Computational Physics - Project 5

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1 Execution

In order to analyse our data we need to find the potential energy and the kinetic energy at a given time t. Down here is the void function *KinpotEnergy* which calculates both the kinetic and potential energy for each particle. When ever this function is called in our RK4 or verlet method it calculates these values for one time step.

```
kineticEnergy <vector> //where we store each particle kinetic energy
potentialEnergy <vector> //where we store each particle potential energy

theTotalEnergy // where we store the total energy for all particles
total_kin // where we store the total kinetic energy only for the particles in system
total_pot // where we store the total potential energy only for the particles in system
numplanetsInSystem // the number of particles still in the system
ergodic //the value of ergodic ratio
```

```
void solarsystem::kinPotEnergy(){

    kineticEnergy = new double[ this->numplanets];
    total_kin = 0.0;
    total_pot = 0.0;

    double potenial = 0.0;
    double totalKinetic = 0.0;
    double totalPotenial = 0.0;
    double velocitySquared= 0.0;

    //kineticEnergy = 1/2 * m * v^2
    for (int i = 0; i < this->numplanets;i++){
        velocitySquared = A(3*i,1)*A(3*i,1)+A(3*i+1,1)*A(3*i+1,1)+A(3*i+2,1)*A(3*i+2,1);
        kineticEnergy[i] = 0.5*planets[i].m*velocitySquared;

        totalKinetic += kineticEnergy[i];
    }

    //potineal energy U = -G Mm/r----------------
    potentialEnergy = new double[ this->numplanets];
    double r;
    Mat<double> p = Mat<double>(this->numplanets,this->numplanets,fill::zeros); //matrix p will includ

    for (int i = 0;i < this->numplanets; i++ ){
        for (int j = i+1; j < this->numplanets; j++){
            r = (A(3*i,0)- A(3*j,0))*(A(3*i,0)- A(3*j,0)) + (A(3*i+1,0)- A(3*j+1,0))*(A(3*i+1,0)- A(3*
            r = sqrt(r);
            p(i,j)=-planets[i].m*planets[j].m*G/r;
            p(j,i)=p(i,j);
            totalPotenial += p(j,i);
        }
    }
    //calcuting the potenial energy for each planet from the marix P
    for(int i = 0; i < this->numplanets; i++){
        for(int j = 0; j < this->numplanets; j++){
            potenial += p(i,j);
        }
        potentialEnergy[i] = potenial;
        potenial = 0;
    }
    theTotalEnergy = totalKinetic+totalPotenial;

    //Virial analysis
     numplanetsInSystem = 0;
```

```
    //clac the energy of the bound system ! virial !!!
    for (int i = 0;i < this->numplanets; i++ ){
        if (( kineticEnergy[i]+potentialEnergy[i])<0.0){
            numplanetsInSystem += 1;
            total_kin += kineticEnergy[i];
            total_pot += potentialEnergy[i];
        }

    }
    total_pot = total_pot/2;
    ergodic = total_pot/total_kin;
}
```

In the first part of the function, we calculate the kinetic energy for each particle as $1\frac{1}{2}mv(t)^2$

In the second part, we calculate all the potentials between different particles in a matrix p in the following way:

$$p = \begin{bmatrix} 0 & \frac{-Gm_1m_0}{r} & \frac{-Gm_2m_0}{r} & \dots & \frac{-Gm_nm_0}{r} \\ \frac{-Gm_0m_1}{r} & 0 & \frac{-Gm_2m_1}{r} & \dots & \frac{-Gm_nm_1}{r} \\ \dots & \dots & \dots & \dots & \dots \\ \frac{-Gm_0m_n}{r} & \frac{-Gm_1m_n}{r} & \frac{-Gm_2m_n}{r} & \dots & 0 \end{bmatrix} \tag{1}$$

Afterwards, we perform a new for loop, where we calculate the potential energy for a particle i as the sum over al elements of the ith row, and finally calculate the total potential and kinetic of the system by summing only over the bounded particle by using an if test to get only the particles with negative total energy.

In the method *centermassfunction*, we calculate the centre of mass $\mathbf{r}_c$ of the system. We loop over all bounded particles $\mathbf{r}_c = \frac{\sum_{i=1}^{n} m_i * \mathbf{r}_i}{m_{\text{total}}}$

```
void solarsystem::centermassfunction(){
    centermass = new double[3]; //(centrMassX,centerMassY,centerMassZ)
    double centermassX = 0.0;
    double centermassY = 0.0;
    double centermassZ = 0.0;
    double totalmass = 0.0;
    for (int i = 0;i<this->numplanets;i++){
     if (( kineticEnergy[i]+potentialEnergy[i])<0.0){
        totalmass  += planets[i].m;
        centermassX += A(3*i,0)*planets[i].m;
        centermassY += A(3*i+1,0)*planets[i].m;
        centermassZ += A(3*i+2,0)*planets[i].m;
      }
   }
    centermassX = centermassX/totalmass;
    centermassY = centermassY/totalmass;
    centermassZ = centermassZ/totalmass;
    centermass[0] = centermassX;
    centermass[1] = centermassY;
    centermass[2] = centermassZ;
}
```