

University of Dundee

# Spatial self-organisation enables species coexistence in patterned ecosystems

Spatial Ecology Workshop - University of Sheffield

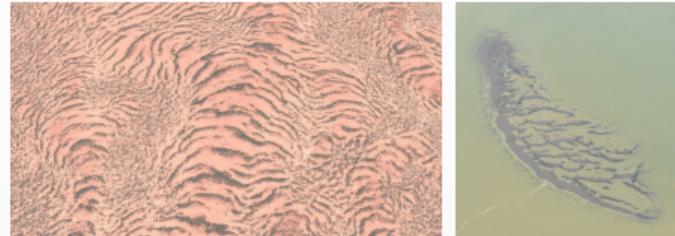
19/04/2022

*Lukas Eigentler*

# Patterned ecosystems

- Scale dependent feedback loops cause pattern formation in ecological systems.
- Local facilitation: e.g. increased water infiltration in vegetated areas, ...
- Long-range competition: e.g. competition for a limiting resource.
- Self-organisation into colonised and uncolonised areas is typically associated with high environmental stress.
- Unidirectional resource flux leads to stripe patterns.

Vegetation pattern & mussel beds.



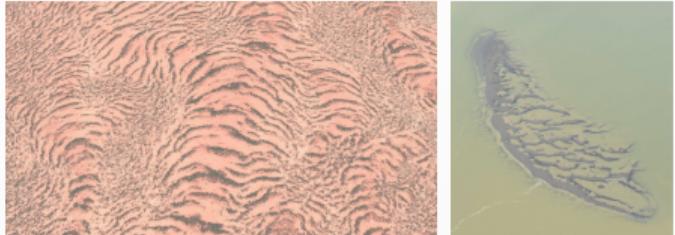
Ribbon forest



# Patterned ecosystems

- Coexistence typically occurs despite competition for a single limiting resource.
- Coexistence occurs on the scale of a single stripe (i.e. no spatial segregation).
- What mechanisms cause coexistence?

Vegetation pattern & mussel beds.



Ribbon forest



# Klausmeier model

One of the most basic phenomenological models is the **extended Klausmeier reaction-advection-diffusion model**.<sup>1</sup>

$$\frac{\partial u}{\partial t} = \underbrace{u^2 w \left(1 - \frac{u}{k}\right)}_{\text{consumer growth}} - \underbrace{Bu}_{\text{consumer death}} + \underbrace{\frac{\partial^2 u}{\partial x^2}}_{\text{consumer dispersal}},$$
$$\frac{\partial w}{\partial t} = \underbrace{A}_{\text{resource input}} - \underbrace{w}_{\text{natural resource depletion}} - \underbrace{u^2 w}_{\text{resource consumption by consumers}} + \underbrace{\nu \frac{\partial w}{\partial x}}_{\text{unidirectional resource flux}} + \underbrace{d \frac{\partial^2 w}{\partial x^2}}_{\text{resource diffusion}}.$$

The model describes interactions between the limiting resource and **a single consumer species**.

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<sup>1</sup>Klausmeier, C. A.: *Science* 284.5421 (1999).

