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Algorithm Cheat Sheet (Pageless)
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  QuickSelect
1
QuickSelect is an algorithm to find the k-th smallest (or largest) element in an unsorted
array. It is related to QuickSort but only recurses on the side containing the $k$-th element.
 • Average time complexity: O(n)
 • Worst-case time complexity: O(n^2)
 • Space complexity: O(1) (in-place, recursive stack O(\log n) on average)
1.1
  Implementation
// Partition function: rearranges elements around a pivot
// After partitioning:
// - elements <= pivot are on the left</pre>
// - elements > pivot are on the right
// Returns the final index of the pivot
```

int partition(vector<int>& arr, int left, int right) { // Randomly pick a pivot index to reduce worst-case int pivot_idx = left + rand() % (right - left + 1); int pivot = arr[pivot_idx]; // Move pivot to the end temporarily swap(arr[pivot_idx], arr[right]); int i = left; // i points to the next position for swapping smaller elements for (int j = left; j < right; j++) {</pre> // If element <= pivot, move it to if (arr[j] <= pivot) {</pre> swap(arr[i], arr[j]); i++; } } // Place pivot in its correct sorted position swap(arr[i], arr[right]); return i; // return the index of the pivot // QuickSelect: finds the k-th smallest element (1-indexed) int quickSelect(vector<int>& arr, int left, int right, int k) { if (left == right) return arr[left]; // only one element // Partition the array and get pivot index int pivot_idx = partition(arr, left, right); int count = pivot_idx - left + 1; // number of elements <= pivot</pre> if (count == k) { return arr[pivot_idx]; // pivot is the k-th smallest element } else if (k < count) {</pre> // k-th element lies in left partition return quickSelect(arr, left, pivot_idx - 1, k); } else { // k-th element lies in right partition // adjust k because we discard left partition return quickSelect(arr, pivot_idx + 1, right, k - count); } Practice Problems • K-th Largest Element in an Array (LeetCode) Trie (Prefix Tree) Efficient data structure for string retrieval problems (prefixes, alphabets, etc). Implementation 2.1

} // Insert a string into the trie void insert(TrieNode *node, string s) { for (char c : s) { int idx = c - 'a'; if (!node->children[idx])

create it

return node;

node->terminal = 0;

struct TrieNode {

int terminal; node

TrieNode *new_node() {

}

}

};

}

node -> children[idx] = new_node(); node = node->children[idx]; // move to the child } // mark end of word node->terminal++;

const int ALPHABET = 26; // number of lowercase letters

// Create and initialize a new Trie node

TrieNode *node = new TrieNode; for(int i = 0; i < ALPHABET; ++i)</pre>

TrieNode *children[ALPHABET]; // pointers to child nodes

node->children[i] = nullptr; // initialize all children to

// number of words ending at this

// no word ends here yet

// map char to index 0-25

// if child does not exist,

```
// Remove a string from the trie
void remove(TrieNode *node, string s) {
    for (char c : s) {
         int idx = c - 'a';
         if (!node->children[idx]) return; // word not found
         node = node->children[idx];
    }
    if (node->terminal > 0) node->terminal--; // unmark end of word
}
// Search for a string in the trie
bool search(TrieNode *node, string s) {
    for (char c : s) {
         int idx = c - 'a';
         if (!node->children[idx]) return false; // missing letter
         node = node->children[idx];
    return node->terminal > 0; // true if word ends here
}
      Practice Problems
2.2
   • Codeforces 706D
    Huffman Coding
3
Huffman Coding is a lossless data compression algorithm that assigns variable-length codes
to characters based on their frequency. More frequent characters get shorter codes, while
less frequent characters get longer codes.
   • Time complexity: O(n \log n) where n is the number of unique characters
  • Space complexity: O(n) for the tree structure
      Key Properties
3.1
  • Prefix-free codes: The tree structure ensures that no character's code is a prefix
    of another character's code. This eliminates the need for separators between encoded
    characters and allows unambiguous decoding.
   • Optimal compression: For a given set of character frequencies, Huffman coding
    produces the minimum possible average code length.
