

A12 · Linear Regression

Introduction

Assignment Goals

This assignment uses Excel to build on the least squares analysis you learned in ENGR 131 and then adds two MATLAB linear regression problems with engineering contexts.

Successful Completion

This assignment has **3** problems. The deliverables list contains everything you are expected to submit individually.

Submit Problem 1 to the Gradescope online assignment A12 – Skills Problems		
Problem	Type	Deliverables
Problem 1: Excel Linear Regression	Individual	<input type="checkbox"/> A12Prob1_bugReports_login.xlsx <input type="checkbox"/> Requested results and information <input type="checkbox"/> A12Prob1_figure_login.png*
Submit Problems 2 and 3 to the Gradescope programming assignment A12 – Context Problems		
Problem	Type	Deliverables
Problem 2: Greenhouse Gas Analysis	Individual	<input type="checkbox"/> A12Prob2_airPollution_login.m <input type="checkbox"/> Supporting files: <ul style="list-style-type: none"> ○ A12Prob2_CO2figure_login.png ○ A12Prob2_SF6figure_login.png ○ Data_NOAA_ESRL_co2_trend_1980-2020.csv ○ Data_NOAA_ESRL_sf6_trend_1997-2020.csv
Problem 3: Solar Panel Output	Individual	<input type="checkbox"/> A12Prob3_panelOutput_login.m <input type="checkbox"/> Supporting files: <ul style="list-style-type: none"> ○ A12Prob3_figure_login.png ○ Data_panelX5_output_measurements.csv

1. Read *Notes Before You Start*, on **Page 2**.
2. Read each problem carefully. You are responsible for following all instructions within each problem.
 - a. Problems 2 and 3 has a team planning component that you are expected to submit separately from your deliverables. Read the instructions within that problem.
3. Complete the problems using the problem-specific m-file templates provided in the assignment download. Replace *template* in the filename with your Purdue Career Account login
4. When your work is complete, confirm your deliverables and your team plans are submitted to Gradescope.

Learning Objectives & Grading

This course uses learning objectives (LOs) to assess your work. You can find a list of the course LOs on Brightspace (Content > Key Course Info > Learning Objectives). Review the assignment grading for each problem in this assignment, which starts on **Page 10**. This outlines how your work will be graded for each problem.

Notes Before You Start

Helpful MATLAB Commands

Learn about the following built-in MATLAB commands, which might be useful in your solutions:

`polyfit`, `polyval`

Gradescope

You will submit all your deliverables to Gradescope for grading. This homework has **two** Gradescope submission assignments for the individual submissions, plus a **third** assignment for the team planning component:

- **A12 – Skills Problems:** submit your deliverables for Problem 1
- **A12 – Context Problems:** submit your deliverables for Problems 2 and 3
- **A12 – Team Planning:** submit your team plan for Problems 2 and 3 as a team

Problem 1: Excel Linear Regression

Introduction

This problem has you using Excel to determine least squares model and goodness of fit for a data set. You will compare models and discuss their differences. And, you will use your knowledge of your data set to make reasonable predictions using your model.

Problem

A software bug is an unexpected result or failure in a released software package. All complex software has bugs in it. Most are minor, and some are even famous, like the [Minus World](#) in Super Mario Bros. But sometimes a software bug contributes to a catastrophic failure, as in the massive 2003 electrical grid [blackout](#) in the United States and Canada that affected approximately 50 million people.

To minimize negative effects, software producers track, manage, and fix bugs through new updates or new releases. A software firm has provided data that contains bug reports for one of their major software packages. The company determined a model to predict how the number of bug reports changes over time, $N = -5.4t_r + 220$, where N is the number of bugs reported and t_r is the time since release (in months).

You must perform least-squares regression to find a new model for the number of software bugs reported as a function of time since the software's initial release. You will find the data in the CALCULATIONS sheet of the provided Excel template.

Instructions

Excel Calculations

Using the **CALCULATIONS** sheet in the Excel template, you must

1. Use the data and the least-squares equations to determine the least-square line for the data.
2. Plot the data and confirm your least-squares line using Excel's "add a trendline" feature. Show both the model equation and the r-squared value. Update the equation display using clear and appropriate variable names in place of x and y . Format the plot for technical presentation.
3. Determine the goodness of fit (SSE, SST, and r^2) for both the provided model and your least-squares model.

Save a plot image

After you have completed the calculations and created the plot, you need to save an image of your Excel plot that shows the data, the trendline, and the least-squares model (as described in Step 2 above). Save an image of your Excel plot with the trendline and r-squared value visible.

