

Applied Natural Language Processing

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Where are we?

Previously

- Documents
 - document pre-processing
 - document classification and similarity
- Words
 - semantic relationships
 - distributional semantics

Still to go

- Word sequences
 - **part-of-speech tagging**
 - Named Entity Recognition
 - Question Answering

Part-of-speech tagging

Part 1

- Parts of speech (PoS)
 - what are they?
 - what are they useful for?
- Open and closed PoS classes
- PoS Tagsets
 - The Penn Treebank Tagset
- Simple PoS Tagging
 - PoS ambiguity
 - Unigram tagging
 - Evaluation

Part 2

- Sequence Labelling
- Hidden Markov Models (HMMs)
 - Forward algorithm
 - Viterbi algorithm

Parts of speech

Parts of speech

- Words can be categorised according to how they behave grammatically
- Traditionally, linguists distinguish about 9 or 10 lexical categories, referred to as **parts of speech (PoS)**:
 - adjective
 - adverb
 - auxiliary verb
 - conjunction
 - determiner
 - interjection
 - noun
 - preposition
 - pronoun
 - verb

Can you give an example of each one?

Are parts of speech useful?

Identifying parts of speech can be a useful pre-processing step

- Can help to disambiguate words
 - information retrieval
 - text-to-speech
 - document classification
- Tells us what sorts of words are likely to occur nearby:
 - adjectives often followed by nouns: *happy student*
 - personal pronouns often followed by verbs: *you laugh*
- Important for identifying larger grammatical structures
 - grammatical plausible sequences / parsing
 - named entity recognition
 - information extraction

Nouns and pronouns

- used to identify people, places and things
- **Nouns** often divided into
 - Proper nouns
 - *England, Kim, Microsoft*
 - Common nouns
 - count nouns: *window, tyre, idea*
 - mass nouns: *snow, rice, courage*
- **Pronouns** stand in place of a noun
 - *she, you, I, who*

Verbs and auxiliary verbs

- Actions and processes
 - run, chase, say, believe
 - it is *believed* that he *chased* the thief
- Auxiliary verbs usually precede a main verb
 - he *should* chase the thief

Adjectives and adverbs

- Adjectives:
 - properties and qualities
 - modify nouns
 - *green, small, clever, mythical*
- Adverbs:
 - usually modify verbs or verb phrases
 - *slowly, now, unfortunately, possibly, tomorrow*

Determiners

- A modifying word that determines the kind of reference a noun or noun group has
 - I would like *a* cake; vs
 - I would like *the* cake; vs
 - I would like *every* cake; vs
 - I would like *some* cake
- Also called articles

Prepositions and particles

- Prepositions
 - specify the relative positions of two words or elements
 - I saw the boy *on* the bridge; vs
 - I saw the boy *under* the bridge
 - *On, under, over, to, with, by*
- Particles
 - sometimes distinguished from prepositions
 - generally modify a verb; sometimes referred to as phrasal verbs
 - I tidied *up* the room
 - *up, down, at, by, to*

Conjunctions and interjections

- Conjunctions

- join words and phrases together

- co-ordinating: *and, but, or, nor*

- sub-ordinating: *because, if, when, as, since, until*

- correlative: *either ... or ...; both ... and ...*

- Interjections

- exclamations without any grammatical connection to other words

- *hey, ouch, darn, aha, huh*

Open and closed classes

- **Open** classes: so-called because they are not fixed
 - new words may be added fairly often
 - other words may go out of the language
 - content-bearing
- **Closed** classes: these classes are fixed
 - words are functional rather than content-bearing
 - frequently occurring and often short in length
 - may be considered as **stopwords** in some applications
 - may specify how different concepts in the sentence relate to each other

Language change

New English Words 2024

- boop
- ick
- bussin'
- AGI
- cuffing season
- shrinkflation

Archaic words, no longer in use?

- ambuscade
- beldam
- camelopard
- dispraise
- sanative

Do you know what these words mean?
What parts of speech do you think they are?

