

Recollecting Haskell, Part IV

User Defined Types

CIS 352/Spring 2016

Programming Languages

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Enumerated Types, 1

Recall type synonyms:

```
type Point = (Float,Float) -- A shorthand name for a type
```

You also have many means of creating new types. E.g.,

```
data Season = Winter | Spring | Summer | Fall
```

- This is called an enumerated type.
- We can use Season just like any other type. E.g.,

```
hasSnow :: Season -> Bool
hasSnow Summer = False
hasSnow _      = True
```

- However, there are problems with our definition. E.g.,
 - Haskell doesn't know how to print values of type Season
 - Haskell doesn't know how to compare values of type Season
 - Etc.

Enumerated Types, 2

```
data Season = Winter | Spring
            | Summer | Fall
```

!!! Haskell doesn't know how to
(print, compare, ...) Season-values.

Quick fix. Change the definition to:

```
data Season = Winter | Spring | Summer | Fall
    deriving (Eq,Ord,Show)
```

Now, the following work just fine:

```
Winter == Winter
succ Winter
Winter < Summer
```

What is the magic?

- `deriving (Eq,Ord,Show)` joins up the just defined type (Season) to type classes Eq,Ord,Show with default definitions.
- E.g., for Season the derived Ord-ordering is
Winter < Spring < Summer < Fall

Class Exercise: Rock-Paper-Scissors

```
data Move = Rock | Paper | Scissors
    deriving (Show,Eq)
```

```
data Result = Win1 | Win2 | Tie
    deriving (Show,Eq)
```

```
game :: Move -> Move -> Result
      ???
```

Product Types

Here is another form of DIY type:

```
data Location = Address Int String
               deriving (Show)

nextDoor :: Location -> Location
nextDoor (Address num street) = Address (num+1) street

showAddr :: Location -> String
showAddr (Address num street) = (show num) ++ " " ++ street
```

We could have defined:

```
type LocationToo = (Int,String)
```

Pros of Location

*Many things can be of type (Int,String),
but a Location is labeled as an address—so hard to confuse.*

Pros of LocationToo

All the tuple stuff (e.g., fst, zip, ...) works for LocationToo

Aside: Record Types, 1

A street address as a product type

```
data Location = Address Int String
               deriving (Eq,Show)
```

A street address as a record type

```
data Location' = Address' { number :: Int ,
                           street :: String }
                  deriving (Eq,Show)
```

What do we gain?

```
*Main> let wh = Address' 1600 "Penn. Ave."
*Main> wh
Address' number = 1600, street = "Penn. Ave."
*Main> :t number
number :: Location' -> Int
*Main> number wh
1600
*Main> street wh
"Penn. Ave."
```

Aside: Record Types, 2

A street address as a record type

```
data Location' = Address' { number :: Int, street :: String }
                  deriving (Eq,Show)
```

```
*Main> let baxter = Address' { street = "East 42nd Street",
                               number = 39}
```

```
*Main> baxter {number=100}
Address' {number = 100, street = "East 42nd Street"}
```

```
*Main> baxter
Address' {number = 39, street = "East 42nd Street"}
```

- So you have getters and “setters” if you need them. (Why the scare quotes?)
- Handy for data-types with lots of fields.
- **Do not use these to avoid pattern matching!!!!** (Why the fuss?)
- See Chapter 7 of LYAH for more details.

Making a Type an Instance of a Type Class, 1

Consider

```
-- Time h m represents a time Zeit of h hours & m mins
data Zeit = Time Integer Integer
```

Making Zeit an instance of Eq

```
instance Eq Zeit where
    Time h1 m1 == Time h2 m2 = (60*h1+m1==60*h2+m2)
```

Now:

- Time 0 20 == Time 0 20 ~> True
- Time 1 20 == Time 0 80 ~> True
- Time 1 21 /= Time 0 80 ~> True

Making Zeit an instance of Ord

```
instance Ord Zeit where
    Time h1 m1 <= Time h2 m2 = (60*h1+m1 <= 60*h2+m2)
```

Making a Type an Instance of a Type Class, 2

```
-- Time h m represents a time Zeit of h hours & m mins
data Zeit = Time Integer Integer
```

Making Zeit an instance of Num

```
instance Num Zeit where
    Time h1 m1 + Time h2 m2 = Time h m
        where (h,m) = quotRem (60*(h1+h2)+m1+m2) 60
    Time h1 m1 - Time h2 m2 = Time h m
        where (h,m) = quotRem (60*(h1-h2)+m1-m2) 60
    fromInteger n = Time h m
        where (h,m) = quotRem n 60
```

