



Universidad de
los Andes



**FACULTAD
DE INGENIERÍA
Y CIENCIAS
APLICADAS**

Finite Elements

Homework N°3 - Final Report

Professor:

Jose Antonio Abell

Assistance:

Nicolás Mora

Students:

Felipe Vicencio

Lukas Wolff

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1 Introduction

Over the course of this exercise, we have deepened our understanding of three core aspects. Comprehending the Quad4 and Quad9 elements, implementing design and analysis of structures on GMSH *software* and optimizing the structures depending on its internal stresses and displacements.

2 Results

As the complete structure to analyze was symmetrical, only a half of it was modeled with a transfinite mesh and studied, as shown bellow.

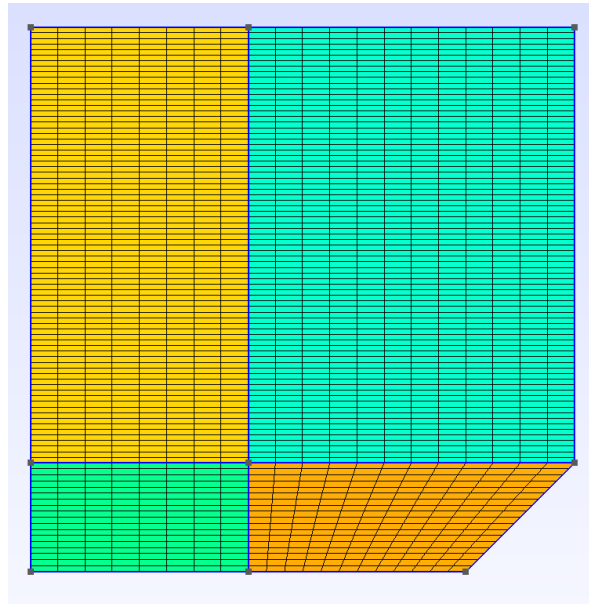


Figure 1: Half structure modeled in GMSH

2.1 Part b) PONER LOS GRAFICOS LOCALES

In this section, a stress analysis was made over 4 different mesh sizes using two refinement techniques, global and local refinement, for both element types.

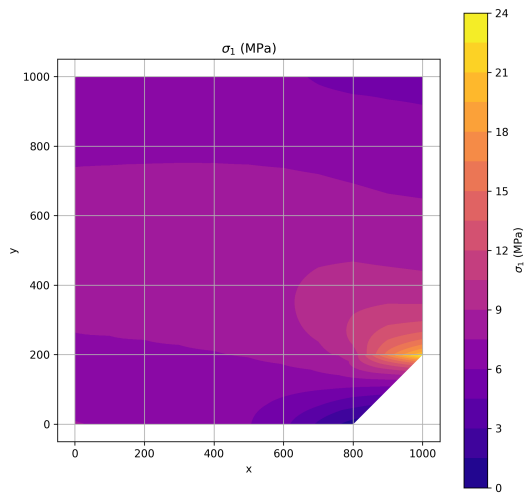
For the global refinement, the characteristic size h was modified uniformly across the entire mesh, varying its value from 2 mm up to 1.25 mm. These values were determined based on the time required for the simulation to run and the capacity of the software to refine the mesh.

In the case of local refinement, the characteristic size h was modified in a specific region of the mesh, near the stress concentration area, in other words, the right border. For this to be studied, the number of elements was higher in that zone compared to the left border.

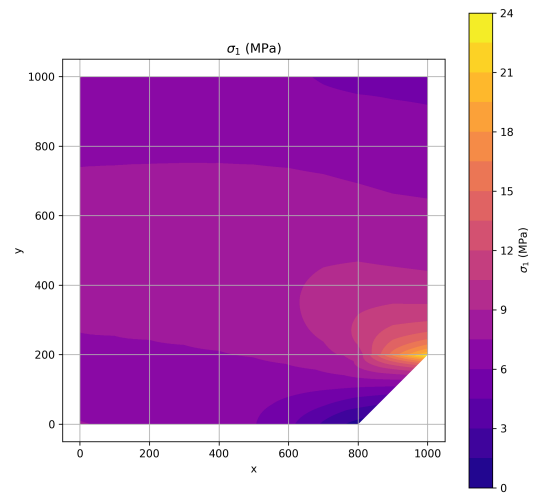
The results of refining the mesh globally and locally are shown in the following sections.