Part-of-Speech tagsets

- A tagset provides a set of labels for marking PoS classes.
- Different tag sets have been derived from work on text corpora:
 - Brown corpus: 80 tags
 - Penn Treebank: 45 tags
 - Susanne corpus: 350 tags
 - British National Corpus (BNC): 60 tags

The Penn TreeBank tagset (1)

| | | |
|------------|--------------------------|---------------------|
| <i>CC</i> | Coordinating conjunction | <i>and, but, or</i> |
| <i>CD</i> | Cardinal number | <i>one, two</i> |
| <i>DT</i> | Determiner | <i>the, some</i> |
| <i>EX</i> | Existential there | <i>there</i> |
| <i>FW</i> | Foreign word | <i>hoc</i> |
| <i>IN</i> | Preposition | <i>of, in, by</i> |
| <i>JJ</i> | Adjective | <i>big</i> |
| <i>JJR</i> | Adjective, comparative | <i>bigger</i> |
| <i>JJS</i> | Adjective, superlative | <i>biggest</i> |
| <i>LS</i> | List item marker | <i>1, One</i> |
| <i>MD</i> | Modal | <i>can, should</i> |

The Penn TreeBank tagset (2)

| | | |
|-------------|------------------------|--------------------|
| <i>NN</i> | Noun, singular or mass | <i>dog</i> |
| <i>NNS</i> | Noun, plural | <i>dogs</i> |
| <i>NNP</i> | Proper noun, sing. | <i>Edinburgh</i> |
| <i>NNPS</i> | Proper noun, plural | <i>Orkneys</i> |
| <i>PDT</i> | Predeterminer | <i>all, both</i> |
| <i>POS</i> | Possessive ending | <i>'s</i> |
| <i>PP</i> | Personal pronoun | <i>I, you, she</i> |
| <i>PP\$</i> | Possessive pronoun | <i>my, theirs</i> |
| <i>RB</i> | Adverb | <i>quickly</i> |
| <i>RBR</i> | Adverb, comparative | <i>faster</i> |
| <i>RBS</i> | Adverb, superlative | <i>fastest</i> |

the penn treebank tagset (3)

| | | |
|------------|-----------------------|--------------------|
| RP | Particle | <i>up, off</i> |
| SYM | Symbol | <i>+, %, &</i> |
| TO | The word "to" | <i>to</i> |
| UH | Interjection | <i>oh, oops</i> |
| VB | verb, base form | <i>eat</i> |
| VBD | verb, past tense | <i>ate</i> |
| VBG | verb, gerund | <i>eating</i> |
| VBN | verb, past participle | <i>eaten</i> |
| VBP | Verb, non-3sg, pres | <i>eat</i> |
| VBZ | Verb, 3sg, pres | <i>eats</i> |
| WDT | Wh-determiner | <i>which, that</i> |
| WP | Wh-pronoun | <i>what, who</i> |

the Penn treebank tagset (4)

| | | |
|-------------|----------------------------|-------------------|
| <i>WP\$</i> | Possessive-wh | <i>whose</i> |
| <i>WRB</i> | Wh-adverb | <i>how, where</i> |
| <i>\$</i> | Dollar sign | <i>\$</i> |
| <i>#</i> | Pound sign | <i>#</i> |
| <i>"</i> | Left quote | <i>"</i> |
| <i>"</i> | Right quote | <i>"</i> |
| <i>(</i> | Left parenthesis | <i>(</i> |
| <i>)</i> | Right parenthesis | <i>)</i> |
| <i>,</i> | Comma | <i>,</i> |
| <i>.</i> | Sentence-final punctuation | <i>. ! ?</i> |
| <i>:</i> | Mid-sentence punctuation | <i>: ; — ...</i> |

Part-of-speech tagging

PoS tagging is the process of assigning a single part-of-speech tag to each word (and punctuation marker) in some text.)

"/* The/*DT* guys/*NNS* that/*WDT* make/*VBP* traditional/*JJ* hardware/*NN* are/*VBP* really/*RB* being/*VBG* obsoleted/*VBN* by/*IN* microprocessor-based/*JJ* machines/*NNS* /, /* said/*VBD* Mr./*NNP* Benton/*NNP* /.

