Superstar Teams:

The Micro Origins and Macro Implications of Coworker Complementarities

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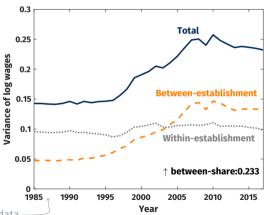
IIES

Wage inequality has risen – and firms appear to play a key role



"the variance of firm [wages] explains an increasing share of total inequality in a range of countries"

[Song-Price-Guvenen-Bloom-von Wachter, 2019]

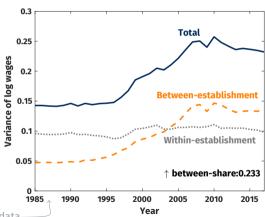


German matched employer-employee data—

Wage inequality has risen – and firms appear to play a key role



Applied question: what is/are the causal driver(s)? implications?



German matched employer-employee data—

Paper offers a structural explanation by modeling firms as team assemblies

• Motivation: wage inequality is increasingly a between-firm phenomenon



• Firm: an organized collection of workers performing tasks for production (team)

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• Motivation: wage inequality is increasingly a between-firm phenomenon



- Firm: an organized collection of workers performing tasks for production (team)
- **Hypothesis** for \(\gamma\) wage inequality between firms:
 - \bullet the set of tasks that each worker can perform very well has narrowed (specialization \uparrow)
 - ② firms become more vulnerable to "weak links" in teams (complementarities ↑)
 - 3 individuals of similar talent increasingly work together (positive assortative matching ↑)
 - 4 this generates greater between-firm wage dispersion

Roadmap: main steps

1 Develop task-based theory of firm production with teams

2 Embed into equilibrium search model & take to panel data

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Roadmap: main steps, contributions

- Develop task-based theory of firm production with teams
 - ⇒ analytical microfoundation for coworker complementarity

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- 3 Analyze trends using structural model + DE data

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- 1 Develop task-based theory of firm production with teams
 - ⇒ analytical microfoundation for coworker complementarity
 - ⇒ ↑ specialization endogenously generates ↑ coworker talent complementarity
- 2 Embed into equilibrium search model & take to panel data
 - \Rightarrow \uparrow coworker complementarity leads to \uparrow positive assortative coworker sorting
 - ⇒ identification result: measure coworker complementarity
- 3 Analyze trends using structural model + DE data
 - ⇒ quantitative & structural account of the "firming up" of inequality
 - ⇒ coworker complementarity doubled since 1985 & talent sorting has intensified
 - \Rightarrow this explains \approx 40% of \uparrow between-firm wage inequality share
 - ⇒ increased talent sorting helped keep TFP close to potential

Key takeaways

- **1** ↑ Skill specialization endogenously generates ↑ coworker talent complementarity
- ↑ Coworker complementarity leads to ↑ positive assortative coworker sorting
- **3** Coworker complementarity has doubled since 1985 & talent sorting has intensified
- **1** This explains \approx 40% of \uparrow between-firm wage inequality share
- 6 Increased talent sorting helped keep TFP close to potential

Relation & contributions to 3 strands of literature

- Wage inequality: structural model of ↑ firm-level inequality due to technological △
 Technology: Katz & Murphy, 1992; Krusell et al., 2000; Autor, Levy & Murnane, 2003; Jones, 2009; Deming, 2017; Acemoglu & Restrepo, 2018; Alon, 2018; Neffke, 2019; Jones, 2021; Atalay et al., 2021

 Firms: Card et al., 2013; Barth et al., 2016; Alvarez et al., 2018; Bloom et al., 2019; Aeppli & Wilmers, 2021; Criscuolo et al. 2021; Hakanson et al., 2021; Sorkin & Wallskog, 2021; Kleinman, 2022; Cortes et al., 2023
- Firm organization: tractable model of team production → frictions & quantification
 Firms: Lucas, 1978; Rosen, 1982; Becker & Murphy, 1992; Kremer, 1993; Kremer & Maskin, 1996; Garicano,
 2000; Garicano & Rossi-Hansberg, 2006; Kohlhepp, 2022; Kuhn et al., 2022; Minni, 2023; Bassi et al., 2023
 Task assignment: Costinot & Vogel, 2010; Acemoglu & Restrepo, 2018; Ocampo, 2021; Adenbaum, 2022
 Teams: Akcigit et al., 2018; Jarosch et al., 2021; Herkenhoff et al., 2022; Pearce, 2022
- Frictional labor market sorting: endogenize & measure complementarities

 Shimer & Smith, 2000; Cahuc et al., 2006; Eeckhout & Kircher, 2011/2018; Hagedorn et al., 2017; de Melo, 2018; Chade & Eeckhout, 2020; Herkenhoff et al., 2022; Lindenlaub & Postel-Vinay, 2023

Theory

Overview of environment



- · Many workers and many firms
- Ex-ante homogeneous firms assemble hire workers & assign tasks teams
- · Workers are heterogeneous in productivity
 - ightarrow workforce composition is source of ex-post differences across firms
- Analyze in 2 steps:
 - organization of production: allocate workers' time across tasks
 - 2 team formation: hire multiple workers

Step 1: production in a single team of given composition

• Firm: 1 team of $n \in \mathbb{Z}_{++}$ workers produces output from unit continuum of tasks \mathcal{T}

$$\ln Y = \int_{\mathcal{T}} \ln q(\tau) d\tau \tag{1}$$

Task aggregation:

$$q(\tau) = \sum_{i=1}^{n} y_i(\tau) \tag{2}$$

• Workers o tasks: each supplies 1 time unit, task-specific productivities $\{\mathbf{z_i}(au)\}_{ au\in\mathcal{T}}$

$$y_i(\tau) = z_i(\tau)l_i(\tau) \tag{3}$$

$$1 = \int_{\mathcal{T}} l_i(\tau) d\tau \tag{4}$$

Firm's optimization problem

• Firm solves mini-planner problem: max Y s.t. (1)-(4)

$$\mathcal{L}(\cdot) = \mathbf{Y} + \lambda \left[\underbrace{\left(\int_{\mathcal{T}} \ln q(\tau) d\tau \right) - \ln \mathbf{Y}}_{\text{tasks} \to \text{output}} \right] + \int_{\mathcal{T}} \lambda(\tau) \left(\underbrace{\sum_{i=1}^{n} y_{i}(\tau) - q(\tau)}_{\text{task aggregation}} \right) d\tau$$

$$+ \sum_{i=1}^{n} \lambda_{i}^{L} \underbrace{\left(\int_{\mathcal{T}} \frac{y_{i}(\tau)}{\mathbf{z}_{i}(\tau)} d\tau - 1 \right)}_{\text{time constraint} + \text{task production}} + \text{non-negativity constraints}$$

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• FOCs imply

simply
$$\lambda(\tau) = \min_{i} \left\{ \frac{\lambda_{i}^{L}}{z_{i}(\tau)} \right\}$$
 opportunity cost of i 's time shadow cost of τ opportunity of i for τ

Tractability: leverage insight from trade literature



Assumption: Distribution of worker-task efficiencies

$$\{z_i(\tau)\}_{\tau\in\mathcal{T}}\stackrel{\mathrm{iid}}{\sim} \mathsf{Fr\'echet}: \qquad \mathsf{Pr}\{z_i(\tau)\leq z\} = \exp\left(-\left(\frac{z}{\iota x_i}\right)^{-1/\chi}\right)$$

- · Low-dimensional representation of worker-task productivity distribution
 - ∘ "talent" type $x_i \in [0, 1]$
 - o parameter χ : specialization \sim productivity dispersion across tasks

Illustration of worker-task productivity distribution: talent types

• "Talent" type $x_i \in [0, 1]$

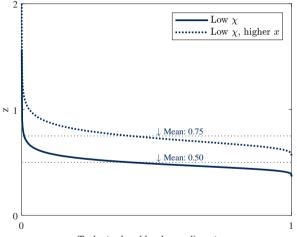
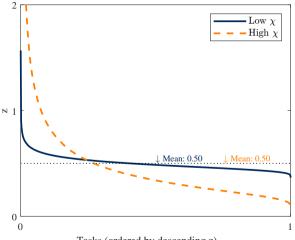
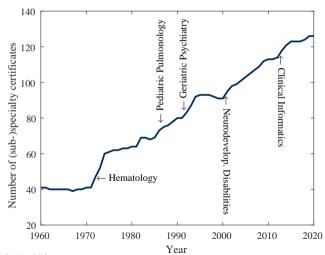


Illustration of worker-task productivity distribution: specialization parameter

• Parameter χ : specialization



Example of χ \uparrow : progressive specialization among medical professionals



Tractability: leverage insight from trade literature

- $\{z_i(au)\}_{ au\in\mathcal{T}}\stackrel{\mathrm{iid}}{\sim}\mathsf{Fr\'echet}$
- Max-stability property allows closed-form characterization of key objects
 - \circ e.g., $\lambda(au)\sim \mathsf{Weibull}$

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- $\{z_i(\tau)\}_{\tau \in \mathcal{T}} \stackrel{\mathrm{iid}}{\sim} \mathsf{Fr\'echet}$
- Max-stability property allows closed-form characterization of key objects

$$\circ$$
 e.g., $\lambda(au) \sim \mathsf{Weibull}$

• **Preview**: integrate over tasks under the optimal assignment to derive an 'aggregate' team production function f as the solution to the mini-planner problem:

$$f(...) = \max Y$$

s.t. (1)-(4)

...but first some intuition

Solution of firm's mini-planner problem implies:

- Complete division of labor
- Tasks assigned by comparative advantage

$$\circ \ \textit{i's} \ \mathsf{task} \ \mathsf{set} \ \mathcal{T}_{\textit{i}} = \left\{ \tau \in \mathcal{T} : \tfrac{\mathsf{z}_{\textit{i}}(\tau)}{\lambda_{\textit{i}}^{\textit{L}}} \geq \mathsf{max}_{k \neq \textit{i}} \, \tfrac{\mathsf{z}_{\textit{k}}(\tau)}{\lambda_{\textit{k}}^{\textit{L}}} \right\}$$

3 i's share of tasks \uparrow in i's talent, \downarrow in coworkers' talent

$$\circ$$
 i's task share $\pi_i = (x_i^{\frac{1}{1+\chi}})(\sum_{k=1}^n (x_k)^{\frac{1}{1+\chi}})^{-1}$

Intuition for optimal organization: comparative statics for task shares

- Suppose that $x_i > x_j$. Then
 - **1** i performs a strictly larger share of tasks than j for $\chi < \infty$



Intuition for optimal organization: comparative statics for task shares

- Suppose that $x_i > x_j$. Then
 - **1** *i* performs a strictly larger share of tasks than *j* for $\chi < \infty$
 - $oldsymbol{2}$ the difference in task shares is decreasing in χ



⇒ Deeper specialization raises the share of tasks performed by low-x team member(s)

Micro-founded production function

• 'Aggregate' team production function is the solution to the mini-planner problem:

$$f(...) = \max Y$$

s.t. (1)-(4)

Micro-founded production function

• 'Aggregate' team production function is the solution to the mini-planner problem:

$$f(x_1, ..., x_n; \chi) = \max Y$$

s.t. (1)-(4)

Proposition: Aggregation result

The vector of talent types $(x_1,...,x_n)$ is a sufficient statistic for team output Y...

Proposition: Aggregation result

The vector of talent types $(x_1,...,x_n)$ is a sufficient statistic for team output Y, s.t.

$$f(x_1,\cdots,x_n)=n^{1+\chi}\times\left(\frac{1}{n}\sum_{i=1}^n(x_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}$$

Proof sketch

Proposition: Aggregation result

$$f(x_1, \cdots, x_n) = \underbrace{n^{1+\chi}}_{\text{efficiency gains}} \times \underbrace{\left(\frac{1}{n} \sum_{i=1}^{n} (x_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}}_{i=1}$$

 \rightarrow vs. no-division-of-labor: $f(x_1,...,x_n)=n\times (\frac{1}{n}\sum_i^n x_i)$

1 Efficiency gains from teamwork $\nearrow \chi$

Micro-founded production function: characterization

Proposition: Aggregation result

$$f(x_1, \dots, x_n) = \underbrace{n^{1+\chi}}_{\text{efficiency gains}} \times \underbrace{\left(\frac{1}{n} \sum_{i=1}^{n} (x_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}}_{\text{complementarity}},$$

- **2** Coworker complementarity $\nearrow \chi$: output more 'vulnerable' to lowest-x member(s)
 - elasticity of complementarity $\gamma := \frac{\partial \ln(f_j/f_i)}{\partial \ln(x_i/x_i)} = \frac{\chi}{1+\chi}$

Key takeaways

1 ↑ Skill specialization endogenously generates ↑ coworker talent complementarity

Step 2: firm organization meets frictional matching



- Step 1 yields *tractable* team production function $f(\cdot)$
- Step 2: embed $f(\cdot)$ into frictional equilibrium matching model
 - o random-search + multi-worker firms [Herkenhoff-Lise-Menzio-Phillips 2022]
 - o infinitely lived, risk-neutral agents; no entry/exit
 - o no learning, i.e. types are invariant
 - o $n_{\text{max}} = 2$: decreasing returns in production w/ representative coworker
 - \circ employment states: unemp., employed alone, employed with $x' \in [0,1]$
 - Nash bargaining w/ continuous renegotiation
 - o baseline: only unemployed search for jobs OJS considered in extension
 - stationary equilibrium

HJ-Bellman equations → values & matching policies

► HJBs

• Flows between/**distribution** over types × employment states

► KFEs

Definition: Stationary equilibrium

A stationary equilibrium consists of a tuple of value functions and a distribution of agents, such that

- 1 the value functions satisfy the HJB equations given the distribution;
- 2 the distribution is stationary given the policy fn's implied by the value fn's.

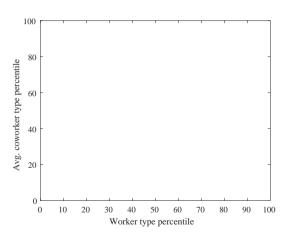
Step 2: matching - quantitative model

- Embed $f(\cdot)$ into frictional equilibrium matching model
- 2 main results
 - $\mathbf{1}$ mechanism: complementarities \rightarrow sorting
 - 2 identification: measuring complementarities

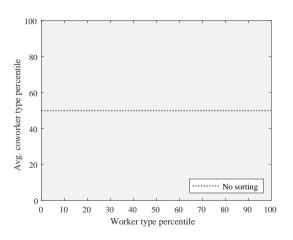
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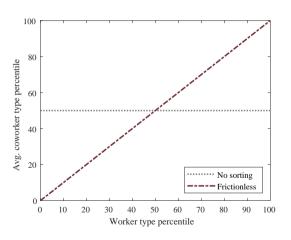
In equilibrium, who tends to work with whom?



