

Recollecting Haskell, Part I

(Based on Chapters 1 and 2 of LYAH*)

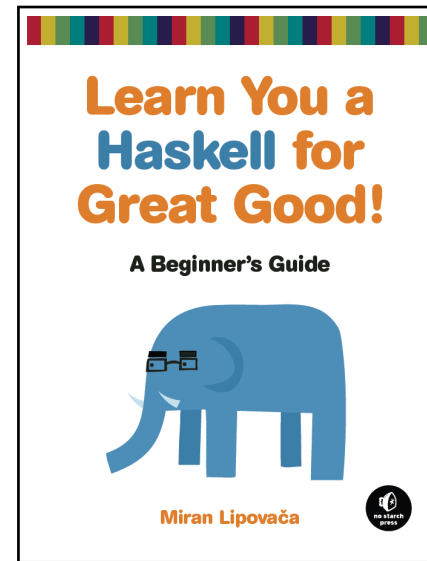
CIS 351/Spring 2016

Programming Languages

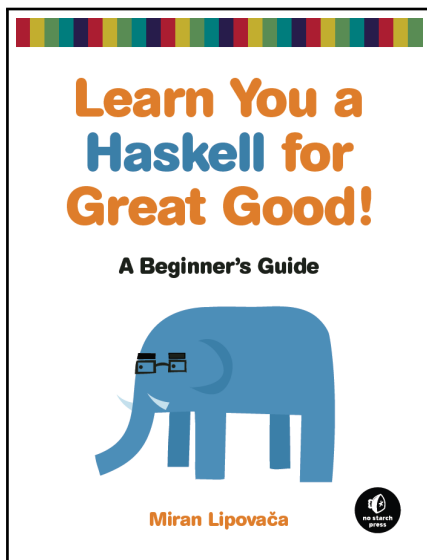
January 19, 2016

*LYAH = *Learn You a Haskell for Great Good*

Two (too?) big assumptions

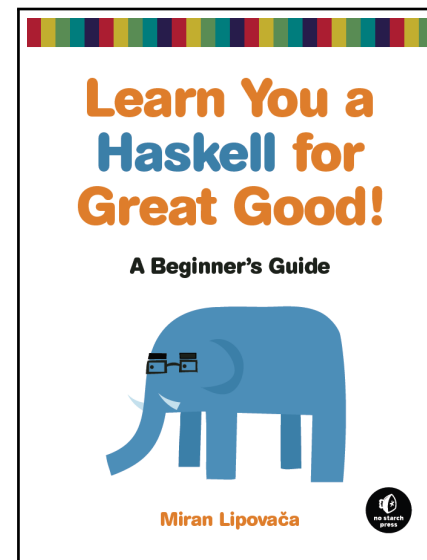


Two (too?) big assumptions



① You *can* read LYAH

Two (too?) big assumptions



① You *can* read LYAH

② You *will* read LYAH.

The Blurb from `wiki.haskell.org`

*Haskell is an advanced purely-functional programming language.
... it allows rapid development of robust, concise, correct software.*

With strong support for

- *integration with other languages,*
- *built-in concurrency and parallelism,*
- *debuggers,*
- *profilers,*
- *rich libraries and*
- *an active community,*

*Haskell makes it **easier** to produce flexible, maintainable, high-quality software.*

So *why* do we care about Haskell in this course?

- Haskell is great for prototyping.
- Forces you to think compositionally.
- Semi-automated testing: QuickCheck
- Haskell can give you executable specifications.
- Good for “model building”
e.g., direct implementations of operational semantics

So *why* do we care about Haskell in this course?

- Haskell is great for prototyping.
- Forces you to think compositionally.
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- Haskell can give you executable specifications.
- Good for “model building”
e.g., direct implementations of operational semantics

...and beyond this course

- Many of the new systems/applications languages
(e.g., Swift and Rust) steal lots of ideas from Haskell and ML.
- These ideas are a lot clearer in Haskell and ML
than the munged versions in Swift, Rust, etc.,

Set up

- Go visit <https://www.haskell.org/downloads#platform>.
- Download the appropriate version of the **current** Haskell Platform and install it.

!!! Do the above even if you have an old copy of the Haskell Platform from a previous year.
You want the latest version of the GHC compiler and libraries.

