

#19.

Modeling: A Study in Words and Meanings

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Out on site, you were never parted from your plans. They were your Bible. They got dog-eared, yellowed, smeared with mud, peppered with little holes from where you had unrolled them on the ground. But although so sacred, the plans were only the start. Once you got out there on the site everything was different. No matter how carefully done, the plans could not foresee the variables. It was always interesting, this moment when you saw for the first time the actual site rather than the idealised drawings of it.

He knew men who hated the variables. They had their plans and by golly they were going to stick to them. If the site did not match the drawings it was like a personal insult.

He himself liked the variables best. He liked the way that the solution to one problem created another problem further down the line, so that you had to think up something else, and that in turn created another problem to solve. It was an exchange, backwards and forwards. Some men thought of it as a war, but to him it was more like a conversation.

Kate Grenville, *The Idea of Perfection* (Sydney: Picador, 1999): 62–3

##**Introduction** The question of modeling arises naturally for humanities computing from the prior question of what its practitioners across the disciplines have in common. What are they all *doing* with their computers that we might find in their diverse activities indications of a coherent or cohesible practice? How do we make the best, most productive sense of what we observe? There are, of course, many answers: practice varies from person to person, from project to project, and ways of construing it perhaps vary even more. In this chapter I argue for modeling as a model of such a practice. I have three confluent goals: to identify humanities computing with an intellectual ground shared by the older disciplines, so that we may say how and to what extent our field is *of as* well as *in* the humanities, how it draws from and adds to them; at the same time to reflect experience with computers “in the wild”; and to aim at the most challenging problems, and so the most intellectually rewarding future now imaginable.

My primary concern here is, as Confucius almost said, that we *use the correct word* for the activity we share lest our practice go awry for want of understanding (*Analects* 13.3). Several words are on offer. By what might be called a moral philology I examine them, arguing for the most popular of these, “modeling.” The nominal form, “model”, is of course very useful and even more popular, but for reasons I will adduce, its primary virtue is that properly defined it defaults to the present participle, its semantic lemma. Before getting to the philology I discuss modeling in the light of the available literature and then consider the strong and learned complaints about the term.

##Background Let me begin with provisional definitions¹. By “modeling” I mean the *heuristic process of constructing and manipulating models*’, a “model” I take to be either *a representation of something for purposes of study*, or *a design for realizing something new*. These two senses follow Clifford Geertz’s analytic distinction between a denotative “model of” such as a grammar describing the features of a language, and an exemplary “model for” such as an architectural plan [Geertz (1973), p. 93]². In both cases, as the literature consistently emphasizes, a model is by nature a simplified and therefore fictional or idealized representation, often taking quite a rough-and-ready form: hence the term “tinker toy” model from physics, accurately suggesting play, relative crudity, and heuristic purpose (Cartwright 1983, 158). By nature modeling defines a ternary relationship in which it mediates epistemologically, between modeler and modeled, researcher and data or theory and the world (Morgan and Morrison 1999). Since modeling is fundamentally relational, the same object may in different contexts play either role: thus, e.g., the grammar may function prescriptively, as a model *for* correct usage, the architectural plan descriptively, as a model *of* an existing style. The distinction also reaches its vanishing point in the convergent purposes of modeling: the model *of* exists to tell us that we do not know, the model *for* to give us what we do not yet have. Models *realize*.

Perhaps the first question to ask is what such a process has to do with computing, since as the examples suggest neither of the two senses of “model” assumes it unless the definition is further qualified. In history, for example, Gordon Leff has

¹My definitions reflect the great majority of the literature explicitly on modeling in the history and philosophy of the natural sciences, especially of physics (Bailer-Jones 1999). The literature tends to be concerned with the role of modeling more in formal scientific theory than in experiment. The close relationship between modeling and experimenting means that the rise of a robust philosophy of experiment since the 1980s is directly relevant to our topic; see Hacking (Hacking 1983); Gooding (Gooding 2017). Quite helpful in rethinking the basic issues for the humanities are the writings from the disciplines other than physics, e.g., Clarke (Clarke 1972) on archaeology; Wimsatt (Wimsatt 1987) on biology; Del Re (Del Re 2002), on chemistry; and on the social sciences, the essays by de Callatay, Mironesco, Burch, and Gardin in Franck (Franck 2002). For interdisciplinary studies see Shanin (Shanin 1972) and Morrison and Morgan (1999), esp. “Models as Mediating Instruments” (Morgan and Morrison 1999, 10–37). For an overview see Lloyd (Lloyd 1998).