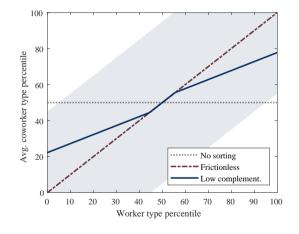
No complementarities: everyone matches with everyone



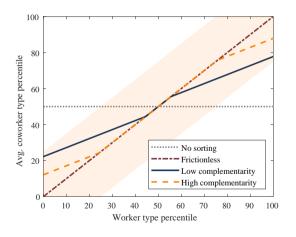
 Complementarities + frictionless: pure positive assortative matching



- Search frictions: trade-off team match quality vs. cost of searching
 - \Rightarrow range of acceptable matches



- $\chi \uparrow \Rightarrow$ smaller acceptable range
 - **1** coworker sorting ↑
 - between-firm share of var(wages) ↑



Key takeaways

- ② ↑ Coworker complementarity leads to ↑ positive assortative coworker sorting

Step 2: matching - quantitative model

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- Strategy: recover χ directly, rather than inferring from sorting

 \Rightarrow How to quantify $\frac{\partial^2 f(x,x')}{\partial x \partial x'}$?

- **Q:** How to quantify $\frac{\partial^2 f(x,x')}{\partial x \partial x'}$?
- **Theory:** wage level for worker x with coworker x'

► Wage eq. with y-het.

$$w(x|x') = \omega(f(x,x') - f(x')) + \underbrace{(1 - \omega)\rho V_u(x)}_{\text{function of } x' \text{ only}}$$
$$- \underbrace{\omega(1 - \omega)\lambda_{v.u} \int \frac{d_u(\tilde{x}'')}{u} \max\{S(\tilde{x}''|x'), O\}d\tilde{x}''}_{\text{function of } x' \text{ only}}$$

 \circ ω : worker bargaining power; $V_u(x)$: value of unemployment for x; $\lambda_{v.u}$: rate of meeting unemployed; $d_u(x)$: density of type-x unemp.; u: unemp. rate; $S(\tilde{x}''|x')$: surplus from hiring \tilde{x}'' to work with x'

- **Q:** How to quantify $\frac{\partial^2 f(x,x')}{\partial x \partial x'}$?
- **Theory:** wage level for worker x with coworker x'

$$w(x|x') = \omega f(x,x') + g(x) - h(x')$$

where $g:[0,1] \to \mathbb{R}$ and $h:[0,1] \to \mathbb{R}$ are strictly increasing

- **Q:** How to quantify $\frac{\partial^2 f(x,x')}{\partial x \partial x'}$?
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$$w(x|x') = \omega \times f(x,x') + g(x) - h(x')$$

Proposition: Identification result

Coworker complementarities (CC) in production are proportional to CC in wages:

$$\frac{\partial^2 f(x,x')}{\partial x \partial x'} \propto \boxed{\frac{\partial^2 w(x|x')}{\partial x \partial x'}}$$
 can measure this

Model Meets Data

Bringing the model to data

- Matched employer-employee panel data
- Mapping model objects to data
- Model calibration
- Validation (brief today, more in paper)

Primary data: SIEED matched-employer employee panel for W Germany



- 1.5% sample of establishments + entire biographies of associated workers; social security information on employer, daily wage, occupation, demographics
- o initially focus on 2010-2017, later extend to 1985-2017
- \circ selection: full-time employees aged 20-60 and meeting min. earnings requirements, \geq 10 observations per establishment-year
- Supplement with:
 - Portuguese matched employer-employee panel + balance sheet data
 - o German repeated cross-sections of individual-level survey data on tasks

Mapping theory to data: worker & coworker types



- Worker types from 2-way fixed effect (FE) wage regressions [Abowd et al., 1999 AKM]
 - intuition: job switching identifies time-invariant "worker types," controlling for possibility that some employers pay more to all workers
 - \circ pre-est. k-means clustering \rightarrow address limited mobility bias [Bonhomme et al., 2019]
 - o robustness: non-param. ranking algo instead of AKM [Hagedorn et al., 2017]
 - \Rightarrow Worker "type" \hat{x}_i : decile rank of worker FE

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- "Representative coworker type" \hat{x}_{-it} : average \hat{x}_i of coworkers in same establishment-year



Mapping theory to data: coworker complementarity

· Recall structural wage equation:

$$w(\mathbf{x}|\mathbf{x}') = \omega f(\mathbf{x}, \mathbf{x}') + g(\mathbf{x}) - h(\mathbf{x}')$$

$$\Rightarrow \frac{\partial^2 w(\mathbf{x}|\mathbf{x}')}{\partial \mathbf{x} \partial \mathbf{x}'} \propto \frac{\partial^2 f(\mathbf{x}, \mathbf{x}')}{\partial \mathbf{x} \partial \mathbf{x}'}$$

• Estimating equation:

$$\begin{aligned} \frac{w_{it}}{\bar{w}_t} &= \beta_0 + \beta_1 \hat{\mathbf{x}}_i + \beta_2 \hat{\mathbf{x}}_{-it} + \beta_c \left(\hat{\mathbf{x}}_i \times \hat{\mathbf{x}}_{-it} \right) \\ &+ \psi_{j(it)} + \nu_{o(i)t} + \xi_{s(i)t} + \epsilon_{it} \end{aligned}$$

 \circ alternative: non-parametrically approximate $\frac{\partial^2 w(x|x')}{\partial x \partial x'}$

Evidence on coworker complementarity (2010-2017)

ightharpoonup Robustness ightharpoonup B-o-E calc. γ ightharpoonup Peer effects

• Estimating equation:

coworker complementarity

$$\frac{\mathbf{w}_{it}}{\bar{\mathbf{w}}_{t}} = \beta_{0} + \beta_{1}\hat{\mathbf{x}}_{i} + \beta_{2}\hat{\mathbf{x}}_{-it} + \beta_{c}\left(\hat{\mathbf{x}}_{i} \times \hat{\mathbf{x}}_{-it}\right) \\
+ \psi_{j(it)} + \nu_{o(i)t} + \xi_{s(i)t} + \epsilon_{it}$$

	\hat{eta}_{c}	Non-parametric FD method
Coworker complementarity	0.0091 *** (0.00035)	0.0097
Obs. (1000s)	4,410	4,410

Notes. Regressions include FEs for employer; occupation-year; industry-year. Employer-clustered standard errors in parentheses. Observations weighted by the inverse employment share of the respective type and (rounded) coworker type cell. FD: finite differences.

Robustness checks: measuring coworker complementarity



• Types from non-parametric ranking algorithm instead of AKM-based

▶ Jump

Schooling as a non-wage measure of types

▶ Jump

Lagged types

▶ Jump

· Small teams

▶ Jump

Movers

► Jump

· Non-parametric, finite-differences approximation

► Jump

Excluding managers

▶ Jump

Log specification

Model parameterization: approach



- Calibrate the model to the W German economy (2010-2017)
 - externally calibrated: discount rate, team-benefit, bargaining power
 - offline estimation: job separation hazard
 - **3 online estimation** (indirect inference): meeting rate, unemp. flow benefit, production
 - \circ targets: \hat{eta}_c , total wage variance, avg. wage level, replacement rate, job finding rate
- Production complementarity informed by \hat{eta}_c
- Macro moments of interest are untargeted: sorting, between-firm wage inequality

Calibration results & model validation

• Recovered elasticity of complementarity γ equal to 0.84

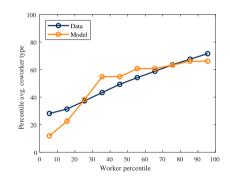
► Parameter values

- Match coworker sorting patterns
 - $\rho_{xx} = 0.53$ (vs. 0.62 in data)
- Match between-firm wage inequality
 - between-share 0.56 (vs. 0.57 in data)
 - o adjust for small-*n* bias

▶ Details

Extensive validation exercises

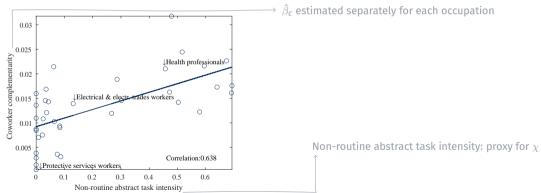
▶ Details



Cross-sectional validation: tasks \Rightarrow complementarity (occ's)



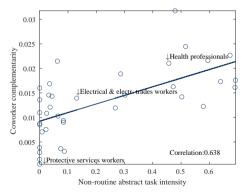
- ullet \uparrow Non-routine abstract task intensity
 - $\Rightarrow \uparrow$ coworker complementarity



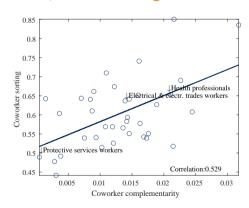
Notes. Quadros de Pessoal microdata. Analysis at ISCO-08-2d level.

Cross-sectional validation: tasks \Rightarrow complementarity \Rightarrow sorting (occ's)

↑ Non-routine abstract task intensity
 ⇒ ↑ coworker complementarity



↑ Coworker complementarity
 ⇒ ↑ coworker sorting



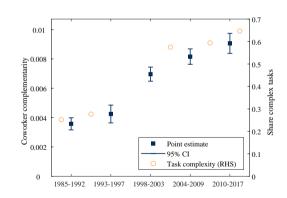


Coworker complementarity has strengthened over time...



• **Theory:** specialization $(\chi) \uparrow$ is associated with coworker complementarity \uparrow

✓Coworker complementarity has more than doubled between 1985-1992 and 2010-2017



...consistent with descriptive evidence of specialization (χ) \uparrow

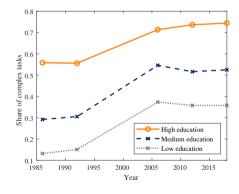
► Occ. movements ► Science

Task complexity ↑:
 "extensive margin" of x

o DE longitudinal task survey

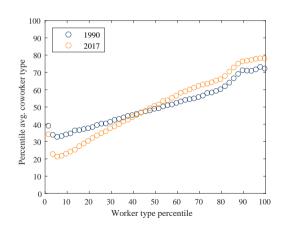


 "complex": cognitive non-routine (e.g., organizing, researching)



• **Theory:** complementarity ↑ is associated with talent sorting ↑

✓ Coworker matching has become more positively assortative

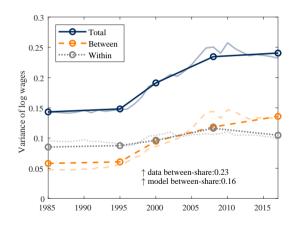


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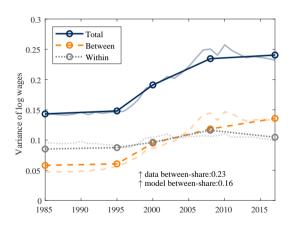
Model matches changes in firm-level wage distribution

- Re-calibrate model: 4 earlier sample periods
- Model replicates untargeted rise of between-share in data
 - 68% of ↑ between-share in data,
 ('85-'92)→('10-'17)



Model matches changes in firm-level wage distribution - why?

- Model replicates untargeted rise of between-share in data
- Reflects several parameters changing
 - elasticity of compl.: 0.43 in '85-'92 (vs. 0.84 in '10-'17)
 - job arrival & separation ↑
 - 0 ...



Complementarity \uparrow explains pprox 40% of observed between-share \uparrow

• **Q:** How much of \uparrow between-firm share of wage var. is due to \uparrow complementarities?

Complementarity \uparrow explains pprox 40% of observed between-share \uparrow

- **Q:** How much of \uparrow between-firm share of wage var. is due to \uparrow complementarities?
- **Counterfactual:** between-firm share in 2010s absent $\chi \uparrow$ since '85-'92

Complementarity \uparrow explains \approx 40% of observed between-share \uparrow

- **Q:** How much of \uparrow between-firm share of wage var. is due to \uparrow complementarities?
- **Counterfactual:** between-firm share in 2010s absent $\chi \uparrow$ since '85-'92
- A: $\chi \uparrow$ accounts for 59% of model-predicted $\Delta \leftrightarrow \approx$ 40% of empirical Δ

	△ model	Implied % Δ model due to Δ parameter	
Model baseline	0.16	-	
Cf.: fix period-1 complementarity	0.065	59	

Overview of model robustness checks

- · Declining search frictions
- Within-industry calibration
- Outsourcing & within-occupation analysis
- OJS
- Matching on task-specific skills
- Increased talent dispersion

▶ Jump

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Key takeaways

- ↑ Skill specialization endogenously generates ↑ coworker talent complementarity
- ↑ Coworker complementarity leads to ↑ positive assortative coworker sorting
- S Coworker complementarity has doubled since 1985 & talent sorting has intensified
- ${\bf 0}$ This explains \approx 40% of \uparrow between-firm wage inequality share

Productivity implications & more

Overview of extensions & other implications

- Aggregate productivity
- Productivity dispersion
- "Coworker job ladders"
- Person-level inequality
- · For fun: generative AI

- **▶** Jump
- ▶ Jump
- ▶ Jump
- **▶** Jump

Production complementarities imply coworker sorting matters for agg productivity

$$\circ f(x_1,\cdots,x_n)=n^{1+\chi}\times\left(\frac{1}{n}\sum_{i=1}^n(x_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}$$

Production complementarities imply coworker sorting matters for agg productivity

$$\circ f(\mathbf{x}_1,\cdots,\mathbf{x}_n)=\mathbf{n}^{1+\chi}\times\left(\frac{1}{n}\sum_{i=1}^n(\mathbf{x}_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}$$

- Search frictions induce misallocation \sim coworker mismatch

Implications for aggregate productivity

· Production complementarities imply coworker sorting matters for agg productivity

$$\circ f(\mathbf{X}_1,\cdots,\mathbf{X}_n)=n^{1+\chi}\times\left(\frac{1}{n}\sum_{i=1}^n(\mathbf{X}_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}$$

- Search frictions induce misallocation \sim coworker mismatch
- Quantify mismatch costs: compare eqm outcome vs to productivity under pure PAM
 ⇒ 2010s gap: 2.05%, similar for earlier periods

• Production complementarities imply coworker sorting matters for agg productivity

$$\circ f(x_1, \cdots, x_n) = n^{1+\chi} \times \left(\frac{1}{n} \sum_{i=1}^n (x_i)^{\frac{1}{1+\chi}}\right)^{1+\chi}$$

- Search frictions induce misallocation \sim coworker mismatch
- Quantify mismatch costs: compare eqm outcome vs to productivity under pure PAM
 ⇒ 2010s gap: 2.05%, similar for earlier periods
- Trends: ↑ talent sorting limited ↑ in mismatch costs given χ ↑
 ⇒ no-reallocation counterfactual: productivity gap 4.65%

Key takeaways

- Skill specialization endogenously generates coworker talent complementarity
- ↑ Coworker complementarity leads to ↑ positive assortative coworker sorting
- $oldsymbol{3}$ The strength of coworker complementarity has pprox doubled since 1985
- ho This explains pprox 40% of \uparrow between-firm wage inequality share
- **⑤** Increased talent sorting helped keep TFP close to potential

Conclusion

Conclusion: firms form & organize teams – matters for macro

- This paper:
 - 1 task-based microfoundation for coworker complementarity
 - \Rightarrow specialization + team production \rightarrow complementarity
 - 2 measurement of complementarities
 - ⇒ empirical support for model mechanisms
 - 3 structural & quantitative explanation for the "firming up" of inequality
 - ⇒ role of increased complementarities
 - ⇒ increased talent sorting helped keep TFP close to potential
- Step to **broader agenda**: firms as "team assemblies" in macro

Thank You!



