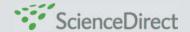
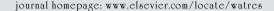


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A new plant-wide modelling methodology for WWTPs

P. Grau*, M. de Gracia, P.A. Vanrolleghem, E. Ayesa

CEIT, Environmental Engineering, P. Manuel Lardizabal, 2018 San Sebastian, Guipuzcoa, Spain

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ABSTRACT

This paper presents a new plant-wide modelling methodology for describing the dynamic behaviour of water and sludge lines in WWTPs. The methodology is based on selecting the set of process transformations needed for each specific WWTP to model all unit-process elements in the entire plant. This "transformation-based" approach, in comparison with the conventional "process-based" approach, does not require the development of specific transformers to interface the resulting unit-process models, facilitates the mass and charge continuity throughout the whole plant and is flexible enough to construct models tailored for each plant under study. As an illustrative example, a plant-wide model for a WWTP that includes carbon removal and anaerobic digestion has been constructed, and the main advantages of the proposed methodology for integrated modelling have been demonstrated. As a final consequence, this paper proposes a rewriting of the existing unit-process models according to the new standard transformation-based approach for integrated modelling purposes.

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1. Introduction

Mathematical modelling and dynamic simulation of the processes in a WWTP is a useful tool in the selection of operational strategies that improve process stability, effluent quality and operational costs. Optimum solutions for the design or operation of an entire WWTP, including the mutual relationships among the different unit-process elements involved in water and sludge lines, frequently differ from the simple compilation of solutions achieved for the design or operation of each unit-process element separately. Therefore, models used to analyse the entire WWTP must be rigorously developed taking into account the dynamic description of all the relevant processes in water and sludge lines (physicochemical treatments, primary and secondary settling, activated sludge reactors, anaerobic digesters, etc.), and the effect of reject flows among the different lines.

Consequently, if the behaviour of the entire plant must be evaluated in order to establish optimum design and operational criteria, the construction of integrated WWTP models including water and sludge lines is required. But obtaining integrated WWTP models that guarantee mass and charge continuity throughout the model plant is not a straightforward task (Vanrolleghem et al., 2005; Wentzel et al., 2006). The main challenges in obtaining integrated model plants arise from the incompatibilities and different descriptions of the components and transformations in standard process models. These include varying descriptions of organic carbonaceous substrates and organic nitrogen, as well as pH and buffer capacity in water or sludge and the different processes considered, etc. With respect to this problem, two main plant-wide modelling approaches have been proposed so far.

The first approach is based on the construction of a Supermodel consisting of all the components and transformations needed to reproduce every process within the entire plant (Jones and Tákacs, 2004; Seco et al., 2004). In this model, components and transformations are common to every unit-process model (UPM) in the WWTP and, therefore, specific transformers connecting different process models are not required. Nevertheless, the use of a unique Supermodel for any

WWTP lacks the flexibility to add or remove components as well as transformations depending on the case study and model aims. Another significant drawback to this approach is the continuous increase of the model size required to progressively adapt the *Supermodel* to reproduce new processes (Volcke et al., 2006).

The second approach, known as the interfaces approach, is based on the construction of transformers among existing standard models. An illustrative example of transformers between the activated sludge model (ASM1) (Henze et al., 2000) and the anaerobic digestion model (ADM1) (Batstone et al., 2002) has been proposed by Copp et al. (2003) for the simulation of a standard WWTP in the benchmark study (BSM2) (Jeppsson et al., 2006). In order to guarantee mass and charge continuity in the model interfaces, Vanrolleghem et al. (2005) propose a general methodology (CBIM) for the interface of any two standard models (Zaher et al., 2007; Volcke et al., 2006). However, although the interfaces approach facilitates the construction of integrated models tailored to the case study, there are some limitations when it comes to properly transforming the model components among existing models, guaranteeing mass and charge continuity under any dynamic condition (Grau et al., 2007).

Combining aspects from both approaches, in this paper, a new plant-wide modelling methodology based on the most appropriate transformations for each specific case study is proposed. This transformation-based approach, specially adequate for integrated modelling purposes, permits the construction of models tailored to the WWTP being studied without the need for specific transformers among process models and guarantees the mass and charge continuity at any point in the plant.

2. Plant-wide modelling methodology

This paper proposes a new plant-wide modelling methodology for the systematic and rigorous construction of the most appropriate mathematical models for describing, in an integrated way, the dynamic behaviour of the entire WWTP under study, including the main unit-process elements of both the water and sludge lines. The proposed methodology is based on selecting, for each specific WWTP, the set of compatible process transformations needed to model all unit-process elements throughout the entire plant. This "transformation-based" approach, in comparison with the conventional "process-based" approach, does not require the development of specific transformers to interface the resulting unit-process models and additionally facilitates the mass and charge continuity throughout the whole plant.

The proposed modelling methodology requires, as a preliminary step, the compilation of the stoichiometry and kinetics (Petersen matrix) of all the most relevant biochemical, chemical and physico-chemical transformations that can occur in a WWTP, in order to create a general list of transformations (LT) for plant-wide modelling objectives.

This list should be approved and standardized within the scientific community and serve as the common base for the building of any WWTP model. Additional transformations or alternative descriptions of the existing ones could be

introduced when needed without changes in the modelling methodology.

Once the general LT has been defined and compiled, the construction of every plant-wide model (PWM) under study is based on a systematic procedure. The compilation of the LT and the systematic procedure proposed in this paper for the construction of PWMs for WWTPs are described in detail in the following paragraphs.

2.1. The general LT for plant-wide modelling

The basic sources for the selection of the most relevant transformations involved in WWTPs are the well-known IWA models ASM1, ASM2d, ASM3 (Henze et al., 2000) and ADM1 (Batstone et al., 2002). However, in order to obtain a standardized and compatible LT for a PWM objective, some modifications should be made to the original models.

On the one hand, stoichiometry must be defined in order to avoid redundancies in component definition and to guarantee elemental mass (in terms of C, N, O, P and H) and charge continuity for all transformations included within the LT. With this in mind, all model components must be characterized by constant values for their elemental mass composition and charge density. Furthermore, some components must act as source-sink or compensation terms accounting for possible imbalances in C, N, O, P, H and charge (Reichert et al., 2001; De Gracia et al., 2006). This role of compensation is usually associated with components in their oxidation reference state (Reichert et al., 2001; Gujer et al., 1999). On the other hand, kinetic equations have to incorporate all required activation or inhibition terms in order to reproduce the appropriate activity under every possible environmental condition in a WWTP (aerobic, anoxic and anaerobic).

Fig. 1 shows an example of a possible LT that can be compiled for PWM objectives. Readily and slowly biodegradable organic matter, known in the AS models as S_s and X_s, have been described as a set of different components (monomers and VFAs for soluble substrate, and carbohydrates, proteins and lipids for particulates) to properly describe the biological activity under anaerobic conditions. Organic nitrogen, known in the ASM1 model as S_{nd} and X_{nd} , has been considered as part of the soluble and particulate carbonaceous substrates. Buffer capacity and pH prediction have been described by means of the component S_{h+} with a set of acid-base transformations related to inorganic carbon, nitrogen, VFAs, etc., that reproduce buffer capacity and permit a more realistic prediction of pH variations in the water line than in standard AS models (Sötemann et al., 2005). Furthermore, liquid-gas transfer and acid-base transformations have been considered to guarantee mass continuity of the process throughout the whole WWTP. Another modification is the decoupling of the composites and inert matter entering with the influent (Xc1, Xi, Si) from those obtained as decay by-products (X_{c2}, X_p, S_p) , in order to avoid the common discrepancies in elemental mass characterization between both groups of components (Huete et al., 2006). In addition, decay of microorganisms has been described under aerobic, anoxic and anaerobic conditions to reproduce a realistic behaviour of biological activity under all environmental conditions (Siegrist et al., 1999). Finally, some transformations

