plot_acf(residuos3_2.dropna(), lags=50, ax=axes[0])
 plot_pacf(residuos3_2.dropna(), lags=50, ax=axes[1])
                       Autocorrelation
                                                                                 Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                            0.75
0.50
                                                            0.50
0.25
                                                            0.25
0.00
                                                            0.00
-0.25
                                                           -0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
-1.00
                                                           -1.00
                       20
                                                                                             30
                                                                                                     40
                                                                                   20
                       Autocorrelation
                                                                                 Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                            0.75
0.50
                                                            0.50
                                                            0.25
0.25
0.00
                                                            0.00
                                                           -0.25
-0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
-1.00
                                                           -1.00
              10
                       20
                                                                          10
                                                                                   20
                                                                                                      40
 fig, axes = plt.subplots(1,2,figsize=(16,3), dpi= 100)
 plot_acf(ejemplo3["Kwh"].tolist(), lags=50, ax=axes[0])
 plot_pacf(ejemplo3["Kwh"].tolist(), lags=50, ax=axes[1])
                       Autocorrelation
                                                                                 Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                            0.75
                                                            0.50
0.50
0.00
                                                            0.00
                                                           -0.25
-0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
                                                           -1.00
-1.00
              10
                                          40
                                                                                                      40
                                                                                 Partial Autocorrelation
                       Autocorrelation
1.00
                                                            1.00
0.75
                                                            0.75
                                                            0.50
0.50
0.25
                                                            0.25
0.00
                                                            0.00
                                                           -0.25
-0.25
-0.50
                                                           -0.50
                                                           -0.75
-0.75
-1.00
              10
                       20
                                30
                                         40
                                                   50
                                                                          10
                                                                                   20
                                                                                             30
                                                                                                      40
                                                                                                              50
```

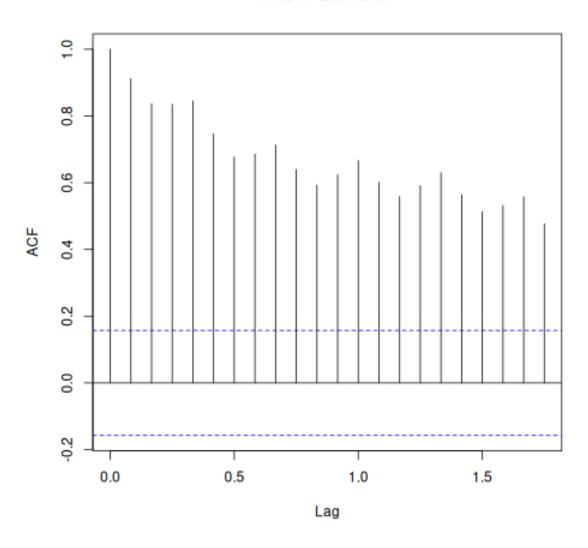
```
fig, axes = plt.subplots(1,2,figsize=(16,3), dpi= 100)
 plot_acf(ruido, lags=49, ax=axes[0])
 plot_pacf(ruido, lags=49, ax=axes[1])
                                                                               Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                           0.75
                                                            0.50
0.25
                                                           0.25
0.00
                                                           0.00
-0.25
                                                           -0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
-1.00
                                                           -1.00
                                                                                                              50
              10
                       20
                                30
                                                                         10
                                                                                            30
                                                                                                     40
                                                                                  20
                       Autocorrelation
                                                                               Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                           0.75
0.50
                                                            0.50
0.25
                                                           0.25
0.00
                                                            0.00
-0.25
                                                           -0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
-1.00
                                                           -1.00
                                                                         10
 fig, axes = plt.subplots(1,2,figsize=(16,3), dpi= 100)
 plot_acf(residuos2_1.dropna(), lags=50, ax=axes[0])
 plot_pacf(residuos2_1.dropna(), lags=50, ax=axes[1])
                       Autocorrelation
                                                                               Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                            0.75
0.50
                                                            0.50
0.25
                                                           0.25
0.00
                                                           0.00
-0.25
                                                           -0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
-1.00
                                                           -1.00
                       20
                                                                         10
                                                                                  20
                       Autocorrelation
                                                                               Partial Autocorrelation
1.00
                                                            1.00
0.75
                                                            0.75
0.50
                                                            0.50
                                                            0.25
                  ••••
0.00
                                      0.00
-0.25
                                                           -0.25
-0.50
                                                           -0.50
-0.75
                                                           -0.75
-1.00
                                                           -1.00
                       20
                                                                                                    40
 fig, axes = plt.subplots(1,2,figsize=(16,3), dpi= 100)
 plot_acf(residuos3_1.dropna(), lags=50, ax=axes[0])
 plot_pacf(residuos3_1.dropna(), lags=50, ax=axes[1])
```



ACF y PACF en R

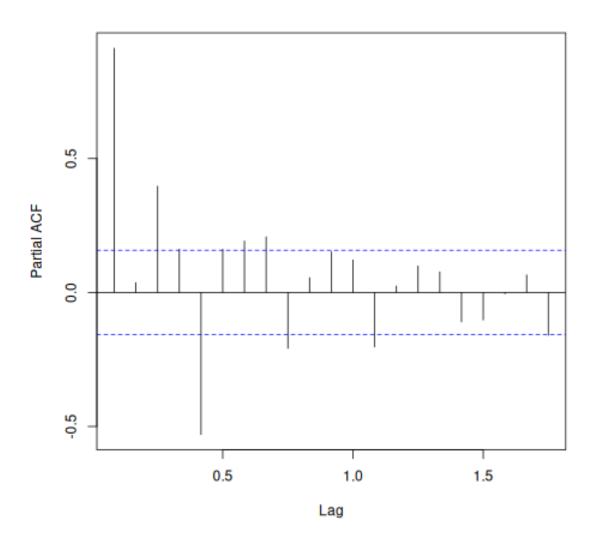
```
%R
acf(BricksTS)
```

Series BricksTS



```
%%R
pacf(BricksTS)
```

Series BricksTS



Session

```
import session_info
session_info.show(html=False,excludes=['dplyr','readxl','utils','base','stats','lubridate'])
```

```
ipywidgets 7.8.5
matplotlib 3.10.6
numpy 2.3.3
pandas 2.3.3
rpy2 NA
```

```
seaborn
                   0.13.2
session_info
                   v1.0.1
statsmodels
                   0.14.5
IPython
                   9.6.0
                   8.6.3
jupyter_client
                  5.8.1
jupyter_core
jupyterlab
                  4.4.9
notebook
                   7.4.7
Python 3.13.5 | packaged by conda-forge | (main, Jun 16 2025, 08:27:50) [GCC
13.3.0]
Linux-6.8.0-85-generic-x86_64-with-glibc2.39
Session information updated at 2025-10-13 04:55
```