- If you have a Mac, right click the chart and select "Save as picture".
- If you have Windows, you may need to Copy the figure, paste into Powerpoint as an image, right click the image in Powerpoint and select "Save as picture".

*You can use any image file type (png, jpg, tiff, etc.) but name the file appropriately.

Answer Questions & Submit to Gradescope

After you complete the calculations, open Gradescope and select the assignment **A12 – Skills Problems**. You will find 5 parts within **Q1**. Excel – Linear Regression. Answer all the questions and their parts. Save your answers periodically in case you lose internet connection or need to stop working on the assignment before it is complete.

- a. Submit your XLSX file, with the appropriate file name.
- b. Submit your plot image, with the appropriate file name.
- c. Answer the questions presented in Gradescope.

Note: Failure to submit the XLSX workbook will result in a 0 on this problem.

Problem 2: Greenhouse Gas Analysis

Introduction

This problem will allow you to apply linear regression concepts to data sets that contain environmental data used in news, commercial, academic, and scientific settings. You will discuss what you know about the models using your knowledge of the data.

Problem

Environmental engineers develop solutions to minimize air pollution. Carbon dioxide (CO₂) and sulfur hexafluoride (SF₆) emissions are significant greenhouse gases. The National Oceanic and Atmospheric Administration's Earth System Research Laboratory (ESRL) maintains records of atmospheric greenhouse gas concentrations.

For this problem, you must model the global trend in CO₂ and SF₆ atmospheric concentrations. You will find the CO₂ data, with its complete NOAA header, in the file named **Data_NOAA_ESRL_co2_trend_1980-2020.csv** and the SF₆ data in the file **Data_NOAA_ESRL_sf6_trend_1997-2020.csv**.

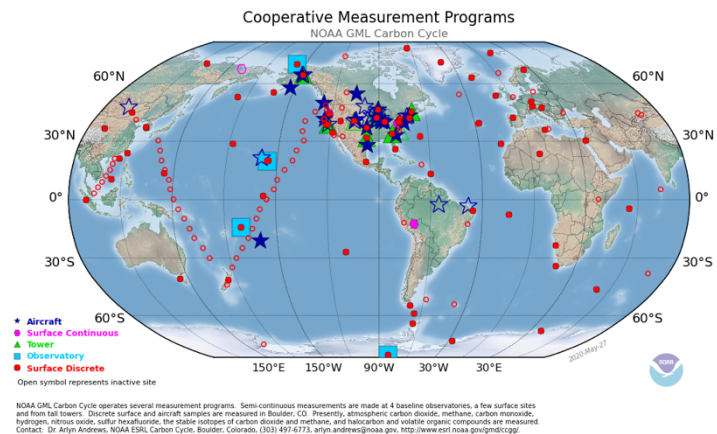
Write a MATLAB no-input, no-output function to perform least squares regression on the provided data. You will model average CO₂ (in ppm) as a function of decimal year and then model average SF₆ (in ppt) as a function of decimal year. Your function must

- Perform linear regression on the data to get the least-squares coefficients, first for CO₂ and then for SF₆.
- Determine the predicted values of each linear model.
- Calculate SSE, SST, and r^2 values for each model.
- Display the linear model equation (with clear variable names), SSE, SST, and r^2 to the Command Window for each model. Make sure you can differentiate between the information for CO₂ and SF₆.
- Generate two figures: one figure that displays the data and the trend line on the same axes for CO₂ and a second figure that displays the data and trend line on the same axes for SF₆. Format both figures for technical presentation.

In the **ANALYSIS** section, answer the following questions:

- Q1. With the given data, can you draw a conclusion about the accuracy of the data measurements? Provide justification for your answer.
- Q2. For which data set does a linear model best explain the variation that exists in the data? Clearly state the basis of your reasoning.
- Q3. You want to see the long-term trends in CO₂ over a 100-year span. Predict the CO₂ levels at year 1950.0, 2000.0, and 2050.0. Report your results and justify your response using your knowledge of the data.

You will need to submit an image file for each of your figure windows. From the figure window, select **File > Save As**. Set the file format to PNG. Name the files using the format given in the assignment instructions.