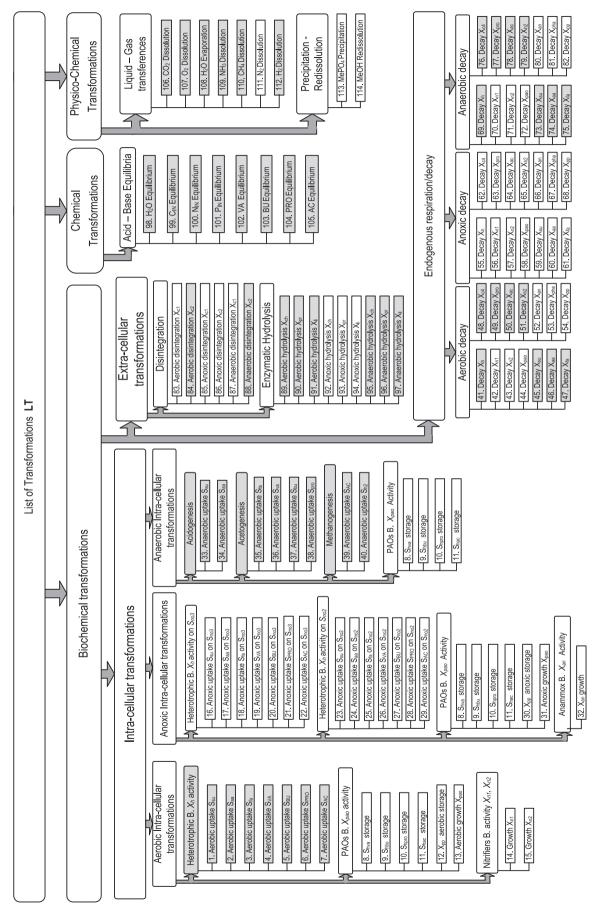


Fig. 1 – List of transformations proposed in this paper.

have been described in a more detailed way so that more biological processes occurring in a WWTP can be modelled. For example, the nitrification and denitrification described as two-step transformations will permit developing models to reproduce processes for treating reject water with high nitrogen content, like the Sharon–Anammox process.

The elemental mass characterization for all the components, combined with the use of source–sink components, makes it possible to calculate transformations stoichiometry while guaranteeing mass and charge continuity. Table 1 includes the list of all non-redundant components involved in the transformations with their mass composition and charge density. As C, N, O, P and H are considered to be the most relevant elements for the description of the organic compounds, and X summarizes all other elements, any model component can be described according to the following general formula:

$$\left[C_{(\alpha_{C,i}/12)}H_{(\alpha_{H,i})}O_{(\alpha_{O,i}/16)}N_{(\alpha_{N,i}/14)}P_{(\alpha_{P,i}/31)}X_{(\alpha_{X,i}/Mx)}\right]^{\alpha_{Ch,i}}\text{,}\tag{1}$$

where Mx is the molar mass of the element X.

This elemental characterization does not imply a significant increase in model complexity because the mass fractions of most model components can be reasonably estimated from their known stoichiometric formula, bibliography or experimental data (Huete et al., 2006). Additionally, the description of the model component's elemental mass permits a straightforward conversion of their mass to the theoretical oxygen demand (ThOD) using, for example, the oxidation state of the elements in the compounds (Gujer et al., 1999) or the mineralization equation (Reichert et al., 2001). Components selected as source–sink components of the LT are dissolved CO_2 for C, NH_4^+ for N, HPO_4^{2-} for P, dissolved O_2 for O, H_2O for H and H^+ for charge.

The LT proposed in Fig. 1, with its corresponding components shown in Table 1, is logically expandable with additional transformations and components that could be incorporated into the proposed modelling methodology without any necessary alterations. This may include those related to HPO_4^{2-} precipitation processes, for example.

A systematic procedure for constructing PWMs for WWTPs

Once the general LT has been defined and compiled, the construction of every PWM under study is based on a systematic procedure with three consecutive steps:

- (a) Selection of relevant transformations from the general list LT and construction of the specific plant transformation model (PTM) appropriate for the case study.
- (b) Construction of a set of compatible UPMs describing each unit of the plant under study.
- (c) Construction of the integrated PWM by direct interfacing between the UPMs previously developed.

2.2.1. Construction of the PTM

Construction of the PTM consists of the selection of the relevant biochemical, chemical and physico-chemical transformations that should be considered to model the WWTP under study. Selection of appropriate transformations requires sufficient insight into biochemical processes and, consequently, must be systematized in order to simplify the tasks undertaken by model users. Therefore, the following procedure is proposed for easy construction of a PTM.

2.2.1.1. Selection of biological processes. In this first step, the modeller has to decide which biological processes should be included in the PWM, according to the plant configuration and model aims. Some of the most common processes that can take place in a WWTP can be listed as follows:

- activated sludge process for carbon removal (AS-C),
- activated sludge process for carbon and nitrogen removal (AS-CN) (e.g. ASM1),
- activated sludge process for C, N and P removal (AS-CNP) (e.g. ASM2),
- acid fermentation,
- anaerobic digestion (e.g. ADM1),
- Sharon process for reject water treatment,
- · Anammox process for reject water treatment,
- others.

2.2.1.2. Selection of the active microorganism populations required to describe the selected biological processes. The key to selecting process transformations in each specific plant model is the correct identification of the microorganism populations involved in the biological processes. As shown in Table 2, each of the biological processes implies the activity of one or more microorganism population and, therefore, from the biological processes previously selected by the model user, the active microorganism population for each plant under study can be easily identified and selected.

2.2.1.3. Selection of the biochemical transformations associated with the activity of different microorganism populations. The presence of microorganism populations in a plant involves a set of biochemical transformations associated with their corresponding metabolisms under different environmental conditions. Therefore, once the appropriate set of microorganism populations has been selected according to Table 2, the biochemical transformations which describe for each one of them growth, decay and enzymatic hydrolysis under all environmental conditions (aerobic, anoxic and anaerobic) must be selected from the general LT and incorporated into the PTM. As an example, the transformations associated with the activity of heterotrophic bacteria $X_{\rm h}$ and anaerobic sugar-consuming bacteria $X_{\rm su}$ are shown in Fig. 2 according to the LT previously presented in Fig. 1.

Once all transformations that describe the activity of the microorganisms have been selected, all components involved in these transformations are easily identified.

2.2.1.4. Incorporation of acid-base and liquid-gas equilibria. The last step in the construction of the PTM is the incorporation of the acid-base equilibria and liquid-gas transfer to the PTM constituted in 3.1.3 In this manner, when the model components selected in 3.1.3 are involved in acid-base or liquid-gas equilibria with their respective