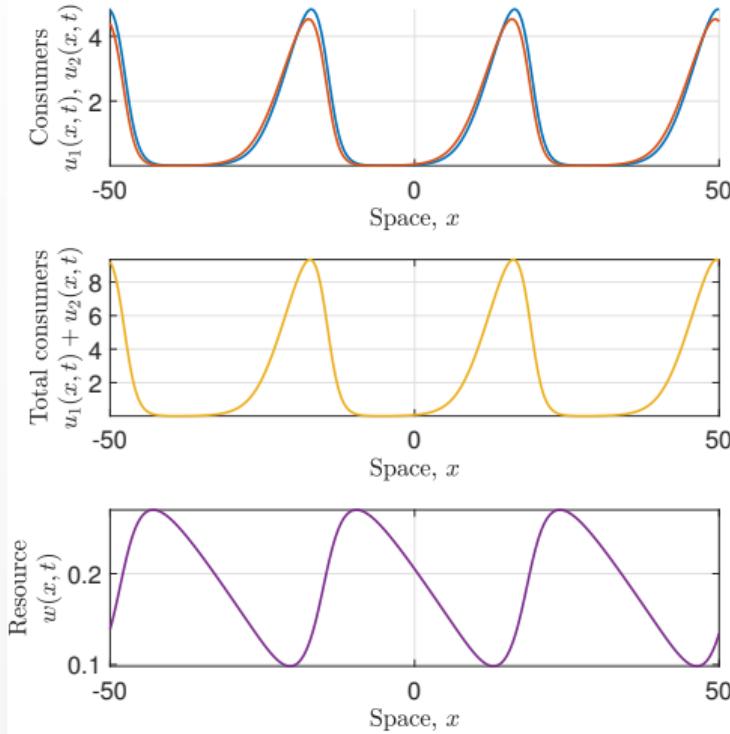
# Multispecies Model

Multispecies model:

$$\begin{aligned}\frac{\partial u_1}{\partial t} &= \underbrace{wu_1(u_1 + Hu_2)\left(1 - \frac{u_1}{k_1}\right)}_{\text{consumer growth}} - \underbrace{B_1 u_1}_{\text{consumer mortality}} \\ &\quad + \underbrace{\frac{\partial^2 u_1}{\partial x^2}}_{\text{consumer dispersal}}, \\ \frac{\partial u_2}{\partial t} &= \underbrace{Fwu_2(u_1 + Hu_2)\left(1 - \frac{u_2}{k_2}\right)}_{\text{consumer growth}} - \underbrace{B_2 u_2}_{\text{consumer mortality}} \\ &\quad + \underbrace{D \frac{\partial^2 u_2}{\partial x^2}}_{\text{consumer dispersal}}, \\ \frac{\partial w}{\partial t} &= \underbrace{A}_{\text{resource input}} - \underbrace{w}_{\text{natural resource depletion}} \\ &\quad - \underbrace{w(u_1 + u_2)(u_1 + Hu_2)}_{\text{resource consumption by consumer}} + \underbrace{\nu \frac{\partial w}{\partial x}}_{\text{unidirectional resource flux}} + \underbrace{d \frac{\partial^2 w}{\partial x^2}}_{\text{resource diffusion}}.\end{aligned}$$

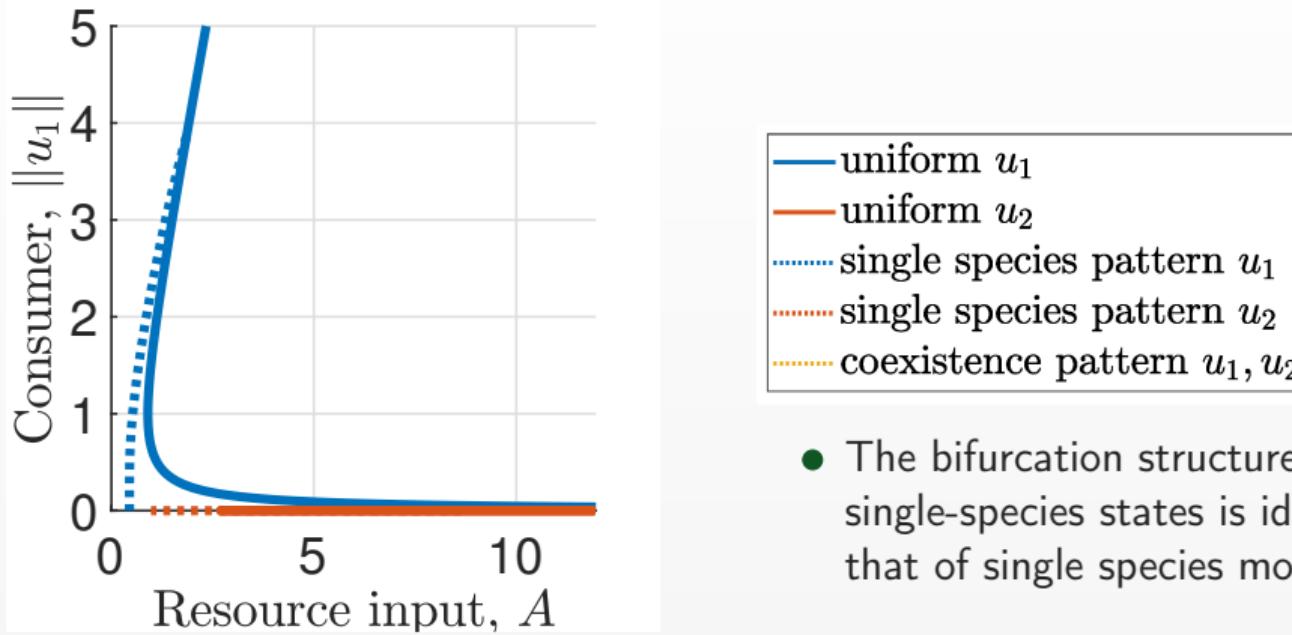
Species only differ quantitatively (i.e. in parameter values) but not qualitatively (i.e. same functional responses). Assume  $u_1$  is superior coloniser;  $u_2$  is locally superior.

