



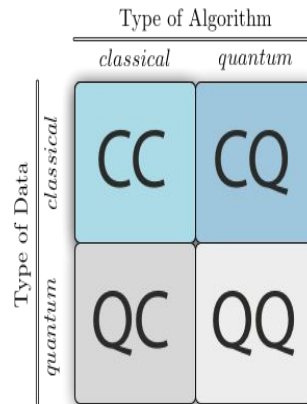
Quantum AI Mini Seminar Series:

Session 2: Quantum Machine Learning

- Overview
- Variational Quantum Eigensolver
- Quantum Approximate Optimization Algorithm (QAOA)
- Data Encoding in Quantum Systems
- Challenges in Quantum AI

Overview

- Quantum Machine Learning
- Applications
 - Classification: QSVM
 - Optimization: VQE, QAOA
 - Pattern Recognition: Quantum Clustering
- Capabilities



Four different approaches to combine the disciplines of quantum computing and machine learning.



Definition of QML:

- QML is the integration of **quantum mechanics** into **machine learning models** to solve complex problems with enhanced speed and efficiency.

Applications in ML Tasks:

- **Classification:** Quantum Support Vector Machines (QSVM).
- **Optimization:** Algorithms like **VQE** and **QAOA** reduce steps in cost function minimization.
- **Clustering and Pattern Recognition:** Quantum-based clustering shows promise for high-dimensional data analysis.

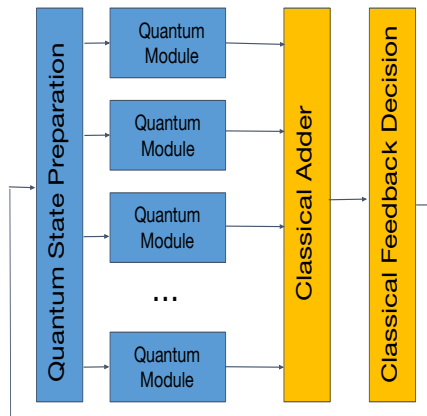
Potential Impact on Machine Learning:

- **Enhanced processing power** for complex models.
- **Parallelism** allows evaluation of multiple states at once.
- May reduce computation times for **optimization, data processing, and training** tasks.

Session Focus:

- Key QML algorithms: **Variational Quantum Eigensolver (VQE)**, **Quantum Approximate Optimization Algorithm (QAOA)**.
- **Data encoding** methods in quantum systems.
- Current **challenges** limiting quantum computing in AI.

Variational Quantum Eigensolver (VQE)



- Hybrid Algorithm
 - Initialize parameters (θ)
 - Layers of rotation/entangling gates
 - Quantum measurement
 - Classical Optimization
 - Repeat until convergence on minimum eigenvalue
- Suitable for optimizing neural network hyperparameters.



VQE Overview:

- **Hybrid Algorithm:** Combines **quantum processing** and **classical optimization** to solve for the lowest eigenvalue of a Hamiltonian.
- Used in **optimization** problems, analogous to finding the minimum of a **cost function** in AI.

How VQE Works:

1. **Parameterized Quantum Circuit:**
 - Initialize parameters $\theta = \{\theta_1, \theta_2, \dots, \theta_n\}$
 - Circuit structure: Layers of **rotation gates** and **entangling gates**.
2. **Quantum Measurement:**
 - Evaluate $\langle \psi(\theta) | H | \psi(\theta) \rangle$ for cost function.
3. **Classical Optimization:**
 - Adjust parameters θ to minimize the cost function with classical optimizers (e.g., **gradient descent**).
 - Repeat until convergence on **minimum eigenvalue**.

Circuit Example:

- **Circuit Layout:** Alternating layers of **single-qubit rotation gates** and **CNOT gates** for entanglement.
- **Equation for Expectation:** $E(\theta) = \langle \psi(\theta) | H | \psi(\theta) \rangle$

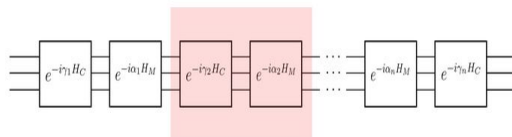
- $H | \psi(\theta) \rangle E(\theta) = \langle \psi(\theta) | H | \psi(\theta) \rangle$
- Goal: Minimize $E(\theta)$ to approximate the ground state energy.

AI Application:

- VQE can be applied to **optimize neural networks** by encoding network parameters in the quantum circuit.
- Uses fewer steps for **cost function minimization** than classical methods, potentially speeding up training times.

Quantum Approximate Optimization Algorithm (QAOA)

- Algorithm
 - Initialize parameters β and γ : Define layers based on problem
 - Two-step circuit
 - Phase Operator
 - Mixing Operator
 - Iterate Parameters to maximize solution probability
- Well-suited for graph-based optimization



QAOA Overview:

- **Objective:** Approximate solutions for **combinatorial optimization problems**.
- Uses a **parameterized quantum circuit** to iteratively adjust solution probabilities.