	Name	Formula	Description	Stoichiometric Unit			Mass fract	ions and ch	arge density		
					$\alpha_{\mathrm{C,i}}$	$\alpha_{\mathrm{H,i}}$	$\alpha_{\mathrm{O,i}}$	$\alpha_{\mathrm{N,i}}$	$\alpha_{\mathrm{P,i}}$	$\alpha_{\mathrm{Ch,i}}$	α_{X}
luble	components										
	S_{H_2O}	H ₂ O	Water	$\mathrm{gH_2O}$	-	0.1111	0.8889	-	-	-	-
	S_{O_2}	O_2	Dissolved oxygen	gO ₂ /m ³	-	-	1	-	-	-	
	S_{H^+}	H ⁺	Protons	gH/m³	-	1	-	-	-	1	
	S_{OH}	OH^-	Hydroxyl ions	gH/m³	-	0.0588	0.9412	-	-	-0.0588	
	S_{HPO_4}	HPO_4^{2-}	Hydroxy phosphate	gP/m³	-	0.0104	0.6667	-	0.3229	-0.0208	
	$S_{H_2PO_4}$	$H_2PO_4^-$	Dihydroxy phosphate	gP/m³	-	0.0206	0.6598	-	0.3196	-0.0103	
	$S_{ m NH_4}$	NH ₄	Ammonium	gN/m³	-	0.2222	_	0.7778	-	0.0556	
	S _{NH₃}	NH ₃	Ammonia	gN/m³	-	0.1765	-	0.8235	-	-	
	S _{CO2}	CO ₂	Dissolved carbon dioxide	gC/m ³	0.2727	_	0.7273	_	_	_	
	S _{HCO3}	HCO ₃	Bicarbonate	gC/m ³	0.1967	0.0164	0.7869	_	_	-0.0164	
	S _{su}	C ₆ H ₁₂ O ₆	Monosaccharide	gCOD/m ³	0.4	0.0667	0.5333	_	_	_	
	S _{aa}	C ₄ H _{6.1} O _{1.2} N	Amino acids	gCOD/m³	0.5498	0.0699	0.2199	0.1604	_	_	
	S_{fa}	C ₁₆ O ₂ H ₃₂	LCFAs	gCOD/m ³	0.75	0.125	0.125	-	_	_	
	S _{hva}	C ₅ H ₁₀ O ₂	Valeric acid	gCOD/m³	0.5882	0.098	0.3137	_	_	_	
	S _{va} _	C ₅ H ₉ O ₂ -	Valerate	gCOD/m³	0.5941	0.0891	0.3168	_	_	-0.0099	
	S _{hbu}	$C_4H_8O_2$	Butyric acid	gCOD/m ³	0.5455	0.0909	0.3636	_	_	_	
	S _{bu}	$C_4H_7O_2^-$	Butyrate	gCOD/m ³	0.5517	0.0805	0.3678	_	_	-0.0115	
	$S_{ m hpro}$	$C_3H_6O_2$	Propionic acid	gCOD/m ³	0.4865	0.0811	0.4324	_	_	_	
	S _{pro}	C ₃ H ₅ O ₂	Propionate	gCOD/m ³	0.4932	0.0685	0.4384	_	_	-0.0137	
	$S_{\rm hac}$	$C_2H_4O_2$	Acetic acid	gCOD/m³	0.4	0.0667	0.5333	-	-	-	
	S_{ac-}	$C_2H_3O_2^-$	Acetate	gCOD/m³	0.4068	0.0508	0.5424	-	-	-0.0169	
	S_{H_2}	H_2	Dissolved hydrogen	gCOD/m³	-	1	-	-	-	-	
	S _{CH₄}	CH ₄	Dissolved methane	gCOD/m ³	0.75	0.25	-	-	-	-	
	S_{N_2}	N_2	Dissolved nitrogen	gN/m ³	_	_	_	1	_	_	
	S _{NO2}	NO ₂	Nitrites	gN/m³	_	_	0.6957	0.3043	_	-0.0217	
	S _{NO₃}	NO ₃	Nitrates	gN/m ³	_	_	0.7742	0.2258	_	-0.0161	
	S_{K^+}	K ⁺	Potassium ions	gK/m ³	_	_	_	_	_	0.0256	
	$S_{Mg^{2+}}$	Mg ²⁺	Magnesium ions	gMg/m³	_	_	_	_	_	0.0823	
	S _I	6	Soluble inerts	gCOD/m ³	~	~	~	~	~		
	S _I	_	Soluble decay products	gCOD/III gCOD/m ³	α _{C,29}	α _{H,29} α _{H.30}	α _{O,29}	α _{N,29} α _{N,30}	α _{P,29}	α _{Ch,29}	α
		_	Soluble decay products	gCOD/III	α _{C,30}	αH,30	α _{O,30}	αN,30	α _{P,30}	$\alpha_{\mathrm{Ch,30}}$	α
си	late and gaseou	is components	Compositor 1	aCOD/m3							
	X _{c1}	_	Composites 1	gCOD/m ³	α _{C,31}	α _{H,31}	α _{O,31}	α _{N,31}	α _{P,31}	α _{Ch,31}	α
	X_{c2}	- CH OB	Composites 1 Carbohydrates	gCOD/m³ gCOD/m³	$\alpha_{C,32}$ 0.4401	α _{H,32} 0.0608	α _{O,32} 0.489	α _{N,32}	$\alpha_{P,32}$ 0.01	α _{Ch,32}	α
	X _{ch}	$C_6H_{9.95}O_5P_{0.05}$	Proteins	gCOD/m ³	0. 44 01 0.5498	0.0608	0.489	- 0.1604	0.01	_	
	X _{pr}	(C ₄ H _{6.1} O _{1.2} N) _x		gCOD/m ³	0.5498	0.0699	0.2199	0.1604	0.01	_	
	$X_{ m li} \ X_{ m h}$	$C_{51}H_{97.9}O_6P_{0.1}$ $C_5H_{6.9}O_2NP_{0.1}$	Lipids Heterotrophic B.	gCOD/m ³	0.752	0.1201	0.118	0.1203	0.01	_	
	$X_{\rm h}$ $X_{\rm n1}$	C ₅ H _{6.9} O ₂ NP _{0.1} C ₅ H _{6.9} O ₂ NP _{0.1}	Nitrosomona B.	gCOD/m ³	0.5155	0.0592	0.275	0.1203	0.03		
	X_{n1} X_{n2}	C ₅ H _{6.9} O ₂ NP _{0.1} C ₅ H _{6.9} O ₂ NP _{0.1}	Nitrobacter B.	gCOD/III gCOD/m ³	0.5155	0.0592	0.275	0.1203	0.03	_	
	X_{n2} X_{pao}	C ₅ H _{6.9} O ₂ NP _{0.1}	Phosphorous acum. B.	gCOD/III gCOD/m ³	0.5155	0.0592	0.275	0.1203	0.03	_	

Table 1 - Model components included in the LT

i	Name	Formula	Description	Stoichiometric Unit			Mass fract	ions and ch	arge density		
					$\alpha_{C,i}$	$\alpha_{H,i}$	$\alpha_{\mathrm{O,i}}$	$\alpha_{N,i}$	$\alpha_{\mathrm{P,i}}$	$\alpha_{\mathrm{Ch,i}}$	$\alpha_{X,i}$
40	$X_{\rm pha}$	C ₄ H ₆ O ₂	Cell internal storage	gCOD/m ³	0.2790	0.0698	0.3721	_	_	-	_
41	X_{pp}	$K_{0.33}Mg_{0.33}PO_3$	Poly-phosphate	gP/m³	_	_	0.4793	_	0.3096	-	0.2110
42	X_{su}	$C_5H_{6.9}O_2NP_{0.1}$	Sugar degraders	gCOD/m ³	0.5155	0.0592	0.275	0.1203	0.03	-	-
43	X_{aa}	$C_5H_{6.9}O_2NP_{0.1}$	Aminoacid degraders	gCOD/m³	0.5155	0.0592	0.275	0.1203	0.03	-	-
44	X_{fa}	$C_5H_{6.9}O_2NP_{0.1}$	LCFA degraders	gCOD/m³	0.5155	0.0592	0.275	0.1203	0.03	-	-
45	X_{c4}	$C_5H_{6.9}O_2NP_{0.1}$	Valeric/butyric degrad.	gCOD/m³	0.5155	0.0592	0.275	0.1203	0.03	-	-
46	X_{pro}	$C_5H_{6.9}O_2NP_{0.1}$	Propionic degraders	gCOD/m³	0.5155	0.0592	0.275	0.1203	0.03	-	-
47	X _{ac}	$C_5H_{6.9}O_2NP_{0.1}$	Acetid degraders	gCOD/m ³	0.5155	0.0592	0.275	0.1203	0.03	-	-
48	X_{H_2}	C5H6.9O2NP0.1	Hydrogen degraders	gCOD/m³	0.5155	0.0592	0.275	0.1203	0.03	-	-
49	X _{an}	$C_5H_{6.9}O_2NP_{0.1}$	Anammox degraders	gCOD/m³	0.5155	0.0592	0.275	0.1203	0.03	-	_
50	$X_{\rm I}$	_	Inert particulate material	gCOD/m ³	$\alpha_{C,50}$	α _{H,50}	α _{0,50}	$\alpha_{N,50}$	$\alpha_{P,50}$	$\alpha_{\mathrm{Ch,50}}$	$\alpha_{X,50}$
51	$X_{\rm P}$	-	Part. decay	gCOD/m ³	α _{C,51}	α _{H,51}	α _{0,51}	α _{N,51}	α _{P,51}	$\alpha_{\mathrm{Ch,51}}$	α _{X,51}
52	$X_{Me(OH)}$	Fe(OH) ₃	Ferric hydroxide	g/m³	_	0.0281	0.4492	_	_	_	0.5227
53	X_{MeP}	FePO ₄	Ferric phosphate	g/m³	_	-	0.4243	_	0.2055	-	0.3703
54	X_{II}	-	Inorganic inert	g/m ³	_	-	_	_	-	_	1
55	G_{CO_2}	CO_2	Carbon dioxide gas	gC/m ³ _(g)	0.2727	-	0.7273	-	-	-	-
56	$G_{\rm H_2}$	H_2	Hydrogen gas	gCOD/m ³	-	1	-	-	-	-	_
57	G _{CH4}	CH ₄	Methane gas	gCOD/m ³	0.75	0.25	_	_	_	_	_
58	$G_{ m NH_3}$	NH ₃	Ammonia gas	gN/m ³ _(g)	-	0.1765	-	0.8235	-	-	-
59	G_{N_2}	N_2	Nitrogen gas	gN/m ³ _(g)	-	-	-	1	-	-	-
60	G_{O_2}	O_2	Oxygen gas	$gO_2/m_{(g)}^{3}$	_	-	1	_	-	-	-
61	G _{H2} O	H_2O	Water steam	gH ₂ O/m ³ (g)	_	0.1111	0.8889	-	_	_	-