PoS Tagging

Carrying out PoS tagging

- comparatively shallow form of processing
 - one tag per word
 - no larger structures created
- non-trivial
 - must resolve ambiguities
 - the same word can have different tags in different contexts

PoS ambiguity

- In the Brown corpus:
 - **11.5% of word types and 40% of word tokens** are ambiguous with respect to POS tag i.e., could be labelled with multiple PoS tags
 - Why is the percentage of ambiguous word tokens higher than the percentage of ambiguous word types?
- Which of the words below are ambiguous with respect to PoS?

| Word | PoS? | Word | PoS? |
|-------|------|---------|------|
| dream | | desert | |
| the | | rebel | |
| word | | bravely | |
| green | | over | |

Local vs global ambiguity

- Which words can have multiple PoS tags in the following sentence:

Fruit flies like a banana

- This is an example of **global** ambiguity.
 - There are different plausible tag sequences which can be assigned to the sentence
 - Often rare in real text. Why?
- Most words are only **locally** ambiguous. The intended PoS can be determined from the context

Time always flies like an arrow

Evaluating taggers

- Compare output of a tagger with a human-labelled gold standard
 - assume that performance will be similar on other similar unlabelled text
- Measure accuracy: proportion of tags which are correct
 - could measure (average) precision of each class
- On well-formed text, best methods have accuracy of 96-97%
 - using the Penn Treebank tagset
 - average of one error every couple of sentences
- Inter-annotator agreement is also around 97% accurate

Information sources for PoS tagging

What information can be used to determine the most likely PoS tag for a word token?

- Word identity (the likelihood of a tag given the word)
- Adjacent PoS tags (the likelihood of a sequence of tags)

Word identities

- A word may have different possible PoS tags
- But they are not all equally likely
- **Entropy** can be used to measure the uncertainty in the tag distribution
 - 50:50 is high entropy (high uncertainty)
 - 90:10 is low entropy (low uncertainty)
 - See the lab
- Tag distributions for words are often low entropy:
 - one tag is far more likely than the other possibilities

A unigram Pos tagger

- Choose the most likely tag for each word

$$\text{tag}(w) = \operatorname{argmax}_t P(t|w)$$

- Use labelled training data to estimate these probabilities

$$P(t|w) = \frac{\text{number of occurrences of } w \text{ tagged as } t}{\text{number of occurrences of } w}$$

- Always chooses same tag for a word regardless of context
- Usually results in a tagger with about 90% accuracy

Beyond unigram PoS tagging

- Which of these look like a possible tag sequence in well-formed English?
 - DET DET JJR NN NNS VBD
 - DET NNS VBD DET JJR NN
 - VBD JJR NNS DET NN DET
- How can we incorporate information about likely tag sequences into a tagger?
 - Hidden Markov Models (HMMs)

Part 2: Hidden Markov Models

Consider this example

“Every night I dream the same dream.”

- What PoS tag would you associate with each token in the sentence above?
- Which word type(s) are ambiguous with respect to PoS tag?
- How do you know the correct tag?

The PoS tagging problem

- Input: a sequence of words w_1^n :

$$w_1^n = (w_1, w_2, \dots, w_n)$$

- Output: a sequence of tags t_1^n :