# Simulations



- Consumer species coexist in a spatially patterned solution.
- Coexistence requires a balance between species' local average fitness and their colonisation abilities.
- Solutions are periodic travelling waves and move in the direction opposite to the unidirectional resource flux.

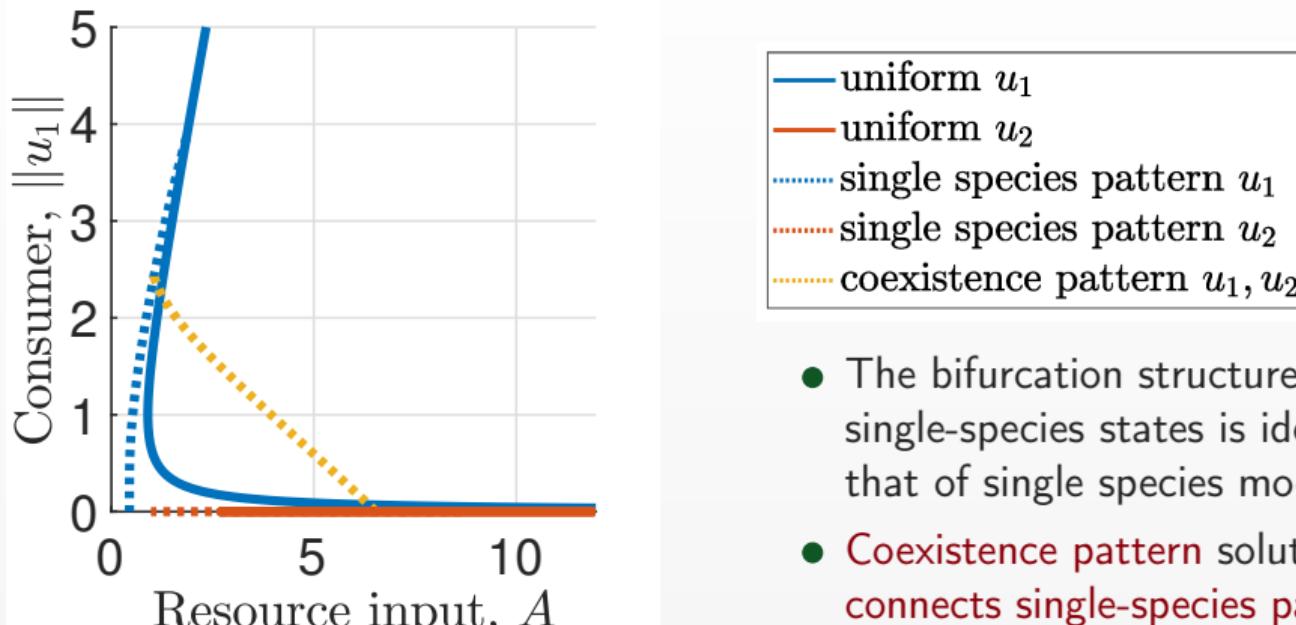
# Bifurcation diagram



- The bifurcation structure of single-species states is identical with that of single species model.