Table 1 (continued)

		_				Microorganism Populations											
BIO	iogicai	Process	ses			X an	X_h	X_{nl}	X_{n2}	X_{pao}	X_{su}	X_{aa}	X_{fa}	X_{c4}	X_{pro}	X_{ac}	X_{h2}
				Ana	nerobic oxidation of N-NH ₄ ⁺	×											
		AS-C		Car	Carbon oxidation		×										
жош				cation	Nitritation			×									
Anammox		AS-CN Sharon		Nitrification	Nitratation				×								
	N.	l «	· / -	ication	Denitrification on NO ₃		×										
	AS-CNP			Denitrification	Denitrification on NO ₂		×										
				Bio	-P storage and release					×							
			Ferm	Aci	dogenesis						×	×					
		Anaerobic digestion		Ace	togenesis								×	×	×		
		₫₽		Met	hanogenesis											×	×

acid/base couples or gas phase components, these transformations must also be incorporated into the PTM and the corresponding acid/base-conjugated and gas-phase components must also be added to the list of selected model components. The set of resulting model components obtained will constitute the plant components vector (PCV), which will be the common state vector used for the process description at any point of the plant and will additionally act as a common model interface between all UPMs that will be described in the following section.

Once these four steps have been completed, the resulting set of transformations and the vector of model components (PCV) make up the PTM (Fig. 3). The selected transformations should be able to reproduce the biological activity in the liquid phase for the WWTP under study, including the buffer capacity of the liquid phase and the mass transfer between the liquid and gaseous phase in contact with it.

It is important to point out that the selection of biological processes considered in 3.1.1 is the only "subjective" decision left to the modeller when constructing the PTM. The selection of active microorganisms, transformations and model components is a straightforward procedure that can be carried out automatically according to predefined rules.

2.2.2. Construction of the set of UPMs of the plant

The set of UPMs is the collection of mathematical models describing the most relevant units included in the water and sludge lines of the plant under study. Each UPM must incorporate the mathematical description of both the mass transport and the internal transformations and must use, as a common model interface, the PCV previously described.

The mathematical description of the mass transport in each UPM is logically quite diverse for different elements of the plant (for e.g. CSTR reactors, primary or secondary settlers, filters or other solid separation systems, etc.) and sometimes even based on lumped additional variables that are usually a combination of the model components included in the common PCV (a typical example of this is the use of total

solids concentration in the modelling of clarification or settling processes).

The mathematical description of the internal transformations for all UPMs should be, as a general rule, based on the previously constructed PTM. The use of a common set of transformations for all UPMs will facilitate a coherent description of the processes throughout the whole plant and guarantee mass continuity. Additionally, the use of the common PCV, as the internal components vector for describing transformations, allows for a direct connection between the UPMs without introducing specific transformers. However, in order to reduce the model complexity and to increase computational efficiency, some simplifications could be considered for some UPMs operating under specific conditions:

- The models describing a unit process without any significant biochemical activity can be based only on mass transport equations. Typical examples include the mathematical models commonly used for primary or secondary settlers.
- The models describing a unit process that is always working under stable environmental conditions can "switch off" or eliminate transformations that are irrelevant under these specific conditions. For example, anaerobic transformations can be "switched off" when describing conventional activated sludge reactors in the water line.
- For simplicity or computational efficiency, some UPMs could be developed based on internal "lumped" variables and transformations. Typical examples can include the use of lumped variables for the slowly (X_S) or easily (S_S) biodegradable carbonaceous substrates or lumped transformations as the one-step nitrification from ammonia to nitrates. However, the convenience of this kind of simplification should be carefully analysed in each case, as the resulting UPM must incorporate transformers among its internal model variables and the PCV (the common model

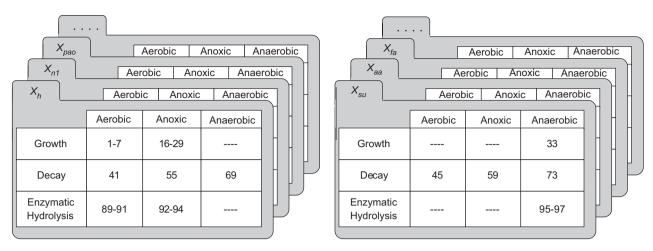


Fig. 2 - Transformations related to X_h and X_{su} activity.

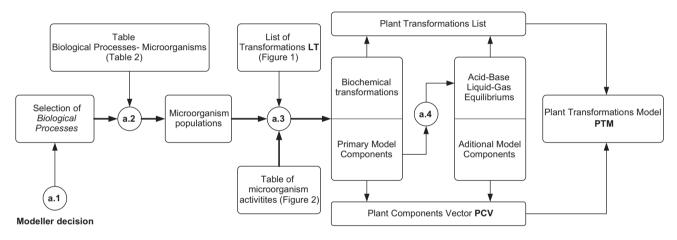


Fig. 3 - Scheme of the procedure for PTM construction.

interface within the whole plant). In many cases, the design of these transformers guaranteeing mass and charge continuity under different operating conditions is not a straightforward task (Vanrolleghem et al., 2005).

Therefore, although the modeller could develop specific UPMs, it is important to note that any UPM must guarantee mass and charge continuity for every internal process transformation and must use the PCV as the common interface with the other UPMs of the entire plant. Consequently, when computational time is not a critical restriction, the direct incorporation of the general PTM for internal transformations in all UPMs is strongly recommended in terms of modelling coherence and conceptual simplicity.

2.2.3. Construction of the PWM for the whole plant Once the set of UPMs has been constructed in accordance with the proposed methodology, the PWM can be easily created, without additional transformers, by the direct connection of the mass fluxes among the UPMs. The resulting

integrated model will guarantee mass and charge conservation for all process transformations and through all UPM interfaces.

3. Example: PWM for a conventional activated sludge process with anaerobic digestion

Once the methodology for model construction has been defined, tailored PTMs can easily be built including all the biological processes required for the description of the water and sludge lines at each specific case study, for example, carbon oxidation, nitrification, denitrification, biological phosphorus removal, fermentation or complete anaerobic digestion, etc.

As an example, this paper shows a PWM for a conventional WWTP that includes an aerated activated sludge reactor for C removal, a secondary settler and an anaerobic digester for sludge treatment.

3.1. PTM construction

The PTM for the WWTP proposed in this example has been constructed following the sequential procedure indicated in Section 2.

3.1.1. Selection of biological processes

According to plant configuration and model objectives, the biological processes considered have been limited to the activated sludge process for carbon removal (AS-C), which occurs mainly in the aerated activated sludge tank, and the

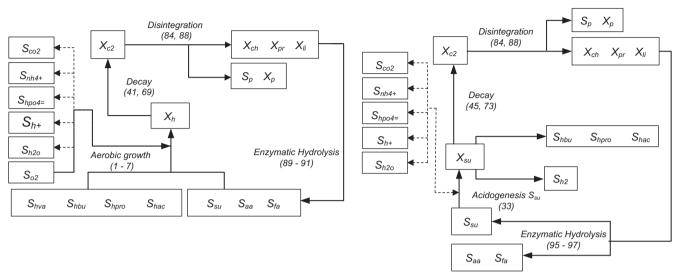


Fig. 4 - Components and biochemical transformations involved in the X_h and X_{su} activity.