Instructions

1. Read through the entire problem statement.
2. **With your teammates:** develop and document a plan to solve this problem.
 - a. Understand the expectations of the problem.
 - b. Discuss strategies for solving the problem. These can include citing examples from class notes, drawing pictures, outlining a plan using text or pseudocode, etc. **DO NOT SHARE CODING SOLUTIONS.**
 - c. Submit your plan to the team assignment in Gradescope
 1. Open the Gradescope assignment **A12 – Team Planning**.
 2. In the area for Problem 2:
 - a. Enter the names of your teammates who participated in the planning.
 - b. Enter a brief description of your team's plan to solve the problem. The plan should be connected to the problem and have at least 2-3 steps. It should not be a detailed explanation of every step necessary to solve the problem.
 - c. If you have image files, etc., that you would prefer to share, you may add them in the *Optional* file submission area.
 3. Save your results.
 - d. Add your teammates to the submission. Select 1 team member to submit the plan. Work together to make sure it is done correctly.
 1. Click **Submit & View Submission** at the bottom of the assignment
 2. Add all teammates to the group ([Gradescope instruction link](#))
 3. All teammates confirm that you get an email confirming the submission and verify that you can see the submission in your Gradescope.
3. **Individually:**
 - a. Complete your function, run it to get your results, and save the figure window as an image.
 - The team plan is an initial start on the problem. It may not be completely correct, and you may find flaws in the plan once you start coding. You should make any individual changes that are necessary to obtain the best solution. You will be assessed on your individual solution to the problem.
 - b. Cite the teammates you worked with in your script header if their help changed how you decided to solve the problem.
 1. Make sure you also completed the rest of the script header.
 - c. Submit your properly named files to **A12 – Context Problems** in Gradescope.

Problem 3: Solar Panel Output

Introduction

You will combine linear regression, selection structures, and user-defined functions in this problem. Use your knowledge of functions to allow a user to predict values using the model you develop within the program. Use your knowledge of your data to design the function to make reasonable predictions using the model.

Problem



You work for a solar energy company and are interested in the electricity production of a new residential solar panel your team is developing. Your teammates ran an experiment where they installed a test panel and monitored the electric output at different sunlight levels. The experiment results are in the data file

Data_panelX5_output_measurements.csv. The amount of sunlight is measured in [peak sun hours](#) (hr) and the electrical output is measured in kilowatt-hours (kWh).

You must create a model of the data provided that can be used to estimate a panel's output for a range of peak sun hours. Write a user-defined function that does two things.

First, it will find the least squares model for the data and second, it will accept one peak sun value and return the predicted electrical output. Your function must do the following:

- Use the data to determine the least-squares model for the data.
- Plot the data and model on the same axes, formatted for technical presentation.
- Display the linear model equation (with clear variable names), SSE, SST, and r^2 to the Command Window.
- Accept one input: a value for peak sun hours
- Return one output: a predicted electrical output value for the input peak sun value.
- Display the predicted electrical output to the Command Window along with the peak sun time used to make the prediction.
 - Use your knowledge of the data to determine if there needs to be an explanation of the reliability of the prediction. Use a selection structure to display different justifications, if necessary.
 - Your function must determine a value for the predicted electrical output so that the program does not generate an error.

Once your function is working properly, call it from the Command Window. First, use a peak sun value of 4.8 hours and then use a peak sun value of 7.5 hours. Copy your function calls and the text displays and paste them as comments into the **RESULTS** section of your function.

You will need to submit an image file for each of your figure windows. From the figure window, select **File > Save As**. Set the file format to PNG. Name the files using the format given in the assignment instructions.

Instructions

4. Read through the entire problem statement.
5. **With your teammates:** develop and document a plan to solve this problem.
 - a. Understand the expectations of the problem.
 - b. Discuss strategies for solving the problem. These can include citing examples from class notes, drawing pictures, outlining a plan using text or pseudocode, etc. **DO NOT SHARE CODING SOLUTIONS.**
 - c. Submit your plan to the team assignment in Gradescope
 1. Open the Gradescope assignment **A12 – Team Planning**.
 2. In the area for Problem 3:
 - a. Enter the names of your teammates who participated in the planning.
 - b. Enter a brief description of your team's plan to solve the problem. The plan should be connected to the problem and have at least 2-3 steps. It should not be a detailed explanation of every step necessary to solve the problem.
 - c. If you have image files, etc., that you would prefer to share, you may add them in the *Optional* file submission area.
 3. Save your results.
 - d. Add your teammates to the submission. Select 1 team member to submit the plan. Work together to make sure it is done correctly.
 1. Click **Submit & View Submission** at the bottom of the assignment
 2. Add all teammates to the group ([Gradescope instruction link](#))
 3. All teammates confirm that you get an email confirming the submission and verify that you can see the submission in your Gradescope.
6. **Individually:**
 - a. Complete your function, run it to get your results, and save the figure window as an image.
 - The team plan is an initial start on the problem. It may not be completely correct, and you may find flaws in the plan once you start coding. You should make any individual changes that are necessary to obtain the best solution. You will be assessed on your individual solution to the problem.
 - b. Cite the teammates you worked with in your script header if their help changed how you decided to solve the problem.
 1. Make sure you also completed the rest of the script header.
 - c. Submit your properly named files to **A12 – Context Problems** in Gradescope.