!!! Use a reasonable editor.
Using Notepad or Word is a waste of your time.
See <http://www.haskell.org/haskellwiki/Editors>.
Emacs is my weapon of choice.

A sample session: ghci as a calculator

```
[Post:~] jimroyer% ghci
GHCi, version 7.10.3: http://www.haskell.org/ghc/  :? for help
Prelude> 2+3
5
Prelude> 2*3
6
Prelude> 2-3
-1
Prelude> 2/3
0.6666666666666666
Prelude> :q
Leaving GHCi.
[Post:~] jimroyer%
```

Fussy bits

✗ $5 * -3$
✓ $5 * (-3)$
✗ $5 * 10 - 49 \neq 5 * (10 - 49)$
✓ $5 * 10 - 49 \equiv (5 * 10) - 49$
✗ $5 * \text{True}$

```
Prelude> 5 + True
```

```
<interactive>:2:3:
    No instance for (Num Bool) arising from a use of '+'
    In the expression: 5 + True
    In an equation for 'it': it = 5 + True
```

(What does all this mean?)

Using functions

```
Prelude> succ 4
5
Prelude> succ 4 * 10
50
Prelude> succ (4 * 10)
41
Prelude> max 5 3
5
Prelude> 1 + max 5 3
6
Prelude> max 5 3 + 1
6
Prelude> max 5 (3 + 1)
5
Prelude> 10 'max' 23
23
Prelude> (+) 3 5
8
```

Using functions

```
Prelude> succ 4
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```

baby.hs

```
doubleMe x = x + x
```

Using functions

```
Prelude> succ 4
5
Prelude> succ 4 * 10
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Prelude> 1 + max 5 3
6
Prelude> max 5 3 + 1
6
Prelude> max 5 (3 + 1)
5
Prelude> 10 'max' 23
23
Prelude> (+) 3 5
8
```

baby.hs

```
doubleMe x = x + x
```

```
Prelude> :load baby
```

```
[1 of 1] Compiling Main
         ( baby.hs, interpreted )
Ok, modules loaded: Main.
```