Table 3 – Expressions utilized in the kinetic equations

Lumped variables used to simplify the k	rinetic equations description	1	
Valerate	$S_{VA} = S_{hva} + S_{va} -$	Readily degradable substrate	$S_S = S_{su} + S_{aa} + S_{fa} + S_{VA} + S_{BU} + S_{PRO} + S_{AC}$
Butyrate	$S_{BU} = S_{hbu} + S_{bu} -$	Inorganic carbon	$S_{IC} = S_{CO_2} + S_{HCO_3^-}$
Propionate	$S_{PRO} = S_{hpro} + S_{pro^-}$	Ammoniacal nitrogen	$S_{\rm IN} = S_{\rm NH_4^+} + S_{\rm NH_3}$
Acetate	$S_{AC} = S_{hac} + S_{ac^-}$	Inorganic phosphorus	$S_{IP} = S_{HPO_{4=}} + S_{H_2PO_4}$
Activation/inhibition terms depending or	n the environmental condit	ions	
Oxygen activation	$A_{O_2} = \frac{s_{O_2}}{s_{A,O_2} + s_{O_2}}$	Oxygen inhibition	$I_{O_2} = \frac{\kappa_{A,O_2}}{\kappa_{A,O_2} + S_{O_2}}$
Nitrates activation	$A_{NO_3} = \frac{s_{NO_3^-}}{s_{A,NO_3} + s_{NO_2^-}}$	Nitrates/nitrites inhibition	$I_{nox} = \frac{\kappa_{A,nox}}{\kappa_{A,nox} + (S_{NO_2} + S_{NO_2})}$
Nitrites activation	$A_{NO_2} = \frac{s_{NO_2^-}}{s_{A,NO_2^-} + s_{NO_2^-}}$		
Activation terms for source–sink compo	nents		
Inorganic nitrogen	$A_{IN} = \frac{S_{IN}}{K_{A INI} + S_{INI}}$	Inorganic carbon	$A_{IC} = \frac{S_{IC}}{K_{A} \cdot IC + S_{IC}}$
Inorganic phosphorous	$A_{\rm IP} = \frac{S_{\rm IP}}{K_{\rm A,IP} + S_{\rm IP}}$		Ajid 11 Id
Activation/inhibition terms depending or	n pH values		
pH inhibition of the acidogenesis an	d acetogenesis transform	nations	$I_{pH,aa} = \frac{\kappa_{I,H,aa}^2}{\kappa_{I,H,aa}^2 + S_{I,L}^2}$
pH inhibition of the acetoclastic med	thanogenesis		$I_{pH,ac} = \frac{\kappa_{I,H,ac}^2}{\kappa_{I,H,ac}^2 + \kappa_{I,H,ac}^2}$
pH inhibition of hydrogenotrophic m	nethanogenesis		1,11,ac H ⁺
pri minordon or nydrogenotropine n	iculanogenesis		$I_{\text{pH,H}_2} = \frac{\kappa_{\text{I,H,H}_2}^2}{\kappa_{\text{I,H,H}_2}^2 + s_{\text{H}^+}^2}$
Inhibition terms caused by inhibiting co	mponents		
VFAs hydrogen inhibition during the acidogenesis	$I_{H_2,fa} = \frac{K_{I,H_2,fa}}{K_{I,H_2,fa} + S_{H_2}}$	Propionic hydrogen inhibition during the	$I_{\rm H_2,pro} = \frac{\kappa_{\rm LH_2,pro}}{\kappa_{\rm LH_2,pro} + S_{\rm H_2}}$
Valeric and butyric hydrogen inhibition during the acetogenesis	$I_{H_2,C_4} = \frac{\kappa_{I,H_2,C_4}}{\kappa_{I,H_2,C_4} + S_{H_2}}$	acetogenesis Ammonia inhibition	$I_{NH_{3}} = \frac{\kappa_{I,NH_{3}}}{\kappa_{I,NH_{3}} + s_{NH_{3}}}$

anaerobic digestion process (ADM1), which is active in the digester.

3.1.2. Selection of the microorganism populations required to describe the selected biological processes

As a consequence of the biological processes considered in 3.1.1, as shown in Table 2, the selected active microorganism populations are X_h , and the set of anaerobic microorganisms X_{su} , X_{aa} , X_{fa} , X_{c4} , X_{pro} , X_{ac} and X_{H_2} .

3.1.3. Selection of the biochemical transformations associated with the activity of the microorganism populations

Once active microorganism populations have been determined, the biochemical transformations describing their growth, decay and enzymatic hydrolysis are selected under all environmental conditions as shown in Fig. 2. In this case, the selected transformations are 1–7, 16–29, 33–40, 41, 45–51, 55, 59–65, 69, 73–79 and 89–97. In addition to these biochemical transformations, X_{c2} disintegration under aerobic, anoxic and anaerobic conditions must be selected (84, 86 and 88).

Although disintegration of X_{c2} is not related to activities of the microorganisms, this transformation has been considered as an intermediate transformation between the microorganisms' decay and the enzymatic hydrolysis as it is proposed for X_c in the ADM1. The list of all these transformations will reproduce the biological activity that occurs in the whole WWTP. However, as in this particular case, anoxic conditions do not exist at any point in the plant, transformations occurring under this specific condition (16–29, 55, 59–65, 86 and 92–94) can be eliminated.

The set of components involved in the selected transformations will correspond to the soluble substrate, the microorganism populations selected in 3.1.2, the decay products and the particulate substrate. Furthermore, source–sink components have been considered by default to guarantee the mass and charge continuity in the biochemical transformations regardless of the components' mass compositions. Fig. 4 shows, as an illustrative example, the biochemical transformations and components involved in the X_h and X_{su} activities.

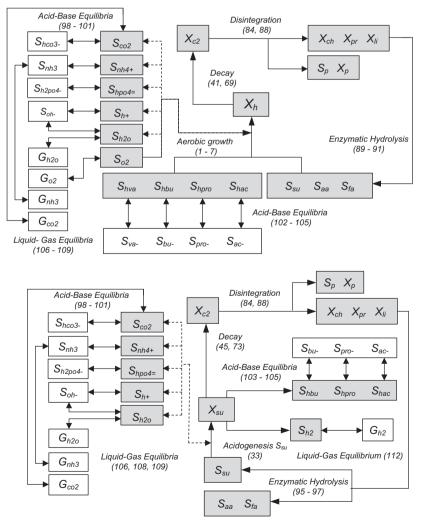


Fig. 5 - Components and transformations incorporated in the X_h and X_{su} activity.

3.1.4. Incorporation of acid–base and liquid–gas equilibria According to the set of components selected in 3.1.3, the required acid–base equilibria (98–105) and liquid–gas transfers (106–110, 112) have been incorporated into the PTM. Finally, additional components needed to describe these acid–base and liquid–gas equilibria have been included in the PCV. Fig. 5 shows the transformations and components incorporated in this step according to the components selected for the $X_{\rm h}$ and $X_{\rm su}$ biological activity description (Fig. 4).

The PTM obtained is presented in Tables 3–7 in terms of stoichiometry and kinetics (Petersen matrix). The stoichiometry associated with the biological activity and the physicochemical transformations is shown in Tables 5 and 6, respectively. In Table 7, the source–sink stoichiometric values have been expressed by a set of formulas since their exact values depend on the mass composition of the components involved in each transformation. On the other hand, the kinetic equations include the appropriate activation and inhibition terms for the environmental conditions. Therefore,

when the environmental conditions change from one unitprocess element to another, the conversion of non-viable microorganisms under specific conditions into decay products is described by continuous decay kinetics regulated by the specific environmental conditions prevailing at each point of the WWTP. Finally, it must be taken into account that the kinetic equations selected for the construction of the PTM should be revised for each case study to ensure that the monod terms included in them are coherent with the components considered in the model. In some cases, if the kinetic equations were modified, the values of the parameters included in them should be readjusted.

3.2. Construction of the set of UPMs

Once the PTM is obtained, UPMs for the activated sludge reactor, the secondary settler and the anaerobic digester must be constructed by means of the mass transport description and internal transformations.