2.1.1 Quad4 Element

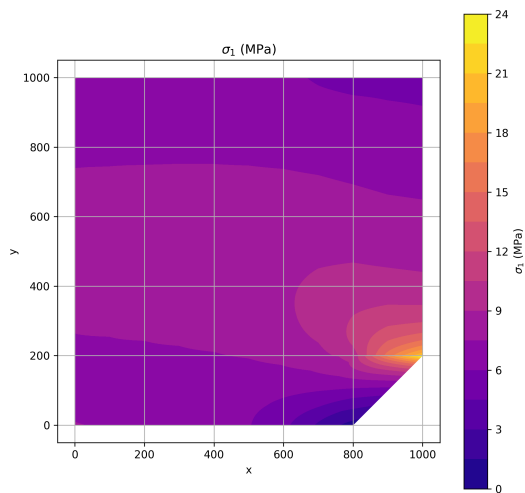
The following maps shows how the stress distribution changes with the mesh size as it is refined using Quad4 elements.



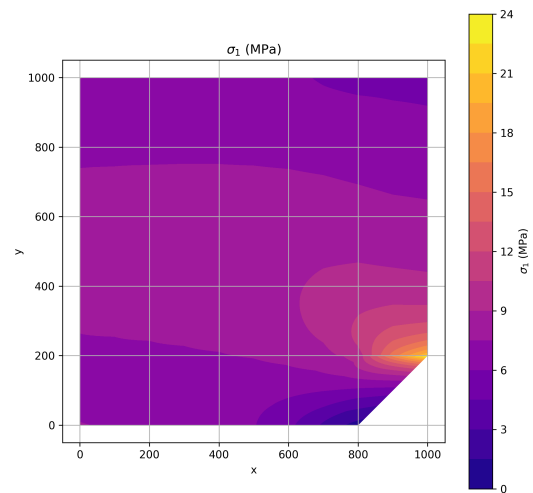
(a) Global mesh refinement - $h = 2mm$



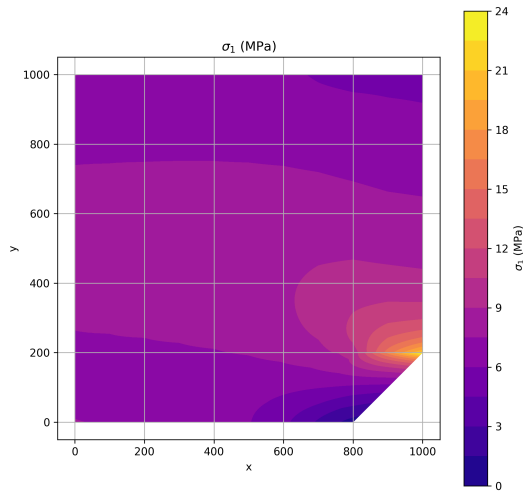
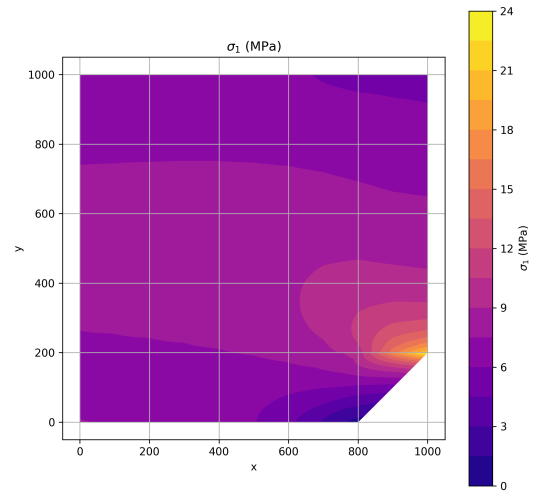
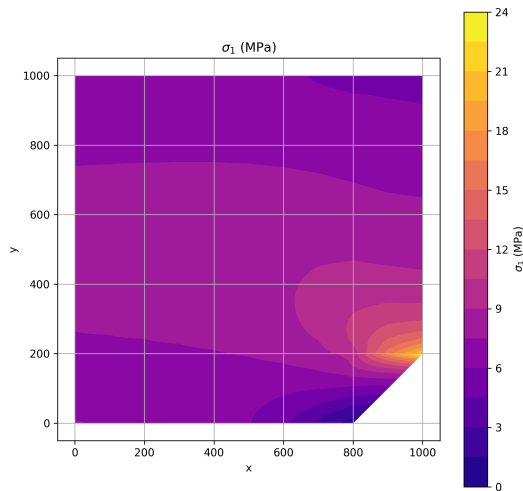
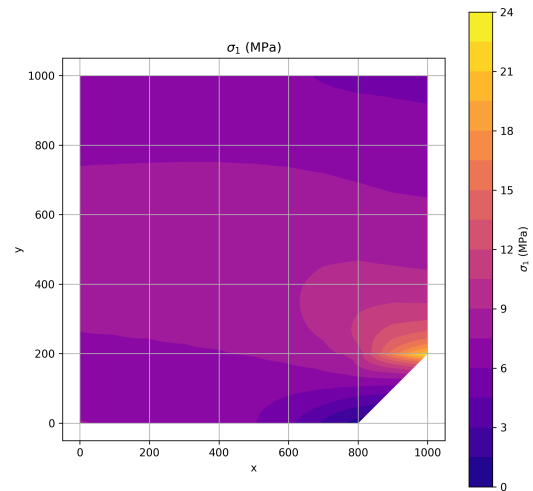
(b) Local mesh refinement - $h = 2mm$