```
*Main> doubleMe 5
```

```
10
```

```
*Main> doubleMe 7.7
```

```
15.4
```

Defining and using functions, continued

baby.hs

```
doubleMe x          = x + x
```

```
doubleUs x y         = 2*x+2*y
```

```
doubleUs' x y        = doubleMe x + doubleMe y
```

```
doubleSmallNumber x  = if x > 100 then x else x * 2
```

```
doubleSmallNumber' x = (if x > 100 then x else x * 2)+1
```

```
conanO'Brien       = "It's a-me, Conan O'Brien!"
```

Lists

- A *list*: a sequence of things *of the same type*.

✓ [2,3,5,7,11,13,17,19]	:: [Int]
✓ [True,False,False,True]	:: [Bool]
✓ ['b','o','b','c','a','t'] ≡ "bobcat"	:: [Char]
✓ []	:: [a]
✓ [], [1], [2,3], [4,5,6]	:: [[Int]]
✗ [[1], [2], [3]]	<i>fuss</i>
✗ [2, True, "foo"]	<i>fuss</i>

- If you want to bundle together things of different types, use tuples (*e.g.*, (2,True,"foo") ...*explained later*).

Lists

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✓ [], [1], [2,3], [4,5,6]	:: [[Int]]
✗ [[1], [2], [3]]	<i>fuss</i>
✗ [2, True, "foo"]	<i>fuss</i>

- If you want to bundle together things of different types, use tuples (*e.g.*, (2,True,"foo") ...*explained later*).

Notation

$expression_1 \rightsquigarrow expression_2$ means $expression_1$ evaluates to $expression_2$

E.g.: $2+3 \rightsquigarrow 5$

Lists: Building them up

Write them down: $[item_1, item_2, \dots, item_n]$

- $[2,3,5,7,11,13,17,19], [], \text{etc.}$

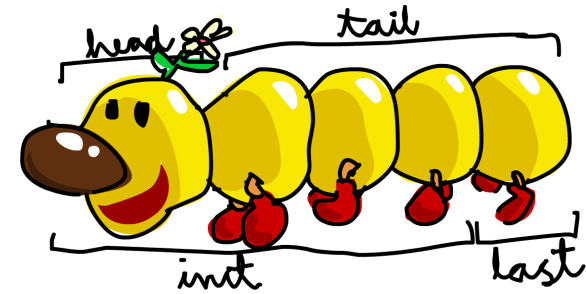
Concatenation: $list_1 ++ list_2$

- $[1,2,3,4] ++ [10,20,30] \rightsquigarrow [1,2,3,4,10,20,30]$
- $"salt" ++ "potato" \rightsquigarrow "saltpotato"$
- $[] ++ [1,2,3] \rightsquigarrow [1,2,3]$ $[1,2,3] ++ [] \rightsquigarrow [1,2,3]$
- $1 ++ [2,3] \rightsquigarrow \text{ERROR}$ $[1,2] ++ 3 \rightsquigarrow \text{ERROR}$

Cons: $item : list$

- $1 : [2,3] \rightsquigarrow [1,2,3]$ $[1,2] : 3 \rightsquigarrow \text{ERROR}$
- $[1,2,3]$ is *syntactic sugar* for $1 : 2 : 3 : [] \equiv 1 : (2 : (3 : []))$
- You can tell $(:)$ is important because they gave it such a short name.

Lists: Tearing them down



- $\text{head } [1,2,3] \rightsquigarrow 1$
- $\text{tail } [1,2,3] \rightsquigarrow [2,3]$
- $\text{head } [] \rightsquigarrow \text{ERROR}$
- $\text{tail } [] \rightsquigarrow \text{ERROR}$
- $\text{last } [1,2,3] \rightsquigarrow 3$
- $\text{init } [1,2,3] \rightsquigarrow [1,2]$
- $\text{last } [] \rightsquigarrow \text{ERROR}$
- $\text{init } [] \rightsquigarrow \text{ERROR}$

Lists: More operations

- $\text{length} :: [a] \rightarrow \text{Int}$
- $(!!) :: [a] \rightarrow \text{Int} \rightarrow a$
- $\text{null} :: [a] \rightarrow \text{Bool}$
- $\text{reverse} :: [a] \rightarrow [a]$
- $\text{drop}, \text{take} :: \text{Int} \rightarrow [a] \rightarrow [a]$
- $\text{sum}, \text{product} :: (\text{Num } a) \Rightarrow [a] \rightarrow a$
- $\text{minumum}, \text{maximum} :: (\text{Ord } a) \Rightarrow [a] \rightarrow a$
- $\text{elem}, \text{notElem} :: (\text{Eq } a) \Rightarrow a \rightarrow [a] \rightarrow \text{Bool}$

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- $\text{elem}, \text{notElem} :: (\text{Eq } a) \Rightarrow a \rightarrow [a] \rightarrow \text{Bool}$

You can look up what these do on:

- Hoogle: <https://www.haskell.org/hoogle/>
- Hayoo: <http://hayoo.fh-wedel.de>

Ranges

$[m..n] \rightsquigarrow [m, m+1, m+2, \dots, n]$

- $[1..5] \rightsquigarrow [1, 2, 3, 4, 5]$
- $[5..1] \rightsquigarrow []$
- $['a'..'k'] \rightsquigarrow "abcdefghijk"$
- $[1..] \rightsquigarrow [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, \dots]$

$[m, p..n] \rightsquigarrow [m, m+(p-m), m+2(m-p), \dots, n^*]$

- $[3, 5..10] \rightsquigarrow [3, 5, 7, 9]$
- $[5, 4..1] \rightsquigarrow [5, 4, 3, 2, 1]$
- $[9, 7..2] \rightsquigarrow [9, 7, 5, 3]$

*Or the “closest” number before n that is in the sequence.

List comprehensions

Set comprehensions in math (CIS 275 review)

- $\{x \mid x \in N, x = x^2\} = \{0, 1\}$
- $\{x \mid x \in N, x > 0\} = \text{the positive integers}$
- $\{x^2 \mid x \in N\} = \text{squares}$
- $\{(x, y) \mid x \in N, y \in N, x \leq y\}$

Suppose we have `lst = [5, 10, 13, 4, 10]`

- $[2*n+1 \mid n \leftarrow \text{lst}] \rightsquigarrow [11, 21, 27, 9, 21]$
- $[\text{even } n \mid n \leftarrow \text{lst}] \rightsquigarrow [\text{False}, \text{True}, \text{False}, \text{True}, \text{True}]$
- $[\underbrace{2*n+1}_{\text{transform}} \mid \underbrace{n \leftarrow \text{lst}}_{\text{generator}}, \underbrace{\text{even } n}_{\text{filter}}, \underbrace{n > 5}_{\text{filter}}] \rightsquigarrow [21, 21]$

Example: Squaring every element of a list

squares.hs