Extra Slides

Research agenda

Business-cycle dynamics

- Workers, Capitalists, and the Government: Fiscal Policy & Income (Re)Distribution (w/ Cantore, JME)
- o Volatile Hiring: Uncertainty in Search & Matching Models (w/ Den Haan & Rendahl, JME)
- The Risk-Premium Channel of Uncertainty (w/ Lee & Rendahl, RED)

Structural trends in firm organization, labor markets, and technology

- Superstar Teams
- o Frictional Worker and Firm Dynamics with Two-sided Heterogeneity (w/ Ifergane)
- Ideas Are Harder to Manage (w/ Carvalho)
- Medium-term: business cycle analysis with disaggregate labor demand & supply

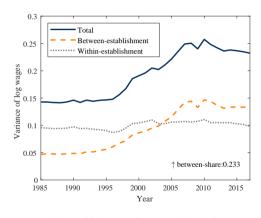
Fact 1: ↑ between-firm share of wage inequality



- Large empirical literature: "firming up inequality" [e.g., Card et al., 2013; Song et al., 2019]
 - o "superstar firms" [e.g., Autor et al., 2020]
- Fact 1: ↑ wage inequality primarily due to between-component
- Robust pattern

```
► Cross-country ► Panel est. ► Wage resid. alternatives

► Within-occ ► Within-ind
```



Notes. Model-free statistical decomposition, where the "between" component corresponds to the person-weighted variance of est.-level avg. log wage.

Fact #2: talented workers increasingly collaborate



To what extent do "talented workers" tend to have "talented coworkers"?

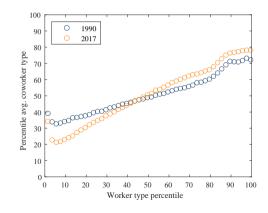
Fact 2: + assortative coworker sorting \(\)

o
$$\rho_{xx} = \operatorname{corr}(\hat{x}_i, \hat{x}_{-it})$$
: 0.43 ('85-'92) \nearrow 0.62 ('10-'17)

· Robust pattern

```
► Table ► Within-occ. nonlinear

► Hakanson et al. (2021)
```





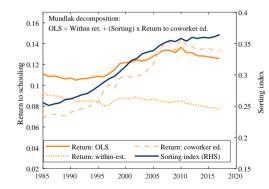
- Fact 3: increase in return to schooling is primarily due to workplace effects
- Mundlak decomposition of year-specific OLS return to schooling:

$$\beta_t^{\text{ols}} = \beta_t^{\text{within}} + \rho_t \times \beta_t^{\text{estab.}}$$

In
$$w_{it} = eta_{ ext{o}} + eta_{ ext{t}}^{ ext{within}} \mathsf{S}_{i} + eta_{ ext{t}}^{ ext{estab}} ar{\mathsf{S}}_{j(i,t),t} + e_{it}$$

where $\bar{S}_{j(i,t),t}$ is avg. years of schooling in establishment j of worker i in year t

- $\mathbf{1}$ β_t^{within} : within-establishment return
- \mathfrak{D} $\beta_t^{\mathrm{estab.}}$: return to avg. establishment schooling



Notes. Plot of coefficients from year-by-year regressions of log wages.

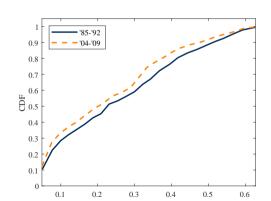


• \(\sqrt{Workers move to jobs with similar tasks, rather than randomly \)

Comparison

• Q: are workers becoming more likely to perform similar tasks across jobs, over time?

- **Yes:** distribution of moves in ('04-'09) is stochastically dominated by that in ('85-'92)
 - \circ uncond. average: 0.253 ightarrow 0.227: 10% decline
- Robust in regression design
 - o quantile regressions: ✓at different quantiles



Brief summary of methodology: occupations and task space



- Measure task similarity between occupations
 - $\circ \ \overline{\mathbf{l}}_o = (\overline{l}_{o_1}, \dots, \overline{l}_{o|\hat{\mathcal{T}}|})$: vector of task content of occupation o, with $\overline{l}_{o_{\mathcal{T}}}$ denoting the fraction of workers in occupation o performing task $\tau \in \hat{\mathcal{T}}$, where $|\hat{\mathcal{T}}| \in \mathbb{Z}_{++}$ (i.e., discretized)
 - o distance in task space between any two occupations o and o',

$$\varphi(\overline{\mathbf{I}}_{o},\overline{\mathbf{I}}_{o'}) = \frac{1}{\pi} cos^{-1} \left(\frac{\overline{\mathbf{I}}_{o}' \overline{\mathbf{I}}_{o'}}{||\overline{\mathbf{I}}_{o}|| \cdot ||\overline{\mathbf{I}}_{o'}||} \right) \in [0,1]$$

- o **implementation:** BIBB longitudinal microdata ($|\hat{T}|$ = 15)
- **Occupational movers:** an individual i who in period t is employed at j in occupation o counts as an *occupational mover* if in t+1, i is employed at $j' \neq j$ and $o' \neq o$
 - o implementation: matched employer-employee micro data (entire biography!)
- \P Merge $\{\varphi(\bar{\mathbf{l}}_o,\bar{\mathbf{l}}_{o'})\}_{oo'}$ into mover sample \to project moves onto task distance space
 - o harmonized occupational classification KldB1988-2d



- · Occupations as points in task space definitions:
 - $\circ \ \overline{\mathbf{l}}_o = (\overline{l}_{o1}, \dots, \overline{l}_{o|\hat{\mathcal{T}}|})$: vector of task content of occupation o, with $\overline{l}_{o\tau}$ denoting the fraction of workers in occupation o performing task $\tau \in \hat{\mathcal{T}}$, where $|\hat{\mathcal{T}}| \in \mathbb{Z}_{++}$ (i.e., discretized)
 - distance in task space between any two occupations o and o',

$$\varphi(\overline{\mathbf{l}}_{o},\overline{\mathbf{l}}_{o'}) = \frac{1}{\pi}\mathsf{cos}^{-1}\left(\frac{\overline{\mathbf{l}}_{o}'\overline{\mathbf{l}}_{o'}}{||\overline{\mathbf{l}}_{o}||\cdot||\overline{\mathbf{l}}_{o'}||}\right) \in [0,1]$$

- Implementation: BIBB longitudinal microdata
 - 15 harmonized tasks across survey waves
 - o measure $\bar{l}_{o\tau}$: share of individuals belonging to o performing τ
 - o construct matrix of bilateral distances for each wave, then take average of $\varphi(\bar{\mathbf{l}}o,\bar{\mathbf{l}}o')$ across waves for each (o,o')
 - o note: I thus hold the distance in task space between any two occupations fixed over time

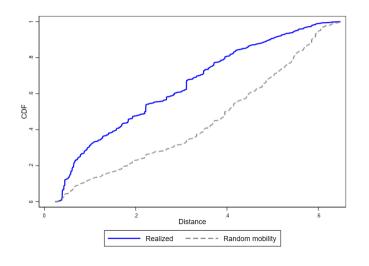
Methodology (2): occupational movers

- Consider individual i who in period t is employed at j in occupation o. I consider i an occupational mover if in t+1, i is employed at $j' \neq j$ and $o' \neq o$.
 - o only counted as occ. mover if employed in different job: cf. Kambourov and Manovskii (2008)
 - o considering switch in adjacent periods: more likely that it is a voluntary move
- Function $\varphi(\bar{\mathbf{l}}_o, \bar{\mathbf{l}}_{o'})$ maps each $o \to o'$ move onto [0, 1]
- Implementation: merge $\{\varphi(\bar{\mathbf{l}}_o,\bar{\mathbf{l}}_{o'})\}_{oo'}$ into SIEED
 - o harmonized occupational classification KldB1988-2d
 - restrict myself to 1985-2009, because subsequent stark change in occupational classification limits comparability (missing notifications, etc.)



▶ Back

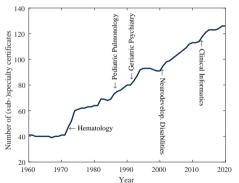
Comparison of realized movements in task space vs. random mobility



Examples: rising specialization

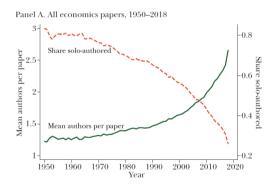


• Deepening medical specialization



Notes. Data from American Board of Medical Specialities. For each year, it shows the number of unique speciality or sub-speciality certificates that have been approved and issued at least once by that year and which are are still beine issued.

• Rise of research teams [Jones, 2021]



Data sources: short description of main datasets



- Germany: SIEED linked employer-employee dataset
 - o establishment and individual data generated in administrative processes, spell level
 - built up from a 1.5% sample of all establishments, but includes comprehensive employment biographies of individuals employed at these establishments
 - o worker info: (real) daily wage, occupation, education, ...
 - o top coding (affects >50% of university-educated men in regular full-time employment)
 - ightarrow adopt standard imputation methods (Dustmann et al., 2009; CHK, 2013)
 - o much larger sampling frame than more familiar LIAB
- Portugal: Quadros de Pessoal & Relatório Único, 1986-2017
 - $\circ \approx$ universe of private sector firms and workers employed by them, annual
 - worker info: detailed earnings measures (base wage, regular benefits, irregular benefits (performance-pay, bonuses, etc.), overtime pay); no top-coding; also hours worked within the month (regular and overtime) ⇒ (real) total hourly wage
 - firm information includes income and balance sheet data from 2004 onward

Sample restrictions



- Data cleaning ⇒ broadly harmonized samples
- · Main restrictions
 - o age 20-60
 - o full-time employed
 - o drop agriculture, public sector, utilities industries
 - o firms (and their employees) with at least 10 employees
- DE: West Germany
- Transform SIEED spell-level data into annual panel
- PRT: at least. official minimum wage

Wage Imputation procedure

- Follow imputation approach in CHK2013, building on Gartner et al. (2005) and Dustmann et al. (2009)
 - 1 fit a series of Tobit models to log daily wages
 - then impute an uncensored value for each censored observation using the estimated parameters of these models and a random draw from the associated (left-censored) distribution
- Fit 16 Tobit models (4 age groups, 4 education groups) after having restricted the sample (to include West German men only, in particular) and I follow CHK in the specification of controls by including not only age, firm size, firm size squared and a dummy for firms with more than ten employees, but also the mean log wage of co-workers and fraction of co-workers with censored wages. Finally, following Dauth & Eppselheimer (2020) I limit imputed wages at 10 × 99th percentile.

Mapping model to data: coworker types



• Defining $S_{-it} = \{k : j(kt) = j(it), k \neq i\}$ as the set of *i*'s coworkers in year *t*, compute the average type of *i*'s coworkers in year *t* as $\hat{x}_{-it} = \frac{1}{|S_{-it}|} \sum_{k \in S_{-it}} \hat{x}_k$.

· Coworker group:

- o alternative: same establishment-occupation-year cell
- but CC arise precisely when workers are differentiated in their task-specific productivities

Averaging step:

- o equally-weighted averaging ignores non-linearity in coworker aggregation
- paper: show using non-linear averaging method that baseline results in bias, but it's minor in magnitude
- **Firm size variation:** averaging ensures that a single move will induce a smaller change in the *average* coworker quality in a large team than in a small one

Mapping model to data: identification strategy for χ



- **Literature:** complementarities primarily between workers and firms usually inferred indirectly from sorting patterns
 - o exception: Hagedorn-Law-Manovskii (2017)
- This paper: directly measure coworker complementarity in the data, recover χ structurally given $\gamma=\frac{\chi}{\chi+1}$
- Paper does $\it not$ use microfoundation itself to measure χ , respectively γ
- Experiment: fit a (truncated) Fréchet distribution to Grigsby's (2023) non-parametric estimates of the multi-dimensional skill dist. estimated from CPS data
 - $\circ \ \ {
 m recover} \ \gamma = {
 m o.84} \ {
 m for 2006} \ {
 m but} \ {\it very noisy estimates}$



• Ongoing work: use the extended microfoundation to identify χ



Direct estimation of χ : proof of concept

- Grigsby (2023): only paper that provides a cardinal measure of skill task-specificity
- Evidence on time trends are qualitatively consistent with "specialization hypothesis": cross-type average of within-type variance across specific skills grew by nearly 50% b/w 1980s and 2000s & skill transferability has declined amongst high-skill occupations
- His operationalization of worker types and tasks does not directly map onto my model (no identifying assumption; coarse occupational skills; US vs DE data)
- **Proof of concept:** but suppose we just take those data, extract moments capturing average within-worker cross-task efficiency dispersion, fit a (truncated) Fréchet, recover $\gamma = \frac{\chi}{1+\chi}$
 - \Rightarrow / γ similar to structural estimation result based on evidence from wage CC

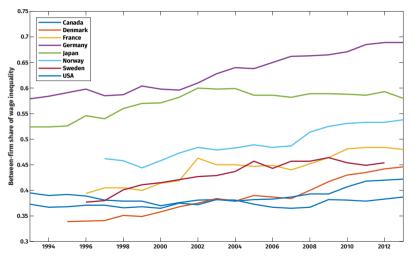
Semi-structural back-of-envelope calculation for γ



- Structurally recover $\gamma \frac{\chi}{\chi+1}$ by estimating $\frac{\partial^2 w(x|x')}{\partial x \partial x'}$ in the data, which was shown to be proportional to $\frac{\partial^2 f(x,x')}{\partial x \partial x'}$
- But how is $\frac{\partial^2 f(x,x')}{\partial x \partial x'}$ related to γ ?
- Definitionally, $\gamma = (ff_{ij})/(f_if_j)$ for any $i \neq j$
- Can we avoid full structural model? \Rightarrow If have measures not only of f_{ij} but also output f and marginal products f_i
- Suppose, for any x and x', we use wages to back out marginal products –
 competitive wage determination rather bargaining! and recover output from sum
 of wages divided by labor share
- Find $\gamma \approx$ 0.79 very close to structural estimate!

Firming up inequality: cross-country evidence



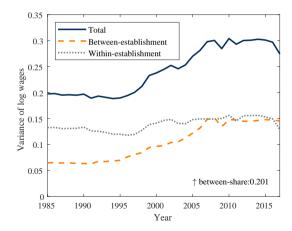


Notes. Data from Tomaskovic-Devey et al. (2020), Measures of earnings differ across countries and, for Germany, between T-D et al. and my study based on the SIEED.