Bifurcation diagram: one wavespeed only

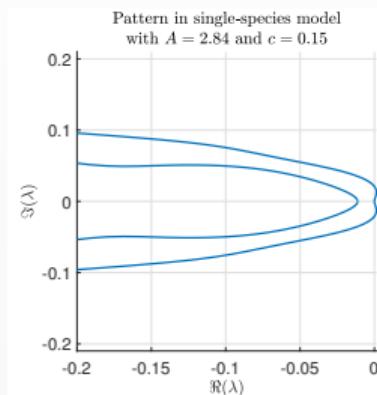
# Bifurcation diagram



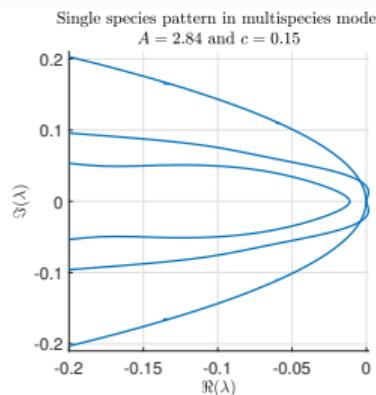
Bifurcation diagram: one wavespeed only

- The bifurcation structure of single-species states is identical with that of single species model.
- **Coexistence pattern** solution branch connects single-species pattern solution branches.

# Pattern onset



Essential spectrum in  
single-species model

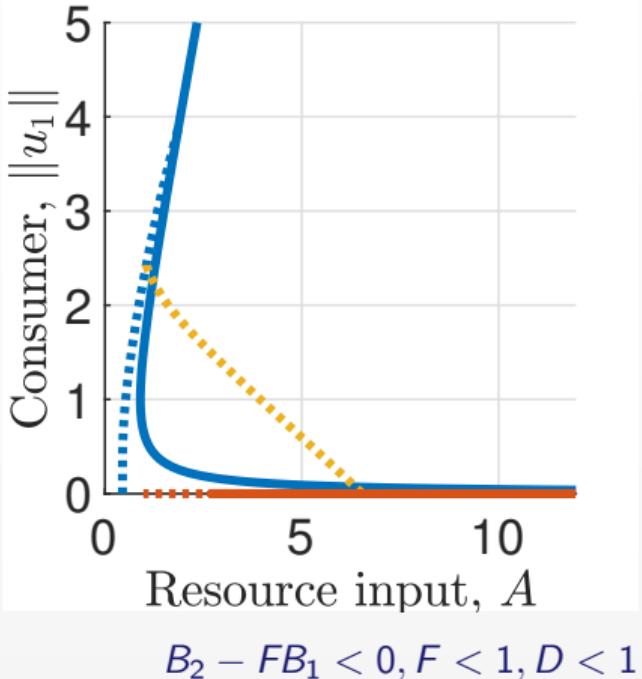


Essential spectrum in  
multispecies model

- The key to understand **coexistence pattern onset** is knowledge of **single-species pattern's stability**.
- Tool: **essential spectra** of periodic travelling waves, calculated using the numerical continuation method by Rademacher et al.<sup>2</sup>
- Pattern onset occurs as the single-species pattern loses/gains stability to the introduction of a competitor.

<sup>2</sup>Rademacher, J. D., Sandstede, B. and Scheel, A.: *Physica D* 229.2 (2007)