²Cf. Goodman’s distinction between “denotative” and “exemplary” models, respectively (Goodman 1976, 172–3); H. J. Groenewold’s “more or less poor substitute” and “more or less exemplary ideal” (Groenewold 1960, 98). Similar distinctions are quite common in the literature.

argued that models have always been *implicit* in scholarly practice (Leff 1972). Leff cites, e.g., the historic-graphical notion of “epoch”, but any well-articulated idea would qualify as a model *of its* subject. Nevertheless, Leff notes that as M. I. Finley said in *Ancient History: Evidence and Models*, “model-construction is rare among all but economic historians”; Finley recommends Max Weber’s parallel concept of “ideal types”, which “expresses clearly the nature and function of models in historical inquiry” (Leff 1972, 60f). Explicit model-construction is still rare in mainstream humanities scholarship. Even for non-computational research in the social sciences, it is more common, as Finley’s demarcation suggests. For example, political schemes by nature model *for* a better or at least different world, even if like Marx’s historiography they begin as models *of* it; delineating them as models is the scholar’s obvious work (Mironesco 2002). Nevertheless, outside computationally affected scholarly practice Marvin Minsky’s simple, straightforward definition remains alien in style and in thought: “To an observer B, an object A* is a model of an object A to the extent that B can use A* to answer questions that interest him about A” (Minsky 1995).

A strong temptation for us here is to dismiss the residual alienness of Minsky’s formulation and to accept, as we have accepted computing, the reified, explicit “model” of Minsky’s definition as what we *really* have been doing all along. This would, however, be a serious error. As with the relationship of hypertext to earlier ways of referring (McCarty 2002), the new form of expression, with its vocabulary and tools, means an altered way of thinking. A historical imagination is required to see what this means.

Two effects of computing make the distinction between “idea” or other sort of mental construct on the one hand, and on the other “model” in the sense we require: first, the demand for computational tractability, i.e., for complete explicitness and absolute consistency; second, the manipulability that a computational representation provides.

The first effects a sea-change by forcing us to confront the radical difference between what we know and what we can specify computationally, leading to the epistemological question of *how we know what we know*. On the one hand, as Michael Polanyi observed, “we can know more than we can tell” (Polanyi 2011, 4–5). Computational form, which accepts only that which can be told explicitly and precisely, is thus radically inadequate for representing the full range of knowledge – hence useful for isolating the tacit or inchoate kinds. On the other hand, we need to trust what we somehow know, at least provisionally, in order not to lose all that goes without saying or cannot be said in computational form.

Take, for example, knowledge one might have of a particular thematic concentration in a deeply familiar work of literature. In modeling one begins by privileging this knowledge, however wrong it might later turn out to be, then building a computational representation of it, e.g., by specifying a structured vocabulary of word-forms in a text-analysis tool. In the initial stages of use, this model would be almost certain to reveal trivial errors of omission and commission. Gradually, however, through perfective iteration trivial error is replaced by

meaningful surprise. There are in general two ways in which a model may violate expectations and so surprise us: either by a success we cannot explain, e.g., finding an occurrence where it should not be; or by a likewise inexplicable failure, e.g., not finding one where it is otherwise clearly present. In both cases modeling problematizes. As a tool of research, then, modeling succeeds intellectually when it results in failure, either directly within the model itself or indirectly through ideas it shows to be inadequate. This failure, in the sense of expectations violated, is, as we will see, fundamental to modeling.

The second quality of “model” that distinguishes it from “idea” is manipulability, i.e., the capability of being handled, managed, worked, or treated by manual and, by extension, any mechanical means (*OED*: la.). Change is common to both models and ideas, but at greater or lesser metaphorical distance, “model” denotes a concrete, articulated plan inviting the etymological sense of action-by-hand (L. *manus*) in response. Manipulation in turn requires something that can be handled (physical objects, diagrams, or symbols of a formal language) – and a time-frame sufficiently brief that the emphasis falls on the process rather than its product. In other words, the modeling system must be interactive. Manipulable objects from the physical to the metaphorical have characterized mathematics, engineering, the physical sciences, and the arts *ab wo*, but with exceptions the necessary time-frame, allowing for interactivity, has been possible only with computing. With its advent, Minsky has noted, models could be “conceived, tested, and discarded in days or weeks instead of years” (Minsky 1991). Computing met research easily in fields where modeling was already an explicit method because, Brian Cantwell Smith has pointed out, models are fundamental to computing: to do anything useful at all a computer must have a model of something, real or imaginary, in software. But in the context of computing, models *per se* are not the point. What distinguishes computers from other kinds of machines, Smith notes, is that “they run by *manipulating* representations, and representations are always formulated in terms of models” (Smith 1995), (Fetzer 1999, 23).

In other words, computational models, however finely perfected, are better understood as *temporary states in a process of coming to know* rather than fixed structures of knowledge. It is of course possible to argue ideologically, as some still do, that we are converging on and will achieve such structures,³ but in any case these structures would not then be *models* and would no longer have reason to exist in software. (Note that the history of computing is the story of ever more complex and extensive software, not less, despite the fact that implementations in hardware are faster and can be cheaper.) For the moment and the foreseeable future, then, *computers are essentially modeling*

³This is usually done in “the rhetoric of technohype . . . the idiom of grant proposals and of interviews in the Tuesday New York Science Times: The breakthrough is at hand; this time we’ve got it right; theory and practice will be forever altered; we have really made fantastic progress, and there is now general agreement on the basics; further funding is required” (Fodor, n.d.). More serious criticism is leveled by Terry Winograd [winograd_thinking_1991, p. 207–8]; see below.

machines, not knowledge jukeboxes. To think of them as the latter is profoundly to misunderstand human knowledge – and so to constrict it to the narrow scope of the achievably mechanical.

