Aproximaciones

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Input

Method

```
In [ ]: x = GaussSeidel(Matrix, Independent, 2000, 0.0000000001)
print(x)
```

Gauss-Seidel

```
In [ ]: def GaussSeidel(m, it, n, e):
            print(len(m), "x", len(m), " System:\n", sep = "", end = "")
            for i in range(len(m)):
                print("\t[", end = "")
                for j in range(len(m[i])):
                    print(m[i][j], end = " ")
                print("= ", it[i], "]", sep = "")
            print()
            x = [0 \text{ for in } range(len(m))]
            for i in range(len(m)):
                d = m[i][i]
                for j in range(len(m[i])):
                    m[i][j] /= d
                it[i] /= d
            for i in range(len(m)):
                s = it[i]
                for j in range(len(m[i])):
                    if i != j:
                        s -= m[i][j]*x[j]
                x[i] = s
            for in range(n):
                print("x[", _, "] = ", x, sep = "")
                c = 1
                for i in range(len(m)):
                    o = x[i]
                    s = it[i]
                    for j in range(len(m[i])):
                        if i != j:
                             s -= m[i][j]*x[j]
                    x[i] = s
                    if c and x[i]:
                        error = 100*abs((x[i]-o)/x[i])
                        if error > e:
                             c = 0
                if c: break;
            return x
```

Aproximación

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Input

```
In [ ]: #expression = "2*x**3 - 4*log(x)"
#expression = "x**(1/3)"
expression = "x**3*log(x)"
```

Method

```
In [ ]: f = Taylor(expression, 3, 2)
print("\n", f, "\n")
print("f(x) ≈", N(f.subs(x, 2.1)))
```

Taylor

Run First

```
In [ ]: from sympy import *
x = symbols("x")
```

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 using 11 = long long;
4 int main(){
5 string a;
6 11 r = 0;
    cin >> a;
    int n = a.size() - 1;
9
    for(int i = 0; i < n + 1; i++){</pre>
10
       a[n - i] -= '0';
11
       r += a[n - i] * (1 << i);
12
13
     cout << r;
14
     return 0;
15 }
16
```

localhost:8888/edit/BinarytoDecimal.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 string ntoB(){
    int n;
    cin >> n;
    string s = "";
    while(n){
      s = to_string(n \% 2) + s;
 9
       n /= 2;
10
11
     return s;
12 }
13 long long btoD(string s){
14
     string s;
15
    cin >> s;
    int n = s.size();
16
17
    long long res = 0, m = 1;
    for(int i = n - 1; i >= 0; i--, m <<= 1)
18
19
       if(s[i] == '1') res += m;
20 }
21 int main(){
22
     return 0;
23 }
24
```

localhost:8888/edit/BinDec.cpp 1/1

Aproximación de un Polinomio Característico

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Input

```
In [ ]: #matrix = np.array([[3, 1, 5], [3, 3, 1], [4, 6, 4]]) #1, -10, 4, -40
#matrix = np.array([[3, 2, 4], [2, 0, 2], [4, 2, 3]]) #1, -6, -15, -8
matrix = np.array([[1, -1, 4], [3, 2, -1], [2, 1, -1]])
#matrix = np.array([[5, -2, 0], [-2, 3, -1], [0, -1, 1]])
```

Method

```
In [ ]: Leverrier_Faddeev(matrix)
In [ ]: Krilov(matrix, np.array([1, 0, 0]))
```

Krilov

```
In []: def Krilov(A, y = np.ones(0)):
    n = A.shape[0]
    b = np.empty((n, n))
    if y.size == 0: y = np.ones(n)
    b[0] = y
    print("Matrix:\n\n", A, "\n\nUsing vector:\n\n", y, "\n\nVectors calculated:\n")
    for i in range(1, n): b[i] = A @ b[i-1]
    print(b)
    a, s = np.linalg.solve(np.transpose(b), A @ b[n-1]), "\lambda\n" + str(n)
    for i in np.flip(a):
        n -= 1
        s += " + " + str(-i) + "\lambda\n" + str(n)
    return s
```

Leverrier Faddeev

```
In []:

def Leverrier_Faddeev(A):
    print("Matrix:\n\n", A, "\n\n")
    n = A.shape[0]
    b, B, i = np.empty(n+1), np.empty((n+1, n, n)), np.identity(n)
    b[n], B[0] = 1, np.zeros((n, n))
    for k in range(1, n+1):
        B[k] = (A @ B[k-1]) + (b[n-k+1] * i)
        b[n-k] = -np.trace(A @ B[k])/k
    s = ""
    n += 1
    for i in np.flip(b):
        n -= 1
        if len(s): s += " + "
        s += str(i) + "*\lambda^n + str(n)
    return s
```