$$t_1^n = (t_1, t_2, \dots, t_n)$$

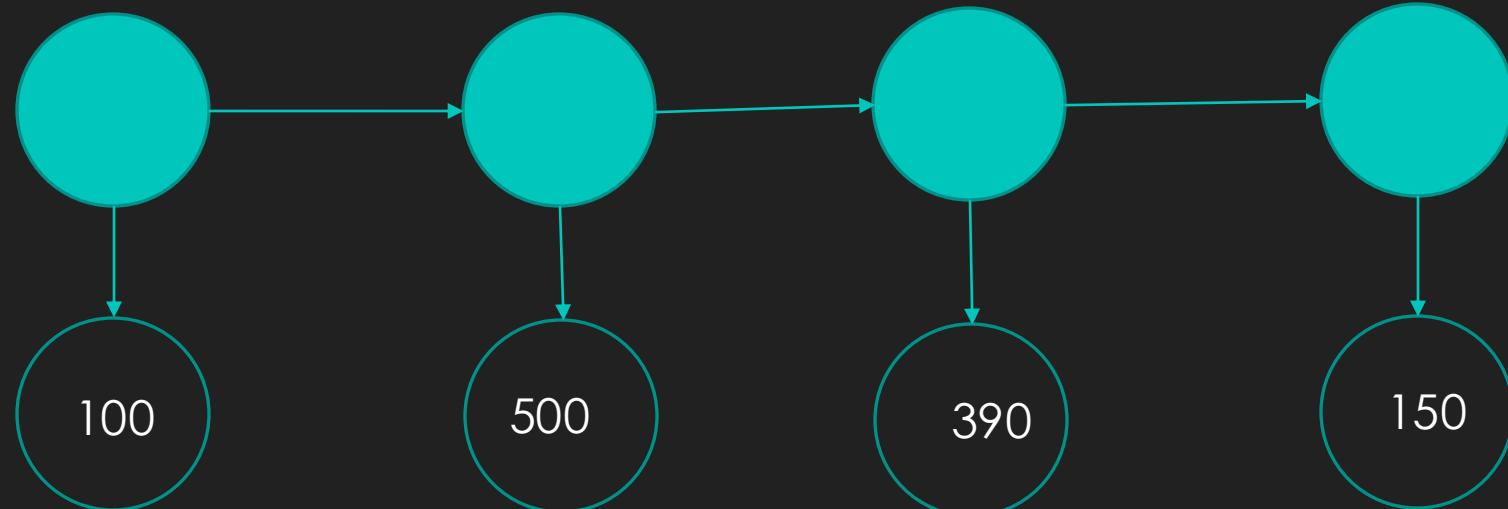
- In particular, find the most probable PoS tag sequence \hat{t}_1^n :

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n)$$

Hidden Markov Models (HMMs)

A sequence of **observations** is generated by a sequence of **hidden states**.

Can we *infer* the most likely sequence of hidden states from the observations



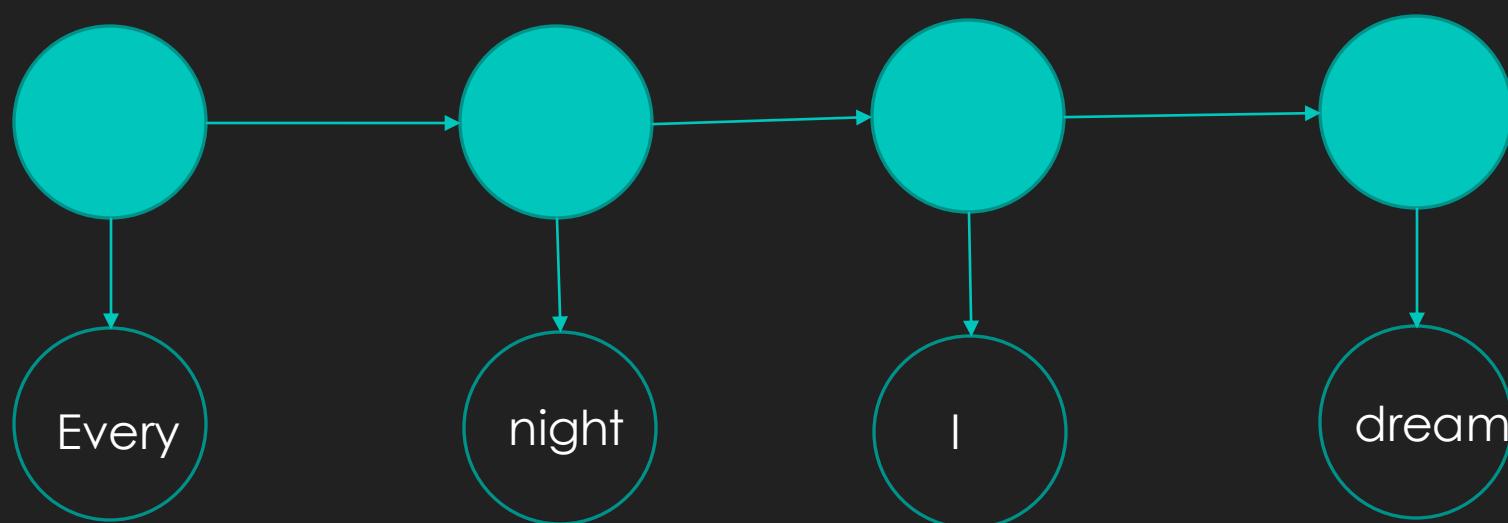
Markov Assumption:
current state
depends only on
previous state

