Aproximación de Ecuaciones Diferenciales

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Input

```
In [25]: \begin{cases} # \ yp, \ a, \ b, \ n, \ c = \ 'y - \ t**2 + 1 \ ', \ 0, \ 2, \ 10, \ 0.5 \\ # \ yp, \ a, \ b, \ n, \ c = \ '-2*t**3 + 12*t**2 - 20*t + 8.5', \ 0, \ 4, \ 8, \ 1 \\ yp, \ a, \ b, \ n, \ c = \ 'y - \ t**2 + 1 \ ', \ 0, \ 2, \ 10, \ 0.5 \end{cases}
```

Method

```
In [14]: Euler(yp, a, b, n, c)
Out[14]: [5.250000000000000,
           5.875000000000000,
           5.125000000000000,
           4.5000000000000000,
           4.7500000000000000,
           5.8750000000000000
           7.1250000000000000,
           7.000000000000000]
In [34]: RunggeKutta(yp, a, b, n, c)
Out[34]: [0.8292933333333333,
           1.21407621066667,
           1.64892201704160,
           2.12720268494794,
           2.64082269272875,
           3.17989417023223,
           3.73234007285498,
           4.28340949831841,
           4.81508569457943,
           5.30536300069265]
```

Euler

```
In [15]: def Euler(fun, a, b, n, c):
    f = parse_expr(fun)
    h = (b - a)/n
    tT, yV, p = a, c, []
    for i in range(1, n+1):
        yV += h*N(f.subs([(t, tT), (y, yV)]))
        tT += h
        p.append(yV)
    return p
```

Rungge Kutta (Cuarto Grado)

```
In [33]:

def RunggeKutta(fun, a, b, n, c):
    f = parse_expr(fun)
    h = (b - a)/n
    tT, yV, p = a, c, []
    for i in range(n):
        ku = h*N(f.subs([(t, tT), (y, yV)]))
        kd = h*N(f.subs([(t, tT + h/2), (y, yV + ku/2)]))
        kt = h*N(f.subs([(t, tT + h/2), (y, yV + kd/2)]))
        kc = h*N(f.subs([(t, tT + h), (y, yV + kt)]))
        yV += (ku + 2*kd + 2*kt + kc)/6
        tT += h
        p.append(yV)
    return p
```

Run first

```
In [5]: from sympy import *
t, y = symbols("t"), symbols("y")
```