Table 4 - Kinetic equations of the PTM transformations

```
\rho_1 = k_{\text{m,h}} \frac{S_{\text{SU}}}{K_{\text{SU\_h}} + S_{\text{SU}}} \frac{S_{\text{SU}}}{S_{\text{S}}} [A_{\text{O}_2} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{H}}
                                                                                                                                                                                                                                    \rho_{41} = k_{\text{dec aer,xh}} A_{O_2} X_H
\rho_2 = k_{m,h} \frac{S_{aa}}{K_{aa}} \frac{S_{aa}}{h + S_{aa}} \frac{S_{aa}}{S_S} [A_{O_2} A_{IN} A_{IP} A_{IC}] \stackrel{\checkmark}{\leftarrow} X_H
                                                                                                                                                                                                                                    \rho_{45} = k_{\text{dec\_aer,xsu}} A_{O_2} X_{\text{su}}
\rho_{3} = k_{m,h} \frac{s_{fa}}{s_{fa} + s_{fa}} \frac{s_{fa}}{s_{S}} [A_{O_{2}} A_{IN} A_{IP} A_{IC}] X_{H}
                                                                                                                                                                                                                                   \rho_{46} = k_{\text{dec aer,xaa}} A_{O_2} X_{\text{aa}}
\rho_{4} = k_{\text{m,h}} \frac{s_{\text{VA}}}{s_{\text{VA},h} + s_{\text{VA}}} \frac{s_{\text{VA}}}{s_{\text{S}}} [A_{\text{O}_{2}} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{H}}
                                                                                                                                                                                                                                   \rho_{47} = k_{\text{dec aer,xfa}} A_{\text{O}_2} X_{\text{fa}}
\rho_5 = k_{m,h} \frac{\bar{S}_{BU}}{K_{BU}} \frac{S_{BU}}{h^{+}S_{BU}} \frac{S_{BU}}{S_S} [A_{O_2} A_{IN} A_{IP} A_{IC}] X_H
                                                                                                                                                                                                                                   \rho_{48} = k_{\text{dec\_aer}, xc_4} A_{O_2} X_{C_4}
\rho_6 = k_{m,h} \frac{s_{PRO}}{\kappa_{PRO}} \frac{s_{PRO}}{h^{+S}_{PRO}} \frac{s_{PRO}}{s_S} [A_{O_2} A_{IN} A_{IP} A_{IC}] X_H
                                                                                                                                                                                                                                   \rho_{49} = k_{\text{dec aer,xpro}} A_{O_2} X_{\text{pro}}
                                                                                                                                                                                                                                   \rho_{50} = k_{\text{dec aer,xac}} A_{0_2} X_{\text{ac}}
 \rho_7 = k_{\text{m,h}} \frac{s_{\text{AC}}}{\kappa_{\text{AC,h}} + s_{\text{AC}}} \frac{s_{\text{AC}}}{s_{\text{S}}} [A_{\text{O}_2} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{H}}
                                                                                                                                                                                                                                   \rho_{51} = k_{\text{dec\_aer}, xh_2} A_{O_2} X_{H_2}

\rho_{33} = k_{\text{m,su}} \frac{S_{\text{SU}}}{K_{\text{S su}} + S_{\text{SU}}} [I_{\text{O}_2} I_{\text{nox}} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}} I_{\text{pH,aa}}] X_{\text{su}}

\rho_{34} = k_{m,aa} \tfrac{S_{aa}}{K_{S,aa} + S_{aa}} [I_{O_2} I_{nox} A_{IN} A_{IP} A_{IC} I_{pH,aa}] X_{aa}
                                                                                                                                                                                                                                   \rho_{69} = k_{\text{dec\_an,xh}} I_{\text{O}_2} I_{\text{nox}} X_{\text{H}}
\rho_{35} = k_{m,fa} \frac{s_{fa}}{\kappa_{S,fa} + s_{fa}} [A_{IN}A_{IP}A_{IC}I_{O_2}I_{nox}I_{H_2,fa}I_{ph,aa}]X_{fa}
                                                                                                                                                                                                                                   \rho_{73} = k_{\text{dec\_an,xsu}} I_{\text{O}_2} I_{\text{nox}} X_{\text{su}}
\rho_{36} = k_{m,C_4} \frac{s_{VA}}{\kappa_{S,C_4} + s_{VA}} \frac{1}{1 + s_{BII}/s_{VA}} [A_{IN} A_{IP} A_{IC} I_{O_2} I_{nox} I_{H_2,C_4} I_{ph,aa}] X_{C_4}
                                                                                                                                                                                                                                   \rho_{74} = k_{\text{dec an.xaa}} I_{O_2} I_{\text{nox}} X_{\text{aa}}
\rho_{37} = k_{m,C_4} \frac{s_{BU}}{\kappa_{S,C_4} + s_{BU}} \frac{1}{1 + s_{VA}/s_{BU}} [A_{IN} A_{IP} A_{IC} I_{O_2} I_{nox} I_{H_2,C_4} I_{ph,aa}] X_{C_4}
                                                                                                                                                                                                                                   \rho_{75} = k_{\text{dec\_an,xfa}} I_{O_2} I_{\text{nox}} X_{\text{fa}}
\rho_{38} = k_{\text{m,pro}} \frac{s_{\text{PRO}}}{\kappa_{\text{S,pro}} + s_{\text{PRO}}} [A_{\text{IN}} A_{\text{IP}} A_{\text{IC}} I_{O_2} I_{\text{nox}} I_{\text{H}_2,\text{pro}} I_{\text{ph,aa}}] X_{\text{pro}}

\rho_{76} = k_{\text{dec an,xc_4}} I_{O_2} I_{\text{nox}} X_{C_4}

\begin{split} \rho_{39} &= k_{m,ac} \frac{s_{AC}}{\kappa_{S,ac} + s_{AC}} [I_{O_2} I_{nox} A_{IN} A_{IP} A_{IC} I_{NH_3} I_{ph,ac}] X_{ac} \\ \rho_{40} &= k_{m,H_2} \frac{s_{H_2}}{\kappa_{S,H_2} + s_{H_2}} [I_{O_2} I_{nox} A_{IN} A_{IP} A_{IC} I_{ph,H_2}] X_{H_2} \end{split}
                                                                                                                                                                                                                                    \rho_{77} = k_{\text{dec an.xpro}} I_{O_2} I_{\text{nox}} X_{\text{pro}}
                                                                                                                                                                                                                                   \rho_{78} = k_{\text{dec\_an,xac}} I_{O_2} I_{\text{nox}} X_{\text{ac}}
 \rho_{84} = k_{d\_Aer}[A_{O_2}A_{IN}A_{IP}A_{IC}]X_{C_2} \leftarrow

\rho_{79} = k_{\text{dec\_an,xH}_2} I_{O_2} I_{\text{nox}} X_{H_2}

 \rho_{88} = k_{d\_Anaer}[I_{nox}I_{O_2}A_{IN}A_{IP}A_{IC}]X_{C_2} \leftarrow
                                                                                                                                                                                                                                    \rho_{98} = k_{ab,H_2O}(k_{a,H_2O} - s_{OH} - s_{H^+})
                                                                                                                                                                                                                                    \rho_{99} = k_{AB,IC}(k_{a,IC}S_{CO_2} - S_{HCO_3} - S_{H^+})
 \rho_{89} = k_{\text{h\_Aer}} [A_{\text{O}_2} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{ch}}
 \rho_{90} = k_{h\_Aer}[A_{O_2}A_{IN}A_{IP}A_{IC}]X_{pr}
                                                                                                                                                                                                                                   \rho_{\rm 100} = k_{\rm AB,IN} (k_{\rm a,IN} S_{\rm NH_4^+} - S_{\rm NH_3} S_{\rm H^+})
 \rho_{91} = k_{\text{h Aer}} [A_{\text{O}_2} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{li}}
                                                                                                                                                                                                                                   \rho_{101} = k_{\rm AB,IP}(k_{\rm a,IP}S_{\rm H_2po_4^-} - S_{\rm Hpo_{4=}}S_{\rm H^+})
                                                                                                                                                                                                                                    \rho_{102} = k_{AB,VA}(K_{a,VA}S_{hva} - S_{va}S_{H^+})
 \rho_{95} = k_{h \text{ Anaer}} [I_{O_2} I_{\text{nox}} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{ch}}
                                                                                                                                                                                                                                    \rho_{103} = k_{AB,BU}(k_{a,BU}S_{hbu} - S_{bu}S_{H}^+)
 \rho_{96} = k_{h\_Anaer}[I_{O_2}I_{nox}A_{IN}A_{IP}A_{IC}]X_{pr}
 \rho_{97} = k_{h \text{ Anaer}} [I_{O_2} I_{\text{nox}} A_{\text{IN}} A_{\text{IP}} A_{\text{IC}}] X_{\text{li}}
                                                                                                                                                                                                                                    \rho_{104} = k_{AB,PRO}(k_{a,PRO}S_{hpro} - S_{pro}S_{H^+})
                                                                                                                                                                                                                                    \rho_{105} = k_{AB,AC}(k_{a,AC}S_{hac} - S_{ac}S_{H^+})
                                                                                                                                                                                                                                    \rho_{106} = k_L a_{CO_2} (k_{H,Co_2} P_{gas,CO_2} - S_{CO_2})
                                                                                                                                                                                                                                    \rho_{107} = k_{L} a_{CO_{2}} (k_{H,CO_{2}} P_{gas,CO_{2}} - S_{O_{2}})
                                                                                                                                                                                                                                    \rho_{108} = k_{\rm M} a_{\rm H_2O} (P_{\rm H_2O}^{\rm SAT} - P_{\rm H_2O})

\rho_{109} = k_{\rm L} a_{\rm NH_3} (k_{\rm H,NH_3} P_{\rm gas,NH_3} - S_{\rm NH_3})

                                                                                                                                                                                                                                   \rho_{110} = k_{\mathrm{L}} a_{\mathrm{NH_4}} (k_{\mathrm{H,CH_4}} P_{\mathrm{gas,CH_4}} - S_{\mathrm{NH_4}})
                                                                                                                                                                                                                                    \rho_{112} = k_{L} a_{H_2} (k_{H,H_2} P_{gas,H_2} - S_{H_2})
```