Output Assumption:
current output
depends only on
current state

HMMs for PoS Tagging

POS tags
are the
hidden
states

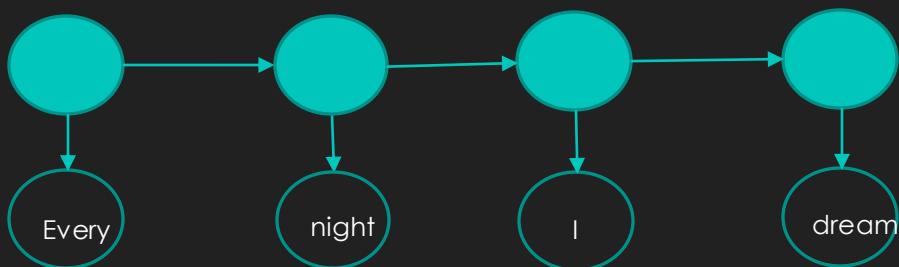
Words are
the
observations



Markov assumption:
current POS tag
depends only on
single previous tag

Output assumption:
word depends only
on current POS tag

Encoding the assumptions probabilistically



Markov assumption: current POS tag depends only on single previous tag

$$P(t_i | t_1^{i-1}) = P(t_i | t_{i-1})$$

Output assumption: word depends only on current POS tag

$$P(w_1^n | t_1^n) = \prod_i^n P(w_i | t_i)$$

Parameters for an HMM

To define a HMM tagger, we need to specify:

- **Emission** or **observation** probabilities:
 - $P(w|t)$ for each word w and tag t
- **Transition** or **bigram** probabilities:
 - $P(t_j|t_i)$ for each pair of tags t_i and t_j

These probabilities can be:

- calculated directly from POS-tagged corpora (supervised approach)
- learnt from untagged corpora (unsupervised approach) using Expectation Maximisation (EM)

Calculating emission probabilities

- For each possible tag, we need to count the number of occurrences of each word.

```
train  
[('Pierre', 'NNP'),  
 ('Vinken', 'NNP'),  
 ('', ''),  
 ('61', 'CD'),  
 ('years', 'NNS'),  
 ('old', 'JJ'),  
 ('', ''),  
 ('will', 'MD'),  
 ('join', 'VB'),  
 ('the', 'DT'),  
 ('board', 'NN'),  
 ('as', 'IN'),  
 ('a', 'DT'),  
 ('nonexecutive', 'JJ'),  
 ('director', 'NN'),  
 ('Nov.', 'NNP'),  
 ('29', 'CD'),  
 ('', '')]
```

```
def calculate_emissions(trainlist):
    #trainlist is a list of (word,tag) pairs
    emissions={}
    for word,tag in trainlist:
        current=emissions.get(tag,{})
        current[word]=current.get(word,0)+1
        emissions[tag]=current
    return {tag:{word:value/sum(worddist.values()) for word,value in worddist.items()}
            for tag,worddist in emissions.items()}
```

```
: calculate_emissions(train)
: { 'NNP': {'Pierre': 6.613100552193897e-05,
:             'Vinken': 2.204366850731299e-05,
:             'Nov.': 0.0026231965523702454,
:             'Mr.': 0.04412040251738694,
:             'Elsevier': 1.1021834253656494e-05,
:             'N.V.': 0.0001432838452975344,
:             'Dutch': 8.817467402925195e-05,
```