Algorithm Steps:

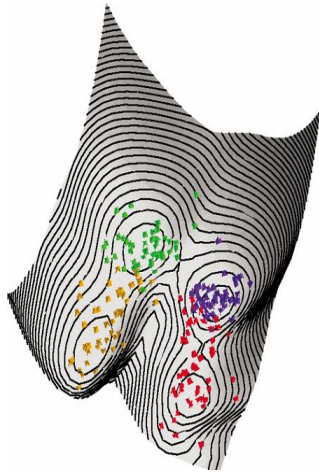
1. **Initialize Parameters** β and γ :
 - Define layers based on the optimization problem.
2. **Two-Step Circuit:**
 - **Phase Operator:** Applies constraints of the problem, rotating by γ .
 - **Mixing Operator:** Rotates state with parameter β , exploring other potential solutions.
3. **Iterate Parameters:**
 - Adjust β and γ to maximize probability of finding optimal solution.

Circuit Structure:

- **Phase Separation Layer:** Applies $e^{-i\gamma H_C} e^{-i\gamma H_M}$ to encode constraints.
- **Mixing Layer:** Applies $e^{-i\beta B} e^{-i\beta B}$ to mix states, encouraging exploration.

- QAOA is well-suited for **graph-based optimization** in AI, including tasks like **graph partitioning**, **scheduling**, and **route optimization**.
- Faster than classical algorithms for problems with complex constraints.

Quantum Clustering



- Quantum Clustering
 - a. Amplitude Encoding
 - b. Distance Measurement
 - c. Entanglement
- Dynamic Quantum Clustering
 - a. Continuously adapts clusters
 - b. Field gradient evolutions
 - c. Wavefunction representation
- Limited Basis Approach
 - a. Limits number of basis states
 - b. Conserves resources



Quantum Clustering Overview:

- Quantum clustering involves mapping data points into **quantum states** to perform clustering with quantum principles like **superposition** and **entanglement**.
- Each data point is represented as a quantum state $|x\rangle$ in a high-dimensional **Hilbert space**. Clusters are then identified by measuring the similarities between these states.
- Quantum clustering algorithms are effective for high-dimensional data and **complex clustering problems** where traditional clustering methods are computationally expensive.

How Quantum Clustering Works:

- **Amplitude Encoding:** Encodes each data point as an amplitude vector in a quantum state: $|x\rangle = \sum_{i=0}^{N-1} x_i |i\rangle$
- **Distance Measurement:** The overlap (or fidelity) between quantum states can be used as a measure of similarity. The closer two states are in the Hilbert space, the more likely they belong to the same cluster.
- **Entanglement for Multi-dimensional Relations:** Entanglement can be used to create relationships across multiple features, making clustering based on **multi-dimensional correlations** more effective.

Dynamic Quantum Clustering (DQC):

- **Adaptability:** DQC continuously adapts clusters based on **real-time data updates**. It's effective for applications where data points are constantly changing, such as real-time sensor data or financial markets.
- **Wavefunction Evolution:** DQC uses a **Schrödinger equation** approach to simulate data point movements over time in a potential field that represents the cluster structure.
- **Algorithm Mechanics:**
 - Each data point is represented by a **quantum state** in a potential field. The field is defined so that points within the same cluster experience a similar potential.
 - Over time, data points evolve according to the field's gradient, allowing for dynamic adjustments to cluster memberships.
 - The time evolution of each point's wavefunction can be represented by: $i\hbar \frac{\partial \psi(x,t)}{\partial t} = H\psi(x,t)$ where H is the Hamiltonian representing the potential landscape of the clusters.

Limited Basis Approaches:

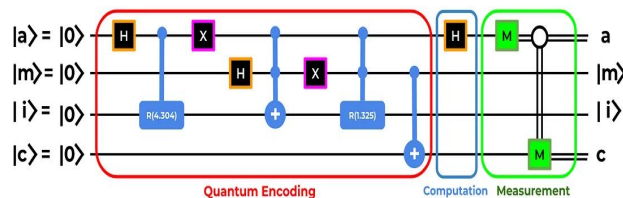
- **Basis Restriction:** Uses a limited number of basis states for data representation, reducing the **computational resources** required.
- In practice, only a subset of possible quantum states is used to approximate clusters. This approach is useful when quantum resources are constrained or when data points are sparse.
- **Example Application:** For simple binary clustering, a limited basis could reduce the space to two primary states, representing distinct classes or clusters.

Applications in AI:

- **Dynamic Environments:** DQC is particularly suited for clustering in environments where data changes frequently (e.g., financial trading, dynamic sensor networks).
- **Large-Scale Data:** Limited basis approaches make it feasible to apply quantum clustering techniques to **large datasets** by focusing on key basis states.
- **Pattern Recognition:** Quantum clustering methods, especially with dynamic and limited basis approaches, excel in **pattern recognition** and **anomaly detection** in high-dimensional datasets, where traditional methods are less efficient.

