

Curvy Little Bottles

Por ICPC 2012 World Finals  Poland

Timelimit: 3

In her bike rides around Warsaw, Jill happened upon a shop that sold interesting glass bottles. She thought it might make an interesting project to use such bottles for measuring liquids, but this would require placing markings on the bottles to indicate various volumes. Where should those volume marks be placed?

Jill formalized the problem as follows. Assume a bottle is formed by revolving a shape that is the same as the graph of a polynomial P between $x = x_{\text{low}}$ and $x = x_{\text{high}}$ around the x -axis. Thus the x -axis is coincident with a vertical line through the center of the bottle. The bottom of the bottle is formed by a solid circular region at $x = x_{\text{low}}$, and the top of the bottle, at $x = x_{\text{high}}$, is left open.

The first sample input represents a bottle formed using the simple polynomial $4 - 0.25x$, with $x_{\text{low}} = 0$ and $x_{\text{high}} = 12$. The bottom of this bottle is a circle with a radius of 4, and the opening at the top is a circle with a radius of 1. The height of this bottle is 12. Volume markings are in increments of 25.

Given a polynomial P , x_{low} , x_{high} , and the volume increment between successive marks on the bottle, compute the distances up from x_{low} for the marks at successive volume increments. A mark cannot be made past the top of the bottle, and no more than the first 8 increments should be marked. Assume the value of P is greater than zero everywhere between x_{low} and x_{high} .

Entrada

Each test case consists of three lines of bottle data:

- Line 1: n , the degree of the polynomial (an integer satisfying $0 \leq n \leq 10$).
- Line 2: a_0, a_1, \dots, a_n , the real coefficients of the polynomial P defining the bottle's shape, where a_0 is the constant term, a_1 is the coefficient of x^1 , \dots , and a_n is the coefficient of x^n . For each i , $-100 \leq a_i \leq 100$, and $a_n \neq 0$.
- Line 3:
 - x_{low} and x_{high} , the real valued boundaries of the bottle ($-100 \leq x_{\text{low}} < x_{\text{high}} \leq 100$ and $x_{\text{high}} - x_{\text{low}} > 0.1$).
 - inc , an integer which is the volume increment before each successive mark on the bottle ($1 \leq \text{inc} \leq 500$).

Saída

For each test case, display the case number and the volume of the full bottle on one line. On a second line, display the increasing sequence of no more than 8 successive distances up from the bottom of the bottle for the volume markings. All volumes and height marks should be accurate to two decimal places. If the bottle does not have a volume that allows at least one mark, display the phrase 'insufficient volume'. No test case will result in a mark within 0.01 from the top of the bottle. The volume of the bottle will not exceed 1 000. All rounded distances for marks on a bottle differ by at least 0.05.

Exemplo de Entrada	Exemplo de Saída
1	Case 1: 263.89
4.0 -0.25	0.51 1.06 1.66 2.31 3.02 3.83 4.75 5.87
0.0 12.0 25	Case 2: 263.89

1	Exemplo de Entrada	insufficient volume	Exemplo de Saída
4.0 -0.25		Case 3: 50.00	
0.0 12.0 300		2.00 4.00	
0		Case 4: 31.42	
1.7841241161782		3.18 6.37 9.55	
5.0 10.0 20			
0			
1.0			
0.0 10.0 10			