Contents

```
QuickSelect
1
QuickSelect is an algorithm to find the k-th smallest (or largest) element in an unsorted
array. It is related to QuickSort but only recurses on the side containing the $k$-th element.
```

```
• Average time complexity: O(n)
• Worst-case time complexity: O(n^2)
• Space complexity: O(1) (in-place, recursive stack O(\log n) on average)
```

// Returns the final index of the pivot

int pivot = arr[pivot_idx];

- 1.1 Implementation
- // Partition function: rearranges elements around a pivot // After partitioning: // - elements <= pivot are on the left // - elements > pivot are on the right

// Randomly pick a pivot index to reduce worst-case int pivot_idx = left + rand() % (right - left + 1);

int partition(vector<int>& arr, int left, int right) {

- // Move pivot to the end temporarily swap(arr[pivot_idx], arr[right]); int i = left; // i points to the next position for swapping smaller elements for (int j = left; j < right; j++) {</pre> if (arr[j] <= pivot) {</pre> // If element <= pivot, move it to swap(arr[i], arr[j]); i++; } // Place pivot in its correct sorted position swap(arr[i], arr[right]); return i; // return the index of the pivot // QuickSelect: finds the k-th smallest element (1-indexed) int quickSelect(vector<int>& arr, int left, int right, int k) { if (left == right) return arr[left]; // only one element // Partition the array and get pivot index int pivot_idx = partition(arr, left, right); int count = pivot_idx - left + 1; // number of elements <= pivot</pre> **if** (count == k) { return arr[pivot_idx]; // pivot is the k-th smallest element $}$ else if (k < count) { // k-th element lies in left partition return quickSelect(arr, left, pivot_idx - 1, k); // k-th element lies in right partition // adjust k because we discard left partition return quickSelect(arr, pivot_idx + 1, right, k - count); }
- TrieNode *children[ALPHABET]; // pointers to child nodes // number of words ending at this int terminal; node };

// Create and initialize a new Trie node

void insert(TrieNode *node, string s) {

int idx = c - 'a';

Practice Problems

Trie (Prefix Tree)

Implementation

struct TrieNode {

• K-th Largest Element in an Array (LeetCode)

Efficient data structure for string retrieval problems (prefixes, alphabets, etc).

const int ALPHABET = 26; // number of lowercase letters

// no word ends here yet

// map char to index 0-25

// mark end of word

if (!node->children[idx]) // if child does not exist,

node -> children[idx] = new_node();

node = node->children[idx]; // move to the child

TrieNode *node = new TrieNode; for(int i = 0; i < ALPHABET; ++i)</pre> node->children[i] = nullptr; // initialize all children to null

node->terminal = 0;

for (char c : s) {

node->terminal++;

}

return node; } // Insert a string into the trie

TrieNode *new_node() {

}

1.2

2

2.1

```
// Remove a string from the trie
void remove(TrieNode *node, string s) {
    for (char c : s) {
         int idx = c - 'a';
         if (!node->children[idx]) return; // word not found
         node = node->children[idx];
    if (node->terminal > 0) node->terminal--; // unmark end of word
}
// Search for a string in the trie
bool search(TrieNode *node, string s) {
    for (char c : s) {
         int idx = c - 'a';
         if (!node->children[idx]) return false; // missing letter
         node = node->children[idx];
    }
    return node->terminal > 0; // true if word ends here
}
      Practice Problems
2.2
   • Codeforces 706D
   • Word Search II (Leetcode)
3
    Huffman Coding
Huffman Coding is a lossless data compression algorithm that assigns variable-length codes
to characters based on their frequency. More frequent characters get shorter codes, while
less frequent characters get longer codes.
   • Time complexity: O(n \log n) where n is the number of unique characters
   • Space complexity: O(n) for the tree structure
      Key Properties
  • Prefix-free codes: The tree structure ensures that no character's code is a prefix
    of another character's code. This eliminates the need for separators between encoded
    characters and allows unambiguous decoding.
```

• Optimal compression: For a given set of character frequencies, Huffman coding

produces the minimum possible average code length.

2. Create leaf nodes for each character and build a min-heap

• Extract two nodes with minimum frequency

• Set frequency as sum of children frequencies

• Create new internal node with these as children

4. Root of remaining tree is the Huffman tree 5. Assign codes: left edge = 0, right edge = 1

struct HuffmanNode { char data; int freq;

struct Compare {

Implementation

HuffmanNode* left; HuffmanNode* right;

Algorithm Steps

1. Count frequency of each character

3. While heap has more than one node:

Insert back into heap

3.2

3.3

HuffmanNode(char d, int f) : data(d), freq(f), left(nullptr), right(nullptr) {} data('\0'), freq(f), left(nullptr), right(HuffmanNode(int f) nullptr) {} };

// Comparator for priority queue (min-heap based on frequency)

bool operator()(HuffmanNode* a, HuffmanNode* b) {

return a->data > b->data; // tie-breaker for consistency return a->freq > b->freq; } };

// Build Huffman tree from character frequencies

if (a-)freq == b-)freq {

// Build tree bottom-up

freq);

}

while (minHeap.size() > 1) {

// Create internal node

merged->left = left; merged->right = right;

minHeap.push(merged);

HuffmanNode* buildHuffmanTree(unordered_map<char, int>& freq) { priority_queue < HuffmanNode*, vector < HuffmanNode*>, Compare> minHeap; // Create leaf nodes and add to heap for (auto& pair : freq) { minHeap.push(new HuffmanNode(pair.first, pair.second)); }

