Ústav fyziky a technologií plazmatu Přírodovědecké fakulty Masarykovy univerzity

FYZIKÁLNÍ PRAKTIKUM

Fyzikální praktikum 3

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Úloha č. 8: Band gap width

1. Introduction

An important characteristic of semiconductors is the band gap, influencing their electrical conductivity and optical properties. Our aim is to determine the band gap energy (E_g) of silicon and germanium using the inner photoelectric effect.

2. Theory

Electrons bound to atoms can only exist at some discrete set of energy levels and to move around, they have to absorb or emit energy to keep it conserved. Both emission and absorption can happen via light, which is also discretized with photon particles. Each has an associated wavelength λ and it's energy is given by

$$E = \frac{hc}{\lambda} \tag{1}$$

Semiconductors are special in that they have a certain energy gap E_g of banned states between it's electrons in the valance band and the conductive band. If we create a PN junction of these atoms and shine monochromatic light at it with increasing frequency, there comes a point where the photon energy exceeds the band gap E_g . At this threshold, electrons jump to the conduction band, get carried by the junction's voltage, and a measurable voltage begins to build up.

3. Measurement procedure

The scheme of the experiment can be found in Figure 1. We have a source of white light shining into a monochromator, which is then directed onto the diode which has a connected voltmeter. To find the band gap energy E_g , all we need to do is find the largest wavelength λ_{max} , where the voltage starts to build up and plug into equation (1), to get

$$E_g = \frac{hc}{\lambda_{max}} \tag{2}$$

We will then also proceed to measure the induced voltage for the whole spectrum. To do this, we also have to account for the fact, that our halogen lamp does not shine light with the same intensity at each wavelength. To correct for this, we have a table of values of relative intensity $D(\lambda)$ emitted by lamp, and we will correct with

$$S(\lambda) = \frac{U(\lambda)}{D(\lambda)} \tag{3}$$

As the last step, we will express each wavelength λ as energy of the photon E and plot the calculated function S(E).

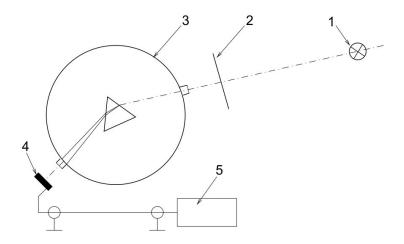


Figure 1: Scheme of the experiment: 1 - Halogen lamp, 2 - Convex lens, 3 - Monochromator, 4 - Semiconductor photodiode, 5 - Voltmetr

4. Results

We've measured one germanium diode and one made from silicon. The resulting voltages, as functions of wavelength, are presented in Table 1 and 2 and illustrated in Graphs 1 and 2. From these graphs, we can directly determine the maximum wavelengths λ_{max} and calculate the corresponding energy gaps using Equation (2).

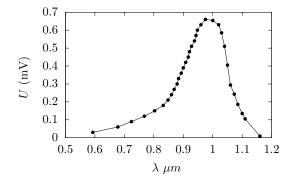
	$\lambda_{max} \text{ (nm)}$	$E_g \text{ (eV)}$
silicon	1160	1.069
germanium	1930	0.642

λ (nm)	$U_m \text{ (mV)}$	E (eV)	$S \cdot 10^6$	λ (nm)	$U_m \text{ (mV)}$	E (eV)	$S \cdot 10^6$	λ (nm)	$U_m \text{ (mV)}$	E (eV)	$S \cdot 10^6$
0.792	0.03	1.56	0.14	1.154	0.58	1.07	4.27	1.525	0.46	0.81	4.45
0.853	0.06	1.45	0.31	1.160	0.57	1.06	4.24	1.550	0.42	0.79	4.19
0.879	0.09	1.41	0.49	1.175	0.57	1.05	4.27	1.575	0.42	0.78	4.31
0.899	0.12	1.37	0.67	1.200	0.62	1.03	4.69	1.600	0.36	0.77	3.90
0.914	0.15	1.35	0.86	1.225	0.67	1.01	5.19	1.625	0.33	0.76	3.70
0.925	0.18	1.34	1.05	1.250	0.72	0.99	5.70	1.650	0.32	0.75	3.75
0.942	0.21	1.31	1.25	1.275	0.74	0.97	5.88	1.675	0.27	0.74	3.37
0.960	0.24	1.29	1.46	1.300	0.77	0.95	6.22	1.680	0.24	0.73	3.04
0.975	0.27	1.27	1.67	1.325	0.78	0.93	6.44	1.700	0.20	0.72	2.68
0.985	0.30	1.25	1.88	1.350	0.75	0.91	6.29	1.725	0.21	0.71	3.04
1.000	0.33	1.23	2.11	1.362	0.69	0.91	5.83	1.750	0.17	0.70	2.62
1.015	0.36	1.22	2.34	1.375	0.66	0.90	5.63	1.775	0.20	0.69	3.62
1.030	0.39	1.20	2.57	1.400	0.63	0.88	5.49	1.800	0.19	0.68	3.79
1.045	0.42	1.18	2.81	1.425	0.70	0.87	6.15	1.825	0.15	0.67	3.64
1.061	0.45	1.16	3.06	1.450	0.75	0.85	6.76	1.850	0.10	0.67	2.93
1.075	0.48	1.15	3.31	1.475	0.72	0.84	6.63	1.875	0.08	0.66	3.17
1.092	0.51	1.13	3.57	1.485	0.66	0.83	6.14	1.900	0.05	0.65	3.89
1.107	0.54	1.11	3.83	1.500	0.60	0.82	5.69	1.930	0.01	0.64	7.35
1.130	0.57	1.09	4.12	1.515	0.54	0.81	5.18				