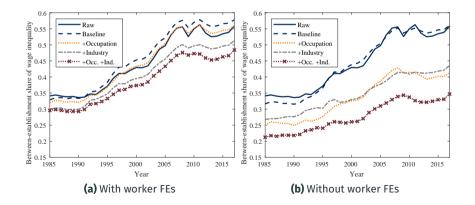
• Instead of considering all employers, restrict attention to "panel establishments"

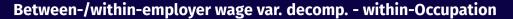


Between-/within-employer wage var. decomp. - alternative w-residuals

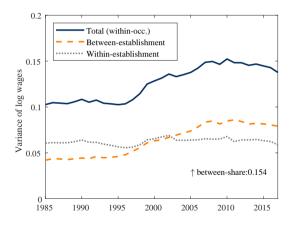


- "With worker FEs": regress $\ln \tilde{w}_{it} = \alpha_i + X'_{it}\hat{\beta} + \epsilon_{it}$, construct $\ln w_{it} = \ln(\tilde{w}_{it} X'_{it}\hat{\beta})$.
- "Without worker FEs": regress $\ln \tilde{w}_{it} = \alpha_0 + X_{it}' \hat{\beta} + \epsilon_{it}$, and consider residuals ϵ_{it}



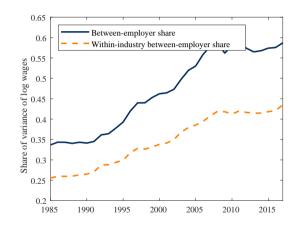






Between-/within-employer wage var. decomp. - within-Industry





Notes. Based on 'baseline' residualized wages.

Evolution of coworker sorting: correlation coefficient



- Estimate \hat{x}_i and \hat{x}_{-it} separately for 5 periods
- In addition to the baseline, also consider ranking within-occupation

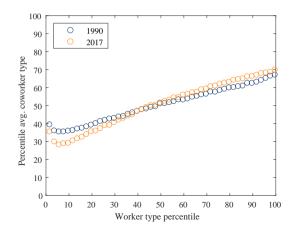
	Sorting		
Period	Spec. 1	Spec. 2	
1985-1992	0.427	0.423	
1993-1997	0.458	0.443	
1998-2003	0.495	0.452	
2004-2009	0.547	0.470	
2010-2017	0.617	0.519	

Notes. The column labelled "Sorting" indicates the correlation between a worker's estimated type and that of their average coworker, separately for five sample periods. Under "Spec. 1" workers are ranked economy wide (baseline), while under "Spec. 2" they are ranked within occupations.

Evolution of coworker sorting: within-occupation ranking binscatter



• Reproduce non-linear sorting plot, but now \hat{x}_i is based on within-occupation ranking

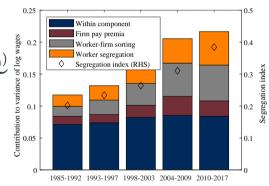


AKM-based wage variance decomposition



$$\begin{aligned} \operatorname{Var}(\textbf{\textit{W}}_{it}) &= \underbrace{\operatorname{Var}(\alpha_i - \bar{\alpha}_{j(i,t)}) + \operatorname{Var}(\epsilon_{i,j})}_{\text{within-component}} \\ &+ \underbrace{\operatorname{Var}(\psi_{j(it)}) + 2\operatorname{Cov}(\bar{\alpha}_{j(it)}, \psi_{j(it)}) + \operatorname{Var}(\bar{\alpha}_{j(it)})}_{\text{between-component}} \end{aligned}$$

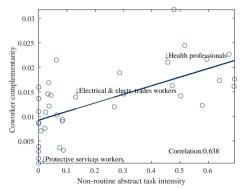
- $\circ \ \operatorname{Var}(\psi_i)$: firm-specific pay premia
- $\circ \operatorname{Cov}(\bar{\alpha}_i, \psi_i)$: (worker-firm) sorting
- $Var(\bar{\alpha}_j)$: (worker-worker) segregation
- Segregation index [Kremer-Maskin, 1996]: $Var(\bar{\alpha}_{i(it)})/Var(\alpha_i)$



Occupations: task complexity \Rightarrow complementarity \Rightarrow sorting

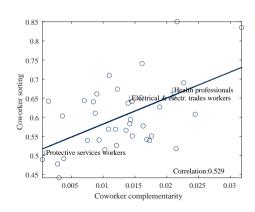


↑ Non-routine abstract task intensity
 ⇒ ↑ coworker wage complementarity



Notes. Quadros de Pessoal microdata. Horizontal axis indicates occupation's reliance on non-routine. abstract (NRA) tasks [Mihaylov and Tidens. 2019].

↑ Coworker wage complementarity
 ⇒ ↑ coworker sorting



Industries: coworker importance \Rightarrow complementarity \Rightarrow sorting



- ↑ Teamwork [Bombardini et al., 2012]
 ⇒ ↑ coworker wage complementarity
- 0.035 Coworker complementarity 0.02 Correlation:0 319 0.5 1.5 O*NET complementarity z-score

Notes. Horizontal axis measures the industry-level weighted mean score of an occupation-level index constructed from O*NET measuring the importance of: teamwork. impact on coworker output. Communication. and contact.

↑ Coworker wage complementarity
 ⇒ ↑ coworker sorting

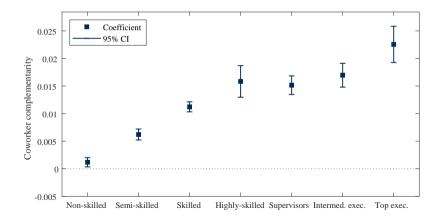


Notes. NACE-4-digit industries.

Hierarchies: complexity \Rightarrow complementarities



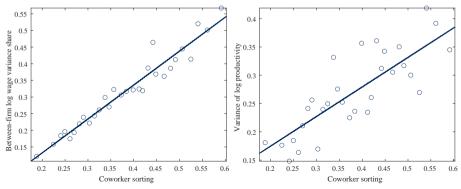
⇒ Coworker wage complementarities are (weakly) ↑ in the layer of a firm's hierarchy



Industries: coworker sorting ⇒ between-firm inequality



⇒ Measures of between-firm inequality in productivity and pay are increasing in the degree of coworker sorting at the industry-level.



(a) Between-firm share of wage dispersion

(b) Productivity dispersion

Cluster-based methodology: motivation



- Standard AKM approach estimates large number of firm-specific parameters, identified solely off worker mobility \Rightarrow incidental parameters problem \approx limited mobility bias $\Rightarrow var(\psi) \uparrow \& cov(\psi, \alpha) \downarrow$
- Bonhomme, Lamadon, and Malresa (2019, Ecma): 2-step grouped FE estimation
 - Recover firm classes using k-means clustering, based on similarity of earnings dist.
 - Estimate parameters of correlated random effects model by maximum likelihood, conditional on the estimated firm classes

Potential advantages

- mitigate limited mobility bias
 - sufficient number of workers who move between any given cluster to identify the cluster fixed effects
- allows relaxing sample restrictions (*n*-connected set restriction when estimating group-specific firm/cluster FEs)
- 3 if also take step 2, can estimate match complementarities between firms and workers

Cluster-based methodology: implementation

• Obtain clusters by solving weighted k-means problem

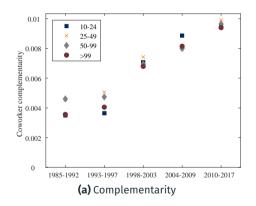
$$\min_{k(1),...,k(J),H_1,...,H_K} \sum_{j=1}^J n_j \int (\hat{F}_j(w) - H_{K_j}(w))^2 d\mu(w),$$

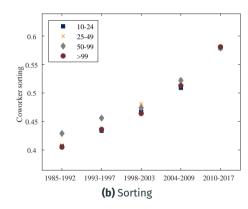
- o k(1), ..., k(J): partition of firms into K known classes; \hat{F}_j : empirical cdf of log-wages in firm j; n_j : average number of workers of firm j over sample period; $H_1, ..., H_K$: generic cdf's
- Implementation here:
 - \circ baseline value of K = 10, as in BLM, but experiment with K = 20 and K = 100
 - o use firms' cdf's over entire sample period on a grid of 20 percentiles
- "Half-BLM": take step (1), impute class to each worker-year observation, then estimate 2-way FE wage regression using cluster effects instead of firm effects:

$$W_{it} = \alpha_i + \sum_{k=1}^{K} \psi_k \mathbb{1}(i, t) = k + \beta X'_{it} + r_{it}$$

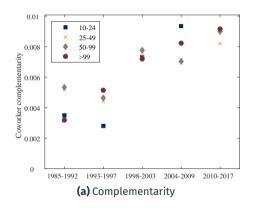
Coworker complementarity & sorting by team size

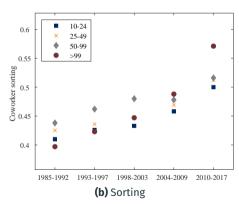




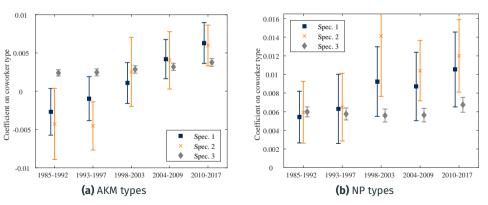


Coworker complementarity & sorting by team size - panel estab. only





$$\ln w_{it} = \beta_0 + \beta_1 \hat{x}_i + \frac{\beta_2}{2} \hat{x}_{-it} + \psi_{j(it)} + \nu_{o(i)t} + \xi_{s(i)t} + \epsilon_{it}$$



Notes. Specifications vary by ranking method – within-economy (spec. 1) vs. within-occupation (spec. 2/spec.3) and coworker group definition – establishment-year (spec. 1/spec.2) vs. establishment-occupation-year (spec.3).

Sorting & complementarity based on non-parametric ranking algorithm



• Instead of ranking workers based on AKM worker FEs, use non-param. ranking algo [Hagedorn et al., 2017]

	Sor	ting	Complementarities		
Period	Spec. 1 Spec. 2		Spec. 1	Spec. 2	
1985-1992	0.47	0.38	0.001	0.000	
1993-1997	0.56	0.46	0.002	0.001	
1998-2003	0.60	0.48	0.004	0.002	
2004-2009	0.65	0.50	0.005	0.002	
2010-2017	0.68	0.51	0.005 0.004		

Notes. This table indicates, under the column "Sorting" the correlation between a worker's estimated type and that of their average coworker, separately for five sample periods. The column "Complementarities" indicates the point estimate of the regression coefficient \(\triangle _C\). Under "Specification 1" workers are ranked economy wide, while under "Specification 2" they are ranked within two-digit occupations. Worker rankings are based on the non-parametric method.

Coworker complementarity: excluding managers



- Concern regarding complementarity estimates: driven by managers?
 - o only managers benefit from team quality, e.g. via larger span of control
 - o the only coworkers that matter are managers

Period	Baseline	Exclude as recipients	Exclude entirely
1985-1992	0.0036***	0.0036***	0.0038***
1993-1997	0.0042***	0.0041***	0.0043***
1998-2003	0.0070***	0.0074***	0.0076***
2004-2009	0.0082***	0.0084***	0.0092***
2010-2017	0.0091***	0.0097***	0.0093***

Notes. Managed are defined based on KldB-1988-3d, as in Jarosch et al. (2023).

- Consider sub-samples of job movers, job movers with contiguous employment spells ($t \rightarrow t+1$), and job movers with non-contiguous E spells ($t \rightarrow t+s$, s>1)
- Caveat: annual panel given data size, no direct observation of U/N spells in SIEED

Period	Baseline	All movers	Contig. E spells	Non-contig. E spells
1985-1992	0.0043***	0.0043***	0.0045***	0.0039***
1993-1997	0.0049***	0.0052***	0.0052***	0.0051***
1998-2003	0.0078***	0.0085***	0.0083***	0.0082***
2004-2009	0.0090***	0.0107***	0.0104***	0.0102***
2010-2017	0.0088***	0.0103***	0.0101***	0.0090***
Obs. in '10-'17 (1000s)	4,410	538	355	375

Notes. Unweighted observations. Regressions include FEs for employer; occupation-year; industry-year. Employer-clustered standard errors in parentheses.

Coworker complementarity: finite-differences approximation



- Regression approach imposes strong functional form assumptions on approximated empirical wage function $\hat{w}(x|x')$
 - ofc, mirrored inside structural model when calibrating
- Alternative: construct non-parametric $\hat{w}(x|x')$, then use finite-difference methods to compute the cross-partial derivative (but w/o FE controls)

Period	Regression	Non-parametric FD method
1985-1992	0.0036	0.0073
1993-1997	0.0042	0.0074
1998-2003	0.0070	0.0081
2004-2009	0.0082	0.0120
2010-2017	0.0091	0.0098

- Concern with both regression approach and non-parametric FD approach: mechanical relationship between wages ("LHS") and (within-period time-invariant) worker types, which are estimated from wages themselves ("RHS")
- Robustness check #1: years of schooling as type measure



- Robustness check #2: assign to each individual i in periods $p \in \{2,3,4,5\}$ the FE estimated for i in period p-1; re-compute worker deciles and average coworker types, \hat{x}_i^{p-1} and $\hat{x}_{-it}^{p-1} = (|S_{-it}|)^{-1} \sum_{k \in \mathcal{S}} \hat{x}_k^{p-1}$; re-estimate wage regression
- Results (see paper): magnitude of estimated $\hat{\beta}_c$ around 50% smaller when using lagged types, but evolution over time similar to baseline

Complementarity estimates using years of schooling



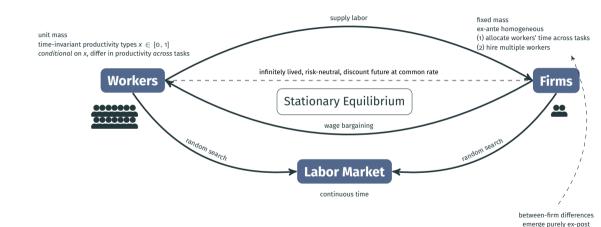
	'85-'92	'93-'97	'98-'03	'04-'09	'10-'17
Interaction	o.oo63***	o.oo6o***	0.0099***	0.0112***	0.0129***
	(o.ooo8)	(o.ooo7)	(0.0008)	(0.0007)	(0.0009)
Obs. (1000s)	3,613	2,508	2,694	3,836	4,376
R ²	0.5033	0.5451	0.5746	0.6330	0.6425

Notes. Dependent variable is the wage level over the year-specific average wage. Independent variables are a constant, years of schooling, coworker years of schooling, and the interaction between those two terms. All regressions include industry-year, occupation-year and employer fixed effects. Employer-clustered standard errors in parentheses. Observations are unweighted. The sample is unchanged from the main text, except that 96,517 observations with missing years of schooling are dropped. Observation count rounded to 1000ss.

