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Statistical Characterisation of Porous Media at the Pore Scale

Parametric Models

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Presentation Outline

- Plane Surface
- Regular Bundle of Tubes
- Regular Bundle of Tubes – High Mesh Res.
- Random Bundle of Tubes
- Array of Spheres
- Array of Ellipsoids

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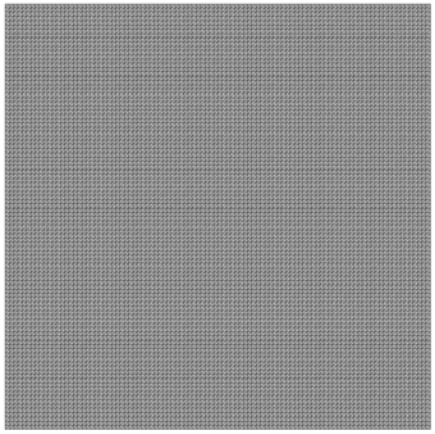
Plane Surfaces

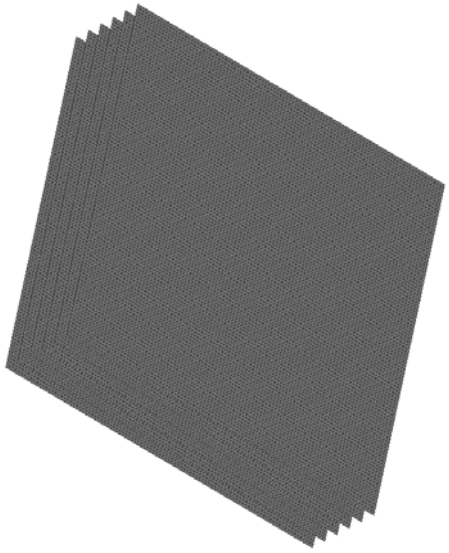
X-Y View



Y-Z View

X-Z View

3D View



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Minkowski Tensors – Plane Surface

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 0.0 & 0 & 0 \\ 0 & 0.0 & 0 \\ 0 & 0 & 2400. \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{0.0 \quad 0.0 \quad 2400.\}$	$\beta_1^{0,2} = not\ def.$
$W_2^{0,2} = \begin{bmatrix} 0.0 & 0 & 0 \\ 0 & 0.0 & 0 \\ 0 & 0 & 0.0 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{0.0 \quad 0.0 \quad 0.0\}$	$\beta_2^{0,2} = not\ def.$

