

TAREA II

6) Serie de Taylor

a) Orden 3 de $f(x) = xe^x$ ^{alrededor de $y=0$}
Usa la aprox para $0.1 \sqrt{e}$

$$\begin{aligned} f(x) &= xe^x & f(0) &= 0 \\ f'(x) &= xe^x + e^x & f'(0) &= 1 \\ f''(x) &= xe^x + e^x + e^x & f''(0) &= 2 \\ f'''(x) &= xe^x + e^x + e^x + e^x & f'''(0) &= 3 \\ &= e^x(x+3) \end{aligned}$$

$$g(x) \approx \frac{0}{0!} + 1 + \frac{2}{2!}x^2 + \frac{3}{3!}x^3 = x + x^2 + \frac{x^3}{2}$$

$$g(0.1) = (0.1) + (0.1)^2 + \frac{(0.1)^3}{2} = 0.1 + 0.01 + \frac{0.001}{2} = 0.1105$$

⇒ b) Aproxima $(0.2)^2$, orden 3 alrededor del origen.

$$\begin{aligned} f(x) &= x^2 & f(0) &= 0 \\ f'(x) &= 2x & f'(0) &= 0 \\ f''(x) &= 2 & f''(0) &= 2 \\ f'''(x) &= 0 & f'''(0) &= 0 \end{aligned}$$

$$g(x) = \frac{2(x)^2}{2!} = x^2$$

$$f(0.2) \approx (0.2)^2 = 0.04$$

Decimal a binario.

a) 272

÷	%
136	0
68	0
34	0
17	0
8	1
4	0
2	0
1	0
0	1

$$= 100010000_2$$

b) 16

÷	%
8	0
4	0
2	0
1	0
0	1

$$= 10000_2$$

c) 133

÷	%
66	1
33	0
16	1
8	0
4	0
2	0
1	0
0	1

$$= 10000101_2$$

Decimal a binario.

a) $2.342_{10} = 10.0101$

$$\begin{array}{r} 0.342 \\ \times 2 \\ \hline 0.646 \\ \times 2 \\ \hline 1.366 \\ \times 2 \\ \hline 0.736 \\ \times 2 \\ \hline 1.472 \end{array}$$

b) $1.1134_{10} = 1.00011_2$

$$\begin{array}{r} 0.2268 \\ \times 2 \\ \hline 0.4536 \\ \times 2 \\ \hline 0.9072 \\ \times 2 \\ \hline 1.8144 \\ \times 2 \\ \hline 1.6288 \end{array}$$

c) $23.1213_{10} = 10111.00011$

$$\begin{array}{r} 23 \div 2 \\ \hline 11 \text{ r } 1 \\ 5 \text{ r } 1 \\ 2 \text{ r } 1 \\ 1 \text{ r } 0 \\ 0 \text{ r } 1 \end{array}$$

$$\begin{array}{r} 0.2426 \\ 0.4852 \\ 0.9704 \\ 1.9408 \\ 1.8816 \end{array}$$

Operaciones

a)
$$\begin{array}{r} 110110 \\ + 100100 \\ \hline 10111010 = 90 \end{array}$$

b)
$$\begin{array}{r} 1011010 \\ - 100111 \\ \hline 110011 = 51 \end{array}$$

c)
$$\begin{array}{r} 1110 \\ - 101 \\ \hline 1110 \\ 0000 \\ \hline 1110 \\ 1000110 \end{array}$$

d)
$$\begin{array}{r} 11011 \\ 10 \overline{) 110110} \\ \underline{10} \\ 011 \\ \underline{10} \\ 0 \end{array}$$

Binarias Operaciones (~2)

a) $225 + 76$

$$\begin{array}{r} 11100001 \\ + 1001100 \\ \hline 100101101 \end{array}$$

b) $-225 + 76$

$$\begin{array}{r} -225 = -11100001 \\ (-225)_2 = \boxed{1}0001111 \end{array}$$

c) $225 - 76$

$$\begin{array}{r} 011100001 \\ \boxed{1}10110100 \leftarrow (-76)_2 \\ \hline 1010010101 \\ \hline 149_{10} \end{array}$$

$$\begin{array}{r} + \boxed{1}00011111 \leftarrow (-225)_2 \\ 0101001100 \leftarrow 76 \\ \hline 101101011 \\ \hline 10010101 = 149 \end{array}$$

d) $-225 - 76$

$$\begin{array}{r} 100011111 \\ \boxed{1}10110100 \\ \hline 1011010011 \\ \hline \text{Se desborda} \end{array}$$