In analytical terms, as I have suggested, modeling has two phases: first, construction; second, manipulation. Examples come readily to mind from ordinary technical practice, e.g., building a relational database, then querying the data thus shaped to explore emergent patterns. As experience with databases shows, the two phases often blur into each other especially in the early stages when use uncovers faults or suggests improvements that direct redesign. A model *of* and a model *for* may be distinct types – because in our terms they are fixed objects. But modeling *of* something readily turns into modeling *for* better or more detailed knowledge of it; similarly, the knowledge gained from realizing a model *for* something feeds or can feed into an improved version. This characteristic blurring of design into use and use into (re)design is what denies modeling of *any* sense of closure. Modeling *for*, Utopian by definition, is denied it in any case.

Learned Complaints

So far so good – but at the cost of averting our gaze from the problems with the word “model.” Indeed, the extensive and growing literature on the topic may seem adrift in a hopeless muddle. “I know of no model of a model”, physicist H. J. Groenewold declared many years ago (Groenewold 1960, 98). The philosopher Peter Achinstein has warned us away even from attempting a systematic theory (Groenewold 1960, 203). The word itself is indeed astonishingly polysemous – or promiscuous, as Nelson Goodman puts it. “Model”, he complains, can be used to denote “almost anything from a naked blonde to a quadratic equation” (Goodman 1976, 171). Nevertheless, the word is often used as if its semantic complexity either did not exist or could be safely ignored. The muddle of partly overlapping, partly contradictory senses is proof enough that we ignore it at our peril. Nor can we simply avoid the problem by dismissing “model” altogether, as Goodman and others recommend, without (as I will argue) hobbling our ability to understand *inter alia* those aspects of computing most important to research – one might even say, as I do, its essence. Despite several other, supposedly less confusing terms on offer, the word remains stubbornly popular in the literature of the social and physical sciences, the history and philosophy of science, cognitive science, artificial intelligence, and related areas.

Theoretical physicist John Ziman and philosopher Stephen Toulmin, for example, recommend “map” on the basis of its conceptual clarity and fitness for describing the relationship between theoretical knowledge and reality (Ziman 2002, 126–38, p. 147–50), (Toulmin 2008, 94–109). Goodman would have us collapse modeling into diagramming, which he thinks less troublesome (Goodman 1976, 171–3). But preference needs to be based on more than such criteria; “map”, for example, serves experiment much less well than theory, as I will show. We require a close

and careful look at the semantic fields of all major alternatives, including “map”, for their disjunctions and overlaps. We need to scrutinize each of these, asking what does it denote *and connote* that the others do not, and vice versa? What do all have in common? What are their individual tendencies of mind, and which of these best suits computing as we are learning to conceive it?

##Philological Analysis of Related Terms So far I have used the term “model” as the default, partly for purposes of convenience, partly because, as I argue, it is right for the job. To answer the learned criticisms and further clarify our topic, however, I propose to question it by comparison against the major alternatives: “analogy”, “representation”, “diagram”, “map”, “simulation”, and “experiment.” As we have seen, the two decisive criteria are that the thing named by the chosen term be computationally tractable and manipulable. Tractability in turn requires complete explicitness and absolute consistency; manipulability resolves into mechanical action and interactivity. Hence the term must denote a continual process of coming to know, not an achievement but an approximation. As I have argued, it is from the difference between the approximation and the reality approximated – which ultimately for the humanities is our humanly known apprehension of that reality – that we learn.

For each of the alternative terms I ask whether and to what degree the word normally denotes a dynamic process and whether it refers to a concrete, i.e. manipulable, form – the requirements of anything whose function is fulfilled through being changed. Corresponding to the two senses of “model” I identified earlier, the denotative model of and the exemplary model *for*, I also ask whether each word tends to the mimetic (imitation) or proleptic (anticipation). The distinction helps in determining whether the action denoted by a term may be said to be bounded, either by a fixed form, as is the case with “analogy”, or by an inherent tendency to reach a definitive or satisfactory conclusion, as in “representation.”

Thus bringing “model” into focus against the semantic background of these other terms will show that the problem has not so much been too many meanings for “model” as use without regard to any of them, often as if the sense of it simply goes without saying. It doesn’t. But perhaps the most important lesson we learn from seeing the word in the context of its synonym set is not the range and variety of its meanings; rather, again, its strongly dynamic potential. Apart from the popularity of “model” taken at face-value, the word would have little to recommend it (and, as the complainers say, much against it) but for the open-ended *present-participial* strength of “modeling.”⁴ Indeed, the manifest confusion in the literature on the topic may be primarily due to a mistaken preference for the noun – as if getting a model right, and so promoting it to the status of theory, were the point. Modeling has an entirely different role to play. There are several better terms if what one wants is to name a stable

⁴I have in mind the present-participial imagination described by Greg Denning, with which we may “return to the past the past’s own present, a present with all the possibilities still in it, with all the consequences of actions still unknown” (Denning 1998, 48); see also (Denning 1996, 35–63).

conceptualization.