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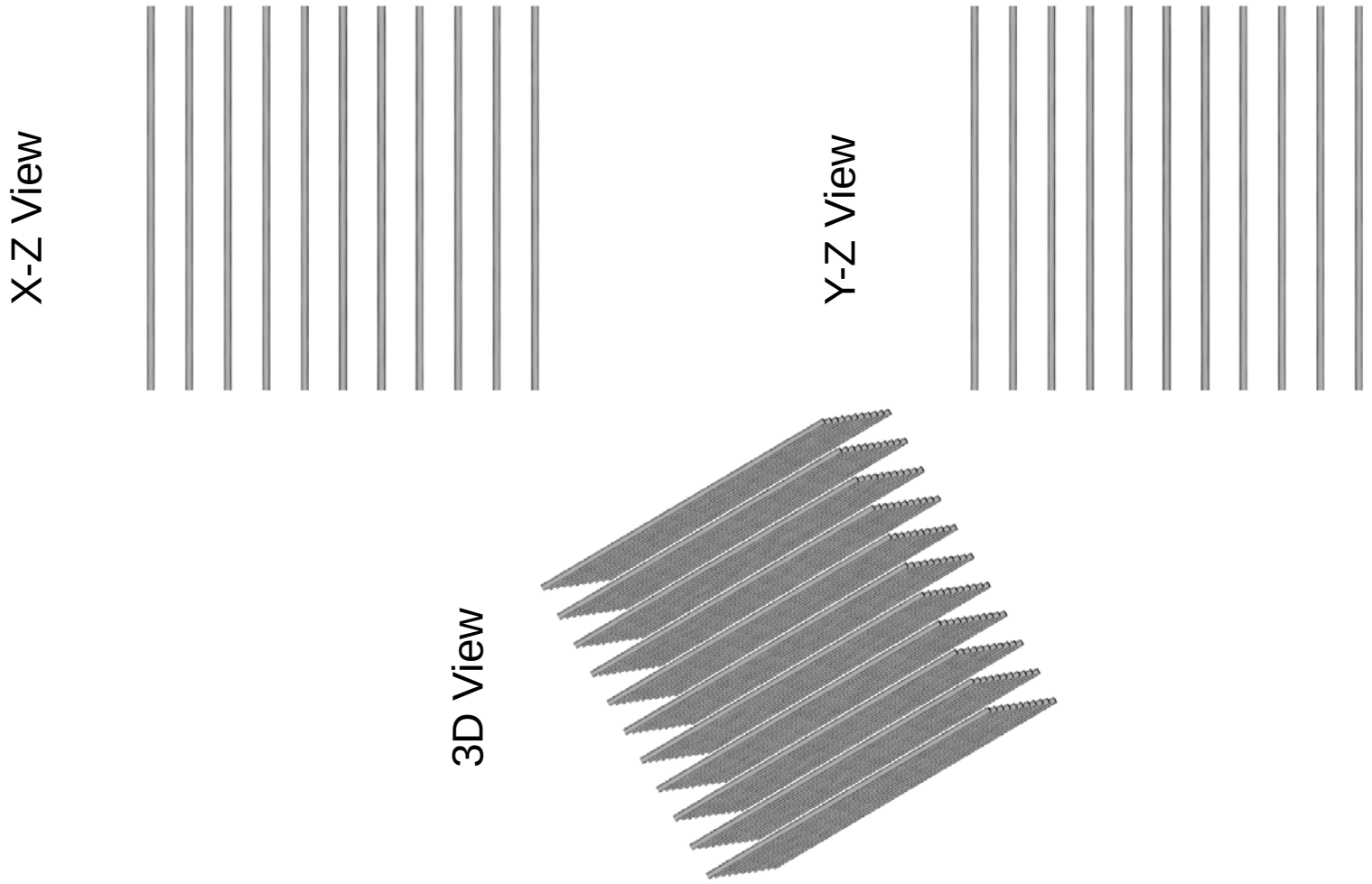
Regular Bundle of Tubes



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Minkowski Tensors – Regular Bundle of Tubes

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 12605 & 0 & 0 \\ 0 & 12605 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{12605 \quad 12605 \quad 0\}$	$\beta_1^{0,2} = not\ def.$
$W_2^{0,2} = \begin{bmatrix} 5960 & 1 & 0 \\ 1 & 6334 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{5960 \quad 6334 \quad 0\}$	$\beta_2^{0,2} = not\ def.$

