

Homework 5 Problem 1

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Question 1. H_0 : Mean engagement of students who become knowledgeable in the material is equal to 0.75
 H_A : Mean engagement of students who become knowledgeable in the material is not equal to 0.75. * We can use z-test

Question 2. Sample Size (N) = 937 z -score = 1.67819

Sample Mean ($\text{avg}-1$) = 0.743 p -value = 0.04665

Standard Error ($SE-1$) = 0.00415

The results are significant at a level of 0.1 and 0.05. However they are not significant at a level of 0.01. At the levels of 0.1 and 0.05 we can conclude that the mean engagement of students is equal to 0.75. At a level of 0.01 we would not conclude this.

Question 3 z -score = 1.65 p -value = 0.95053 (closest p -value that is still significant at a level of 0.05)

Sample Mean ($\text{avg}-1$) = 0.743

$$z = \frac{\bar{X} - \mu}{\frac{SE}{\sqrt{n}}} = \frac{0.743 - 0.75}{\frac{0.00422}{\sqrt{n}}} = -1.65$$

$$0.00422 = \frac{0.12713}{\sqrt{n}} \quad n = 905.78 \quad \text{Largest SE: } 0.00422$$

Smallest Sample: 906

Question 4. H_0 : Mean engagement between groups of students are equal
 H_A : Mean engagement between groups of students is not equal
 We can use a z-test

Question 5. Engagement 0 Sample Size ($N-0$) = 1977

Engagement 1 Sample Size ($N-1$) = 937

Engagement 0 Sample Mean ($\text{avg}-0$) = 0.63995

Engagement 1 Sample Mean ($\text{avg}-1$) = 0.74303

Standard Error ($SE - \text{avg}$) = 0.00493

z -score = 20.88879

p -value = 0

We can conclude that results are not significant at levels 0.1, 0.05, and 0.01. More importantly we reject H_0 and conclude that the engagement level between the groups of students is not equal.

* File HWS Problem 1 was used to answer all Questions on this page

Homework 5 Problem 2

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Question 1. I will use a t-test because the population standard deviation is unknown.

$$\text{Sample Mean (avg)} = -5.83333 \quad \text{standard statistic (t-stat)} = 1.36343$$

$$\text{Standard Error (SE)} = 5.06299 \quad \text{interval} = [1.06969, -12.73636]$$

Question 2. I will use a t-test because the population standard deviation is unknown.

$$\text{Sample Mean (avg)} = -5.83333 \quad \text{standard statistic (t-stat)} = 1.71588$$

$$\text{Standard Error (SE)} = 5.06299 \quad \text{interval} = [3.25921, -14.92588]$$

The intervals are pretty similar but the interval from question 2 is a little bit larger in size.

Question 3. We are now able to use a z-test because we are given the population standard deviation. The standard error will change because of this and we will now have a z-score instead of a t-score.

$$\text{Sample Mean (avg)} = -5.83333 \quad \text{Standard Statistic (ZScore)} = 1.64485$$

$$\text{Standard Error (SE)} = 4.86013 \quad \text{interval} = [2.49434, -14.92587]$$

The results are very similar to the results from part 2. The results are not as close to part 1 though.

Question 4. $CI = (\bar{x} + SE \cdot t_c, \bar{x} - SE \cdot t_c)$ $\bar{x} = \text{Sample Mean} = -5.83333$

$$0 = \bar{x} + SE \cdot t_c \quad \text{Standard Error (SE)} = 5.06299$$

$$0 = -5.83333 + 5.06299(t_c) \quad p = t.cdf(1.15217, N-1)$$

$$t_c = \frac{5.83333}{5.06299} = 1.15217 \quad p = 0.86316$$

$$5.06299$$

We can say with a 86.32% confidence level that the team is expected to lose on average

* File HWS Problem 2 was used to answer all questions on this page