Analogy “Analogy” (Gk. , “equality of ratios, proportion”) is, like “model”, a highly polysemous term with a long and complex career⁵. John Stuart Mill complained that “no word . . . is used more loosely, or in a greater variety of senses, than Analogy” (Mill 1882). Yet Dr Johnson’s pithy definition, “resemblance of things with regard to some circumstances or effects”, and Mill’s even pithier one, “resemblance of relations”, give us an idea of why it is so fruitful. From its original meaning in Greek mathematics, analogy specifies a structured relationship between pairs of related quantities, which for convenience may be represented in the form of an equation, “ $A/B = C/D$ ”, read “as A is to B, so C is to D.” Extended beyond mathematics to other modes of reasoning, analogy yields a powerful (but still poorly understood) means of inferring from the one relation to the other. Like most of the words in our domain, “analogy” is proleptic, a means of inference, based on conjecture, to something unknown or uncertain. Examples in the history of science are plentiful, e.g., Kepler’s discovery of the *vis matrix*, or cause of planetary motion, by reasoning that as the sun radiated light, so it must also radiate this motive power (Gentner 2002).

Here I wish only to argue two points. The first is that analogy is basic to the entire vocabulary. Although not every model is as strictly based on an analogy as Kepler’s, modeling is inherently analogical, with just the features that make the idea attractive for our purposes. Thus we require a structured correspondence between model and artifact, so that by playing with one we can infer facts about the other. (For example, by adjusting choice of words and weightings for a distribution-display across a textual corpus, one can investigate the effect of vocabulary on the interplay of meanings in that corpus.) The second point is that “analogy” is inherently static: it means either a type of relationship or an instance of one, never an object and not, literally or directly, a process. Action is implied in the ratio of quantities – thus Kepler’s “as A *does* B, so C *does* D” – but *acting* is not denoted by the analogy. The word has no commonly used verbal form (“analogize” and “analogizing” are rare if not strange). Although an analogy may be algebraically or geometrically expressed and may refer to concrete objects, it itself is abstract.

Because analogy works so well as a way of describing how we often think, efforts to understand acquisition of new knowledge tend to engage with theories of analogy and to propose many mechanisms, e.g., in cognitive science, educational theory, and artificial intelligence (Hoffman 1995). Because modeling is analogical, this work is potentially relevant to questions raised in computing the artifacts of

⁵For the concept in imaginative language and thought see Gibbs (Gibbs 1994) ; reviewed by (Turner 1995), Turner (Turner 1996); in computer science, Hoffman (Hoffman 1995) – whose summary of research is quite valuable; in cognitive science, including psychology, Mitchell (Mitchell 1993), Holyoak and Thagard (Holyoak and Thagard 1997); in the philosophy of science, Achinstein (Achinstein 1968), Leatherdale (Leatherdale 1974), Gentner (Gentner 2002), Shelley (Shelley 2002); in relation to modeling, Bailer-Jones (Bailer-Jones 1999), Bailer-Jones and Bailer-Jones (Bailer-Jones and Bailer-Jones 2002). I do not deal here with metaphor in relation to modeling, for which see Black (Black 1977), Johnson (Johnson 2002).

the humanities. We need to pay attention here.

###Representation “Representation” in Nelson Goodman’s terms is defined by a symbolic denotative correspondence, not likeness or imitation (Goodman 1976, 3–41)⁶. In a less philosophically precise sense, however, we may say that “representation” displays strong mimetic tendencies, e.g., in the definition given by the OED: “An image, likeness, or reproduction in some manner of a thing A material image or figure; a reproduction in some material or tangible form; in later use esp. a drawing or painting (of a person or thing).” The history of aesthetics from earliest times, in fits and starts of fashion, demonstrates that the copy-theory of representation, though its falsity names its achievement in a *trompe l’oeil*, remains a habit of mind. If in aesthetics, why not in computer science?

A well-attested present participle and a full complement of verbal forms establishes the action of *representing*, but semantically this action is bounded by its relationship to the represented object, whether this be symbolic or imitative.

As with “analogy”, the semantic fields of “model” and “representation” clearly overlap, but the situation is more complex because of the mimetic and proleptic kinds of “model.” Hence (Platonism aside) we may say that modeling *of* is representational but not modeling *for*. In fact a model *of* is a manipulable variety of representation – which any representation in software would of course be. The crucial difference between model *of* and representation is the quality of the action implied. Unlike representing, modeling *of* is denied closure, as I noted earlier. It has no satisfactory *trompe l’oeil* or symbolizing conclusion. If the researcher calls a halt, then the last state of the system, as it were, is better called a “representation.”