Making Zeit an instance of Show

```
instance Show Zeit where
    show (Time h m)
        = show h ++ " hours and " ++ show m ++ " minutes"
```

More later

Class Exercise: Complex Numbers, 1

Complex Numbers (see http://en.wikipedia.org/wiki/Complex_number)

```
data Cmplx = Cmplx Double Double -- Cmplx a b ≡ a+bi
```

```
re, im :: Cmplx -> Double
???
```

```
instance Show Cmplx where
    show (Cmplx x y) = show x ++ "+" ++ show y ++ "i"
```

```
instance Eq Cmplx where
???
```

```
instance Ord Cmplx where
???
```

Exercise: Complex Numbers, 2

Complex Arithmetic (see http://en.wikipedia.org/wiki/Complex_number)

$$\begin{aligned}(x_1 + y_1 i) + (x_2 + y_2 i) &= (x_1 + x_2) + (y_1 + y_2) i. \\ (x_1 + y_1 i) \cdot (x_2 + y_2 i) &= (x_1 \cdot x_2 - y_1 \cdot y_2) + (x_1 \cdot y_2 + x_2 \cdot y_1) i. \\ &\vdots\end{aligned}$$

```
data Cmplx = Cmplx Double Double Cmplx a b ≡ a+bi
```

```
instance Num Cmplx where
???
```

For the standard Haskell complex-numbers package, see: <http://hackage.haskell.org/package/base-4.7.0.2/docs/Data-Complex.html>

Sum Types

```
type Point = (Float,Float) -- not the same as LYAH's
data Shape = Circle Point Float | Rectangle Point Point
            deriving (Show)
-- Circle p r = a circle with center p and radius r
-- Rectangle p1 p2 = a rectangle with opposite corner pts p1 and p2
```

```
area, circum :: Shape -> Float
area (Circle _ r) = pi * r^2
area (Rectangle (x1,y1) (x2,y2)) = abs(x1-x2)*abs(y1-y2)
```

```
circum (Circle _ r) = 2 * pi * r
circum (Rectangle (x1,y1) (x2,y2)) = 2 * (abs(x1-x2) + abs(y1-y2))
```

```
-- nudge s (x,y) = shape s moved by the vector (x,y)
nudge :: Shape -> Point -> Shape
nudge (Circle (x,y) r) (x',y')
    = Circle (x+x',y+y') r
nudge (Rectangle (x1,y1) (x2,y2)) (x',y')
    = Rectangle (x1+x',y1+y') (x2+x',y2+y')
```

General Form of Algebraic Types

```
data Typename = ConstrA t1A ... tkA
               | ConstrB t1B ... tℓB
```

where

- Typename can take parameters
(more on this later)
- Constr^A, Constr^B, ... are constructor names
- t_i^A, t_j^B, ... are types, and
- the definitions can be recursive.

ALGEBRAIC!



Example: A DIY list type

```
data IntList = Empty | Cons Int IntList
              deriving (Show, Eq, Ord)
```

Example: A DIY list type

```
data IntList = Empty | Cons Int IntList
              deriving (Show, Eq, Ord)
```

-- Convert from IntLists to conventional list of Ints

```
convert :: IntList -> [Int]
convert Empty      = []
convert (Cons x xs) = x:(convert xs)
```

-- Convert from conventional list of Ints to IntLists

```
revert :: [Int] -> IntList
revert []      = Empty
revert (x:xs) = Cons x (revert xs)
```

What about a general DIY list data type?

Parameterized Data Type Definitions

– You can parameterize an algebraic type by type params.

A DIY general list data type

```
data MyList a = Empty' | Cons' a (MyList a)
              deriving (Eq, Show)
```

```
convert' :: MyList a -> [a]
convert' Empty'      = []
convert' (Cons' x xs) = x:(convert' xs)
```

```
revert' :: [a] -> MyList a
revert' []      = Empty'
revert' (x:xs) = Cons' x (revert' xs)
```

Making Zeit an Abstract Data Type, 1

Zeit.hs

```
module Zeit (Zeit(..),stretch) where
```

```
data Zeit = Time Integer Integer
```

-- Convert Zeits to minutes (not exported)

```
toMins :: Zeit -> Integer
toMins (Time h m) = 60*h+m
```