Run first

```
In [ ]: import numpy as np
from sympy import *
x, lmbd = symbols("x"), symbols("lambda")
```

```
1 #include <bits/stdc++.h>
 2 using namespace std;
 3 using 11 = long long;
 4 int main(){
    double a;
    cin >> a;
    11 x = a;
    for(int i = 15; i >= 0; i--)
 9
       cout << (bool)(x & (1 << i));</pre>
10
     if((ll)a != a){
11
       cout << ".";
12
       for(int i = 0; i < 10; i++){</pre>
13
         a -= (11)a;
14
         a *= 2;
15
         cout << (11)a;
16
         if((11)a) a--;
17
       }
18
19
     return 0;
20 }
21
```

Aproximación de Ecuaciones Diferenciales

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Input

```
In []: \#yp, a, b, n, c = 'y - t**2 + 1', 0, 2, 10, 0.5 \#yp, a, b, n, c = '-2*t**3 + 12*t**2 - 20*t + 8.5', 0, 4, 8, 1 \#yp, a, b, n, c = 'y - t**2 + 1', 0, 2, 10, 0.5 yp, a, b, n, c = '-5*y + 5*t**2 + 2*t', 0, 1, 10, 1/3
```

Method

```
In [ ]: Euler(yp, a, b, n, c)
In [ ]: RunggeKutta(yp, a, b, n, c)
```

Euler

```
In [ ]: def Euler(fun, a, b, n, c):
    f = parse_expr(fun)
    print("\tf(x) =", f, end = "\n\n")
    h = (b - a)/n
    tT, yV, p = a, c, []
    for i in range(1, n+1):
        print(tT, yV, sep = "\t")
        yV += h*N(f.subs([(t, tT), (y, yV)]))
        tT += h
        p.append(yV)
    return (tT, yV)
```

Rungge Kutta (Cuarto Grado)

```
In []:

def RunggeKutta(fun, a, b, n, c):
    f = parse_expr(fun)
    print("\tf(x) =", f, end = "\n\n")
    h = (b - a)/n
    tT, yV, p = a, c, []
    for i in range(n):
        ku = h*N(f.subs([(t, tT), (y, yV)]))
        kd = h*N(f.subs([(t, tT + h/2), (y, yV + ku/2)]))
        kt = h*N(f.subs([(t, tT + h/2), (y, yV + kd/2)]))
        kc = h*N(f.subs([(t, tT + h), (y, yV + kt)]))
        yV += (ku + 2*kd + 2*kt + kc)/6
        tT += h
        p.append(yV)
        print(tT, yV, sep = "\t")
    return (tT, yV)
```

Run first

```
In [ ]: from sympy import *
t, y = symbols("t"), symbols("y")
```

Aproximaciones

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Input

```
In [ ]: | #xInput = (1, 4, 6, 5) |
        #yInput = "ln(x)"
        #xInput = (1, 4, 6)
        #yInput = "ln(x)"
        \#xInput = (1.0, 1.3, 1.6, 1.9, 2.2)
        #yInput = (0.765197, 0.6200860, 0.4554022, 0.2818186, 0.1103623)
        \#xInput = (1.0, 1.3, 1.6)
        #yInput = (0.7651977, 0.6200860, 0.4554022)
        \#xInput = (8.1, 8.3, 8.6, 8.7)
        #yInput = (16.94410, 17.56492, 18.50515, 18.82091)
        \#xInput = (1.3, 1.6, 1.9)
        #yInput = (0.6200860, 0.4554022, 0.2818186)
        \#dInput = (-0.5220232, -0.5698959, -0.5811571)
        #xInput = (8.3, 8.6)
        #yInput = (17.56492, 18.50515)
        #dInput = (3.116256, 3.151762)
        #xInput = (0, 0.6, 0.9)
        \#vInput = "ln(x+1)"
        #xInput = (8, 9, 11)
        #yInput = "log(x, 10)"
        \#xInput = (8, 9, 11)
        \#yInput = Cloud(xInput, "log(x, 10)")
        \#dInput = Cloud(xInput, "1/(x*log(10))")
        #HERMITE SEGUNDO EXAMEN
        #xInput = (8.3, 8.6)
        #yInput = (17.5649, 18.5051)
        #dInput = (3.1162, 3.1517)
        #NEWTON SEGUNDO EXAMEN
        xInput = (8, 9, 11)
        yInput = Cloud(xInput, "log(x)")
        dInput = Cloud(xInput, "1/x")
        #yInput = (-15, 15, -153, 291)
        #LAGRANGE SEGUNDO EXAMEN
        \#xInput = (1, -4, -7)
        #yInput = (10, 10, 34)
```