Calculating transition probabilities

- For each possible tag, we need to count the number of occurrences of each previous tag.

```
train
[('Pierre', 'NNP'),
 ('Vinken', 'NNP'),
 ('', ''),
 ('61', 'CD'),
 ('years', 'NNS'),
 ('old', 'JJ'),
 ('', ''),
 ('will', 'MD'),
 ('join', 'VB'),
 ('the', 'DT'),
 ('board', 'NN'),
 ('as', 'IN'),
 ('a', 'DT'),
 ('nonexecutive', 'JJ'),
 ('director', 'NN'),
 ('Nov.', 'NNP'),
 ('29', 'CD'),
 ('', '')]
```

```
: def calculate_transitions(trainlist):
    transitions={}
    previous="start"
    for _, tag in trainlist:
        current=transitions.get(previous,{})
        current[tag]=current.get(tag,0)+1
        transitions[tag]=current
        previous =tag
    return {previous:{tag:value/sum(tagdist.values()) for tag,value in tagdist.items()} for previous,tagdist in transitions.items()}
```

```
: calculate_transitions(train)
: {'NNP': {'NNP': 0.09662176841190528,
           ':': 0.05123470200593816,
           'CD': 0.0383040898305879,
           'NNS': 0.06321111977269726,
           'JJ': 0.06465412582586803,
           'MD': 0.010335331177876321,
           'NP': 0.02726265812557221}
```

Forward Algorithm

- calculates the probability of a word sequence given a tag sequence

$$P(w_1^n | t_1^n) = \prod_i^n P(w_i | t_i)$$

remember the output
assumption: the current word only depends on the current tag

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

$$P(\text{flies like flowers} | N V N)$$

$$= P(\text{flies}|N) \cdot P(\text{like}|V) \cdot P(\text{flowers}|N)$$

$$= 0.025 \times 0.034 \times 0.05 = 0.0000425$$

Tagging as decoding

How do we use a HMM to find the most likely tag sequence?

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n)$$

Apply Bayes' Rule

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \frac{P(w_1^n | t_1^n) P(t_1^n)}{P(w_1^n)}$$

Drop the denominator

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(w_1^n | t_1^n) P(t_1^n)$$

Simplifying assumptions

Assume output independence: current observation depends only on current state

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \prod_i^n P(w_i | t_i) P(t_1^n)$$

Make the bigram or first order Markov assumption: current state depends only on the single previous state

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \prod_i^n P(w_i | t_i) P(t_i | t_{i-1})$$

emission probabilities

transition probabilities

Decoding

- Given a tag sequence and a word sequence, we can estimate the probability that the word sequence was generated by that tag sequence

$$P(t_1^n | w_1^n) \propto \prod_i^n P(w_i | t_i) P(t_i | t_{i-1})$$

- So given two possible tag sequences we can choose between them

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \prod_i^n P(w_i | t_i) P(t_i | t_{i-1})$$

Decoding example

- Which is the most likely tag sequence for “flies like flowers”?
 - NVN
 - VNN

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|------------------------------|------------------------------|--------------------------------------|
| N | $P(N N) = 0.13$ | $P(V N) = 0.43$ | $P(\text{start} N) = 0$ |
| V | $P(N V) = 0.35$ | $P(V V) = 0.05$ | $P(\text{start} V) = 0$ |
| start | $P(N \text{start}) = 0.29$ | $P(V \text{start}) = 0.32$ | $P(\text{start} \text{start}) = 0$ |

$P(N \vee N \mid \text{flies like flowers})$

| w | $P(w N)$ | $P(w V)$ |
|---------|--------------|--------------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|------------------------|--------------------------|----------------------------------|
| N | $P(N N) = 0.13$ | P(V N)=0.43 | $P(\text{start} N)=0$ |
| V | P(N V)= 0.35 | $P(V V)=0.05$ | $P(\text{start} V)=0$ |
| start | P(N start)=0.29 | $P(V \text{start})=0.32$ | $P(\text{start} \text{start})=0$ |

$$\begin{aligned}
 P(\text{flies like flowers} \mid N \vee N) &= P(\text{flies}|N) \times P(\text{like}|V) \times P(\text{flowers}|N) \\
 &= 0.025 \times 0.034 \times 0.05 = \textcolor{red}{0.0000425}
 \end{aligned}$$

$$P(N \vee N) = P(N|\text{start}) \times P(V|N) \times P(N|V) = 0.29 \times 0.43 \times 0.35 = \textcolor{red}{0.043645}$$

$$P(N \vee N \mid \text{flies like flowers}) = \textcolor{red}{0.0000425} \times \textcolor{red}{0.043645} = 0.0000018549125$$