> HuffmanNode* left = minHeap.top(); minHeap.pop(); HuffmanNode* right = minHeap.top(); minHeap.pop();

HuffmanNode* merged = new HuffmanNode(left->freq + right->

```
return minHeap.top(); // root of Huffman tree
}
// Generate codes by traversing the tree
void generateCodes(HuffmanNode* root, string code, unordered_map
   char, string>& codes) {
    if (!root) return;
    // Leaf node - store the code
    if (!root->left && !root->right) {
        codes[root->data] = code.empty() ? "0" : code; // handle
           single character case
        return;
    }
    generateCodes(root->left, code + "0", codes);
    generateCodes(root->right, code + "1", codes);
}
// Encode text using Huffman codes
string encode(string text, unordered_map<char, string>& codes) {
    string encoded = "";
    for (char c : text) {
        encoded += codes[c];
    return encoded;
}
// Decode using Huffman tree
string decode(string encoded, HuffmanNode* root) {
    string decoded = "";
    HuffmanNode* current = root;
    for (char bit : encoded) {
        if (bit == '0') {
            current = current->left;
        } else {
             current = current->right;
        }
        // Reached leaf node
        if (!current->left && !current->right) {
            decoded += current->data;
             current = root; // reset to root
        }
    }
    return decoded;
}
// Complete Huffman coding example
void huffmanExample() {
    string text = "abracadabra";
    // Count frequencies
    unordered_map < char, int > freq;
    for (char c : text) {
        freq[c]++;
    }
    // Build tree and generate codes
    HuffmanNode* root = buildHuffmanTree(freq);
    unordered_map < char, string > codes;
    generateCodes(root, "", codes);
    // Print codes
    cout << "Huffman_Codes:" << endl;</pre>
    for (auto& pair : codes) {
        cout << pair.first << ":" << pair.second << endl;
    }
    // Encode and decode
    string encoded = encode(text, codes);
    string decoded = decode(encoded, root);
    cout << "Original: " << text << endl;
    cout << "Encoded: " << encoded << endl;
    cout << "Decoded: " << decoded << endl;
}
3.4
     Example
For text "abracadabra":
  • Frequencies: a(5), b(2), r(2), c(1), d(1)
  • Possible codes: a(0), b(10), r(110), c(1110), d(1111)
  • Original: 88 bits (8 bits per char × 11 chars)
  • Compressed: 27 bits (5\times1+2\times2+2\times3+1\times4+1\times4)
  • Compression ratio: 69% reduction
3.5
    Practice Problems
  • Huffman Tree Construction
  • Text Compression Problems
    Unit Testing
4
How to write unit tests for your code.
4.1
     Pytest
Simple Python program:
```

int add(int a, int b) { return a + b; double divide(double a, double b) { if (b == 0) throw std::runtime_error("Cannot_divide_by_zero");

return a / b;

Catch2

4.2

}

5

6

6.2

6.3

}

at every time.

file: math_utils.py

return a + b

return a / b

file: test_math_utils.py

assert add(2, 3) == 5assert add(-1, 1) == 0assert add(0, 0) == 0

assert divide(6, 3) == 2assert divide(5, 2) == 2.5

divide(1, 0)

How to run the tests:

pytest test_math_utils.py

// file: math_utils.hpp

with pytest.raises(ValueError):

Disjoint Set Union (DSU)

What is it and when to use it

• What is the next **greater/smaller element**?

can every person see on leetcode)

• Next Greater Element I (LeetCode)

• Next Greater Element II (LeetCode)

• Largest Rectangle in Histogram (LeetCode)

vector < vector < pair < int , int >>> adj;

d.assign(adj.size(), INF); fat.assign(adj.size(), -1);

<pair<ll, int>>> q;

pair<ll, int> curr = q.top();

for (pair<int, int> nbr : adj[curr.ss]) {

fat[nbr.ff] = curr.ss;

if (d[nbr.ff] > d[curr.ss] + nbr.ss) {

q.push({d[nbr.ff], nbr.ff});

d[nbr.ff] = d[curr.ss] + (ll) nbr.ss;

adj = adjacency_list;

void search(int source) {

d[source] = 0;

q.pop();

q.push({0, source});

while (!q.empty()) {

• Daily Temperatures (LeetCode)

• Maximal Rectangle (LeetCode)

Principle

Problems

A monotonic stack is a standard stack (LIFO), but the elements mantain a monotonic order

• Who blocks visibility? (think about the problem about heights and how many people

Whenever we want to push an element x, while the top of the stack violates the monotone property, pop it (and posibly update something related to the answer). After this, push x. This has O(n) time complexity, because every element is pushed and popped at most once.

• Increasing stack: elements are in increasing order from bottom to top.

• Decreasing stack: elements are in decreasing order from bottom to top.

This allows us to efficiently answer the following questions:

• How many elements are visible until I hit a blocker?

Monotonic Stack

from math_utils import add, divide

raise ValueError("Cannotudivideubyuzero")

Check that dividing by zero raises an exception

def divide(a, b): **if** b == 0:

def add(a, b):

import pytest

def test_add():

def test_divide():

• Number of Visible People in a Queue (LeetCode) Dijkstra's Algorithm 7.1Implementation class Dijk { public: vector < int > fat; vector <11> d;

Dijk(const vector<vector<pair<int, int>>> &adjacency_list) {

priority_queue < pair < 11 , int > , vector < pair < 11 , int > > , greater

} }; Practice Problems

• CSES 1671 - Shortest Routes I

• CSES 1194 - Flight Discount

• CSES 1202 - Message Route

}

- CSES 1203 Labyrinth • Codeforces 20C - Dijkstra?

1