In the context of computing, the meaning of “representation” is dominated by the subfield of artificial intelligence known as “knowledge representation” (KR). Given the scope of this essay I can do little more than make a few observations, chiefly about the assumptions built into the name and apparently into tendencies in some KR work. In brief, my argument concerning KR is that it needs to be understood as a particularly rigorous control on model-building suitable to that which can be stated in prepositional form.⁷

To the connotations of “representation” I have already reviewed, KR adds the demarcational term “knowledge.” The point I wish to draw from current epistemology is a simple one, for which I quote Michael Williams – at length, because the issues are consequential for us:

⁶Goodman dismantles the copy-theory of representation, arguing that representation is not mimetic but symbolic: object X is always represented as Y, which means that Y is selective with respect to X and stands in symbolic relationship to it. See also Elgin (Elgin 2000), Hopkins (Hopkins 2000).

⁷Possibly the best and least problematic view is afforded by Davis et al. (1993); see also Sowa (Sowa 2000); Barr and Feigenbaum (Barr and Feigenbaum 1981). Lenat (Lenat 1998) illustrates the problematic tendencies in this field; Winograd (Winograd 1991) and Dreyfus (Dreyfus 1981) provide the antidote.

“Knowledge” is an honorific title we confer on our paradigm cognitive achievements More generally, “know” is a “success-term”, like “win” or “pass” (a test). Knowledge is not just a factual state or condition but a particular normative status. Such statuses are related to appropriate factual states: winning depends on crossing the line before any other competitor. But they also depend on meeting certain norms or standards which define, not what you do do, but what you must or ought to do. To characterize someone’s claim as expressing or not expressing knowledge is to pass judgement on it. Epistemic judgements are thus a particular kind of value-judgement

This normative dimension distinguishes philosophical theories of knowledge from straightforwardly factual inquiries and explains why demarcational (and related methodological) issues are so significant. Because epistemological distinctions are invidious, ideas about epistemological demarcation always involve putting some claims or methods above others: mathematics above empirical science, empirical science above metaphysics or religion, logic above rhetoric, and so on. Demarcational projects use epistemological criteria to sort areas of discourse into factual and non-factual, truth-seeking and merely expressive, and, at the extreme, meaningful and meaningless. Such projects amount to proposals for a map of culture: a guide to what forms of discourse are “serious” and what are not. Disputes about demarcation – including disputes about whether demarcational projects should be countenanced at all – are disputes about the shape of our culture and so, in the end, of our lives.

(Williams 2001, 11–12)

Projects such as Cyc, based on what Northrop Frye characterized as the discredited *Wissenschaft-theory* of knowledge – that its accumulation in vast quantities will one day, somehow, result in understanding⁸ – clearly assume if not perfect closure, then a threshold beyond which lack of perfection ceases to matter. But to whom, and for what purposes?⁹ Apart from such questions, and the serious doubts within computer science on the wisdom of building massive knowledge-

⁸Frye (Frye 1991, 4), to which compare Winograd’s analysis of the “almost childish leap of faith” made, e.g., by Marvin Minsky in his “Society of Mind” thesis that “the modes of explanation that work for the details of [the artificial micro-worlds thus represented] will be adequate for understanding conflict, consciousness, genius, and freedom of will” (Winograd 1991, 204–7) – as the ambitious claim; see also Winder (Shin, Lemon, and Mumma 2002).

⁹Note the boast that “Cyc knows that trees are usually outdoors, that once people die they stop buying things, and that glasses of liquid should be carried rightside-up” (Cycorp Company Overview, at <http://www.cyc.com/overview.html>, accessed September 22, 2003).

bases for expert systems¹⁰ – there are, again, the very serious demarcational issues. When, for example, one of the leading theorists of KR writes in passing that, “Perhaps there are some kinds of knowledge that cannot be expressed in logic” (Sowa 2000, 12) our intellectual claustrophobia tells an important tale. Not, of course, the only one. If the point of modeling is to fail well, then KR has a vital quality-control function to serve.

###Diagram A diagram (Gk. *diagramma*, “that which is marked out by lines, a geometrical figure, written list, register, the gamut or scale in music”)¹¹ is an analogical drawing, “a figure drawn in such a manner that the geometrical relations between the parts of the figure illustrate relations between other objects”: thus the physicist James Clerk Maxwell on the graphic, symbolic, and hybrid kinds (“Maxwell, James Clerk,” n.d.). Such a diagram ranges from the precisely drawn schematic, whose measurements are significant, to the rough sketch intended to express symbolic relations only. But what makes a graphic a diagram, properly so called, is the way in which it is read, not its resemblance to anything¹². Reviel Netz argues the point for the lettered diagram in Greek mathematical texts: “It is only the diagram perceived in a certain way which may function alongside the text” – irrelevant discrepancies are overlooked, the important matters denoted by the lettering: “All attention is fixed upon the few intersecting points, which are named” (Netz 1999, 33–35). Even when the diagrammed entity is a physical object, the diagram represents structure and interrelation of essential parts, foregrounding interpretative choice and conscious purpose. The ability to manipulate structures and parts may be implied.

The word “diagram” doubles as noun and verb and has a full range of verbal inflections. Like “represent”, its action is bounded, but more by ideas than appearance, even when that appearance is precisely delineated. As Maxwell notes for physics, diagrams often represent force or movement, even if only implicitly, though the form is static. As a means of communication, e.g., in a lecture or discussion between collaborators, diagramming is the point, not the static trace left behind. That trace may in fact be unintelligible apart from the discussion of which it was a dynamic part.