(a) Global mesh refinement - $h = 1.75mm$

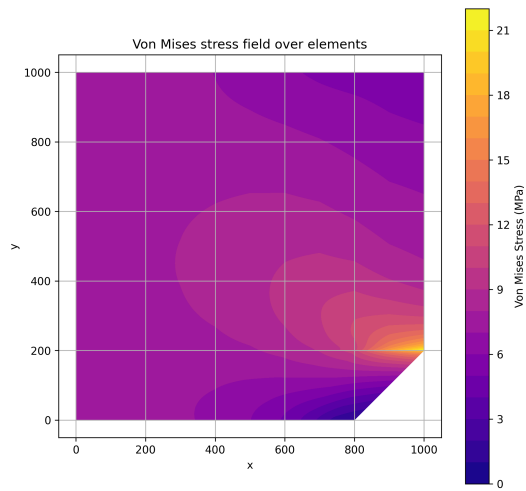


(b) Local mesh refinement - $h = 1.75mm$

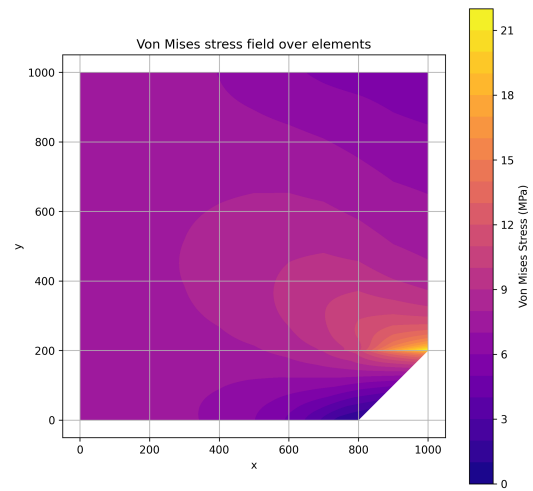
(a) Global mesh refinement - $h = 1.5mm$ (b) Local mesh refinement - $h = 1.5mm$ (a) Global mesh refinement - $h = 1.25mm$ (b) Local mesh refinement - $h = 1.25mm$

2.1.2 Quad9 Element

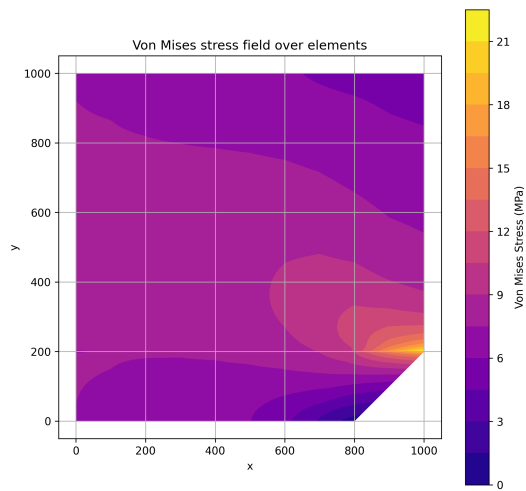
In this section, the same procedure was followed, but increasing the order of the mesh elements to Quad9.