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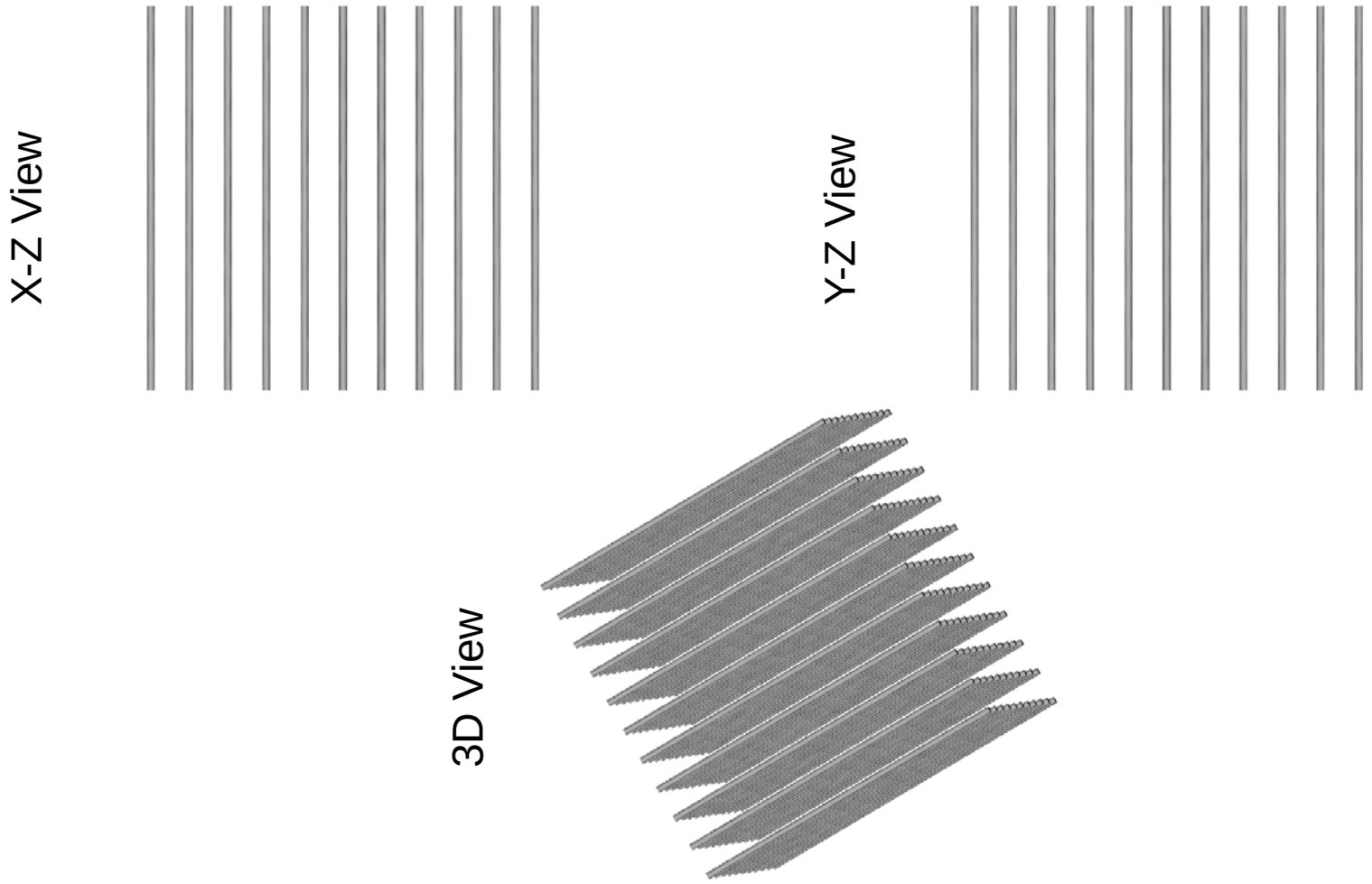
Regular Bundle of Tubes – High Mesh Resolution



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Minkowski Tensors – Regular Bundle – High Mesh Res.

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 12605 & 0 & 0 \\ 0 & 12605 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{12605 \quad 12605 \quad 0\}$	$\beta_1^{0,2} = not\ def.$
$W_2^{0,2} = \begin{bmatrix} 5960 & 0 & 0 \\ 0 & 6334 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{5960 \quad 6334 \quad 0\}$	$\beta_2^{0,2} = not\ def.$

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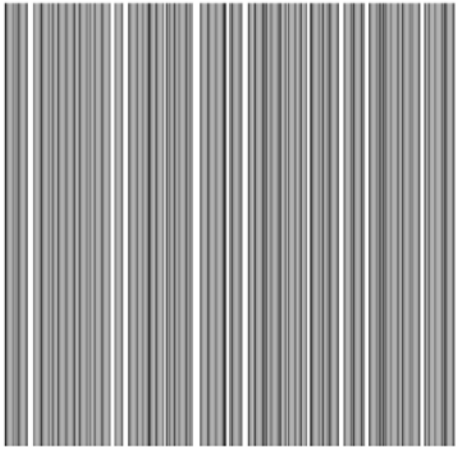
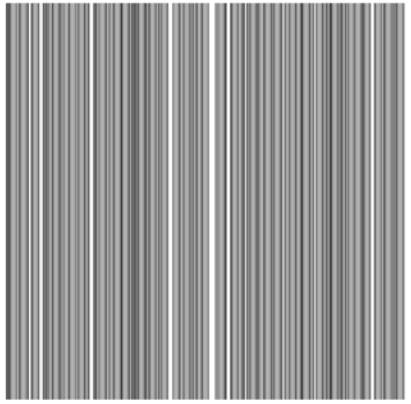
Random Bundle of Tubes