The focus on ideas rather than things *per se*, the role of manipulation where diagramming is heuristic and the kinaesthetics of the action suggest the close relationship between diagramming and modeling for which Goodman argues. Models *of*, he declares, “are in effect diagrams, often in more than two dimensions and with working parts . . . [and] diagrams are flat and static models” (Goodman 1972, 172–3). Nevertheless, the two-dimensionally graphic, geometrical, and finally static qualities of the diagram define it, not “model”, which has considerably broader applications.

¹⁰Winograd and Flores (Winograd and Flores 1987, 97–100, p. 131–3, p. 174–7); Dreyfus (Dreyfus 1981). See also Brooks (Brooks 1991).

¹¹See, however, the discussion in Netz (Netz 1999, 35–38).

¹²Goodman (Goodman 1976, 170f), who distinguishes between analogue and digital diagrams. As Netz explains, the lettered diagram provides a good example of the latter (Netz 1999, 34f).

Sun-Joo Shin and Oliver Lemon note that although diagramming is very likely one of the oldest forms of communication, modern logicians and philosophers have tended until recently to regard it as only of marginal importance.¹³ That is changing very rapidly now. As a cognitive, reasoning process it is studied in relation to Greek mathematics and geometry in particular (Netz 1999). Modern philosophical attention can be traced from Descartes’s “La Geometric” (1637) and Kant’s *Critique of Pure Reason* II.1.1 (1781) to Peirce’s “existential graphs” in the late nineteenth century, significantly as part of his much broader interest in scientific discovery, to which I will return. His work is now central to much current research.

Shin and Lemon delineate three branches of research since the mid-1990s: (1) multi-modal and especially non-linguistic reasoning, in the philosophy of mind and cognitive science; (2) logical equivalence of symbolic and diagrammatic systems, in logic; and (3) heterogeneous systems implementing theories of multi-modal reasoning, in computer science. The close relationship of diagramming and modeling make this research immediately relevant.

##Map A map may be defined as a schematic spatial representation, or following Maxwell, a diagram of “anything that can be spatially conceived.”¹⁴ Indeed, if not for the geographical focus of mapping, the semantic fields of “map” and “diagram” would completely overlap: both are fully verbal, their action bounded by a graphical representation that has both strongly mimetic and ideational aspects; both manipulate data for specific purposes and introduce fictional elements to serve these purposes. But the long history of mapping the physical world for exploration and description gives “map” specific (and evidently powerful) connotations.

Mapping is particularly characteristic of an early, exploratory period, when a territory is unknown to its discoverers (or conquerors). Mapping constructs the world it represents, selectively, therefore shaping thought and guiding action. It orients the newcomer, giving him or her control of the mapped terrain, at the same time expressing, though perhaps covertly, a perspective, a set of interests, and a history. Mapping attaches meaning to place. Like modeling it can be either *of or for* a domain, either depicting the present landscape or specifying its future – or altering how we think about it, e.g., by renaming its places. A map is never entirely neutral, politically or otherwise.

As I have noted, John Ziman, following Stephen Toulmin, has argued persuasively for describing scientific research as mapping – hence the immediate relevance of the cartographic imagination to my project. Mapping particularly fits a Kuhnian view of research: long periods of stable activity within a settled terrain interspersed by revolutionary, and perhaps incommensurable, reconceptualizations of that terrain. Mapping is for our purposes more to the point than representation,

¹³Shin and Lemon (Shin, Lemon, and Mumma 2002); note the extensive bibliography.

¹⁴Robinson and Petchenik (Robinson and Petchenik 1976) ; see also Monmonier (Monmonier 1996); Wood (Wood 1992). Turnbull (Turnbull 1994) argues specifically for the link between maps and theories.

because we always know that there can be many maps for any territory and that all of them have a fictional character (which is why the map is a standard example of an interpretative genre for data¹⁵). But because its action is bounded and its result defines a world, mapping better suits the theoretician's than the experimenter's view.

In computer science, mapping is used in knowledge and argument representation and implementation of schemes for depicting cyberspace in general and the Web in particular. The term surfaces in "Topic Maps", "Concept Maps", and is implicit in talk about, e.g., "semantic networks." This interest seems to originate with Toulmin's mapping of argument (Toulmin 1958), which suggests techniques of automated inferencing in AI. (Maps of argument look like flowcharts.) As a form of data-visualization, mapping also connects with a very strong, recent interest in humanities computing (Kirschenbaum 2002), and so connects this interest with modeling.