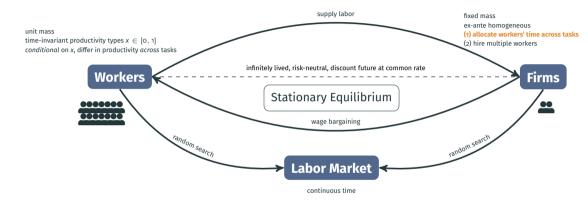
		Baseline				Within-industry avg.			
Sample Period	$\sigma_{\rm W}^2$	$\sigma_{\bar{\mathrm{W}}}^{\mathrm{2}}/\sigma_{\mathrm{W}}^{\mathrm{2}}$	$ ho_{XX}$	$\hat{eta}_{f c}$	$\sigma_{\rm W}^2$	$\sigma_{\bar{\mathrm{W}}}^{\mathrm{2}}/\sigma_{\mathrm{W}}^{\mathrm{2}}$	$ ho_{xx}$	$\hat{eta}_{f c}$	
1	0.143	0.337	0.427	0.0036	0.125	0.249	0.333	0.00283	
2	0.148	0.391	0.458	0.0042	0.125	0.288	0.351	0.00342	
3	0.191	0.456	0.495	0.0070	0.150	0.324	0.369	0.00585	
4	0.234	0.547	0.547	0.0082	0.168	0.388	0.405	0.00738	
5	0.241	0.568	0.617	0.0091	0.171	0.412	0.464	0.00823	

Notes. Within-industry avg. is person-year weighted average across OECD STAN-A38 (2-digit) industries.

Overview of model environment: firm organization meets labor search

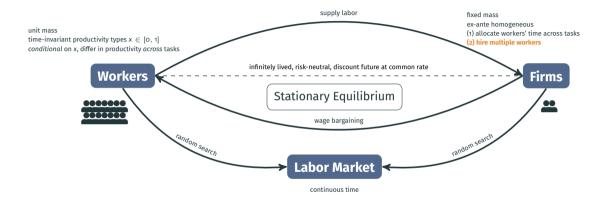


Overview of model environment: firm organization meets labor search



- 1 task assignment: derive production function for one firm, workforce exogenous
- 2 competition for talent: equilibrium matching given production function

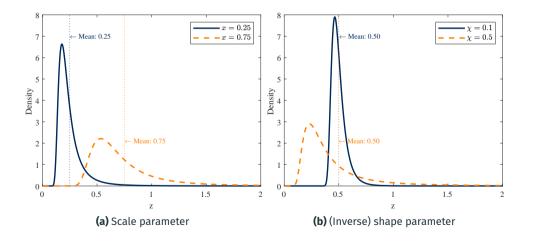
Overview of model environment: firm organization meets labor search



- 1 task assignment: derive production function for one firm, workforce exogenous
- 2 competition for talent: equilibrium matching given production function

Illustration: Fréchet distribution





• Analytically tractable version of the hiring block:

$$f(X_1, X_2) = X_1 + X_2 - \xi(X_1 - X_2)^2$$

 $\circ~$ in the $\kappa=$ 1 special case, ξ maps onto $\frac{\chi}{\chi+1}$ (up to scale)

Remark: Second-order Taylor approximation to CES

The second-order Taylor approximation to $f(x_1, x_2) = (\frac{1}{2}x_1^{\gamma} + \frac{1}{2}x_2^{\gamma})^{1/\gamma}$ around (\bar{x}, \bar{x}) with $\bar{x} = \frac{x_1 + x_2}{2}$ is

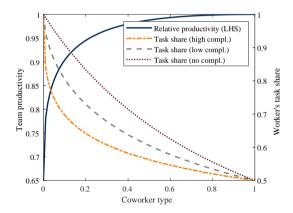
$$\bar{X} - \frac{1}{2} \underbrace{(1-\gamma)}_{\sim \epsilon} \frac{\sigma_X^2}{\bar{X}},$$

where $\sigma_{x}^{2} = (\frac{x_{1}-x_{2}}{2})^{2}$.

Quality mismatch & task mismatch



 When high type is paired with a low type, she ends up "wasting time" on tasks that she is relatively less efficient in and wouldn't have to do if teamed up optimally



Extension: team production with communication costs



- Assumption till now: division of labor incurs no output losses due to coordination frictions
- But implementing the division of labor may \downarrow time available for task production because of $\it communication$ requirements

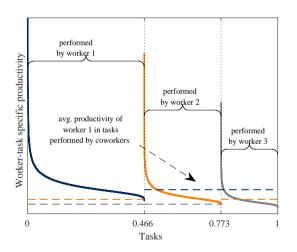
[Becker & Murphy, 1992; Deming, 2017]

- Extension allowing for such coordination costs shows:
 - qualitative link between technology & coworker complementarities exists unless division of labor is prohibitively costly
 - 2 $\chi \uparrow \Rightarrow$ importance of organizational quality for productivity \uparrow
- Ongoing research: rich microdata from Fortune-100 company to describe communication behavior



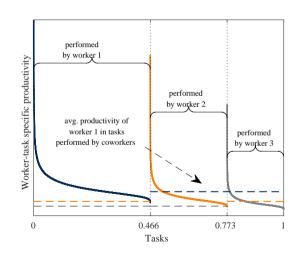
• tasks assigned by comparative advantage

$$\begin{array}{c} \circ \ \textit{i's} \ \mathsf{task} \ \mathsf{set} \\ \mathcal{T}_{\textit{i}} = \left\{ \tau \in \mathcal{T} : \frac{\mathsf{z}_{\textit{i}}(\tau)}{\lambda_{\textit{i}}^{\textit{l}}} \geq \mathsf{max}_{\textit{k} \neq \textit{i}} \ \frac{\mathsf{z}_{\textit{k}}(\tau)}{\lambda_{\textit{k}}^{\textit{l}}} \right\} \end{array}$$

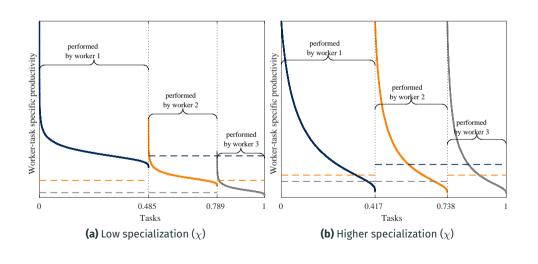


Optimal organization: illustration

- tasks assigned by comparative advantage
- ② i's share of tasks ↑ in i's talent, ↓ in coworkers' talent
 - $\begin{array}{c} \circ \ \textit{i's} \ \text{task share} \\ \pi_i = \big(x_i^{\frac{1}{1+\chi}} \big) \big(\sum_{k=1}^n (x_k)^{\frac{1}{1+\chi}} \big)^{-1} \end{array}$



Optimal organization: illustration – low vs. high χ



Optimal organization: Lemma

Lemma:

If workers' task-specific efficiencies are independently Fréchet-distributed, then:

1 The shadow cost index is

$$\lambda = \left(\sum_{i \in \mathcal{S}} \left(\frac{a_1 x_i}{\lambda_i^L}\right)^{1/\chi}\right)^{-\chi}.$$

2 The fraction of tasks for which worker *i* is the least-cost provider is

$$\pi_i := \Pr\{\lambda_i(\tau) \leq \min_{k \in \mathcal{S} \setminus i} \lambda_k(\tau)\} = \frac{(\mathsf{x}_i/\lambda_i^\mathsf{L})^{1/\chi}}{\sum_{k \in \mathcal{S}} \left(\mathsf{x}_k/\lambda_k^\mathsf{L}\right)^{1/\chi}}.$$

3 The shadow value of all tasks used in final goods production that were produced by worker i, defined as $Q_i := \int_{\mathcal{T}} \tilde{\lambda}(\tau) y_i(\tau) d\tau$, is a fraction π_i of the total shadow value of tasks used:

$$Q_i = \pi_i Q$$
.



- **1** Derive $G(p) := \Pr{\{\tilde{\lambda}(\tau) \leq p\}}$ given $G_i(p) := \Pr{\{\lambda_i(\tau) \leq p\}}$, using FOC and max-stability property
- ② Use G(p) + standard CES shadow price index to solve (int. by sub.) for

$$\lambda = \left(\int_{\mathcal{T}} \tilde{\lambda}(\tau)^{1-\eta} d\tau \right)^{\frac{1}{1-\eta}}.$$
 (5)

- 3 Use G(p) and $G_i(p)$ to derive probability that i produces some task τ , which by LLN (continuum assumption!) is equal to share of tasks produced, π_i
- **Q** Relate λ_i^L to value of all tasks produced by the worker, $\lambda_i^L = \pi_i \lambda Y$
- **6** Normalize $\lambda = 1$, then algebra yields $Y = f(x_1, ..., x_n; \chi)$

Numerical example: setup



- H, H': avg productivity 100 vs. L, L': avg. productivity 50
- · Working alone: realized productivity equal to avg
- Low value of χ

	Ideation	Theory	Matlab	Stata	Write	Present	With L'	With H'	Δ
L	53	52	51	49	48	47			
Н	106	104	102	98	96	94			

- High value of χ

	Ideation	Theory	Matlab	Stata	Write	Present	With L'	With H'	Δ
L	65	60	55	45	40	35			
Н	130	120	110	90	80	70			

Numerical example: teaming up with L'

• Low value of χ

	Ideation	Theory	Matlab	Stata	Write	Present	With L'	With H'	Δ
L	53	52	51	49	48	47	52		
Н	106	104	102	98	96	94	101.2		
Ľ	47	48	49	51	52	53			

• High value of χ

	Ideation	Theory	Matlab	Stata	Write	Present	With L'	With H'	Δ
L	65	60	55	45	40	35	60		
Н	130	120	110	90	80	70	112.5		
Ľ	35	40	45	50	55	60			

Numerical example: teaming up with H'

• Low value of χ

	Ideation	Theory	Matlab	Stata	Write	Present	With L'	With H'	Δ
L	53	52	51	49	48	47	52	53	1
Н	106	104	102	98	96	94	101.2	104	2.8
Ľ	47	48	49	51	52	53			
H'	94	96	98	102	104	106			

• High value of χ

	Ideation	Theory	Matlab	Stata	Write	Present	With L'	With H'	Δ
L	65	60	55	45	40	35	60	62.5	2.5
Н	130	120	110	90	80	70	112.5	120	7.5
Ľ	35	40	45	50	55	60			
H'	70	80	90	110	120	130			

Numerical example: comparison and take-aways

Low value of χ	With L'	With H'	Δ
L	52	53	1
H	101.2	104	2.8
Δ			1.8

High value of χ	With L'	With H'	Δ
L	60	62.5	2.5
H	112.5	120	7.5
Δ			5

Takeaways

- **1** Higher χ : greater benefit from team production ("love for variety")
- $oldsymbol{2}$ Higher χ : coworker quality matters more for own realized productivity

Corollary: Task shares

Suppose that $x_i > x_j$. Then (i) i performs a strictly larger share of tasks than j for $\chi < \infty$; (ii) the difference in task shares is decreasing in χ ; (iii) the ratio of i's relative to j's task share approaches $\frac{x_i}{x_j}$ as $\chi \to \infty$; and (iv) task shares are equalized as $\chi \to \infty$.

Proof:

All four elements of the statement immediately follow by noting that Lemma 1 (ii) implies that $\frac{\pi_i}{\pi_i} = \left(\frac{x_i}{x_i}\right)^{\frac{1}{1+\chi}}$.

· Baseline: worker-task specific productivities are independent draws from Fréchet,

$$Pr(z_i(\tau) \leq z) = \exp\left(-\left(\frac{z}{\iota X_i}\right)^{-1/\chi}\right)$$

- $\circ~\chi$ plays dual role: within-worker dispersion and across-coworker dispersion
- Instead, suppose that joint distribution across workers

$$P[z_i(\tau) \leq z_1, \dots, z_n(\tau) \leq z_n] = \exp \left[-\left(\sum_{i=1}^n \left(\left(\frac{z}{\iota x_i} \right)^{-\frac{1}{\chi}} \right)^{\frac{1}{\xi}} \right)^{\xi} \right]$$

- $\circ~\chi$: now clearly defined as referring to one workers' productivity profile over tasks
- o $\xi \in (0,1]$: captures correlation in draws *across* workers



Proposition: Aggregation result - extended

The vector of talent types $(x_1,...,x_n)$ is a sufficient statistic for team output Y, s.t.

$$Y = f(\mathbf{x}; \chi, \xi) = n^{1+\chi\xi} \left(\frac{1}{n} \sum_{i} (x_i)^{\frac{1}{\chi\xi+1}} \right)^{\chi\xi+1}$$

Interpretation of extended aggregation result

- Intuition: (for n sufficiently large), output is greater if
 - coworkers are similar to each other in terms of talent ("vertical"); as before, but also if
 - coworkers are more different from one another in terms of what tasks they're good at ("horizontal")
- $\chi\uparrow$ strengths dependence of Y on team composition vertically & horizontally
 - \circ suppose x > x'; $\exists \{\chi, \xi, \xi'\}$ where $\xi, xi' \in (0, 1]$: $f(x, x, \xi; \chi) < f(x', x', \xi'; \chi)$
- Coworker talent complementarities now depend on $\chi \times \xi$, hence also on ξ
 - $\circ~$ results in baseline go through with $\hat{\chi}=\chi\xi$

Dynamic setting: ξ is endogenous

- Dynamic setting: ξ is naturally **endogenous** to firms' hiring decisions: to max production, firm will aim to hire workers whose **z** vector has a low corr with existing employee(s)
 - microfoundation thus motivates departure from 'standard' setup w/ matching based on absolute advantage types only [e.g., Herkenhoff et al., 2023]

• assumption of baseline: no hiring based on task-specific skills – implicit through independence of draws across coworkers – is less plausible if $\chi >$ 0

Tractability & timng

- Tractability: treat ξ as a match-specific shock \sim horizontal match quality \leftarrow tractable way of modelling multidimensional skill heterogeneity with matching on both absolute advantage and task-specific skills!
- **Timing:** an unmatched worker x randomly draws (i) a searching firm with current employee x'; and together they draw (ii) a 'horizontal match-quality shock' ξ from an exogenous distribution H
 - task-specific skills as fully observable at time of meeting ('inspection good'), i.e. no gradual learning about horizontal match takes place over time
- Aggregation result implies: (x, x', ξ) are sufficient to determine Y and, hence, matching decisions

Sketch of dynamic model (1): overview

Adjusted values

$$\Omega_{1}(x) := V_{f.1}(x) + V_{e.1}(x)
S(x) := \Omega_{1}(x) - V_{f.0} - V_{u}(x)
\Omega_{2}(x, x', \xi) := V_{f.2}(x, x', \xi) + V_{e.2}(x|x', \xi) + V_{e.2}(x'|x, \xi)
S(x|x', \xi) := \Omega_{2}(x, x', \xi) - \Omega_{1}(x') - V_{u}(x)$$