$P(V N N | \text{Flies like flowers})$

| w | $P(w N)$ | $P(w V)$ |
|---------|--------------|--------------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|-------------------------------------|--|------------------------------------|
| N | $P(N N) = 0.13$ | $P(V N)=0.43$ | $P(\text{start} N)=0$ |
| V | $P(N V)= 0.35$ | $P(V V)=0.05$ | $P(\text{start} V)=0$ |
| start | $P(N \text{start})=0.29$ | $P(V \text{start})=0.32$ | $P(\text{start} \text{start})=0$ |

$$P(\text{flies like flowers} | V N N) = 0.015 \times 0.012 \times 0.05 = 0.00009$$

$$P(V N N) = P(V | \text{start}) \times P(N | V) \times P(N | N) = 0.32 \times 0.35 \times 0.13 = 0.01456$$

$$P(V N N | \text{flies like flowers}) = 0.00009 \times 0.01456 = 0.0000013104$$

Finding the most likely tag sequence

- Brute force?
- Number of possible tag sequences = k^n
 - where $k = |\text{tagset}|$, $n = |\text{word tokens}|$
- With a tagset of size 2 and a sentence of length 3 there are: **$2^3 = 8$** possible tag sequences
 - possible to try every one
- With a tagset of size 10 and a sentence of length 8 there are:
 - $10^8 = 100\,000\,000$ possible tag sequences
 - it would take just over 1 day to check all possible tag sequence at the rate of 1000 per second
- With a tagset of size 45 and a sentence of length 15

Viterbi Algorithm

- finds the best tag sequence without enumerating all possibilities
- exploits HMM assumptions
 - probability of next state only depends on current state
 - probability of current output only depends on current state
- classic example of dynamic programming
 - recursively decompose problem into smaller problems
 - keep track of (tabulate) solutions to sub-problems

Viterbi sub-problems

- For an input sequence w_1^n
- A sub-problem corresponds to a pair (i, t) where:
- i is the position in the sequence, $i < n$
- t is the current PoS tag

flies like flowers

$i=1$, store best path where
 $t_1=N$
 $t_1=V$

Viterbi sub-problems

- For an input sequence w_1^n
- A sub-problem corresponds to a pair (i, t) where:
- i is the position in the sequence, $i < n$
- t is the current PoS tag

flies like flowers



i=2, store best path where
 $t_2=N$
 $t_2=V$

Viterbi sub-problems

- For an input sequence w_1^n
- A sub-problem corresponds to a pair (i, t) where:
- i is the position in the sequence, $i < n$
- t is the current PoS tag

flies like flowers

$i=3$, store best path
 $t_3=N$
 $t_3=V$

Viterbi initialisation

flies like flowers

i=1, store best path where
 $t_1 = N$
 $t_1 = V$

Subproblem 1: $t_1 = N$

$$V(1, N) = P(t_1 = N) = P(flies|N) \times P(N|start) \\ = 0.025 \times 0.29 = 0.00725$$

Subproblem 2: $t_1 = V$

$$V(1, V) = P(t_1 = V) = P(flies|V) \times P(V|start) \\ = 0.015 \times 0.32 = 0.0048$$

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|------------------------------|------------------------------|--------------------------------------|
| N | $P(N N) = 0.13$ | $P(V N) = 0.43$ | $P(\text{start} N) = 0$ |
| V | $P(N V) = 0.35$ | $P(V V) = 0.05$ | $P(\text{start} V) = 0$ |
| start | $P(N \text{start}) = 0.29$ | $P(V \text{start}) = 0.32$ | $P(\text{start} \text{start}) = 0$ |

Recursive Step

- For each subsequent position $i \in \{2, \dots, n\}$ and each tag, t

$$V(i, t) = \max_{t' \in T} (V(i - 1, t') \times P(t|t') \times P(w_i|t))$$

- For each possible previous tag t' , what's the probability of the current tag being t ?
- Which of these is highest? If the current tag is t then the previous tag must have been the one which gave the highest probability