###Simulation "Simulation" is "The technique of imitating the behaviour of some situation or process . . . by means of a suitably analogous situation or apparatus" (*OED*).¹⁶ Its mimetic tendencies and so bounded action are perhaps most emphatic among the terms we are considering. Again, total replication is not at issue; a simulation attends to selected details of the world, thus can be exploratory, as when relevant conditions of flight are simulated for purposes of study or training. Simulation also relies on abstraction from the original to the analogue system (Simon 1969, 15–18), which makes it a kind of representation, subject to the same philosophical argument including the caveat respecting mimesis. But in usage, the connotation, if not denotation, of an *exact* correspondence between simulation and original remains paradoxically alongside knowledge of real difference.¹⁷ That knowledge, however uneasily, can be put aside, as in what we now call "virtual reality" (VR).¹⁸

In its current form VR is of course quite a recent phenomenon, but the essential

¹⁵See Bateson (Bateson 2002, 27–28), who cites Alfred Korzybski's principle that "the map is not the territory" (Korzybski 1995) and points out that "the natural history of human mental process" nevertheless tells a different tale: part of us in fact regularly identifies map and territory, name and thing named. See also Goodman (Goodman 1972, 15); Kent (Kent and Hoberman 2012, xix).

¹⁶On the semantic overlap of "simulation" with "experiment" and "model", see Guala (Guala 2002), who also stresses the necessity of including the designer or initiator as part of the simulation.

¹⁷Hence, perhaps, the deception attributed to the word: "intent to deceive" in a "false assumption or display, a surface resemblance or imitation . . ." (*OED* 1 .a., 2) – an animated *trompe l'oeil*.

¹⁸Recent research in psychology and cognitive science, working with the representational model of mind, might be summarized by the proposition that reality as we know and participate in it is simulated. Thus mental simulation is used to explain aspects of cognition (Markman and Dietrich 2000); (Davies and Stone 2000). Especially relevant here is the idea that perceptual simulations play a significant role in cognition, as when the replay of a kinaesthetic memory, awakened by some corresponding movement or gesture, lends meaning to a diagram or physical model. This is why animations can in principle be more effective than static diagrams: they are more knowledgeable (Craig et al. 2002)

movement of simulation on which it is based, from self-conscious imitation to displacement of reality, is attested from the get-go of applied computing, in the weapons research in nuclear physics immediately following World War II. “Proven on the most complex physical problem that had ever been undertaken in the history of science”, Peter Galison notes, simulation came to replace experimental reality, thus blurring multiple boundaries that had previously defined research, redefining it in new terms (Galison 1987, 690f). Since then the turn away from traditional analytic methods to simulation has spread to several other fields (Burch 2002). As the biologist Glenn W Rowe points out, with this turn has come the realization that “a great many systems seem to have an inherent complexity that cannot be simplified”¹⁹ – and so must be studied as simulations. Thus simulation has opened our eyes to the new problems with which it can deal. In the humanities we have known for some years that computer-based *simulations*, in the form of pedagogical games, can play a role in teaching. An old but very good example is *The Would-Be Gentleman*, a re-creation of economic and social life in seventeenth-century France in which the student-player must realize and put aside his or her modern preconceptions in order to win (Lougee 1988). In other words he or she must *become* a seventeenth-century Frenchman mentally and emotionally. From more recent and far more technically advanced VR applications, such as Richard Beacham’s and Hugh Denard’s reconstruction of the theater of Pompey in Rome (Beacham and Denard 2003), one can predict a scholarly future for simulation in many areas of humanistic research.

Simulation, like game-playing, tends to forgetfulness of the mechanism by which it is created, so long as its terms of engagement (expressed in parameters and algorithms) are fixed. Unfix them – e.g., in *The Would-Be Gentleman* by allowing the player to change the encoded attitude toward marrying above or below one’s station – and the simulation becomes a modeling exercise directed to exploring the question of that attitude. Thus simulation crosses over into modeling when the constants of the system become variables. Modeling, one might say, is a *self-conscious* simulation, and simulation an *assimilated* modeling.

###Experiment In common usage “experiment” (L. *experiri*, to try) is either “An action or operation undertaken in order to discover something unknown ...” or “The action of trying anything, or putting it to proof; a test, trial ...” (*OED*). In its broadest sense, the word embraces “modeling”, indeed any heuristic experience of the world, especially that which involves conscious purpose, defined procedure, or its material instantiation in equipment. Like “modeling”, “experiment” refers to a process whose ending is constructed rather than given: as Peter Galison has argued for the physical sciences, the experimenter *decides* if and when the attempt has succeeded or failed, in “that fascinating moment ... when instrumentation, experience, theory, calculation, and sociology meet” [galison_how_1987, p. 1]. Modeling and experimenting are by nature open-ended; indeed they are often at the time ill-defined, even quite messy.²⁰

¹⁹Rowe (Rowe 1997), quoted by Burch (Burch 2002, 245); see also Winsberg (Winsberg 2001).

²⁰This is true for scientific experiment much more often and more significantly than popular

The semantic overlap of “modeling” and “experiment” is so close that the two can be quite difficult to separate (Guala 2002). Mary S. Morgan, writing about modeling in economics, has argued that they may be discriminated by the degree to which the former involves hypothesis, the latter reality [morgan_model_2002, p. 49]. But, as she notes, hybrids provide exceptions and thought experiments – “devices of the imagination used to investigate nature” (Brown 2002) – a very close analogue to modeling.²¹ Perhaps the relationship is most clearly stated by saying that in the context of research a model is an experimental device, modeling an experimental technique.