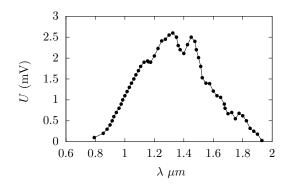
Table 1: Measured spectral photovoltage dependence of germanium diode.

λ (nm)	$U_m \text{ (mV)}$	E (eV)	$S \cdot 10^6$	λ (nm)	$U_m \text{ (mV)}$	E (eV)	$S \cdot 10^6$
0.593	0.03	2.09	0.64	0.938	0.54	1.32	3.05
0.678	0.06	1.82	0.16	0.943	0.57	1.31	3.25
0.724	0.09	1.71	0.29	0.948	0.60	1.30	3.45
0.768	0.12	1.61	0.44	0.960	0.63	1.29	3.71
0.803	0.15	1.54	0.61	0.975	0.66	1.27	3.99
0.832	0.18	1.49	0.79	1.000	0.65	1.23	4.12
0.848	0.21	1.46	0.96	1.020	0.63	1.21	4.09
0.860	0.24	1.44	1.13	1.030	0.59	1.20	3.86
0.869	0.27	1.42	1.30	1.040	0.51	1.19	3.41
0.879	0.30	1.41	1.48	1.050	0.41	1.18	2.74
0.884	0.33	1.40	1.65	1.060	0.29	1.16	2.01
0.893	0.36	1.38	1.84	1.073	0.24	1.15	1.69
0.900	0.39	1.37	2.03	1.085	0.19	1.14	1.31
0.908	0.42	1.36	2.22	1.100	0.14	1.12	0.96
0.917	0.45	1.35	2.43	1.110	0.11	1.11	0.75
0.921	0.48	1.34	2.61	1.160	0.01	1.06	0.06
0.928	0.51	1.33	2.82				

Table 2: Measured spectral photovoltage dependence of silicon diode.



Graph 1: Spectral photovoltage dependence for silicon diode

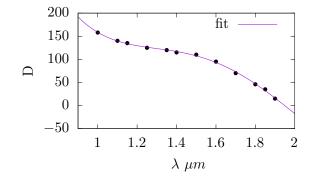


Graph 2: Spectral photovoltage dependence for germanium diode

To also get the correct relative intensities of induced voltage, we need to divide by the relative intensity of light emitted by our lamp. The measured relative intensities can be seen in Table 3 and for the rest we will interpolate by a polynomial fit.

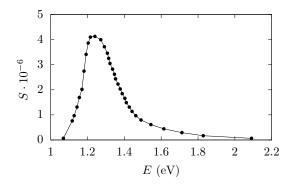
λ (nm)	D	$\lambda \text{ (nm)}$	D
1000	158	1500	110
1100	140	1600	95
1150	135	1700	70
1250	125	1800	46
1350	120	1850	35
1400	115	1900	15

Table 3: Relative intensities of light emitted by our lamp

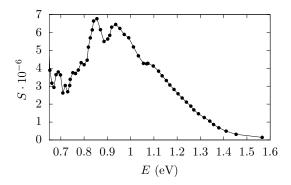


Graph 3: Fit of relative intensities from Table 3

Unfortunately, our data points don't go all the way to the smallest measured wavelengths of $0.6 \ \mu m$. It is not a big problem though, since we are mainly interested in the peaks. Using equation (3) we get the following graphs



Graph 4: Spectral dependence of photon energy for silicon diode



Graph 5: Spectral dependence of photon energy for germanium diode

5. Conclusion

We've measured the spectral dependence of photovoltage induced by a monochromatic beam of light on PN junctions of a germanium and silicon diode which is shown in Graphs 1 and 2. A measured voltage was only seen from the wavelength $\lambda=1160$ nm for silicon and $\lambda=1930$ nm, from which we conclude that the corresponding band gap energies are $E_g=1.069$ eV and $E_g=0.642$ eV respectively. Table values give $E_g=1.12$ eV and E=0.67 eV, which is not a bad result. The slight differences are likely due to measurement inaccuracies on my part.

Our measured voltages were not completely to scale since the source of light did not emit light at even intensities. We've adjusted for this difference using measured relative intensity of the halogen lamp and plotted the corrected Graphs 4 and 5. It can be seen, that both follow a similar shape of one peek, but in the case of germanium there are significant dips at specific wavelengths. It seems like there are other ways of absorbing the photons which only come to effect at those specific wave lengths and reduce the induced voltage.

References

[1] Task instructions https://is.muni.cz/auth/el/sci/jaro2025/F4210/um/fp3-8_sirka_pasu.pdf.