1 2 3 4 5 6 7 33 34 35 36	Aerobic uptake of S _{su} Aerobic uptake of S _{aa} Aerobic uptake of S _{fa} Aerobic uptake of S _{VA} Aerobic uptake of S _{BU} Aerobic uptake of S _{PRO} Aerobic uptake of S _{AC} Acidogenesis of S _{su} Acidogenesis of S _{aa}	-1	-1	-1								
3 4 5 6 7 33 34 35 36	Aerobic uptake of S_{fa} Aerobic uptake of S_{VA} Aerobic uptake of S_{BU} Aerobic uptake of S_{PRO} Aerobic uptake of S_{AC} Acidogenesis of S_{su}		-1	-1								
4 5 6 7 33 34 35 36	Aerobic uptake of S_{VA} Aerobic uptake of S_{BU} Aerobic uptake of S_{PRO} Aerobic uptake of S_{AC} Acidogenesis of S_{su}			-1								
5 6 7 33 34 35 36	Aerobic uptake of S_{BU} Aerobic uptake of S_{PRO} Aerobic uptake of S_{AC} Acidogenesis of S_{su}											
6 7 33 34 35 36 37	Aerobic uptake of S_{PRO} Aerobic uptake of S_{AC} Acidogenesis of S_{su}				-1							
7 33 34 35 36 37	Aerobic uptake of S _{AC} Acidogenesis of S _{su}					-1						
33 34 35 36 37	Acidogenesis of S _{su}						-1	4				
34 35 36 37		1				f (1 V)	f (1 V)	-1	f (1 V)			
35 36 37	Acidoganacie of C	-1				$f_{\rm bu,su}(1-{\rm Y_{su}})$	$f_{\text{pro,su}}(1 - Y_{\text{su}})$	$f_{\rm ac,su}(1-Y_{\rm su})$	$f_{\rm H_2,su}(1-{\rm Y_{su}})$			
36 37			-1		$f_{\text{va,aa}}(1 - Y_{\text{aa}})$	$f_{\text{bu,aa}}(1 - Y_{\text{aa}})$	$f_{\mathrm{pro,aa}}(1-\mathrm{Y_{aa}})$	$f_{\rm ac,aa}(1-Y_{\rm aa})$	$f_{\rm H_2,aa}(1-{ m Y_{aa}})$			
37	Acetogenesis of S_{fa}			-1				$f_{\rm ac,fa}(1-Y_{\rm fa})$	$f_{\rm H_2,fa}(1-{ m Y_{fa}})$			
	Acetogenesis of S _{VA}				-1		$f_{\text{pro,va}}(1 - Y_{\text{C}_4})$	$f_{\mathrm{ac,va}}(1-\mathrm{Y_{C_4}})$	$f_{\rm H_2,va}(1-{\rm Y}_{\rm C_4})$			
	Acetogenesis of S _{BU}					-1		$f_{\text{ac,bu}}(1 - Y_{\text{C}_4})$	$f_{\rm H_2,bu}(1-{\rm Y}_{\rm C_4})$			
38	Acetogenesis of S _{PRO}						-1	$f_{\rm ac,pro}(1-Y_{\rm pro})$	$f_{\rm H_2,pro}(1-{\rm Y_{pro}})$			
39	Acetoclast. Methanog.							ac,pro	5 112,p10	$1-Y_{ac}$		
40	Hydrogen. Methanog.									$1 - Y_{H_2}$		
41, 69	Decay of X _h									**2		
45, 73	Decay of X _{su}											
46, 74	Decay of X _{aa}											
47, 75	Decay of X _{fa}											
48, 76	Decay of X _{C4}											
49, 77	Decay of X _{pro}											
50, 78	Decay of X _{ac}											
51, 79	Decay of XH2											
84, 88	Disintegration of X_{C_2}										$f_{\rm sp,xC_2}$	$f_{\rm CH,x0}$
89, 95	Hydrolysis X _{ch}	1										-1
90, 96	Hydrolysis X _{pr}		1									
91, 97	Hydrolysis $X_{ m li}$	$1-f_{\mathrm{fa,li}}$		$f_{\mathrm{fa,li}}$								
			18	1	9 2	20 21	22					

1	Aerobic uptake of S _{su}											Y_{H}
2	Aerobic uptake of Saa											Y_{H}
3	Aerobic uptake of S _{fa}											Y_{H}
4	Aerobic uptake of S _{VA}											Y_{H}
5	Aerobic uptake of S _{BU}											Y_{H}
6	Aerobic uptake of Spro											Y_{H}
7	Aerobic uptake of S _{AC}											Y_{H}
33	Acidogenesis of $S_{ m su}$				Y_{su}							
34	Acidogenesis of S _{aa}					Y_{aa}						
35	Acetogenesis of S_{fa}						Y_{fa}					
36	Acetogenesis of S _{VA}							Y_{C_4}				
37	Acetogenesis of S_{BU}							Y_{C_4}				
38	Acetogenesis of S _{PRO}								Y_{pro}			
39	Acetoclast. Methanog.											
40	Hydrogen. Methanog.											
41, 69	Decay of X _h			1								-1
45, 73	Decay of X_{su}			1	-1							
46, 74	Decay of X _{aa}			1		-1						
47, 75	Decay of X_{fa}			1			-1					
48, 76	Decay of X_{C_4}			1				-1				
49, 77	Decay of X _{pro}			1					-1			
50, 78	Decay of X_{ac}			1						-1		
51, 79	Decay of X _{H2}			1							-1	
84, 88	Disintegration of X_{C_2}	$f_{\mathrm{pr,xC_2}}$	f_{li,xC_2}	-1		$f_{\rm xp,xC_2}$						
89, 95	Hydrolysis X _{ch}											
90, 96	Hydrolysis X _{pr}	-1										
91, 97	Hydrolysis X _{li}	-	-1									