```
squares :: [Integer] -> [Integer]
squares xs = [ x*x | x <- xs ]
```

```
squares [1,2,3]
```

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```
squares :: [Integer] -> [Integer]
squares xs = [ x*x | x <- xs ]
```

```
squares [1,2,3]
= { xs = [1,2,3] }
  [ x*x | x <- [1,2,3] ]
```

Example: Squaring every element of a list

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```
squares :: [Integer] -> [Integer]
squares xs = [ x*x | x <- xs ]
```

```
squares [1,2,3]
= { xs = [1,2,3] }
  [ x*x | x <- [1,2,3] ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1*1 ] ++ [ 2*2 ] ++ [ 3*3 ]
```

Example: Squaring every element of a list

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squares xs = [ x*x | x <- xs ]
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```
squares [1,2,3]
= { xs = [1,2,3] }
  [ x*x | x <- [1,2,3] ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1*1 ] ++ [ 2*2 ] ++ [ 3*3 ]
=
  [1] ++ [4] ++ [9]
```

Example: Squaring every element of a list

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squares :: [Integer] -> [Integer]
squares xs = [ x*x | x <- xs ]
```

```
squares [1,2,3]
= { xs = [1,2,3] }
  [ x*x | x <- [1,2,3] ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1*1 ] ++ [ 2*2 ] ++ [ 3*3 ]
=
  [1] ++ [4] ++ [9]
=
  [1,4,9]
```

Example lifted from Phil Wadler.

Example: Odd elements of a list

odds.hs

```
odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]
```

```
odds [1,2,3]
```

Example: Odd elements of a list

odds.hs

```
odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]
```

```
odds [1,2,3]
= { xs = [1,2,3] }
  [ x | x <- [1,2,3], odd x ]
```

Example: Odd elements of a list

odds.hs

```
odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]
```

```
odds [1,2,3]
= { xs = [1,2,3] }
  [ x | x <- [1,2,3], odd x ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1 | odd 1 ] ++ [ 2 | odd 2 ] ++ [ 3 | odd 3 ]
```

Example: Odd elements of a list

odds.hs

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odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]
```

```
odds [1,2,3]
= { xs = [1,2,3] }
  [ x | x <- [1,2,3], odd x ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1 | odd 1 ] ++ [ 2 | odd 2 ] ++ [ 3 | odd 3 ]
=
  [ 1 | True ] ++ [ 2 | False ] ++ [ 3 | True ]
```

Example: Odd elements of a list

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```
odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]
```

```
odds [1,2,3]
= { xs = [1,2,3] }
  [ x | x <- [1,2,3], odd x ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1 | odd 1 ] ++ [ 2 | odd 2 ] ++ [ 3 | odd 3 ]
=
  [ 1 | True ] ++ [ 2 | False ] ++ [ 3 | True ]
=
  [1] ++ [] ++ [3]
```


Example: Odd elements of a list

odds.hs

```
odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]

odds [1,2,3]
= { xs = [1,2,3] }
  [ x | x <- [1,2,3], odd x ]
= { x=1 }, { x=2 }, { x=3 }
  [ 1 | odd 1 ] ++ [ 2 | odd 2 ] ++ [ 3 | odd 3 ]
= [ 1 | True ] ++ [ 2 | False ] ++ [ 3 | True ]
= [1] ++ [] ++ [3]
= [1,3]
```

Example lifted from Phil Wadler.

Example: Sum of the squares of the odd elements, 1

sumSqOdds.hs