Data Encoding in Quantum Systems

- Amplitude Encoding - Encodes a vector as an amplitude of a quantum state
- Angle Encoding - Represents vectors as angles on the Bloch sphere
- Quantum feature maps



Data Encoding Challenge:

- Quantum systems require classical data to be encoded as **quantum states** for QML algorithms to process.

Common Encoding Methods:

- **Amplitude Encoding:**
 - Encodes a vector of data into the amplitudes of a quantum state.
 - Example: A vector $x = [x_0, x_1, x_2, \dots, x_{N-1}]$ is mapped to: $|x\rangle = \sum_{i=0}^{N-1} x_i |i\rangle$
- **Angle Encoding:**
 - Represents data points as angles on the Bloch sphere for each qubit.
 - Data point x_i is mapped as: $|x\rangle = \cos(x_i) |0\rangle + \sin(x_i) |1\rangle$

Encoding Example in ML:

- **Quantum Feature Map:** Each feature in a dataset can be mapped onto a qubit state using amplitude or angle encoding, allowing the **quantum model** to operate on it directly.
- In clustering tasks, for example, encoding high-dimensional features into qubit states can enable rapid, complex pattern recognition.

Challenges

- Noise
- Decoherence
- Qubit limitation
- Quantum Error Correction

- **Bit-flip:** Shor code uses 3-qubit bit-flip code for bit-flip errors.

$$|0_L\rangle = |000\rangle, \quad |1_L\rangle = |111\rangle \quad (1.77)$$

- **Phase flip:** Each qubit in the bit-flip code is protected against phase-flip errors with another layer of encoding (A Hadamard transformation followed by a three-qubit phase-flip code):

$$|0_L\rangle = \frac{1}{\sqrt{2}}(|000\rangle + |111\rangle) \quad (1.78)$$

The full Shor Code:

$$|0_L\rangle = \frac{1}{\sqrt{2}}(|000\rangle \otimes |000\rangle \otimes |000\rangle + |111\rangle \otimes |111\rangle \otimes |111\rangle) \quad (1.79)$$

Steane code: A 7-qubit code derived from classical Hamming codes

A 7-qubit QECC based on the [7,4] Hamming code. Correct bit/phase flip errors and encodes 1 logical qubit into 7 physical qubits.

Steane code uses stabilizer formalism-the logical qubit is stabilized by a set of operators. Each error changes the state of the qubits in a predictable way. The error is corrected using syndrome measurements.

The logical states of the Steane code:

$$\begin{aligned} |0_L\rangle &= \frac{1}{\sqrt{8}}(|0000000\rangle + |1010101\rangle + |0110011\rangle + |1100111\rangle \\ &\quad + |0001111\rangle + |1110000\rangle + |0011100\rangle + |1101001\rangle) \\ |1_L\rangle &= \frac{1}{\sqrt{8}}(|1111111\rangle + |0101010\rangle + |1001100\rangle + |0011001\rangle \\ &\quad + |1110000\rangle + |0001111\rangle + |1100110\rangle + |0011010\rangle) \end{aligned} \quad (1.80)$$



Noise and Decoherence:

- **Noise:** Quantum gates are sensitive to external interference, leading to errors in calculations.
- **Decoherence:** Quantum states lose information over time due to interaction with the environment.
- **Effect:** Reduces the accuracy and reliability of quantum computations, limiting circuit depth and runtime.

Scalability:

- **Qubit Limitations:** Current quantum computers have few qubits, restricting the size of data and models they can handle.
- **Quantum Error Correction:** Required to build larger, fault-tolerant quantum systems, but significantly increases hardware requirements.
- **Implications for AI:** Limited qubit numbers and noisy environments make it challenging to apply quantum algorithms at scale for AI tasks involving large datasets.

Current Research Directions:

- **Hardware Improvements:** Developing more stable qubits to reduce noise.
- **Error Correction Techniques:** Quantum error correction codes that increase qubit fidelity.
- **NISQ Era (Noisy Intermediate-Scale Quantum):** Emphasis on algorithms designed for today's limited-capacity quantum systems, like hybrid approaches

- with classical preprocessing.

Session 3 Summary

- Grover's, QFT, QAOA, VQE, and QSVM applications in AI
- Speedups in search, optimization, signal processing, and classification
- Quantum Walks, and QVSM



Key Concepts Recap:

- **Quantum Machine Learning (QML):** Application of quantum principles in ML.
- **VQE:** Quantum algorithm for **cost function minimization**.
- **QAOA:** Quantum algorithm for **combinatorial optimization**.
- **Data Encoding:** Methods to represent classical data as quantum states.

Next Session Preview:

- **Quantum Graph Neural Networks (QGNNs):** Focusing on applying quantum computing to graph-based AI tasks, commonly seen in social networks, biological systems, and recommendation engines.