Compor	nents i Transformation	ns j	4 S _{hva}	5 S _{va} _	6 S _{hbu}	7 S _{bu} _	8 S _{hpro}	9 S_{pro-}	10 S _{hac}	11 S _{ac} _	12 S _{H2}	13 G _{H2}	14 S _{CH4}	15 G _{CH₄}	30 S _{HCO3}
98 99 100 101 102 103 104 105 106 107 108 109 110	Water equilibiru Inorganic carbon equi Inorg. Nitrogen equil Inorganic phosphorous e Valerate equilibri Butyrate equilibri Propionate equilibri CO ₂ dissolution H ₂ O evaporatio NH ₃ dissolution CH ₄ dissolution CH ₄ dissolution	ilibrium librium equilibrium ium rium um um n i in	-1	1	-1	1	-1	1	-1	1			1	-1	1
112	H ₂ dissolution	31	32	33	34	35	36	37	38		39	-1 40	41	42	43
		G_{CO_2}	S_{CO_2}	S _{NH₃}	G _{NH₃}	$S_{NH_4^+}$	S _{H2PO4} -	$S_{HPO_4}=$			S _H +	G _{H2O}	S _{H2} O	G_{O_2}	S _{O2}
98	Water equilibirum		ν _{SCO2,98}			v _{SNH₄} ,98		ν _{SHPO_4,98}	, 1	v	S _{H⁺,98}	v _{SH2O,98}		ν _{SO2,98}	
99	Inorganic carbon equilibrium		$v_{S_{\text{CO}_2,99}}$			vs _{NH⁺₄,99}		ν _{S_{HPO}_,99})		S _{H+,99}		v _{SH2O,99}		$v_{S_{O_2,99}}$
100	Inorg. Nitrogen equilibrium		$v_{\text{S}_{\text{CO}_2,100}}$	1		v _{SNH₄+,100}		ν _{SHPO} ,10	00	v	S _{H+,100}		$v_{\rm S_{H_2O,100}}$		$v_{S_{O_2,100}}$
101	Inorganic phosphorous equilibrium		$v_{\text{S}_{\text{CO}_2,101}}$			ν _{SNH4} ,101	-1	ν _{SHPO4} ,103	1	v	S _{H+,101}		$v_{\rm S_{H_2O,101}}$		$v_{S_{O_2,101}}$
102	Valerate equilibrium		$v_{S_{\mathrm{CO}_2,102}}$			v _{SNH₄+,102}		ν _{SHPO} _,102	2	v	S _{H+,102}		$v_{\rm S_{H_2O,102}}$		$v_{S_{O_2,102}}$
103	Butyrate equilibrium		$v_{\text{S}_{\text{CO}_2,103}}$			v _{SNH₄+,103}		ν _{SHPO} _,103	3	v	S _{H+,103}		$v_{\rm S_{H_2O,103}}$		$v_{S_{O_2,103}}$
104	Propionate equilibrium		$v_{S_{\text{CO}_2,104}}$			vs _{NH₄+,104}		ν _{SHPO} _,104	4	v	S _{H+,104}		v _S _{H2O,104}		$v_{S_{O_2,104}}$
105	Acetate equilibrium		$v_{S_{\text{CO}_2,105}}$			v _{SNH₄+,105}		ν _{SHPO} _,105			S _H +,105		ν _{SH2O,105}		$v_{S_{O_2,105}}$
106	CO ₂ dissolution	-1	v _S _{CO₂,106}			vs _{NH₄} ,106		vs _{HPO} _,106		v	S _{H+,106}		vs _{H2O,106}		v _{SO2,106}
107	O ₂ dissolution		v _{SCO2,107}			v _{SNH₄+,107}		ν _{S_{HPO}_,107}		v	S _{H+,107}		$v_{S_{\mathrm{H}_2\mathrm{O},107}}$	-1	$v_{S_{O_2,107}}$
108	H ₂ O evaporation		v _{SCO2,108}			v _{SNH₄+,108}		ν _{SHPO4} ,108		v	S _H +,108	1	v _{SH2O,108}		$v_{S_{O_2,108}}$
109	NH ₃ dissolution		v _{SCO2,109}	1	-1	v _{SNH⁺,109}		v _{S_{HPO}_,109}			S _{H+,109}		ν _{S_{H2}O,109}		$v_{S_{O_2,109}}$
110	CH ₄ dissolution		$v_{S_{\text{CO}_2,110}}$			v _{SNH₄+,110}		v _{SHPO} _,110			S _{H+,110}		$v_{\rm S_{\rm H_2O,110}}$		$v_{S_{O_2,110}}$
112	H ₂ dissolution		$v_{S_{\text{CO}_2,112}}$			v _S _{NH⁺,112}		ν _{S_{HPO}_,112}			S _{H+,102}		ν _{S_{H2}O,112}		$v_{S_{O_2,112}}$

Table 7 – Stoichiometry of the source–sink components											
32 S _{CO2}	35 S _{NH4} ⁺	37 S _{HPO₄=}	39 S _H +	41 S _{H2O}	43 S _{O2}						
$v_{S_{CO_2,j}} = -\sum_{i=1}^{31} \left(\frac{\beta_{C,i} v_{ij}}{\beta_{C,S_{CO_2}}} \right)$	$v_{S_{NH_{4}^{+},j}} = -\sum_{i=1}^{34} \left(\frac{\beta_{N,i}v_{ij}}{\beta_{N,S_{NH_{4}}^{+}}}\right)$	$v_{S_{\text{HPO}_4}=j} = -\sum_{i=1}^{36} \left(\frac{\beta_{P,i}v_{ij}}{\beta_{P,S_{\text{HPO}_4}=}} \right)$	$v_{\text{Sh}^{+},j} = -\sum_{i=1}^{38} \left(\frac{\beta_{\text{Ch},i} v_{ij}}{\beta_{\text{Ch},\text{Sh}^{+}}} \right)$	$v_{S_{\text{H}_2\text{O},j}} = -\sum_{i=1}^{40} \left(\frac{\beta_{\text{H},i} v_{ij}}{\beta_{\text{H},S_{\text{H}_2\text{O}}}} \right)$	$v_{S_{O_2,j}} = -\sum_{i=1}^{42} \left(\frac{\beta_{O,i} v_{ij}}{\beta_{O,S_{O_2}}} \right)$						

 $\beta_{\rm F,i}$: Mass of the element E per stoichiometric unit of the component i calculated from the i mass fractions.

3.2.1. Mass transport description

The description of the mass transport in the activated sludge reactor and the digester, where transformations occur in a significant way, is based on a biological reactor model. Since the constructed PTM includes components in liquid (dissolved and particulate) and gaseous phases, one must consider these two phases in the biological reactor model. The anaerobic digester consists of two continuous stirred-tank reactors (CSTRs), each with its own interfaces, corresponding to these two phases and where liquid-gas transfers take place. Therefore, mass transport will be described by means of mass balances applied to the liquid and gaseous phases. The activated sludge reactor is composed of a CSTR that represents the liquid phase in contact with the atmosphere, in which the gaseous components present constant concentrations. In this case, the mass transport description is described by mass balances applied to the liquid phase.

On the other hand, the mass transport description of the secondary settler can be reproduced by standard models that are normally utilized (ideal settlers, layered settlers, etc.) using the TSS variable.

3.2.2. Internal transformations

As recommended in Section 2, the set of internal transformations and components considered in each UPM should coincide with the PTM created in the previous step.

According to this suggestion, the PTM obtained in step A has been utilized to describe the internal transformations in the aerated activated sludge tank and in the anaerobic digester. In this manner, mass and charge continuity are guaranteed in these UPMs and the PCV can act as an input-output interface without the need of transformers among specific component vectors and the common PCV.

However, with respect to the secondary settler UPM, as the mass transport is described based on the lumped variable TSS, specific input–output transformers must be included to convert particulate components of the PCV into the variable TSS and vice-versa. Relationships between the COD and the mass of organic components, easily established with the methodology proposed in this paper, permit a direct conversion between organic particulate components and TSS, guaranteeing the mass continuity during stationary and dynamic conditions.

3.3. Construction of the PWM for the whole plant

Finally, the PWM for the WWTP proposed in this example has been created by the direct connection of the mass fluxes among the UPMs. The obtained PWM, specific for this WWTP, is able to reproduce all relevant process transformations and guarantees mass and charge continuity throughout the whole plant without specific transformers among the UPMs.

In addition to the example presented in this paper, other models have been constructed, implemented in the simulation platform WEST (http://www.mostforwater.com) and successfully validated using the methodology proposed in this paper, such as the BSM2 PWM (Grau et al., 2007), the ADM (Huete et al., 2006) and the composting reactor system model (Zurcan et al., 2005).

It is important to point out the advantages of the transformation-based approach from the point of view of developing computer code for simulation platforms. The general LT can be compiled as a general library from which the modeller can construct tailored PWMs as simple or as complex as needed in each case study.

4. Conclusions

The integrated modelling of an entire WWTP, including the mutual relationships among the different unit-process elements of the water and sludge lines, is not as straightforward as the simple connection of existing models. A rigorous model development must analyse the appropriate definition of model components at each unit-process element and the mass continuity among all of them.

The PWM methodology proposed in this paper takes into account the advantages and limitations of existing approaches and develops a systematic procedure for the tailored construction of integrated mathematical models for WWTPs, including water and sludge lines, without the need of specific transformers among UPMs and guarantees mass and charge continuity throughout the WWTP under any dynamic condition. Additionally, the proposed "transformation-based" approach facilitates the development of simulation codes in an efficient modular manner.

The example given in this paper has illustrated the different steps of the systematic procedure to construct integrated models where the mass continuity is guaranteed throughout the whole plant.

Nowadays, it is probably time to rewrite the existing UPMs when they are used for integrated modelling objectives. From an "approved" list of process transformations, agreed upon by modelling experts, a general and systematic procedure can be developed to create compatible UPMs, and integrated models adapted to the specific plant under study.

The fact that the LTist of transformations and components is open and allows the incorporation of new transformations and components provides a useful and flexible modelling approach that facilitates the interchange and contrast of information between modelling teams.

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