Confirm Your Submission

Problem 1

You should save your progress on each question in a skills problem so that you do not lose your progress. To confirm your answers, click the **Submit & View Submission** button at the bottom of the questions in Gradescope (or select the assignment name from the Gradescope dashboard, if you have already saved your answers and navigated away from the original submission page).

Confirm that your submission for **A12 – Skills Problems** includes

- ☐ The expected deliverables and results;
- ☐ Correct file names for any submitted files, including your Career Account login at the end where required.

You can resubmit your work as many times as you want, but only the final submission will be graded.

Problems 2 and 3 – Individual deliverables

Confirm that your submission for **A12 – Context Problems** includes

- ☐ The expected deliverables and results;
 - This includes m-files, data files, and image files for each problem you complete.
- ☐ Correct file names for any submitted files, including your Career Account login at the end where required.

Do NOT upload any document not listed in the deliverables. Do not upload temporary versions of m-files (*.m~ or *.asv) – these files will be ignored by Gradescope and not included in your upload.

You can resubmit your work as many times as you want, but only the final submission will be graded.

Problem 3 – Team plans

Confirm that your submission for **A12 – Team Planning** includes

- ☐ The names of all your teammates who participated in each problem's planning;
- ☐ A brief description of the team's plan for each problem;
- ☐ All team members included in the group submission.

You can resubmit your work as many times as you want, but only the final submission will be graded.

References

Ed Dlugokencky, NOAA/GML (www.esrl.noaa.gov/gmd/ccgg/trends_sf6/)

Ed Dlugokencky and Pieter Tans, NOAA/GML (www.esrl.noaa.gov/gmd/ccgg/trends/)

<https://rtc.sandia.gov/>

Assignment Grading

Your work will be graded using the evidences given in the course learning objectives. Familiarize yourself with the LOs and their evidences listed for each problem, which are below. Each non-skill problem's assignment grading has a table and a flowchart. The table outlines what LOs will be used to grade your work and what point values are assigned to each evidence. The flowchart outlines the grading process that a grader will use to assess your work.

Find the list of the course LOs, with evidences, on Brightspace (Content > Key Course Info > Learning Objectives).

Team Planning

Each problem's plan is worth 1 point.

