

Aproximación

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Input

```
In [4]: #expression = "2*x**3 - 4*Log(x)"
#expression = "x**(1/3)"
#expression = "x**3*Log(x)"
expression = "(E**x+E**(-x))/2"
```

Method

```
In [17]: f = Taylor(expression, 3, 0)
print("\ng(x) =", f, "\n")
#print("f(x) ≈", N(f.subs(x, 2.1)))
```

$$\begin{aligned} f(x) &= \exp(x)/2 + \exp(-x)/2 \\ f'(x) &= \exp(x)/2 - \exp(-x)/2 \\ f''(x) &= \exp(x)/2 + \exp(-x)/2 \\ f'''(x) &= \exp(x)/2 - \exp(-x)/2 \end{aligned}$$

$$g(x) = 1.0000000000000000*(x - 0)**0/(0!) + 0*(x - 0)**1/(1!) + 1.0000000000000000*(x - 0)**2/(2!) + 0*(x - 0)**3/(3!)$$

$$g(x) = 0.5*x**2 + 1.0$$

Taylor

```
In [16]: def Taylor(function, order, a = 0):
    d, fS = [parse_expr(expression)], ""
    for i in range(order + 1):
        if i > 0:
            d.append(diff(d[i-1], x))
            fS += " + "
        print("\tf", end="")
        for j in range(i):
            print("", end="")
        print("(x) =\t", d[i])
        fS += str(N(d[i].subs(x, a))) + "*(x - " + str(a) + ")**" + str(i) + "/" + str(i) + "!"
    print("\ng(x) =", fS)
    return collect(expand(parse_expr(fS)), x)
```

Run First

```
In [2]: from sympy import *
x = symbols("x")
```