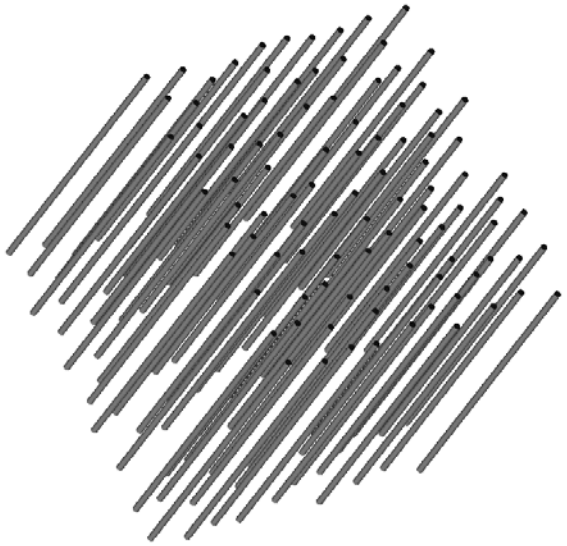
X-Z View



Y-Z View



3D View



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Minkowski Tensors – Random Bundle of Tubes

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 12605 & 0 & 0 \\ 0 & 12605 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{12605 \quad 12605 \quad 0\}$	$\beta_1^{0,2} = not\ def.$
$W_2^{0,2} = \begin{bmatrix} 5960 & 0 & 0 \\ 0 & 6334 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{5960 \quad 6334 \quad 0\}$	$\beta_2^{0,2} = not\ def.$

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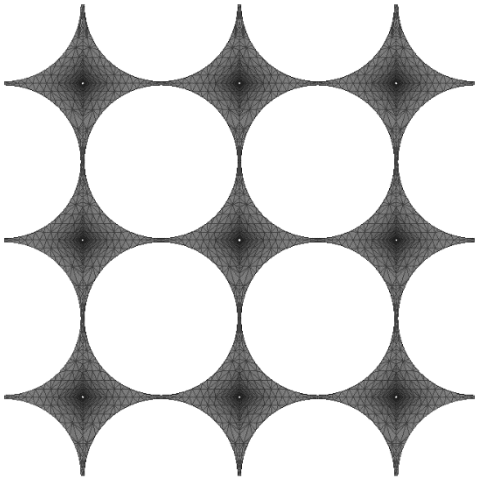
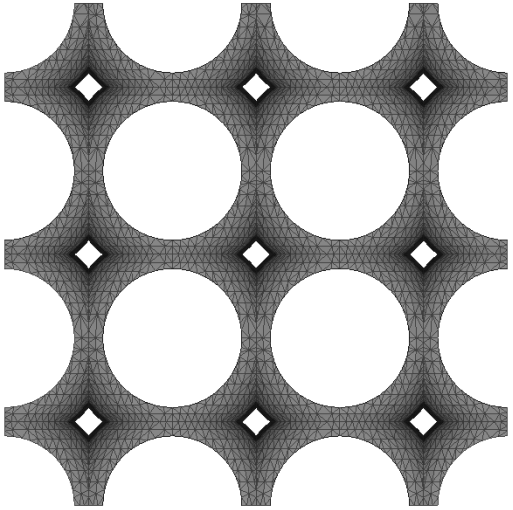
Symmetric Parametric Pore