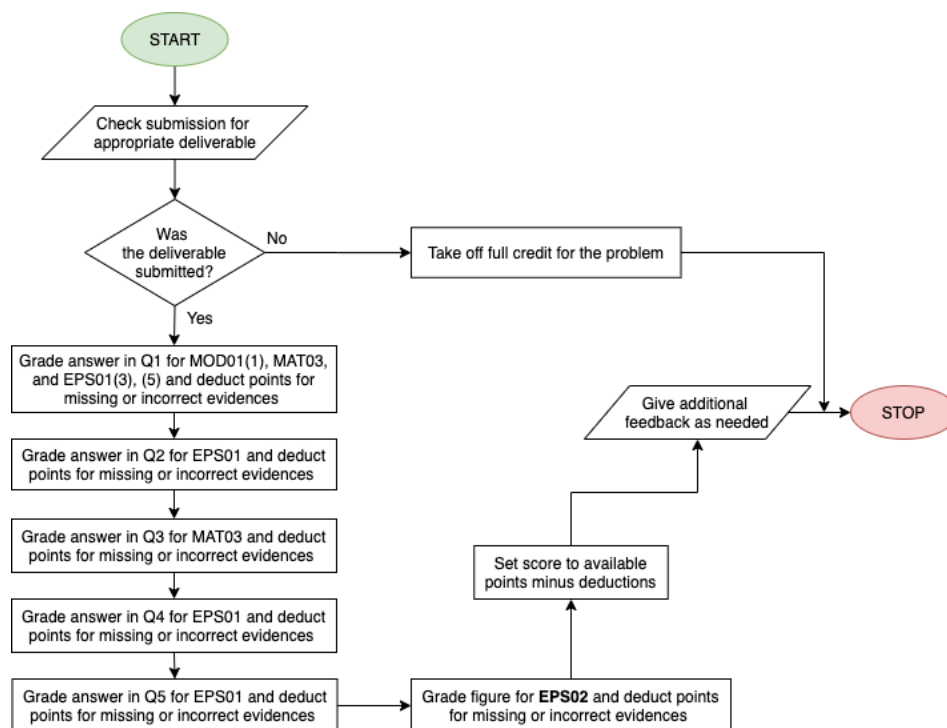
Individual Problems

LO Table

	Points
Q.2.(1)	1.6
Q.2.(2)	0.8
Q.2.(3)	0.8
Q.2.(4)	1.6
Q.2.(5)	1.6
Figure	1.6

Deduct 2 points from PC05 if late, 0.4 points if a file has the incorrect name. Deduct full credit if the XLSX sheet is not submitted.

Grading Process



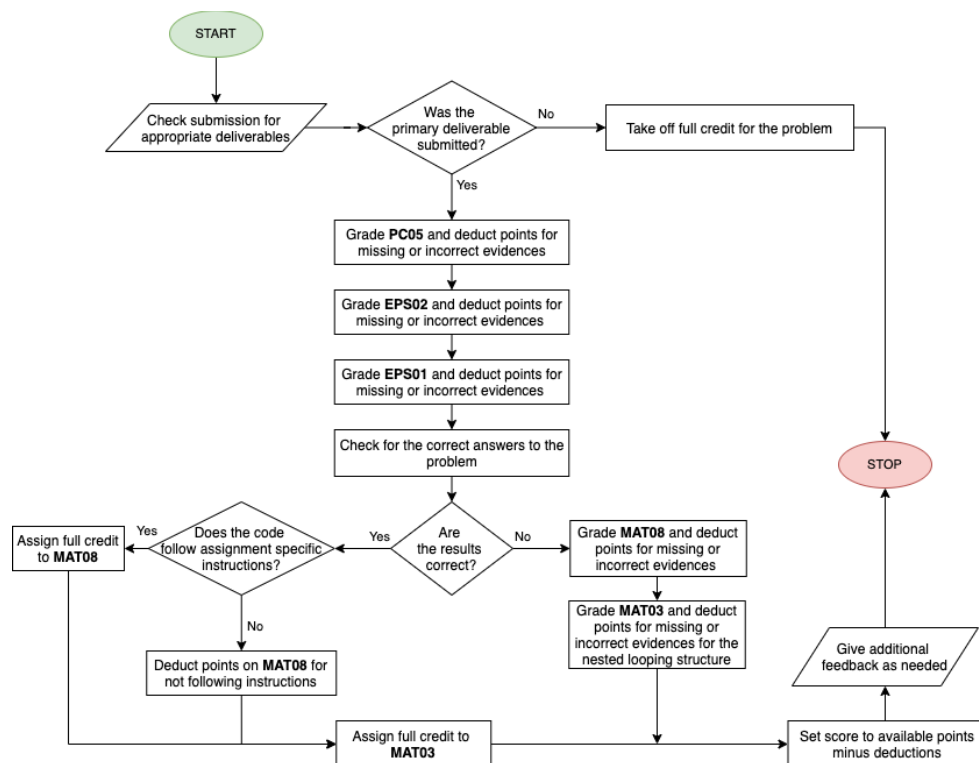
Problem 2

LO Table

Note: PC05 evidences are only deductions since you are expected to follow the assignment instructions.

	PC05	EPS02	EPS01	MAT08	MAT03
(1)	-6	0.3	0.2	0.2	0.2
(2)	-1.5	0.2	1	1	0.2
(3)	-1.5	0.3	0.2	0.5	0.2
(4)	-0.3	0.3	0.2	0	0.2
(5)	0	0.2	0.2	0	0
(6)	0	0.3	0	0	0
(7)	0	0.1	0	0	0
(8)	0	0	0	0	0

Grading Process



Problem 3**LO Table**

Note: PC05 evidences are only deductions since you are expected to follow the assignment instructions.

	PC05	EPS02	EPS01	MAT08	MAT03	MAT05	MAT06
(1)	-6	0.1	0.2	0.5	0.2	0.2	0
(2)	-1.5	0.1	1	1	0.2	0.2	0.1
(3)	-1.5	0.1	0.2	0.5	0.2	0	0.1
(4)	-0.3	0.1	0.2	0	0.2	0	0.1
(5)	0	0.1	0.2	0	0	0	0.1
(6)	0	.1	0	0	0	0	0
(7)	0	0.1	0	0	0	0	0
(8)	0	0	0	0	0	0	0

Grading Process