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Algorithm Cheat Sheet (Pageless)
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```
1 QuickSelect
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```

1.1 Implementation // Partition function: rearranges elements around a pivot

QuickSelect

1

Contents

// After partitioning: - elements <= pivot are on the left // - elements > pivot are on the right // Returns the final index of the pivot

// i points to the next position for swapping

// If element <= pivot, move it to

• Space complexity: O(1) (in-place, recursive stack $O(\log n)$ on average)

QuickSelect is an algorithm to find the k-th smallest (or largest) element in an unsorted array. It is related to QuickSort but only recurses on the side containing the \$k\$-th element.

int partition(vector<int>& arr, int left, int right) { // Kandomly pick a pivot index to reduce worst-case

• Average time complexity: O(n)

• Worst-case time complexity: $O(n^2)$

- int pivot_idx = left + rand() % (right left + 1); int pivot = arr[pivot_idx];
- // Move pivot to the end temporarily

swap(arr[i], arr[right]);

swap(arr[pivot_idx], arr[right]);

swap(arr[i], arr[j]);

// Place pivot in its correct sorted position

return i; // return the index of the pivot

smaller elements for (int j = left; j < right; j++) {</pre> if (arr[j] <= pivot) {</pre>

}

}

}

int i = left;

```
// QuickSelect: finds the k-th smallest element (1-indexed)
int quickSelect(vector<int>& arr, int left, int right, int k) {
    if (left == right) return arr[left]; // only one element
    // Partition the array and get pivot index
    int pivot_idx = partition(arr, left, right);
    int count = pivot_idx - left + 1; // number of elements <= pivot</pre>
    if (count == k) {
        return arr[pivot_idx]; // pivot is the k-th smallest element
    } else if (k < count) {</pre>
        // k-th element lies in left partition
        return quickSelect(arr, left, pivot_idx - 1, k);
    } else {
        // k-th element lies in right partition
        // adjust k because we discard left partition
        return quickSelect(arr, pivot_idx + 1, right, k - count);
    }
}
    Practice Problems
1.2
  • K-th Largest Element in an Array (LeetCode)
    Trie (Prefix Tree)
\mathbf{2}
Efficient data structure for string retrieval problems (prefixes, alphabets, etc).
2.1
     Implementation
const int ALPHABET = 26; // number of lowercase letters
struct TrieNode {
    TrieNode *children[ALPHABET]; // pointers to child nodes
                                    // number of words ending at this
    int terminal;
       node
};
// Create and initialize a new Trie node
TrieNode *new_node() {
    TrieNode *node = new TrieNode;
```

node->children[i] = nullptr; // initialize all children to

if (!node->children[idx]) // if child does not exist,

if (node->terminal > 0) node->terminal--; // unmark end of word

node->children[idx] = new_node();

node = node->children[idx]; // move to the child

// no word ends here yet

// map char to index 0-25

// mark end of word

for (char c : s) { int idx = c - 'a'; if (!node->children[idx]) return; // word not found node = node->children[idx];

for(int i = 0; i < ALPHABET; ++i)</pre>

null

return node;

}

}

}

node->terminal = 0;

for (char c : s) {

node->terminal++;

// Insert a string into the trie

create it

// Remove a string from the trie

// Search for a string in the trie

bool search(TrieNode *node, string s) {

void remove(TrieNode *node, string s) {

int idx = c - 'a';

void insert(TrieNode *node, string s) {

```
for (char c : s) {
          int idx = c - 'a';
         if (!node->children[idx]) return false; // missing letter
         node = node->children[idx];
    return node->terminal > 0; // true if word ends here
2.2
      Practice Problems
   • Codeforces 706D
   • Word Search II (Leetcode)
3
     Huffman Coding
Huffman Coding is a lossless data compression algorithm that assigns variable-length codes
to characters based on their frequency. More frequent characters get shorter codes, while
less frequent characters get longer codes.
   • Time complexity: O(n \log n) where n is the number of unique characters
   • Space complexity: O(n) for the tree structure
3.1
      Key Properties
   • Prefix-free codes: The tree structure ensures that no character's code is a prefix
     of another character's code. This eliminates the need for separators between encoded
     characters and allows unambiguous decoding.
   • Optimal compression: For a given set of character frequencies, Huffman coding
     produces the minimum possible average code length.
3.2
      Algorithm Steps
  1. Count frequency of each character
  2. Create leaf nodes for each character and build a min-heap
  3. While heap has more than one node:
       • Extract two nodes with minimum frequency
       • Create new internal node with these as children
       • Set frequency as sum of children frequencies
       • Insert back into heap
```

HuffmanNode(char d, int f) : data(d), freq(f), left(nullptr),

 $HuffmanNode(int f) : data('\0'), freq(f), left(nullptr), right($

return a->data > b->data; // tie-breaker for consistency

}; // Comparator for priority queue (min-heap based on frequency) struct Compare { bool operator()(HuffmanNode* a, HuffmanNode* b) {

minHeap;

}

}

}

}

};

nullptr) {}

4. Root of remaining tree is the Huffman tree

5. Assign codes: left edge = 0, right edge = 1

Implementation

HuffmanNode* left; HuffmanNode* right;

right(nullptr) {}

if (a-)freq == b-)freq {

return a->freq > b->freq;