Step 2

flies like flowers

i=2, store best path where
 $t_2=N$
 $t_2=V$

Subproblem 1:**V(2,N)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_2 = N) = V(1, N) \times P(N|N) \times P(like|N)$$

$$P(t_2 = N) = 0.00725 \times 0.13 \times 0.012 = 0.00001131$$

- **If it was V:**

$$P(t_2 = N) = V(1, V) \times P(N|V) \times P(like|N)$$

$$P(t_2 = N) = 0.0048 \times 0.35 \times 0.012 = 0.00002016$$

- Which is higher?
- So $V(2,N) = ??$

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|------------------------------|------------------------------|--------------------------------------|
| N | $P(N N) = 0.13$ | $P(V N) = 0.43$ | $P(\text{start} N) = 0$ |
| V | $P(N V) = 0.35$ | $P(V V) = 0.05$ | $P(\text{start} V) = 0$ |
| start | $P(N \text{start}) = 0.29$ | $P(V \text{start}) = 0.32$ | $P(\text{start} \text{start}) = 0$ |

Step 2

flies like flowers

i=2, store best path where
 $t_2=N$
 $t_2=V$

Subproblem 2:**V(2,V)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_2 = V) = V(1,N) \times P(V|N) \times P(like|V) = ??$$

- **If it was V:**

$$P(t_2 = V) = V(1,V) \times P(V|V) \times P(like|V) = ??$$

- Which is higher?
- So $V(2,V) = ??$

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|---------------------|---------------------|----------------------|
| N | $P(N N) = 0.13$ | $P(V N)=0.43$ | $P(start N)=0$ |
| V | $P(N V)=0.35$ | $P(V V)=0.05$ | $P(start V)=0$ |
| start | $P(N start)=0.29$ | $P(V start)=0.32$ | $P(start start)=0$ |

Step 3

flies like flowers

i=3, store best path where
 $t_3 = N$
 $t_3 = V$

Subproblem 1: **V(3,N)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_3 = N) = V(2, N) \times P(N|N) \times P(flowers|N) = ??$$

- **If it was V:**

$$P(t_3 = N) = V(2, V) \times P(N|V) \times P(flowers|N) = ??$$

- Which is higher?
- So $V(3,N) = ??$

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|------------------------------|------------------------------|--------------------------------------|
| N | $P(N N) = 0.13$ | $P(V N) = 0.43$ | $P(\text{start} N) = 0$ |
| V | $P(N V) = 0.35$ | $P(V V) = 0.05$ | $P(\text{start} V) = 0$ |
| start | $P(N \text{start}) = 0.29$ | $P(V \text{start}) = 0.32$ | $P(\text{start} \text{start}) = 0$ |

Step 3

flies like flowers

i=3, store best path where
 $t_3=N$
 $t_3=V$

Subproblem 2:**V(3,V)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_3 = V) = V(2, N) \times P(V|N) \times P(flowers|V) = ??$$

- **If it was V:**

$$P(t_3 = V) = V(2, V) \times P(V|V) \times P(flowers|V) = ??$$

- Which is higher?
- So $V(3,V) = ??$

| w | P(w N) | P(w V) |
|---------|----------|----------|
| flies | 0.025 | 0.015 |
| like | 0.012 | 0.034 |
| flowers | 0.05 | 0.005 |

| | N | V | start |
|-------|------------------------------|------------------------------|--------------------------------------|
| N | $P(N N) = 0.13$ | $P(V N) = 0.43$ | $P(\text{start} N) = 0$ |
| V | $P(N V) = 0.35$ | $P(V V) = 0.05$ | $P(\text{start} V) = 0$ |
| start | $P(N \text{start}) = 0.29$ | $P(V \text{start}) = 0.32$ | $P(\text{start} \text{start}) = 0$ |

Efficiency of Viterbi

- Number of sub-problems = $k \times n$
- In each sub-problem, we have to consider k previous sub-problems
- So complexity = $k^2 \times n$
- In toy example, worse than k^n
 - $12 > 8$
- But with 10 tags and a sentence of length 8
 - $800 << 100000000$
- With 45 tags and sentences of length 15
 - $30375 << \dots$

Next time

- Another sequence labelling problem
 - Named entity recognition

Making progress

- There is 1 associated notebook this week:
 - [Part 1: Lab_8_1.ipynb](#)