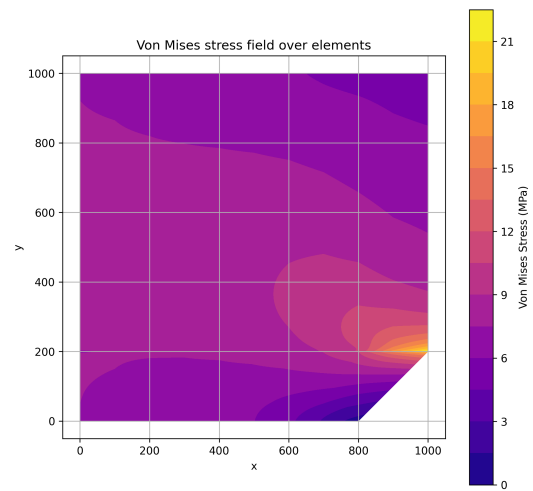
(a) Global mesh refinement - $h = 2mm$



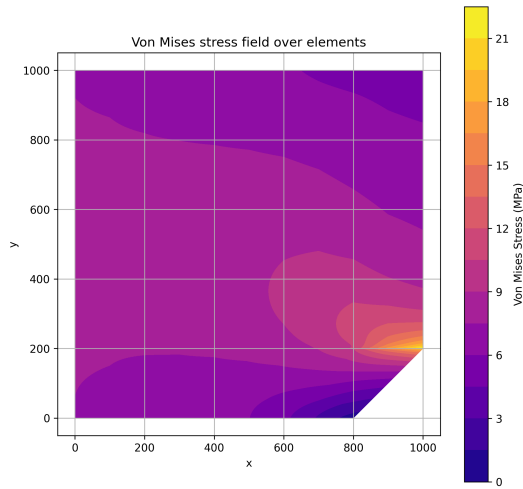
(b) Local mesh refinement - $h = 2mm$



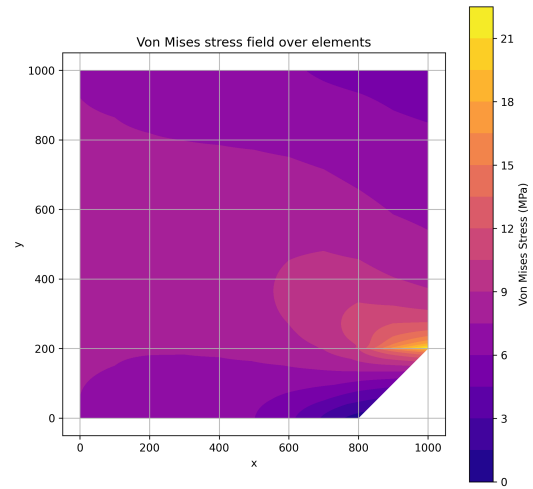
(a) Global mesh refinement - $h = 1.75mm$



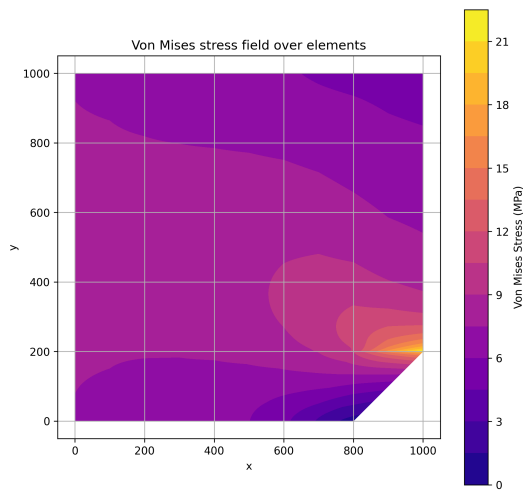
(b) Local mesh refinement - $h = 1.75mm$



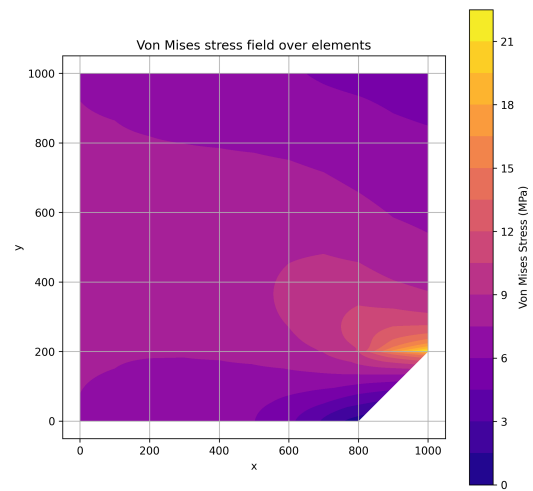
(a) Global mesh refinement - $h = 1.5mm$



(b) Local mesh refinement - $h = 1.5mm$



(a) Global mesh refinement - $h = 1.25mm$



(b) Local mesh refinement - $h = 1.25mm$

2.2 Part c)

In this section, an optimization of the structure was made. Moreover, it was modeled and simulated, resulting in a complete stress and behaviour analysis.

The main objective was to annulate the stress concentration sections, in order to reduce the maximum stress in the structure and compare it with the previous results.