// Build Huffman tree from character frequencies

// Create leaf nodes and add to heap

for (auto& pair : freq) {

// Build tree bottom-up

freq);

while (minHeap.size() > 1) {

// Create internal node

merged->left = left; merged->right = right;

minHeap.push(merged);

return minHeap.top(); // root of Huffman tree

HuffmanNode* buildHuffmanTree(unordered_map < char, int > & freq) { priority_queue < HuffmanNode*, vector < HuffmanNode*>, Compare>

minHeap.push(new HuffmanNode(pair.first, pair.second));

HuffmanNode* merged = new HuffmanNode(left->freq + right->

HuffmanNode* left = minHeap.top(); minHeap.pop(); HuffmanNode* right = minHeap.top(); minHeap.pop();

struct HuffmanNode { char data; int freq;

3.3

```
// Generate codes by traversing the tree
void generateCodes(HuffmanNode* root, string code, unordered_map <</pre>
   char, string>& codes) {
    if (!root) return;
    // Leaf node - store the code
    if (!root->left && !root->right) {
        codes[root->data] = code.empty() ? "0" : code; // handle
           single character case
        return;
    }
    generateCodes(root->left, code + "0", codes);
    generateCodes(root->right, code + "1", codes);
// Encode text using Huffman codes
string encode(string text, unordered_map<char, string>& codes) {
    string encoded = "";
    for (char c : text) {
        encoded += codes[c];
    return encoded;
}
// Decode using Huffman tree
string decode(string encoded, HuffmanNode* root) {
    string decoded = "";
    HuffmanNode* current = root;
    for (char bit : encoded) {
        if (bit == '0') {
            current = current->left;
        } else {
            current = current->right;
        // Reached leaf node
        if (!current->left && !current->right) {
            decoded += current->data;
             current = root; // reset to root
        }
    }
   return decoded;
}
// Complete Huffman coding example
void huffmanExample() {
    string text = "abracadabra";
    // Count frequencies
    unordered_map < char, int > freq;
    for (char c : text) {
        freq[c]++;
    }
    // Build tree and generate codes
    HuffmanNode* root = buildHuffmanTree(freq);
    unordered_map < char, string > codes;
    generateCodes(root, "", codes);
    // Print codes
    cout << "Huffman Codes:" << endl;
    for (auto& pair : codes) {
        cout << pair.first << ":" << pair.second << endl;
    // Encode and decode
    string encoded = encode(text, codes);
    string decoded = decode(encoded, root);
    cout << "Original: " << text << endl;
    cout << "Encoded: " << encoded << endl;
    cout << "Decoded: " << decoded << endl;
}
3.4
     Example
For text "abracadabra":
  • Frequencies: a(5), b(2), r(2), c(1), d(1)
  • Possible codes: a(0), b(10), r(110), c(1110), d(1111)
  • Original: 88 bits (8 bits per char × 11 chars)
  • Compressed: 27 bits (5\times1+2\times2+2\times3+1\times4+1\times4)
  • Compression ratio: 69% reduction
     Practice Problems
  • Huffman Tree Construction
  • Text Compression Problems
    Unit Testing
How to write unit tests for your code.
4.1
     Pytest
Simple Python program:
# file: math_utils.py
def add(a, b):
    return a + b
def divide(a, b):
        raise ValueError("Cannotudivideubyuzero")
    return a / b
# file: test_math_utils.py
import pytest
from math_utils import add, divide
def test_add():
    assert add(2, 3) == 5
    assert add(-1, 1) == 0
    assert add(0, 0) == 0
def test_divide():
    assert divide(6, 3) == 2
    assert divide(5, 2) == 2.5
```

Check that dividing by zero raises an exception

if (b == 0) throw std::runtime_error("Cannotudivideubyuzero");

A monotonic stack is a standard stack (LIFO), but the elements mantain a monotonic order

• Who blocks visibility? (think about the problem about heights and how many people

Whenever we want to push an element x, while the top of the stack violates the monotone property, pop it (and posibly update something related to the answer). After this, push x. This has O(n) time complexity, because every element is pushed and popped at most once.

• Increasing stack: elements are in increasing order from bottom to top.

• Decreasing stack: elements are in decreasing order from bottom to top.

This allows us to efficiently answer the following questions:

• How many elements are visible until I hit a blocker?

with pytest.raises(ValueError):

double divide(double a, double b) {

Disjoint Set Union (DSU)

What is it and when to use it

• What is the next **greater/smaller element**?

can every person see on leetcode)

Monotonic Stack

divide(1, 0)

How to run the tests:

Catch2

4.2

}

5

6

6.1

6.2

6.3

at every time.

pytest test_math_utils.py

// file: math_utils.hpp int add(int a, int b) { return a + b;

return a / b;

• Next Greater Element I (LeetCode) • Next Greater Element II (LeetCode) • Daily Temperatures (LeetCode) • Largest Rectangle in Histogram (LeetCode)

Principle

Problems

• Maximal Rectangle (LeetCode)

• Number of Visible People in a Queue (LeetCode)

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