3.2
      Algorithm Steps
  1. Count frequency of each character
  2. Create leaf nodes for each character and build a min-heap
  3. While heap has more than one node:
       • Extract two nodes with minimum frequency
```

• Create new internal node with these as children

• Set frequency as sum of children frequencies

• Insert back into heap

Implementation

HuffmanNode* left; HuffmanNode* right;

nullptr) {}

struct Compare {

};

right(nullptr) {}

 $if (a->freq == b->freq) {$

while (minHeap.size() > 1) {

// Create internal node

merged->left = left; merged->right = right;

minHeap.push(merged);

// Generate codes by traversing the tree

// Leaf node - store the code

if (!root->left && !root->right) {

single character case

return minHeap.top(); // root of Huffman tree

freq);

char, string>& codes) { if (!root) return;

}

struct HuffmanNode { char data; int freq;

4. Root of remaining tree is the Huffman tree

5. Assign codes: left edge = 0, right edge = 1

return a->freq > b->freq; } }; // Build Huffman tree from character frequencies HuffmanNode* buildHuffmanTree(unordered_map<char, int>& freq) { priority_queue < HuffmanNode*, vector < HuffmanNode*>, Compare> minHeap; // Create leaf nodes and add to heap for (auto& pair : freq) { minHeap.push(new HuffmanNode(pair.first, pair.second)); // Build tree bottom-up

> HuffmanNode* left = minHeap.top(); minHeap.pop(); HuffmanNode* right = minHeap.top(); minHeap.pop();

void generateCodes(HuffmanNode* root, string code, unordered_map

codes[root->data] = code.empty() ? "0" : code; // handle

HuffmanNode* merged = new HuffmanNode(left->freq + right->

HuffmanNode(char d, int f) : data(d), freq(f), left(nullptr),

// Comparator for priority queue (min-heap based on frequency)

bool operator()(HuffmanNode* a, HuffmanNode* b) {

 $HuffmanNode(int f) : data('\0'), freq(f), left(nullptr), right($

return a->data > b->data; // tie-breaker for consistency

```
return;
    }
    generateCodes(root->left, code + "0", codes);
    generateCodes(root->right, code + "1", codes);
}
// Encode text using Huffman codes
string encode(string text, unordered_map < char, string > & codes) {
    string encoded = "";
    for (char c : text) {
        encoded += codes[c];
    return encoded;
}
// Decode using Huffman tree
string decode(string encoded, HuffmanNode* root) {
    string decoded = "";
    HuffmanNode* current = root;
    for (char bit : encoded) {
        if (bit == '0') {
            current = current ->left;
        } else {
            current = current->right;
        // Reached leaf node
        if (!current->left && !current->right) {
            decoded += current->data;
             current = root; // reset to root
        }
    }
   return decoded;
}
// Complete Huffman coding example
void huffmanExample() {
    string text = "abracadabra";
    // Count frequencies
    unordered_map < char, int > freq;
    for (char c : text) {
        freq[c]++;
    }
    // Build tree and generate codes
    HuffmanNode* root = buildHuffmanTree(freq);
    unordered_map < char, string > codes;
    generateCodes(root, "", codes);
    // Print codes
    cout << "HuffmanuCodes:" << endl;</pre>
    for (auto& pair : codes) {
        cout << pair.first << ":" << pair.second << endl;
    }
    // Encode and decode
    string encoded = encode(text, codes);
    string decoded = decode(encoded, root);
    cout << "Original:" << text << endl;
    cout << "Encoded: " << encoded << endl;
    cout << "Decoded:\Box" << decoded << endl;
}
     Example
3.4
For text "abracadabra":
  • Frequencies: a(5), b(2), r(2), c(1), d(1)
  • Possible codes: a(0), b(10), r(110), c(1110), d(1111)
  • Original: 88 bits (8 bits per char × 11 chars)
  • Compressed: 27 bits (5\times1+2\times2+2\times3+1\times4+1\times4)
  • Compression ratio: 69% reduction
     Practice Problems
3.5
  • Huffman Tree Construction
  • Text Compression Problems
4
    Unit Testing
How to write unit tests for your code.
4.1
     Pytest
Simple Python program:
# file: math_utils.py
def add(a, b):
    return a + b
def divide(a, b):
    if b == 0:
        raise ValueError("Cannotudivideubyuzero")
    return a / b
# file: test_math_utils.py
import pytest
from math_utils import add, divide
def test_add():
    assert add(2, 3) == 5
    assert add(-1, 1) == 0
    assert add(0, 0) == 0
def test_divide():
    assert divide(6, 3) == 2
    assert divide(5, 2) == 2.5
    # Check that dividing by zero raises an exception
    with pytest.raises(ValueError):
        divide(1, 0)
```

How to run the tests:

Catch2

4.2

}

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pytest test_math_utils.py

// file: math_utils.hpp int add(int a, int b) { return a + b;

return a / b;

double divide(double a, double b) {

Disjoint Set Union (DSU)

if (b == 0) throw std::runtime_error("Cannot_divide_by_zero");

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