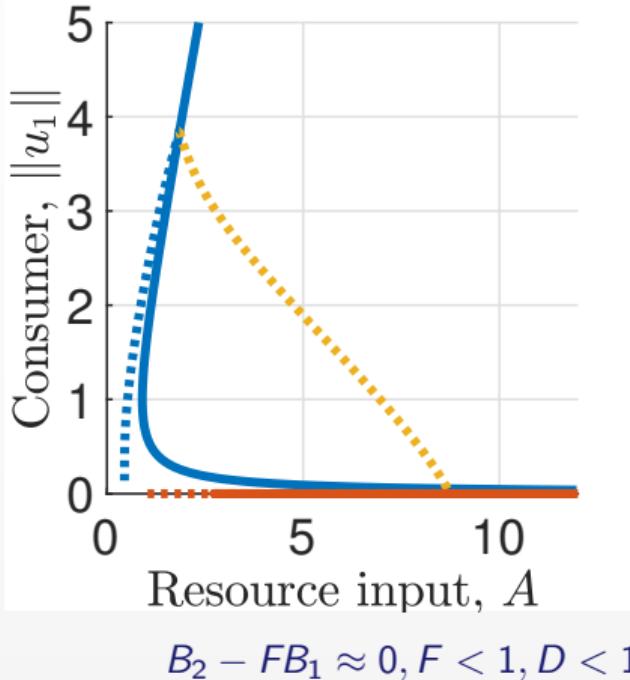
# Pattern existence



- uniform  $u_1$
- uniform  $u_2$
- single species pattern  $u_1$
- single species pattern  $u_2$
- coexistence pattern  $u_1, u_2$

- Key quantity: Local average fitness difference  $B_2 - FB_1$  determines stability of single-species states in spatially uniform setting.
- Condition for pattern existence: Balance between local competitive and colonisation abilities.

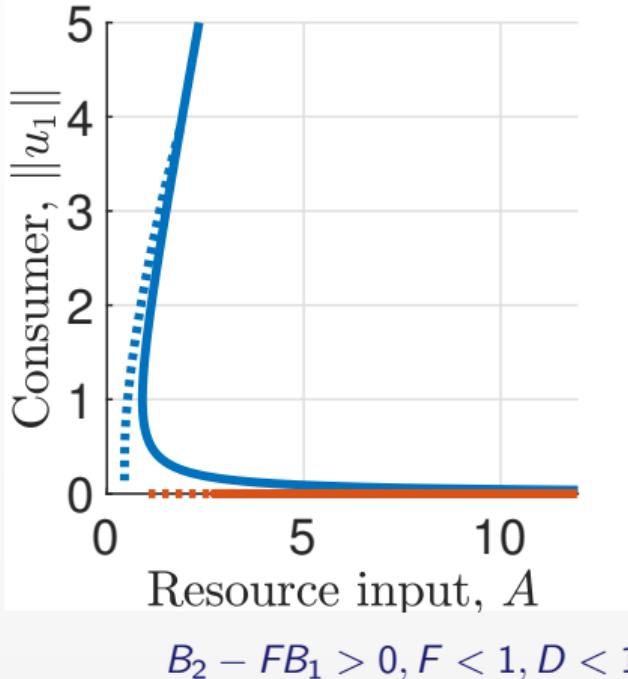
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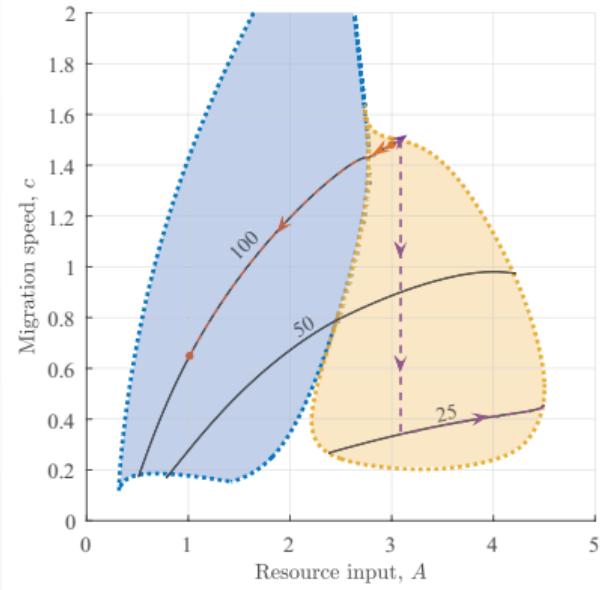
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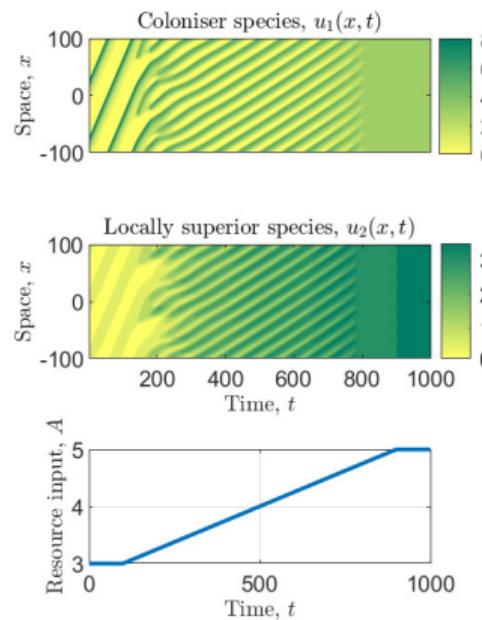
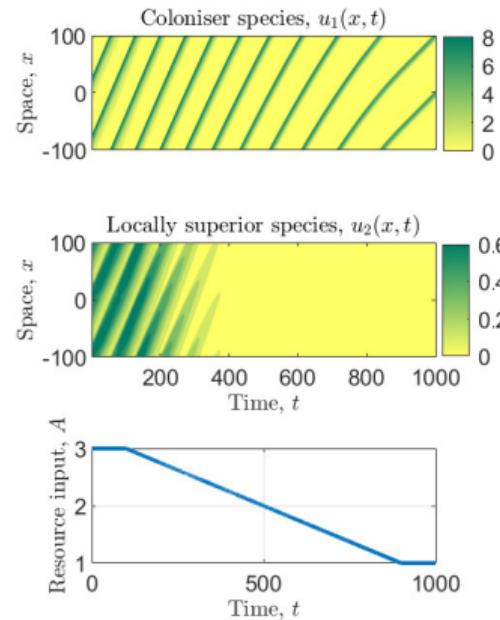
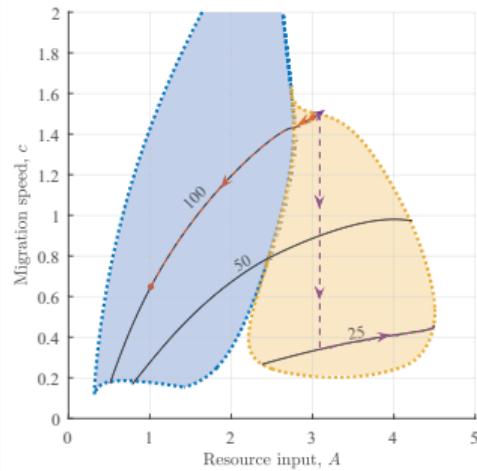
# Pattern stability and hysteresis