- Hiring policy: $h(x|x',\xi) = 1\{S(x|x',\xi) > 0\}$
 - ∘ $h(x|x') = \Pr\{S(x|x',\xi) > 0\}$ ← no longer $h(x|x') : [0,1]^2 \to \{0,1\}$ but instead $h(x|x') : [0,1]^2 \to [0,1]$
 - o $h(x) = 1{S(x) > 0}$
- KFEs: as before, given probabilistic definition of h(x|x')

Sketch of dynamic model (2): values

· Value of unmatched firm:

$$\rho V_{f.o} = (1 - \omega) \lambda_{v.u} \int \frac{d_u(x)}{u} S(x)^+ dx$$

· Value function of unmatched worker

$$\rho V_u(x) = b(x) + \lambda_u \omega \left[\int \frac{d_{f.o}}{v} S(x)^+ + \int \frac{d_{m.1}(\tilde{x}')}{v} S(x|\tilde{x}',\tilde{\xi})^+ dH(\tilde{\xi}) d\tilde{x}' \right]$$
 (6)

Joint value of a firm with employee x

$$\rho\Omega_{1}(x) = f_{1}(x) - \delta S(x) + \lambda_{v.u}(1 - \omega) \int \frac{d_{u}(\tilde{x}')}{u} S(\tilde{x}'|x,\tilde{\xi})^{+} dH(\tilde{\xi}) d\tilde{x}'$$
(7)

• Joint value of firm with (x, x', ξ)

$$\rho\Omega_2(\mathbf{x}, \mathbf{x}', \xi) = f_2(\mathbf{x}, \mathbf{x}', \xi) - \delta S(\mathbf{x}|\mathbf{x}', \xi) - \delta S(\mathbf{x}'|\mathbf{x}, \xi)$$
(8)

• Define threshold values of ξ for each (x, x') such that $S(x|x', \bar{\xi}(x|x')) = 0$. Quadratic equation in ξ , so there are 0, 1 or 2 roots in [0, 1]:

$$\circ O = S(x|x',1) + \frac{f(x,x',\bar{\xi}(x|x')) - f(x,x',1)}{c+2\delta}$$

$$\circ \ \overline{\xi} \colon \xi \in (0,1] : S(x|x',\overline{\xi}(x|x')) > 0 \text{ if } \xi > \overline{\xi}(x|x')$$

∘
$$\xi$$
: ξ ∈ (0, 1] : $S(x|x', \xi(x|x')) > 0$ if $\xi < \xi(x|x')$

• Implied conditional expected values:

$$\circ \ \overline{\xi}^*(k) = \frac{\int_k^1 \xi dH(\xi)}{1 - H(k)} \ ; \ \text{and} \ \xi^*(k) = \frac{\int_0^k \xi dH(\xi)}{H(k)}$$

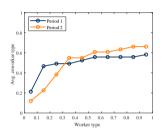
• Then rewrite, e.g., equation (6) as

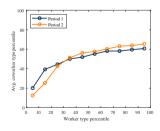
$$\rho V_{u}(x) = b(x) + \lambda_{u} \omega \left[\int \frac{d_{f.o}}{v} S(x)^{+} + \int \frac{d_{m.1}(\tilde{x}')}{v} S^{*}(x|\tilde{x}') \right] d\tilde{x}'$$

$$\text{where } \mathsf{S}^*(\mathsf{x}|\tilde{\mathsf{x}}') = \left[\mathsf{H}\left(\underline{\xi}\left(\mathsf{x}|\tilde{\mathsf{x}}'\right)\right) \times \mathsf{S}\left(\mathsf{x}|\tilde{\mathsf{x}}',\underline{\xi}^*\left(\underline{\xi}\left(\mathsf{x}|\tilde{\mathsf{x}}'\right)\right)\right) + \left(\mathsf{1} - \mathsf{H}\left(\bar{\xi}\left(\mathsf{x}|\tilde{\mathsf{x}}'\right)\right) \times \mathsf{S}\left(\mathsf{x}|\tilde{\mathsf{x}}',\bar{\xi}^*\left(\bar{\xi}\left(\mathsf{x}|\tilde{\mathsf{x}}'\right)\right)\right)\right] + \left(\mathsf{1} - \mathsf{H}\left(\bar{\xi}\left(\mathsf{x}|\tilde{\mathsf{x}}'\right)\right) \times \mathsf{S}\left(\mathsf{x}|\tilde{\mathsf{x}}',\bar{\xi}^*\left(\bar{\xi}\left(\mathsf{x}|\tilde{\mathsf{x}}'\right)\right)\right)\right)$$

Implication: tentative calibration suggests improved quantitative fit

- Extended model (bottom) produces 'smoother' average coworker profiles
 - can also see this when looking at the full conditional coworker distribution
 - \circ also 'smoother' response to $\Delta \chi$
- Reason: matching probabilities conditional on meeting no longer {0,1}





Implication: new strategy to identify χ using the micro-foundation

Corollary: Identification of χ

Variation in wages conditional on x and x' identifies χ :

$$\underbrace{\frac{w(x|x';\xi=1)}{w(x|x';\xi=\bar{\xi}(x|x'))}}_{w_{\min}(x|x')} = \frac{\omega(f(x,x';\xi=1)-f(x'))+g(x)-h(x')}{\omega(f(x,x',\xi=\bar{\xi}(x|x))-f(x'))+g(x)-h(x')}$$

• Intuition: variation in Y – and hence w – conditional on (x,x') reflects differences in horizontal match quality, ξ , and the extent to which variation in ξ translates into variation in Y is increasing in χ

How to implement this...

- Method validated inside theoretical model
- Empirical implementation requires measure of within-(x, x') dispersion
- Discussion:
 - \circ challenge: within-(x, x') wage dispersion could reflect many factors outside of model, as well as measurement error
 - o so naive way of just computing within-cell dispersion not promising
 - job displacement design?
 - o related: movements in task space; which also shows that among occ. switchers, wage penalty for distant moves has increased over time, but v preliminary

Implication: new empirical avenues to test microfoundation

- Occupation-pair specific complementarities should be greater if (i) these two
 occupations are distant in skill/task space, but (ii) they are commonly employed
 together
 - o eg complementarity should be high for the pair hospital-manager/nurse
- Costs of job displacement should be greater if (i) highly specialized, and (ii) it is difficult to find coworkers with 'horizontally matching' skills
 - o team production and Marshallian agglomeration effects
- Probability of being hired conditional on talent mismatch is greater if your task-specific skill set is different from existing workers but typically required in production (as reflected, e.g., by workforce of other firms in the same industry)

Extended Lemma 1

Lemma: Lemma 1 - extended

Implied task share and shadow-cost index equal

$$\pi_{i} = \frac{\left(\mathbf{x}_{i}/\lambda_{i}^{L}\right)^{\frac{1}{\chi\xi}}}{\sum_{k=1}^{n}\left(\mathbf{x}_{i}/\lambda_{i}^{L}\right)^{\frac{1}{\chi\xi}}} \quad \mathbf{x}_{i} \lambda = \left(\sum_{i=1}^{n}\left(\frac{\mathbf{x}_{i}}{\lambda_{i}^{L}}\right)^{\frac{1}{\chi\xi}}\right)^{-\chi\xi}$$

OJS: not currently feasible with match-specific shocks

- **Challenge:** need to track distribution of ξ 's among the (x, x') pairs, but those will be mixtures of distributions that itself depend on team combination and origin
 - o consider a vacant firm attempting to poach x, if x is currently with x' and their horizontal fit is ξ ; then moving decision depends on $S(x) S(x|x', \xi)$
 - o but distribution of ξ conditional on (x, x') will differ depending on how (x, x') was formed, e.g. one coming out of unemployment vs via EE moves itself
 - o attempt to poach x by a firm with x'' when (x,x') is the current team: look at $S(x|x'',\xi') S(x|x',\xi) \to \xi'$ can be drawn from the unconditional distribution H but ξ comes from a distribution H(z|x,x'), which doesn't have a tractable form
- Idea for a solution approach but will be different paper
 - o conjecture: H(z|x,x') is be a mixture of left-truncated versions of H, where the truncation points differ by (x,x'), but crucially also on the origin of that team
 - \circ conceptually, the mixture weights should be obtainable from the ergodic distribution itself \to possibility for a fixed point...

What about shifts in the talent distribution?



- **Q**: could \uparrow economy-wide x-dispersion, σ_x , also explain \uparrow firm-level inequality?
 - \circ Kremer-Maskin (1996): as the dispersion of skills (talent) \uparrow in the economy, the relative dispersion of talent within firms \downarrow
- **Obs. #1:** Hakanson et al. (2021): direct skill measures (from military enlistment tests) point to Flynn effect but not not to increased dispersion (in cognitive test scores)
- Obs. #2: model exercise
 - o method: instead of rank interpretation, i.e. $x \sim U$, we separately parameterize σ_x by assuming a $\mathcal N$ distribution
 - finding: $\sigma_x \uparrow \Rightarrow \rho_{xx} \uparrow$, $\sigma_w \uparrow$, and $\sigma_{\bar{w}}/\sigma_w \uparrow$ but no measured increase in $\hat{\beta}_c$
- **Conclusion:** empirically unclear whether $\sigma_x \uparrow$, and if so, this would not explain the observed increase in coworker complementarity, i.e. latter is a distinct channel

Training policies in a team production context (w-i-p)



- "Training policies" ~ non-parametric perturbations of the talent distribution
 - o left-tail intervention: give everyone in 1st decile productivity of those in 2nd decile
 - o right-tail intervention: give everyone in 9th decile productivity of those in 10th decile
- Team production: effect of "training policies" partially via coworker spillovers!
- Relative effectiveness of left-tail vs right-tail intervention:
 - 1 the stronger are coworker complementarities, the relatively greater are the realized productivity gains from a left-tail intervention, b/c low-x tend to be weak links
 - but raising the productivity of coworkers of workers with high productive potential generates greater gains – and with sorting, those coworkers are themselves high-x
- Equilibrium: relative effectiveness of left-/right-tail training depends on both forces
 - tentative quantitative finding: right-tail intervention boosts average productivity by more but left-tail training also lowers inequality

Environment: demographics & preferences & production technology



- Time: continuous
- · Agents: workers & firms
 - \circ unit mass of workers, types uniformly distributed $x \in \mathcal{X} = [0, 1]$
 - \circ m_f mass of firms ex-ante homogeneous
 - o agents indexed by ranks of prod. dist., hence uniform type dist. [Hagedorn et al., 2017]
 - $\circ~$ agents infinitely-lived, risk-neutral, common discount rate ho, max. PV of payoffs
- **Production technology**: firms are vacant or have 1 or 2 workers
 - o normalize team size to max. $n = 2 \leftarrow$ key is "existing workforce" & "potential hire"
 - o convention: from x's perspective, let x' denote coworker
 - ∘ team production: f(x,x') ← see microfoundation
 - o 1-worker: f(x), short for $f(x, \emptyset)$

Environment: random search & wage bargaining

- **Timing** within *dt*-intervals
 - lacktriangle exogenous separation: Poisson rate δ
 - 2 random search & matching
 - g production & surplus sharing
- **Meeting process**: unemployed meet some firm at Poisson rate λ_u
 - o probability for a firm to be contacted by an(y) unemployed: $\lambda_{v,u} = \lambda_u \times u$
 - baseline: no on-the-job search
- Matching decisions based on joint surplus b/w firm & worker(s): privately efficient
- Surplus sharing: firm bargains with potential new hire, taking into account coworker complementarities; worker bargaining power ω
 - o continuous renegotiation, as if each worker is marginal (i.e., outside option: unemp.)

Stationary equilibrium



 Formally, after defining (i.) HJBs for unemployed & vacant & surplus values, and (ii.) Kolmogorov Forward Equations (KFEs) describing the evolution of the distribution of agents across states:

Definition:

A stationary search equilibrium is a tuple of value functions together with a stationary distribution of agents across states such that (i.) the value functions satisfy the HJB Equations given the distribution; and (ii.) the distribution satisfies the KFEs given the policy functions implied by the value functions.

- Needs to be computed numerically
 - agents' expectations & decisions must conform w/ population dynamics to which they give rise; as distribution evolves, so do agents' expectations

Environment: firm & worker states

• Distribution across states for a **worker** type x:

$$d_{w}(x)=d_{u}(x)+d_{m.1}(x)+\int d_{m.2}(x,\tilde{x}')d\tilde{x}'$$

- o $d_u(x)$: 'density' of unemployed of type x
- o $d_m(x)$, shorthand for $d_m(x, \emptyset)$: 'density' of matches w/ x as only worker
- o $d_m(x, x')$: 'density' of "team matches" b/w x and x'
- Distribution across states for a **firm** type v:

$$d_f = d_{f.0} + \int d_{m.1}(x)dx + \frac{1}{2} \int \int d_{m.2}(x,x')dxdx'.$$

- \circ $\frac{1}{2}$: account for 1 firm having 2 workers
- **Aggregates** can be backed out, e.g. $u = \int d_u(x)dx$

Environment: surplus sharing

· One-worker firm:

$$(1 - \omega)(V_{e,1}(x) - V_u(x)) = \omega(V_{f,1}(x) - V_{f,o})$$
(9)

Two-worker firm

$$(1-\omega)\big(V_{e.2}(x|x')-V_u(x)\big)=\omega\big(V_{e.2}(x'|x)+V_{f.2}(x,x')-V_{e.1}(x')-V_{f.1}(x')\big) \tag{10}$$

Surplus max. determines which worker types a firm w/ worker x hires \bigcirc Main



• Joint value of firm with worker x, $\Omega(x)$, satisfies:

$$\rho\Omega(\mathbf{x}) = f(\mathbf{x}) + \delta\big[-\Omega(\mathbf{x}) + V_u(\mathbf{x}) + V_{f,o}\big] + (1 - \omega)\lambda_{v,u} \int \frac{d_u(\tilde{\mathbf{x}}')}{u} \max\{S(\tilde{\mathbf{x}}'|\mathbf{x}), o\}d\tilde{\mathbf{x}}'$$

- o $V_{\mu}(x)$: value for unemp. worker; $V_{f,o}$: value for vacant firm; S(x): surplus from zero-worker firm hiring x
- o $d_u(x)$: density of unemployed workers of type x; $u = \int d_u(x) dx$
- \circ ω : worker bargaining wgt; δ : sep. rate; $\lambda_{V,U}$: rate of vacancy meeting unmatched worker

Surplus max. determines which worker types a firm w/ worker x hires Main



• Joint value of firm with worker x, $\Omega(x)$, satisfies:

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- \circ ω : worker bargaining wgt; δ : sep. rate; $\lambda_{V,U}$: rate of vacancy meeting unmatched worker
- Surplus S(x|x') reflects complementarities and hiring decisions reflect surplus

$$S(x|x')(\rho + 2\delta) = f(x,x') - \rho(V_u(x) + V_u(x') + V_{f.o}) + \delta S(x) - (\rho + \delta)S(x')$$
$$h(x|x') = \mathbf{1}\{S(x|x') > 0\}$$

HJB: unmatched



· Unmatched firm:

$$\rho V_{f.o} = (1 - \omega) \lambda_{v.u} \int \frac{d_u(x)}{u} S(x)^+ dx \tag{11}$$

· Unmatched worker:

$$\rho V_u(x) = b(x) + \lambda_u \omega \left[\int \frac{d_{f.o}}{v} S(x)^+ + \int \frac{d_{m.1}(\tilde{x}')}{v} S(x|\tilde{x}')^+ d\tilde{x}' \right]$$
 (12)

HJB: surpluses

• Surplus of coalition of firm with worker x

$$(\rho + \delta)S(x) = f(x) - \rho(V_u(x) + V_{f.o}) + \lambda_{v.u}(1 - \omega) \int \frac{d_u(\tilde{x}')}{u} S(\tilde{x}'|x)^+ d\tilde{x}'$$
(13)

• Surplus from adding x to x'

$$S(x|x')(\rho+2\delta) = f(x,x') - \rho(V_u(x) + V_u(x') + V_{f.o}) + \delta S(x) - (\rho+\delta)S(x')$$
(14)

KFE: unemployed

$$\delta\bigg(d_{m.1}(x) + \int d_{m.2}(x,\tilde{x}')d\tilde{x}'\bigg) = d_u(x)\lambda_u\bigg(\int \frac{d_{f.o}}{v}h(x,\tilde{y}) + \int \frac{d_{m.2}(\tilde{x}')}{v}h(x|\tilde{x}')d\tilde{x}'\bigg). \tag{15}$$

KFE: one-worker matches

$$d_{m.1}(x)\left(\delta + \lambda_{v.u} \int \frac{d_u(\tilde{x}')}{u} h(\tilde{x}'|x) d\tilde{x}'\right) = d_u(x) \lambda_u \frac{d_{f.o}}{v} h(x) + \delta \int d_{m.2}(x, \tilde{x}') d\tilde{x}'. \tag{16}$$

KFE: two-worker matches

$$2\delta d_{m.2}(x,x') = d_u(x)\lambda_u \frac{d_{m.1}(x')}{v}h(x|x') + d_u(x')\lambda_u \frac{d_{m.1}(x)}{v}h(x'|x). \tag{17}$$

Lemma: monotonicity of unemployment value and wage in x



Lemma: Monotonicity

Assume that $\frac{f_1(x)}{\partial x} > 0$, $\frac{\partial f_2(x,x')}{\partial x} > 0$, and $\omega > 0$. Then: (i) The value of unemployment $V_u(x)$ is monotonically increasing in x, and (ii) so is the wage function w(x|x').

Proof:

See paper appendix. Key: surplus representation.



• NB: here allow for ex-ante firm heterogeneity ⇒ measurement result extends

$$\begin{split} w(\mathbf{x}|\mathbf{y},\mathbf{x}') &= \rho V_u(\mathbf{x}) + \omega \big[f(\mathbf{x},\mathbf{y},\mathbf{x}') - \rho \left(V_u(\mathbf{x}) + V_u(\mathbf{x}') + V_{f,o}(\mathbf{y}) \right) \\ &+ \delta S(\mathbf{x}|\mathbf{y}) - (\rho + \delta) S(\mathbf{x}'|\mathbf{y}) \big] - \delta \omega S(\mathbf{x}|\mathbf{y}) \\ &= \omega \big(f(\mathbf{x},\mathbf{y},\mathbf{x}') - f(\mathbf{x}',\mathbf{y}) \big) + (1 - \omega) \rho V_u(\mathbf{x}) \\ &- \omega (1 - \omega) \lambda_{v,u} \int \frac{d_u(\tilde{\mathbf{x}}'')}{u} S(\tilde{\mathbf{x}}''|\mathbf{y},\mathbf{x}')^+ d\tilde{\mathbf{x}}''. \end{split}$$



Intuition for how coworker complementarities shape matching can be gained from a stylized model \rightarrow closed-form solutions

- Simplified setup:
 - o no ex-ante firm heterogeneity; mass of firms $m_f = \frac{1}{2}$
 - production: $f(x, x') = x + x' \xi(x x')^2$, where ξ controls complementarity Approx. of microfounded team prod. fn.
 - o no production with 1 employee & abstract from team production benefits
 - o firm has no bargaining power, workers each receive outside option plus half the surplus
- **Explicit search costs**: no discounting, guaranteed match ($M_u = M_f = 1$); but type-invariant worker search costs c
 - o supermodularity in f suffices for PAM [Atakan, 2006]

- **o** Each firm is randomly paired with one worker $x' \in \mathcal{X}$
 - \circ remaining: mass $\frac{1}{2}$ of uniformly distributed workers; mass $\frac{1}{2}$ of firms with one employee
- **1** Each (firm + x') unit is randomly paired with a worker $x \in \mathcal{X} \to \text{decision}$:
 - a. match: form a team
 - + produce & share production value
 - no further actions and zero payoff in stage 2 or
 - search: don't form a team
 - workers pay search cost c
 - + all have opportunity to re-match in stage 2. s.t.
- 2 frictionless matching b/w unmatched firms & workers; production
 - \circ pure PAM: x works with x (\leftarrow deterministic coupling $\mu(x) = x$)
 - o payoffs given pure PAM: $w^*(x) = x$ and $v^* = 0$

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 - no further actions and zero payoff in stage 2
 - **6** search: don't form a team
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- frictionless matching b/w unmatched firms & workers; production
 - o pure PAM: x works with x (\leftarrow deterministic coupling $\mu(x) = x$)
 - o payoffs given pure PAM: $w^*(x) = x$ and $v^* = 0$

Characterization using a stylized model: stage-1 matching decision

• A firm with employee x' that meets a worker of type $x \in \mathcal{X}$ decides to hire her, i.e. h(x,x')=1, if

$$\underbrace{f(x,x')}_{\text{match}} - \underbrace{\left[W^*(x) + W^*(x') + V^* - 2c^W\right]}_{\text{$\equiv S(x,x')$}} > 0$$

- Threshold distance s^* s.t. $h(x, x') = 1 \Leftrightarrow |x' x| < s^*$
- Threshold distance satisfies: $s^* = \sqrt{2c/\xi}$
 - greater complementarities (ξ) render the matching set *narrower*
 - o greater search costs (c) render the matching set wider



Corollary: Stylized model

For a given threshold s, which is decreasing in χ :

- 1 the coworker correlation is: $\rho_{XX} = (2s + 1)(s^2 1)^2$;
- the average coworker type is

$$\hat{\mu}(x) = \begin{cases} \frac{x+s^*}{2} & \text{for} & x \in [0, s^*) \\ x & \text{for} & x \in [s^*, 1-s^*] \\ \frac{1+x-s^*}{2} & \text{for} & x \in (1-s^*, 1]. \end{cases}$$

3 the between-firm share of the variance of wages is decreasing in s

Frictionless matching: assignment and pavoffs



- Working backwards, pin down frictionless payoffs that determine the outside option
- The equilibrium of the frictionless model can be derived in many ways
- Equilibrium assignment and payoffs:
 - PAM: $\mu(x) = x$ given supermodular $f(x_1, x_2)$
 - wage schedule obtained from integrating over FOC

$$w^*(x) = \int_0^x f_x(\tilde{x}, \mu(\tilde{x})) d\tilde{x}$$

where integration constant is zero due to f(o, o) = o

- o firm payoffs in this formulation are o
- Given $f(x_1, x_2) = x_1 + x_2 \gamma(x_1 x_2)^2$, with $\gamma > 0$, we have

$$\mu(x) = x$$

$$w^*(x) = x \quad \text{and } v^* = 0$$



Lemma: Conditional type distribution

Given a threshold distance s, the conditional distribution of coworkers for $x \in \mathcal{X}$ is

$$\Phi(X'|X) = \begin{cases} O & \text{for } X' < \sup\{0, X - s\} \\ \frac{X - \sup\{0, X - s\}}{\inf\{X + s, 1\} - \sup\{0, X + s\}} & \text{for } X' \in [\sup\{0, X - s, \}, \inf\{X + s, 1\}] \\ 1 & \text{for } X' > \inf\{X + s, 1\} \end{cases}$$



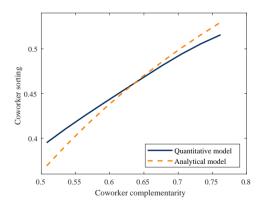
Corollary:

Given a threshold distance s and a value of γ , the between-firm share of the variance of wages is equal to

$$\frac{-\frac{13\,\gamma^2\,s^5}{2400}+\frac{\gamma^2\,s^4}{80}+\frac{5\,s^3}{36}-\frac{s^2}{6}+\frac{1}{12}}{\frac{\gamma^2\,s^4}{45}-\frac{4897\,\gamma^2\,s^5}{10800}-\frac{\gamma^2\,s^6}{324}+\frac{19\,\gamma^2\,s^5\ln(2)}{30}+\frac{1}{12}}.$$

Matching patterns: comparison of stylized model vs. quantitative





Overview of validation exercises: direction EE transitions & cross-section



- 2 additional types of validation exercise:
 - ✓EE transitions reallocate workers to more + assortative matches

▶ Details

- o do model-implied relationships also hold in cross-section?
 - 1 $\chi \uparrow \Rightarrow$ coworker complementarity \uparrow
 - 2 coworker complementarity $\uparrow \Rightarrow$ + assortative matching \uparrow

can test predictions because
we have measures of complementarity!

- Implementation of cross-sectional exercises: rich Portuguese micro data
 - o universe of private-sector actors, employer-employee data & income statements
- · Cross-sectional exercises:
 - ✓ Hierarchies

 - ✓ Occupations



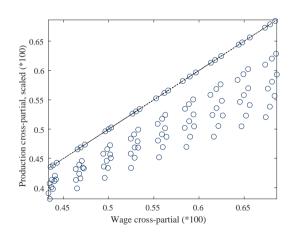








- Solve model for many combinations of χ , λ_e and b
- Compare FD approx of $f_{xx'}(x, x')$, scaled by ω , and $w_{xx'}(x|x')$
- Main parameter driving wedge: λ_e



Parameterization, including estimation results (2010s)



Parameter	Description	Targeted moment	Value	m	m
γ	Elasticity of complementarity	\hat{eta}_{c}	0.837	0.0091	0.0091
a_{o}	Production, constant	Avg. wage (norm.)	0.239	1	1
a_1	Production, scale	Var. log wage	1.557	0.241	0.241
b_1	Replacement rate, scale	Replacement rate	0.664	0.63	0.63
δ	Separation hazard	Job loss rate	0.008	0.008	0.008
λ_u	Meeting hazard	Job finding rate	0.230	0.162	0.162
ρ	Discount rate	External	0.008		
ω	Worker bargaining weight	External	0.50		
a_2	Production, team advantage	External	1.10		

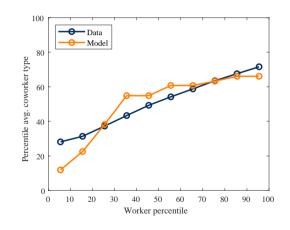
Estimated parameters and targeted moments

		2010-2017			1985-1992		
Parameter	Targeted moment	Value	m	m	Value	m	m
γ	$\hat{eta}_{m{c}}$	0.837	0.0091	0.0091	0.434	0.0035	0.0035
a_{o}	Avg. wage (norm.)	0.239	1	1	0.378	1	1
a_1	Var. log wage	1.557	0.241	0.241	1.216	0.143	0.143
b_1	Replacement rate	0.664	0.63	0.63	0.740	0.69	0.69
λ_{u}	Job finding rate	0.230	0.162	0.162	0.168	0.141	0.141
δ	Job loss rate	0.008	0.008	0.008	0.007	0.007	0.007



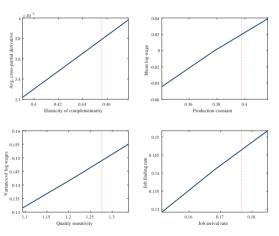


- Key untargeted moment (1): coworker sorting patterns
- Coworker correlation matches data well, $\rho_{\rm XX} = {\rm 0.53}$ (vs. 0.62 in the data)
- Model slightly underestimates the quality of coworkers at both bottom and top
 - OJS will help



Identification validation exercise 1





Notes. This figure plots the targeted moment against the relevant parameter, holding constant all other parameters.

Identification validation exercise 2



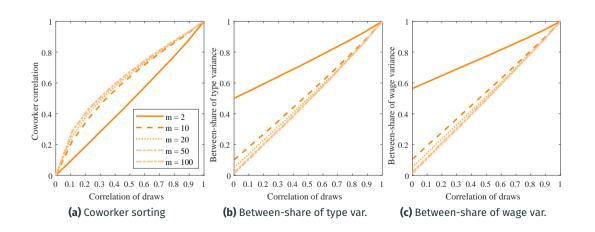
Notes. This figure plots the distance function $\mathcal{G}(\psi_i, \psi_{-i}^*)$ when varying a given parameter ψ_i around the estimated value ψ_i^* . The remaining parameters are allowed to adjust to minimize \mathcal{G} .