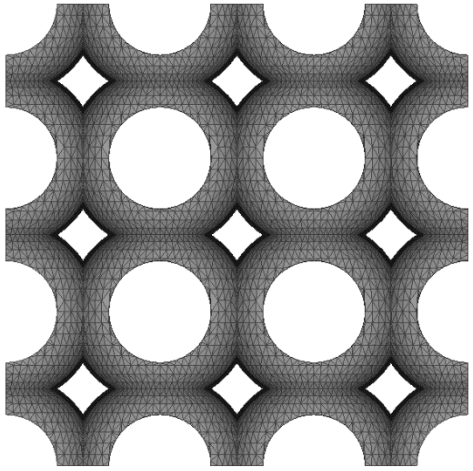
Radius 1.4



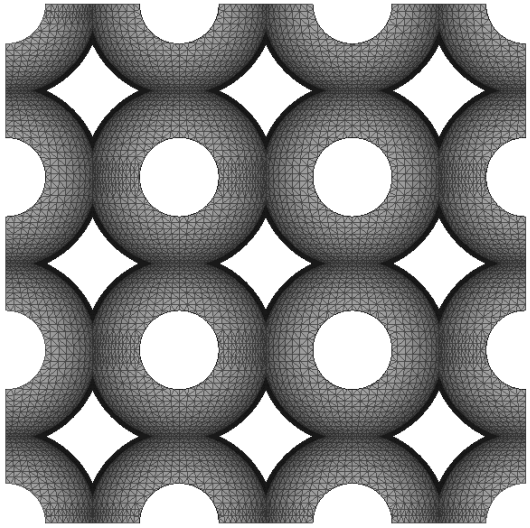
Radius 1.3



Radius 1.2



Radius 1.1



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Minkowski Tensors – Radius 1.4

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 10.6 & 0 & 0 \\ 0 & 10.6 & 0 \\ 0 & 0 & 10.6 \end{bmatrix}$	$\begin{bmatrix} -0.76 \\ 0.66 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0.66 \\ -0.76 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{10.6 \quad 10.6 \quad 10.6\}$	$\beta_1^{0,2} = 1.0$
$W_2^{0,2} = \begin{bmatrix} -6.0 & 0 & 0 \\ 0 & -6.0 & 0 \\ 0 & 0 & -6.0 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{-6.0 \quad -6.0 \quad -6.0\}$	$\beta_2^{0,2} = 1.0$

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Minkowski Tensors – Radius 1.3

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 19.6 & 0 & 0 \\ 0 & 19.6 & 0 \\ 0 & 0 & 19.6 \end{bmatrix}$	$\begin{bmatrix} -0.7 \\ 0.7 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0.7 \\ -0.7 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{19.6 \quad 19.6 \quad 19.6\}$	$\beta_1^{0,2} = 1.0$
$W_2^{0,2} = \begin{bmatrix} -13 & 0 & 0 \\ 0 & -13 & 0 \\ 0 & 0 & -13 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{-13 \quad -13 \quad -13\}$	$\beta_2^{0,2} = 1.0$

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Minkowski Tensors – Radius 1.2

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 27.1 & 0 & 0 \\ 0 & 27.1 & 0 \\ 0 & 0 & 27.1 \end{bmatrix}$	$\begin{bmatrix} -1.0 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1.0 \end{bmatrix} \begin{bmatrix} 0 \\ -1.0 \\ 0 \end{bmatrix}$	$\{27.1 \quad 27.1 \quad 27.1\}$	$\beta_1^{0,2} = 1.0$
$W_2^{0,2} = \begin{bmatrix} -20.7 & 0 & 0 \\ 0 & -20.7 & 0 \\ 0 & 0 & -20.7 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix} \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$	$\{-20.7 \quad -20.7 \quad -20.7\}$	$\beta_2^{0,2} = 1.0$

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Minkowski Tensors – Radius 1.1

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 33.1 & 0 & 0 \\ 0 & 33.1 & 0 \\ 0 & 0 & 33.1 \end{bmatrix}$	$\begin{bmatrix} -0.89 \\ 0.45 \\ 0 \end{bmatrix} \begin{bmatrix} 0.45 \\ -0.89 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{33.1 \quad 33.1 \quad 33.1\}$	$\beta_1^{0,2} = 1.0$