Stability regions of system states.

- For decreasing resource input, coexistence state loses stability to single-species pattern of coloniser species.
- State transitions are affected by **hysteresis**.
- Extinction can occur despite a coexistence state being stable.
- **Ecosystem resilience depends on both current and past states of the system.**

# Hysteresis



# Conclusions

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- Spatial self-organisation is a coexistence mechanism.
- Coexistence is enabled by spatial heterogeneities in the resource, caused by the consumers' self-organisation into patterns.
- A balance between species' colonisation abilities and local competitiveness promotes coexistence.

# Empirical testing

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- Limited field data exist due to long time scales and large spatial scales.
- Vegetation stripes move in direction opposite to resource flux.
- BUT no evidence of hysteresis, extinction events, necessary conditions for coexistence, ...
- Perhaps other ecosystems - with faster timescales and shorter length scales - can be used?

# References

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Slides are available on my website.

<https://lukaseigentler.github.io>

- [1] Eigentler, L.: 'Species coexistence in resource-limited patterned ecosystems is facilitated by the interplay of spatial self-organisation and intraspecific competition'. *Oikos* 130.4 (2021), pp. 609–623.
- [2] Eigentler, L.: 'Intraspecific competition in models for vegetation patterns: decrease in resilience to aridity and facilitation of species coexistence'. *Ecol. Complexity* 42 (2020), p. 100835.
- [3] Eigentler, L. and Sherratt, J. A.: 'Spatial self-organisation enables species coexistence in a model for savanna ecosystems'. *J. Theor. Biol.* 487 (2020), p. 110122.