The point of considering “experiment” here is, however, primarily to locate our topic within the context of a particular history of ideas and so to engage with large and important areas of historical and philosophical research. Indeed, as an experimental technique modeling has shared the fate of experiment in the specialist literature, and so also in the popular understanding. Allow me briefly to summarize the background.²²

By the mid-nineteenth century, understanding of scientific work had begun to polarize into two epistemological conditions, which physicist and philosopher Hans Reichenbach later famously named “the context of discovery” and “the context of justification.”²³ By the early to mid-twentieth century, attention had shifted almost completely to justification and so, as Thomas Nickels has said, discovery was expelled from mainstream epistemology (Nickels 2000, 87). Experiment, the means of discovery, was in consequence also demoted and theory, the focus of justification, promoted. “The asymmetric emphasis on theory in the historical literature”, Peter Galison explains, meant that attention was confined

and earlier philosophical accounts would have us believe. Ian Hacking illustrates the point in an illuminating discussion of the famous Michelson-Morley experiment, “a good example of the Baconian exploration of nature” (1983: 254); see his description (1983: 253–61), and esp. the book as a whole. See also Gooding (Gooding 2000) and Morrison (Morgan and Morrison 1999) for an overview of experiment in current philosophy of science; the triplet of articles presented at a symposium on “The Philosophical Significance of Experimentation”, Hacking (Hacking 1988), Heelan (Heelan 1988), and Galison (*How Experiments End* n.d.); and Franklin (Franklin and Perovic 2016) for physics in particular.

²¹See also Brown (Brown 2000), Gooding (Gooding 1998) and note esp. the careful argument in Kuhn (Kuhn 1964) toward an understanding of how thought experiment can lead to new knowledge, not simply expose logical contradictions or confusions.

²²I rely primarily on Galison (Galison 1987), Hacking (Hacking 1983) and Nickels (Nickels 2000).

²³Reichenbach introduced the distinction to mark “the well-known difference” between “the form in which thinking processes are communicated to other persons [and] the form in which they are subjectively performed”, i.e., justification and discovery, respectively (Reichenbach 1961, chap. 1); compare Feyerabend (Feyerabend 1993, 147–58). This distinction involves a long-standing argument that goes back to the debate between William Whewell (first to use the term “philosophy of science”) and John Stuart Mill; it was then taken up by Charles Sanders Peirce on the one hand and Karl Popper on the other. Popper, in *Logik der Forschung* (translated as *The Logic of Scientific Discovery*) characteristically ruled discovery out of court by identifying it as a matter for psychology, recalling Duhem’s and Reichenbach’s use of that term: “The question of how it happens that a new idea occurs to a man ... may be of great interest to empirical psychology; but it is irrelevant to the logical analysis of scientific knowledge” (Karl R Popper 1992, 7), (Karl Raimund Popper 1992). See Nickels (Nickels 2000).

“to the invention and testing of theories” (Galison 1987, 8), the actual conduct and intellectual role of experiments being largely overlooked. In philosophy too, “experiment *for* theory” dominated until (in Ian Hacking’s paraphrase of Nietzsche) Thomas Kuhn’s *The Structure of Scientific Revolutions* “unwrapped the mummy of science” by historicizing it (Hacking 1988, p. If) – What had actually always been happening in experimental work could then become a proper subject of investigation. Furthermore, Kuhn’s ample demonstration of “the essential role theory plays in the conduct of experimentation, the interpretation of data, and in the definition of ‘relevant’ phenomena” depolarized theory and experiment (Galison 1987, 80) In other words, from an entirely subordinate and observational role, experiment emerged alongside theory as an interdependent partner.

Subsequently, through the work of Hacking, Feyerabend, Galison, and several others, the fiction of a unitary “scientific method”, in which theory cleanly defines the role of experiment, has been dispelled. As Hacking says, calling for a “Back-to-Bacon” movement, “Experiment has a life of its own” (Hacking 1983, 150), sometimes preceded by theory, sometimes not. But the consequent liberation of experiment from the debilitating pretense of grubby handmaiden to “pure” theory has at the same time directed attention back to the very hard, old problem of discovery: how does this happen?

##Conclusion Why do we need an answer to this question? Because, I have argued, ours is an experimental practice, using equipment and instantiating definite methods, for the skilled application of which we need to know what we are doing as well as it can be known. I have labeled the core of this practice “modeling”, and suggested how, properly understood, modeling points the way to a computing that is of as well as in the humanities: a continual process of coming to know by manipulating representations. We are, I have suggested, in good epistemological company. But this only sharpens the epistemological question. The signified of modeling vanishes into the murk because we lack a disciplined way of talking about it. Methods are explicit, actions definite, results forthcoming, yet we have been unable fully and persuasively to articulate the intellectual case for the means by which these results are produced. Hence the just-a-tool status of computing, the not-a-discipline slur, the tradesman’s entrance or other back door into the academy. No one doubts the usefulness of the practice. Rather it’s the intellection of praxis to which the next stage in the argument I have begun here must turn.

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