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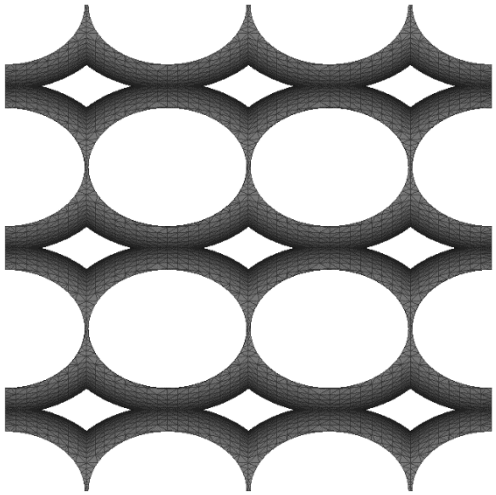
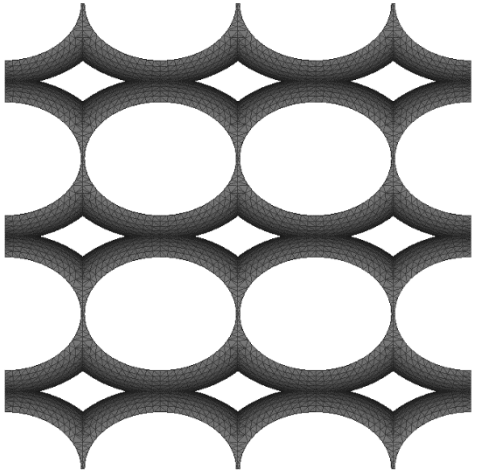
Asymmetric Parametric Pore – R1 = 1.4, R2=1.3

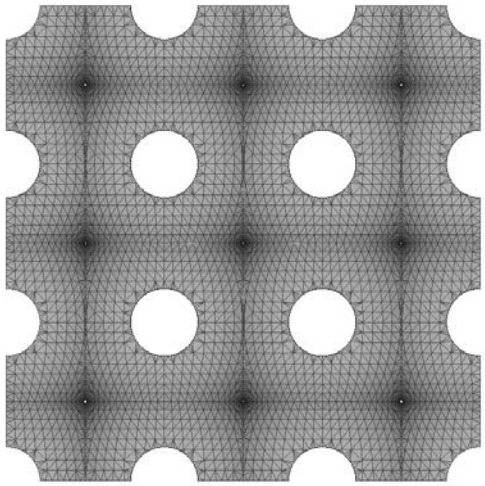
X-Y View



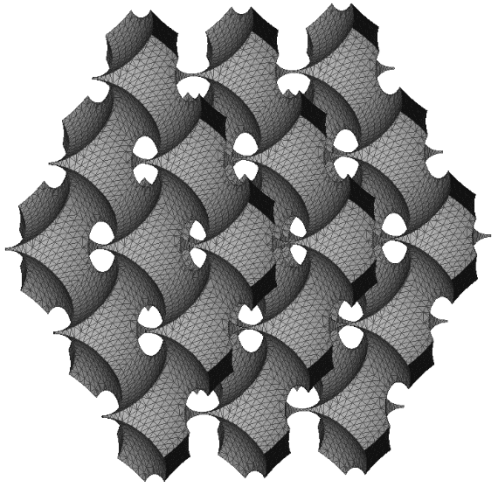
Y-Z View



X-Z View



3D View



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Minkowski Tensors – R1 = 1.4, R2=1.3

Minkowski Tensor	Eigenvectors	Eigenvalues	Anisotropy Index
$W_1^{0,2} = \begin{bmatrix} 11.9 & 0 & 0 \\ 0 & 51.8 & 0 \\ 0 & 0 & 11.9 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{11.9 \quad 51.8 \quad 11.9\}$	$\beta_1^{0,2} = 0.23$
$W_2^{0,2} = \begin{bmatrix} -7.8 & 0 & 0 \\ 0 & -30.9 & 0 \\ 0 & 0 & -7.6 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\{-7.8 \quad -30.9 \quad -7.8\}$	$\beta_2^{0,2} = 0.25$