- **Problem.** For any degree of coworker sorting less than unity, i.e. $\rho_{XX} <$ 1, the level of the between-share in a model with team size m=2 will be biased upward relative to the case of m>2 and, in particular, $m\to\infty$ (LLN...)
 - o implication 1: upward bias in level
 - o implication 2: downward bias in estimated ↑ between-share as sorting increases
- Propose statistical adjustment method
- Consider a random vector $X = (X_1, X_2, \ldots, X_m)'$ whose distribution is described by a Gaussian copula over the unit hypercube $[0,1]^m$, with an $m \times m$ dimensional correlation matrix $\Sigma(\rho^c)$, which contains ones on the diagonal and the off-diagonal elements are all equal to ρ_c
- Interpretation. Each vector of observations drawn from the distributions of X, $x_i = (x_{1i}, x_{2i}, \dots, x_{mi})'$, describes the types of workers in team of size m, indexed by j

Between-share adjustment procedure (2)

- Since the marginals of the Gaussian copula are simply continuous uniforms defined over the unit interval, the variance of the union of all draws is just $\frac{1}{12}$
- The mean of the elements of X is itself a random variable, \bar{X} . That is, for some realization x_j , we can define $\bar{x}_j = \frac{1}{m} \sum_{i=1}^m x_{ij}$
- The variance of \bar{X} will be $\frac{1}{m^2}\left(\frac{m}{12}+m(m-1)(\frac{\rho_c}{12})\right)$
- So $\sigma_{\mathsf{x},\mathsf{between\text{-}share}}^2(\rho_\mathsf{c},m) = \frac{1}{m}\bigg(\mathsf{1} + (m-\mathsf{1})\rho_\mathsf{c}\bigg)$
- Correction-factor $=\frac{1}{2}\bigg(1+\rho_{\rm c}\bigg)-\frac{1}{\hat{m}}\bigg(1+(\hat{m}-1)\rho_{\rm c}\bigg)$ where the empirical average size is \hat{m}

Between-share adjustment procedure (3)



The effect of declining search frictions



- ↓ search frictions could also explain ↑ coworker sorting
- Job arrival & separation rates estimated to ↑ from p1 to p2
- Counterfactual analysis: explains 6% of model-implied ↑ in between-employer share of wage variance

	△ model	Implied % Δ model due to Δ parameter
Model 1: baseline	0.159	-
Cf. a: fix period-1 complementarity	0.065	59
Cf. b: fix period-1 search frictions	0.150	6

Outsourcing & within-occupation ranking analysis



- · Concern: confounding shifts in labor boundary of firm, e.g. outsourcing
- · Address this concern in multiple steps:
 - empirically rank workers within occupation ("good engineer vs. mediocre engineer")
 - ② empirically re-estimate coworker sorting & complementarity (lower but similar ↑)
 - 3 re-estimate model for both periods & re-do counterfactual exercises
- Result: qualitatively & quantitatively similar findings

	△ model	Implied % Δ model due to Δ parameter
Model 2: within-occ. ranking	0.198	-
Cf. a: fix period-1 comp.	0.076	61.47

Robustness: model with OJS - brief overview



- Baseline abstracted from job-to-job transitions but is main story robust when workers can switch to better job after accepting job out of unemployment?
 - $\circ~$ two opposing effects from increased complementarities
- Consider extension where also employed worker meet vacancies at Poisson rate λ_e
- Main findings
 - o better fit to empirical sorting patterns in cross-section



- contribution of ↑ complementarities to ↑ firm-level wage inequality slightly smaller, more attributed to ↑ labor market transitions
 - conservative estimates (endogenous search effort, forward-looking wage specification)
- Opens door to thinking about coworker complementarities and job ladders



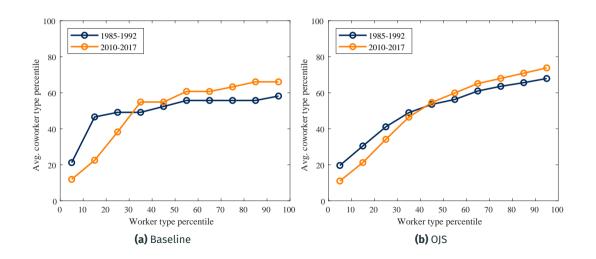
Extension: model with OJS



- Baseline model abstracted from OJS
 - o transparent trade-off, connection to analytical results
- Consider extension to OJS: employed worker meet vacancies at Poisson rate λ_e
 - wages both off and on the job are continuously renegotiated under Nash bargaining, with unemployment serving as the outside option [cf. di Addario et al., 2021]
 - $\circ~$ re-estimate, with empirical labor market flows disciplining λ_e
- Qualitative question: is coworker sorting outcome robust, even if workers can switch to better job after accepting job out of unemployment?
- Analyses:
 - coworker sorting patterns & changes
 - additional model validation: direction of EE flows in model & data

Model-implied coworker sorting patterns: without and with OJS







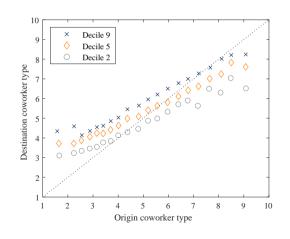
- Theoretical prediction: EE transitions move workers in surplus-maximizing direction $\Rightarrow \Delta \hat{x}_{-it} = \hat{x}_{-i,t} \hat{x}_{-i,t-1}$ should be positively correlated with \hat{x}_i
 - o $h_{2.1}(x, x''|x') = 1$ worker x in a two-worker firm with coworker x'' would move to an employer that currently has one employee of type x' if S(x|x') S(x|x'') > 0
- **Empirical analysis**: use SIEED *spell* data to create worker-originMonth-destinationMonth-originJob-destinationJob panel, with information on characteristics of origin and destination job
 - o subsample period 2008-2013 (huge panel at monthly frequency)
 - o count as "EE" if employer change between two adjacent months
- Regression analysis: regress $\Delta \hat{x}_{-it}$, scaled by std. σ_{Δ} of coworker quality changes, on *own* type and *origin* coworker type

$$\frac{\Delta \hat{\mathbf{x}}_{-it}}{\sigma_{\mathbf{A}}} = \beta_{\mathbf{O}} + \frac{\beta_{\mathbf{1}}}{\beta_{\mathbf{1}}} \hat{\mathbf{x}}_{i} + \beta_{\mathbf{2}} \hat{\mathbf{x}}_{-i,t-1} + \epsilon_{it}$$

Empirical coworker sorting changes due to EE moves



- EE transitions push toward greater coworker sorting: for any given origin, higher x-workers move to workplaces with better coworkers than lower-x workers do
- But in data EE transitions "move up" low types more than theory predicts
- "Coworker job ladder" with both absolute and type-specific dimension?
- **Next:** change in the job ladder [e.g., Haltiwanger-Spetzler, 2021]



Evidence that EE increasingly reallocate toward PAM: in data & model

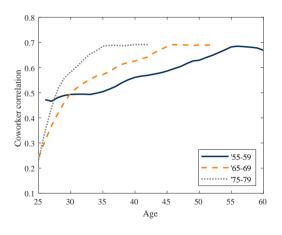
	Da	Model		
Change in coworker type	'85-'92	'10-'17	Period-1	Period-2
Own type	0.0883 *** (0.000799)	0.118 *** (0.000918)	0.214	0.270
Controls	Year FEs, Origin	Year FEs, Origin	Origin	Origin
N	196,098	282,718	∞	∞
adj. R²	0.284	0.204		

Table 1: Change in coworker type due to EE moves positively related to own type – increasingly so

Notes. For the data columns, individual-level clustered standard errors are given in parentheses. Model counterparts are computed simulation-free in population. Dependent variable is scaled throughout by the standard deviation of the change in coworker type.

Related: life-cycle patterns of sorting consistent with cohort effects

- Coworker sorting increases over life-cycle
- Coworker sorting higher in recent cohorts
 - consistent with each cohort becoming more specialized
 - but also with improvement in search frictions over time, which primarily affects sorting of young people
- Currently don't have life-cycle effects in my model, but could be incorporated...

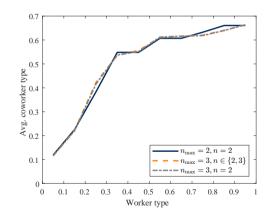


Notes. Figure displays the correlation of own type with average coworker type, by age, for three separate cohorts.

Extension to $n_{\text{max}=3}$

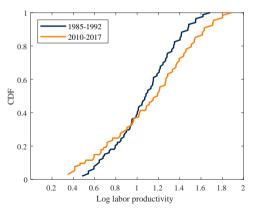


- Baseline model imposes $n_{\rm max}=2$ for reasons of (i) tractability and (ii) transparency
- Can extend to n_{max} = 3 (or n_{max} = 4) & find that results are robust





• Firm dynamics literature: increased firm-level productivity dispersion [Autor et al., 2020; de Ridder, 2023]

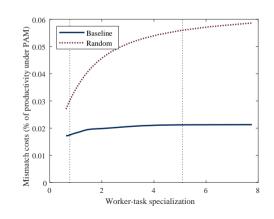






"The benefits of the division of labor are limited by the functioning of the labor market"

- Microfoundation: $\uparrow \chi \Rightarrow \uparrow$ efficiency benefit from teamwork but also \uparrow mismatch costs
- Q: how does the gap to potential vary depending on labor market structure?
- A: under random sorting, productivity gap due to misallocation \uparrow more sharply as $\chi\uparrow$
- Outside model: severe labor mkt frictions (e.g., dev'ing countries [Donovan et al., 2023]) may inhibit specialization [cf. Atencio et al.,



Implications for overall inequality?



- Coworker complementarities do not necessarily ↑ variance of person-level wages
 - (un-)surprising? Varriance decomposition perspective vs. common intuition [Kremer, 1993]
 - o (i) **reallocation effect**, (ii) valuation effect, (iii) outside option effect
- Several mechanisms though through which \uparrow sorting could \uparrow person-level inequality
 - 1 regulation or norms that lead to within-firm wage compression [Akerlof-Yellen, 1990]
 - 2 coworker learning [Jarosch et al., 2021; HLMP, 2023]
 - 3 increasing returns to labor quality [Kremer, 1993]

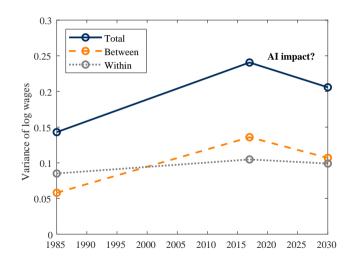
Implications for AI impact on labor markets (1): overview



- Literature moving toward richer way of thinking about tech. change. Here: shifts in across-worker productivity differences and in specialization/interdependence
- Example: AI early/conjectural evidence on impact of LLMs etc
 - o absolute adv. less important ("leveller") [e.g., Brynjolfsson et al., 2023]
 - o comparative adv. less important (e.g., can interpret medical imaging w/o radiologist)
- Illustrative model counterfactual: relative to the 2010s
 - everyone's productivity ↑ by equivalent to 20% of lowest type's productivity so in proportional terms, lower-x benefit more
 - 2 coworker complementarity ↓ by 20%

Implications for AI impact on labor markets (2): illustrative exercise

- Model prediction: Al could lead to reversal of historical trends $\sigma_{\rm W}^2\downarrow$, $\sigma_{\rm W}^2\downarrow$, $\rho_{\rm XX}\downarrow$ along side a productivity boom
 - o driven by ↓ firm-level wage inequality



Implications for AI impact on labor markets (3): conjectures



- Literature moving toward richer way of thinking about tech. change. Here: shifts in across-worker productivity differences and in specialization/interdependence
- Example: AI early/conjectural evidence on impact of LLMs etc
 - o absolute adv. less important? ("leveller") [e.g., Brynjolfsson et al., 2023]
 - o comparative adv. less important? (e.g., can interpret medical imaging w/o radiologist)
- Illustrative model counterfactual: AI could lead to reversal of historical trends...
- ...and perhaps also...
 - $oldsymbol{1}$...**flatter organizations**, with managerial span of control \uparrow
 - ② ...↓ barriers to entry for self-employment/start-ups
 - 3 ...easier job transitions & shorter training durations

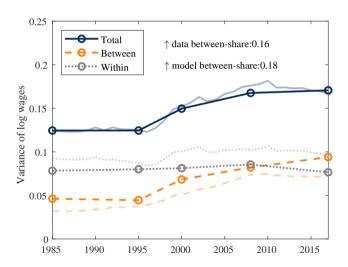
Within-industry calibration: overview



- · Baseline: calibration and evaluation based on economy-wide moments
- But the model does not incorporate between-industry differences in, e.g., production technology
- Alternative considered here: target $\hat{\beta}_c$ and σ_w^2 computed as within-industry average, evaluate against within-industry trends
 - keep other targets (e.g., job separation) as before

Within-industry calibration: model fit & counterfactual

 Counterfactual: χ↑ explains 83% of model-implied↑in between-share



Evolution of the German task structure



- Employment Surveys (ES) carried out by the German Federal Institute for Vocational Training (BIBB)
 - o detailed information on tasks performed at work
 - o individual-level, with consistent occupation codes
 - o repeated cross-sections ranging from 1985/86 to 2018
 - large sample sizes (20,000-30,000 per wave)
- Methodology to study evolution of task content of production follows Spitz-Oener (2006), Antonczyk et al. (2009), Rohrbach-Schmidt & Tiemann (2013)
 - task classification
 - o sample harmonization (West Germany, aged 15 to 65, employed)

Task classification

 Focus on Δ in usage of abstract/complex (non-routine, non-manual) tasks vs. "rest" (manual & routine)

[Autor and Handel, 2009; Acemoglu & Autor, 2011; Rohrbach-Schmidt & Tiemann, 2013]

• Index of complex tasks for worker *i* in period *t* [Antonczyk et al., 2009]

 $T_{it}^{ ext{complex}} = rac{ ext{number of activities performed by } i ext{ in task category "complex" in sample year } t}{ ext{total number of activities performed by } i ext{ in sample year } t}$

Task classification	Task name	Description
Complex	investigating	gathering information, investigating, documenting
	organizing	organizing, making plans, working out operations, decision making
	researching	researching, evaluating, developing, constructing
	programming	working with computers, programming
	teaching	teaching, training, educating
	consulting	consulting, advising
	promoting	promoting, consulting, advising
Other	repairing, buying, accommodat-	
	ing, caring, cleaning, protect-	
	ing, measuring, operating, man-	
	ufacturing, storing, writing, cal-	
	culating	

Increase in aggregate task complexity, driven by within-occupation ↑

- Aggregate task intensity & decompose period-by-period change into:
 - $oldsymbol{0}$ between component: Δ occupational employment shares
 - $\mathbf{2}$ within component: Δ task content within occupations

	Total	Between	Within	Within-share
1986 level	0.252			
1986-1992	0.025	0.002	0.022	0.906
1992-2006	0.298	0.057	0.241	0.809
2006-2012	0.019	0.002	0.017	0.890
2012-2018	0.053	0.028	0.025	0.476
Total change	0.395	0.089	0.306	0.775

Notes. Decompose changes in the usage of abstract tasks between periods t and t - 1 according to $\Delta \bar{t}_t^{abstract} = \sum_0 \omega_{0,t-1} (\bar{t}_{t,0}^{abstract} - \bar{t}_{t-1,0}^{abstract}) + \sum_0 (\omega_{0,t} - \omega_{0,t-1}) \bar{t}_{t,0}^{abstract}$ where $\bar{t}_{t,0}^{abstract}$ measures the average usage of abstract tasks by members of occupation o in period t and $\omega_{0,t}$ is the period- t employment share of occupation.

Large variation in task complexity across occupations

Aggregate individual responses to 2-d occupation level, using 2012 & 2018 waves
 2012 & 2018: ← ISCO-08 codes available

Occupation	$\bar{T}_o^{\text{complex}}$
Business and administration professionals	0.859
Legal, social and cultural professionals	0.830
Business and administration associate professionals	0.827
Administrative and commercial managers	0.820
Teaching professionals	0.807
Drivers and mobile plant operators	0.214
Agricultural, forestry and fishery labourers	0.193
Market-oriented skilled forestry, fishery and hunting workers	0.168
Food preparation assistants	0.131
Cleaners and helpers	0.124





• Direct measures of cognitive and non-cognitive skills across Swedish firms during 1986–2008, using test data from military enlistment