```
squares :: [Integer] -> [Integer]
squares xs = [ x*x | x <- xs ]

odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]

f :: [Integer] -> Integer
f xs = sum (squares (odds xs))

f' :: [Integer] -> Integer
f' xs = sum [ x*x | x <- xs, odd x ]
```

Another example lifted from Phil Wadler.

Example: Sum of the squares of the odd elements, 2

```
f xs = sum (squares (odds xs))
```

```
f [1,2,3]
```

Example: Sum of the squares of the odd elements, 2

```
f xs = sum (squares (odds xs))
```

```
f [1,2,3]
= { xs = [1,2,3] }
  sum (squares (odds [1,2,3]))
```

Example: Sum of the squares of the odd elements, 2

```
f xs = sum (squares (odds xs))
```

```
f [1,2,3]
=   { xs = [1,2,3] }
  sum (squares (odds [1,2,3]))
=
  sum (squares [1,3])
```

Example: Sum of the squares of the odd elements, 2

```
f xs = sum (squares (odds xs))
```

```
f [1,2,3]
=   { xs = [1,2,3] }
  sum (squares (odds [1,2,3]))
=
  sum (squares [1,3])
=
  sum [1,9]
```

Example: Sum of the squares of the odd elements, 2

```
f xs = sum (squares (odds xs))
```

```
f [1,2,3]
=   { xs = [1,2,3] }
  sum (squares (odds [1,2,3]))
=
  sum (squares [1,3])
=
  sum [1,9]
=
  10
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]
```

```
f' [1,2,3]
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]
```

```
f' [1,2,3]
= { xs = [1,2,3] }
  sum [ x*x | x <- [1,2,3], odd x]
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]
```

```
f' [1,2,3]
= { xs = [1,2,3] }
  sum [ x*x | x <- [1,2,3], odd x]
= { x=1 }, { x=2 }, { x=3 }
  sum ([ 1*1 | odd 1 ] ++ [ 2*2 | odd 2 ] ++ [ 3*3 | odd 3 ])
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]
```

```
f' [1,2,3]
= { xs = [1,2,3] }
  sum [ x*x | x <- [1,2,3], odd x]
= { x=1 }, { x=2 }, { x=3 }
  sum ([ 1*1 | odd 1 ] ++ [ 2*2 | odd 2 ] ++ [ 3*3 | odd 3 ])
=
  sum ([ 1 | True ] ++ [ 4 | False ] ++ [ 9 | True])
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]
```

```
f' [1,2,3]
= { xs = [1,2,3] }
  sum [ x*x | x <- [1,2,3], odd x]
= { x=1 }, { x=2 }, { x=3 }
  sum ([ 1*1 | odd 1 ] ++ [ 2*2 | odd 2 ] ++ [ 3*3 | odd 3 ])
=
  sum ([ 1 | True ] ++ [ 4 | False ] ++ [ 9 | True])
=
  sum ([ 1 ] ++ [] ++ [ 9 ])
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]

f' [1,2,3]
= { xs = [1,2,3] }
  sum [ x*x | x <- [1,2,3], odd x]
= { x=1 }, { x=2 }, { x=3 }
  sum ([ 1*1 | odd 1 ] ++ [ 2*2 | odd 2 ] ++ [ 3*3 | odd 3 ])
= sum ([ 1 | True ] ++ [ 4 | False ] ++ [ 9 | True])
= sum ([ 1 ] ++ [] ++ [ 9 ])
= sum [1,9]
```

Example: Sum of the squares of the odd elements, 3

```
f' xs = sum [ x*x | x <- xs, odd x]

f' [1,2,3]
= { xs = [1,2,3] }
  sum [ x*x | x <- [1,2,3], odd x]
= { x=1 }, { x=2 }, { x=3 }
  sum ([ 1*1 | odd 1 ] ++ [ 2*2 | odd 2 ] ++ [ 3*3 | odd 3 ])
= sum ([ 1 | True ] ++ [ 4 | False ] ++ [ 9 | True])
= sum ([ 1 ] ++ [] ++ [ 9 ])
= sum [1,9]
= 10
```

Example: Sum of the squares of the odd elements, 4

sumSqOdds.hs