-- Stretch t f = the Zeit t stretched by amount f

-- E.g.: stretch (Time 1 0) 1.5 = Time 1 30

```
stretch :: Zeit -> Float -> Zeit
stretch t s = fromInteger(round(s * fromIntegral(toMins t)))
```

```
instance Eq Zeit where
```

```
    t1 == t2 = toMins t1 == toMins t2
```

```
instance Ord Zeit where
```

```
    t1 < t2 = toMins t1 < toMins t2
```

Making Zeit an *Abstract Data Type*, 2

-- Zeit.hs *continued*

```
instance Num Zeit where
  t1 + t2      = fromInteger (toMins t1 + toMins t2)
  t1 - t2      = fromInteger (toMins t1 - toMins t2)
  abs t        = fromInteger(abs(toMins t))
  t1 * t2      = error "(*) not defined for Zeit"
  signum t     = error "signum not defined for Zeit"
  fromInteger n = Time h m
    where (h,m) = divMod n 60

instance Show Zeit where
  show (Time h m) = show h ++ " hours and "
    ++ show m ++ " minutes"
```

Digression on Importing Modules, 1

- importing all of a module

```
import Data.List
```

- importing select items from a module

```
import Data.List (nub,union)
```

- importing *all but* select items from a module

```
import Data.List hiding (nub,sort)
```

Digression on Importing Modules, 2

- a qualified import *(to avoid name clashes)*

```
import qualified Data.Map.Strict    includes a function named null
...
  if null lst then ...             the standard null
...
  if Data.Map.Strict.null table then ...    Map's null
```

- a qualified import with a shorthand prefix

```
import qualified Data.Map.Strict as M
...
  if null lst then ...             the standard null
...
  if M.null table then ...          Map's null
```

See LYAH Chapter 6 for more details and some nice examples.
...now back to user defined types

Back to Algebraic Data Types

The Maybe Type \approx (a way of adding a “bottom” value to a type)

```
data Maybe a = Nothing | Just a
```

```
lookup :: Eq a => a -> [(a, b)] -> Maybe b
```

```
lookup "Penny" [("Dixie",4),("Maxie",15),("Penny",8)]
  ~ Just 6
```

```
lookup "Maxie" [("Dixie",4),("Maxie",15),("Penny",8)]
  ~ Just 15
```

```
lookup "Gaspode" [("Dixie",4),("Maxie",15),("Penny",8)]
  ~ Nothing
```

The Rust guys really like maybe types, see:
<http://doc.rust-lang.org/book/generics.html> and
<http://doc.rust-lang.org/book/error-handling.html#handling-errors-with-option-and-result>

Adding Maybe to Some Type Classes

The Maybe Type

```
data Maybe a = Nothing | Just a
```

```
instance (Eq m) => Eq (Maybe m) where
  Just x == Just y   = x == y
  Nothing == Nothing = True
  _ == _             = False
```

```
*Main> :i Maybe
data Maybe a = Nothing | Just a -- Defined in Data.Maybe
instance Eq a => Eq (Maybe a) -- Defined in Data.Maybe
instance Monad Maybe -- Defined in Data.Maybe
instance Functor Maybe -- Defined in Data.Maybe
instance Ord a => Ord (Maybe a) -- Defined in Data.Maybe
instance Read a => Read (Maybe a) -- Defined in GHC.Read
instance Show a => Show (Maybe a) -- Defined in GHC.Show
instance Arbitrary a => Arbitrary (Maybe a)
-- Defined in Test.QuickCheck.Arbitrary
```

Back to Recursive Types

See LYAH's working out of the List and Tree types.

A Type for Propositional Logic

```
type Name = String
data Prop = Var Name
          | F
          | T
          | Not Prop
          | Prop :|: Prop
          | Prop :&: Prop
          deriving (Eq, Ord)
```

```
type Names = [Name]
type Env = [(Name, Bool)]
```

at this point we switch to emacs

References

- Wikipedia's article on algebraic data types:
http://en.wikipedia.org/wiki/Algebraic_data_type
- LYAH: Making Our Own Types and Typeclasses:
<http://learnyouahaskell.com/making-our-own-types-and-typeclasses>
- Jeremy Gibbons: Calculating Functional Programs:
<http://www.cs.ox.ac.uk/people/jeremy.gibbons/publications/acmmmpc-calcfp.pdf>¹
(Explains some of the theory behind algebraic data types.)

¹From Roland Backhouse, Roy Crole, and Jeremy Gibbons, editors. *Algebraic and Coalgebraic Methods in the Mathematics of Program Construction*, volume 2297 of Lecture Notes in Computer Science. Springer-Verlag, 2002.