Method

```
In [ ]: f, e = Lagrange(xInput, yInput), 10
    print("\ng(", e, ") ≈ ", N(f.subs(x, e)), sep = "")

In [ ]: f, e = Newton(xInput, yInput), 10
    print("\nf(", e, ") ≈ ", N(f.subs(x, e)), sep = "")

In [ ]: f, e = Hermite(xInput, yInput, dInput), 10
    print("\nf(", e, ") ≈ ", N(f.subs(x, e)), sep = "")
```

Lagrange

Newton's Polynomial

Hermite

```
In [ ]: | def Hermite(xInput, yInput, dInput):
            n = len(xInput)
            print(n, "points:")
            for i in range(n):
                 print("\tf(", xInput[i], ") = ", yInput[i], "\tf'(", xInput[i], ") = ", dInput[i], sep = "")
            m = [[0 \text{ for i in } range(2*n)] \text{ for j in } range(2*n)]
            for i in range(n):
                m[2*i][0] = m[2*i+1][0] = yInput[i]
                 m[2*i][1] = dInput[i]
                if i: m[2*i-1][1] = (m[2*i][0]-m[2*i-1][0])/(xInput[i]-xInput[i-1])
            for j in range(2, 2*n):
                 for i in range(2*n-j):
                     m[i][j] = (m[i+1][j-1] - m[i][j-1])/(xInput[int((i+j)/2)] - xInput[int(i/2)])
            r, a = str(m[0][0]), ""
            for i in range(1, 2*n):
                 a += "*" + "(x-" + str(xInput[int((i - 1)/2)]) + ")"
                 r += " + " + str(m[0][i]) + a
             return showPoly(r)
```

AuxFucnt

```
In [ ]: def Cloud(xI, yI):
    if isinstance(yI, str):
        a, yI = list(), parse_expr(yI)
        for xVal in xI: a.append(N(yI.subs(x, xVal)))
        yI = tuple(a)
    return yI
    def showPoly(s):
        print("\nPolynomial", s, sep = "\n")
        print("\nSimplified", simplify(parse_expr(s)), sep = "\n")
        print("\nBy Powers", r := collect(expand(parse_expr(s)), x), sep = "\n")
        return r
```

Run First

```
In [ ]: from sympy import *
x = symbols("x")
```

Aproximaciones

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Function

Method

```
In [ ]: NewtonRaphson(3, 0.001, 50)
In [ ]: BinarySearch(0, 3, 0.1, 50)
In [ ]: Secant(3, 4, 0.01, 100)
In [ ]: FixedP(1, 0.001, 100)
```

Newton Raphson

```
In [ ]:
    def NewtonRaphson(p0, e, n):
        f = parse_expr(expression)
        d = diff(f, x)
        print("\tf(x) =", f, "\n\tf'(x) =", d, "\n")
        for i in range(n):
            p = p0 - N(f.subs(x, p0))/N(d.subs(x, p0))
            error = abs(N((p - p0)/p))*100
            print(i + 1, ". ", sep = '', end = '')
            print("P =", p, "\text{tEr =", error})
            if error < e: return p
            p0 = p
            return p</pre>
```

Binary Search

```
In [ ]: def BinarySearch(a, b, e, n):
    f = parse_expr(expression)
    print("\tf(x) = ", f, "\n\t[", a, ", ", b, "]", "\n", sep = "")
    fp0, p0 = N(f.subs(x, a)), a
    for i in range(n):
        p = a + (b - a)/2
        fp = N(f.subs(x, p))
        error = abs((p - p0)/p)*100
        print(i + 1, ". ", sep = '', end = '')
        print("P = ", p, "\tEr = ", error, " %", sep = '')
        if error < e: return p
        if fp * fp0 > 0: a, fp0 = p, fp
        else: b = p
        p0 = p
    return p
```

Secant

```
In []:
    def Secant(pa, pb, e, n):
        f = parse_expr(expression)
        print("\tf(x) =", f, "\n")
        for i in range(n):
            qa, qb = N(f.subs(x, pa)), N(f.subs(x, pb))
            pc = pb - qb*(pa - pb)/(qa - qb)
            error = abs(N((pc - pb)/pc))*100
            print(i + 1, ". ", sep = '', end = '')
            print("P =", pc, "\tEr =", error)
            if error < e: return pc
            pa, pb = pb, pc
            return p</pre>
```

Fixed Point

```
In []:
    def FixedP(pa, e, n):
        f = parse_expr(expression)
        print("\tf(x) =", f)
        f = parse_expr(expression + " + x")
        print("\tx =", f, "\n")
        for i in range(n):
            pb = N(f.subs(x, pa))
            if not pb: return pa
            error = abs((pb - pa)/pb)*100
            print(i + 1, ". ", sep = '', end = '')
            print("P = ", pb, "\text{tEr} = ", error, sep = '')
            if error < e: return pb
            pa = pb
            return pb</pre>
```

Run First

```
In [ ]: from sympy import *
x = symbols("x")
```