```
import Test.QuickCheck
```

```
squares :: [Integer] -> [Integer]
squares xs = [ x*x | x <- xs ]
```

```
odds :: [Integer] -> [Integer]
odds xs = [ x | x <- xs, odd x ]
```

```
f :: [Integer] -> Integer
f xs = sum (squares (odds xs))
```

```
f' :: [Integer] -> Integer
f' xs = sum [ x*x | x <- xs, odd x ]
```

```
f_prop :: [Integer] -> Bool
f_prop xs = f xs == f' xs
```

```
*Main> :load sumSqOdds
[1 of 1] Compiling Main
( sumSqOdds.hs, interpreted )
Ok, modules loaded: Main.
```

```
*Main> quickCheck f_prop
+++ OK, passed 100 tests.
*Main>
```

Tuples

Cartesian products in math (More CIS 275 Review)

Suppose A, B, C, \dots are sets.

$$A \times B = \{ (a,b) \mid a \in A, b \in B \}.$$
$$A \times B \times C = \{ (a,b,c) \mid a \in A, b \in B, c \in C \}.$$

etc.

Tuple types are Haskell's version of Cartesian products

- ✓ $(1,2) :: (\text{Int}, \text{Int})$
- ✓ $(\text{True}, 'a') :: (\text{Bool}, \text{Char})$
- ✓ $(3, 'q', "foo") :: (\text{Int}, \text{Char}, [\text{Char}])$
- ✗ $[(1,2), (3,4,5), (6,7)]$ (Why?)
- ✗ $[(1,2), ('d', \text{False})]$ (Why?)

Pairs

```
✓ fst :: (a,b) -> a
  fst ("muffin",99) ~> "muffin"
✓ snd :: (a,b) -> b
  snd ("muffin",99) ~> 99
✗ fst (4.1,True,'a') ~> ERROR
✗ snd (4.1,True,'a') ~> ERROR
✓ zip :: [a] -> [b] -> [(a,b)]
  zip [1..5] ['a','b','c','d','e']
    ~> [(1,'a'),(2,'b'),(3,'c'),(4,'d'),(5,'e')]
  zip [1..] "abcde"
    ~> [(1,'a'),(2,'b'),(3,'c'),(4,'d'),(5,'e')]
```

Finding Pythagorean Triples

Problem

Find all possible values of (a,b,c) such that a , b , and c are integers ≤ 10 that are the edge-lengths of a right triangle with perimeter 24.

Finding Pythagorean Triples

Problem

Find all possible values of (a,b,c) such that a , b , and c are integers ≤ 10 that are the edge-lengths of a right triangle with perimeter 24.

```
• triples1
  = [(a,b,c) | a <- [1..10], b <- [1..10], c <- [1..10]]
```

Finding Pythagorean Triples

Problem

Find all possible values of (a,b,c) such that a , b , and c are integers ≤ 10 that are the edge-lengths of a right triangle with perimeter 24.

```
• triples1
  = [(a,b,c) | a <- [1..10], b <- [1..10], c <- [1..10]]
• triples2
  = [(a,b,c) | a <- [1..10], b <- [a..10], c <- [b..10]]
```

Finding Pythagorean Triples

Problem

Find all possible values of (a, b, c) such that a, b , and c are integers ≤ 10 that are the edge-lengths of a right triangle with perimeter 24.

- `triples1`
= `[(a,b,c) | a <- [1..10], b <- [1..10], c <- [1..10]]`
- `triples2`
= `[(a,b,c) | a <- [1..10], b <- [a..10], c <- [b..10]]`
- `triples3`
= `[(a,b,c) | a <- [1..10], b <- [a..10], c <- [b..10],
a*a + b*b == c*c]`

Finding Pythagorean Triples

Problem

Find all possible values of (a, b, c) such that a, b , and c are integers ≤ 10 that are the edge-lengths of a right triangle with perimeter 24.

- `triples1`
= `[(a,b,c) | a <- [1..10], b <- [1..10], c <- [1..10]]`
- `triples2`
= `[(a,b,c) | a <- [1..10], b <- [a..10], c <- [b..10]]`
- `triples3`
= `[(a,b,c) | a <- [1..10], b <- [a..10], c <- [b..10],
a*a + b*b == c*c]`
- `triples4`
= `[(a,b,c) | a <- [1..10], b <- [a..10], c <- [b..10],
a*a + b*b == c*c, a+b+c == 24]`