

# Applied Natural Language Processing

Dr Jeff Mitchell, University of Sussex  
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# Where are we?

## Previously

- Documents
  - document pre-processing
  - document classification and similarity
- Words
  - semantic relationships
  - distributional semantics

## Still to go

- Word sequences
  - **part-of-speech tagging**
  - Named Entity Recognition
  - Question Answering

# Part-of-speech tagging

## Part 1

- Parts of speech (PoS)
  - what are they?
  - what are they useful for?
- Open and closed PoS classes
- PoS Tagsets
  - The Penn Treebank Tagset
- Simple PoS Tagging
  - PoS ambiguity
  - Unigram tagging
  - Evaluation

## Part 2

- Sequence Labelling
- Hidden Markov Models (HMMs)
  - Forward algorithm
  - Viterbi algorithm

# Parts of speech

# Parts of speech

- Words can be categorised according to how they behave grammatically
- Traditionally, linguists distinguish about 9 or 10 lexical categories, referred to as **parts of speech (PoS)**:

- adjective
- adverb
- auxiliary verb
- conjunction
- determiner
- interjection
- noun
- preposition
- pronoun
- verb

*Can you give an example of each one?*

# Are parts of speech useful?

Identifying parts of speech can be a useful pre-processing step

- Can help to disambiguate words
  - information retrieval
  - text-to-speech
  - document classification
- Tells us what sorts of words are likely to occur nearby:
  - adjectives often followed by nouns: *happy student*
  - personal pronouns often followed by verbs: *you laugh*
- Important for identifying larger grammatical structures
  - grammatical plausible sequences / parsing
  - named entity recognition
  - information extraction

# Nouns and pronouns

- used to identify people, places and things
- **Nouns** often divided into
  - Proper nouns
    - *England, Kim, Microsoft*
  - Common nouns
    - count nouns: *window, tyre, idea*
    - mass nouns: *snow, rice, courage*
- **Pronouns** stand in place of a noun
  - *she, you, I, who*

# Verbs and auxiliary verbs

- Actions and processes
  - run, chase, say, believe
  - it is *believed* that he *chased* the thief
- Auxiliary verbs usually precede a main verb
  - he *should* chase the thief



# Adjectives and adverbs

- Adjectives:

- properties and qualities
- modify nouns
- *green, small, clever, mythical*

- Adverbs:

- usually modify verbs or verb phrases
- *slowly, now, unfortunately, possibly, tomorrow*

# Determiners

- A modifying word that determines the kind of reference a noun or noun group has
  - I would like *a* cake; vs
  - I would like *the* cake; vs
  - I would like *every* cake; vs
  - I would like *some* cake
- Also called articles

# Prepositions and particles

- Prepositions

- specify the relative positions of two words or elements

- I saw the boy *on* the bridge; vs

- I saw the boy *under* the bridge

- *on, under, over, to, with, by*

- Particles

- sometimes distinguished from prepositions

- generally modify a verb; sometimes referred to as phrasal verbs

- I tidied *up* the room

- *up, down, at, by, to*

# Conjunctions and interjections

## ○ Conjunctions

- join words and phrases together

- co-ordinating: *and, but, or, nor*

- sub-ordinating: *because, if, when, as, since, until*

- correlative: *either ... or ...; both ... and ...*

## ○ Interjections

- exclamations without any grammatical connection to other words

- *hey, ouch, darn, aha, huh*

# Open and closed classes

- **Open** classes: so-called because they are not fixed
  - new words may be added fairly often
  - other words may go out of the language
  - content-bearing
- **Closed** classes: these classes are fixed
  - words are functional rather than content-bearing
  - frequently occurring and often short in length
  - may be considered as **stopwords** in some applications
  - may specify how different concepts in the sentence relate to each other

# Language change

## New English Words 2024

- boop
- ick
- bussin'
- AGI
- cuffing season
- shrinkflation

## Archaic words, no longer in use?

- ambushcade
- beldam
- camelopard
- dispraise
- sanative

Do you know what these words mean?  
What parts of speech do you think they are?

# Part-of-Speech tagsets

- A tagset provides a set of labels for marking PoS classes.
- Different tag sets have been derived from work on text corpora:
  - Brown corpus: 80 tags
  - Penn Treebank: 45 tags
  - Susanne corpus: 350 tags
  - British National Corpus (BNC): 60 tags

# The Penn TreeBank tagset (1)

<i>CC</i>	Coordinating conjunction	<i>and, but, or</i>
<i>CD</i>	Cardinal number	<i>one, two</i>
<i>DT</i>	Determiner	<i>the, some</i>
<i>EX</i>	Existential there	<i>there</i>
<i>FW</i>	Foreign word	<i>hoc</i>
<i>IN</i>	Preposition	<i>of, in, by</i>
<i>JJ</i>	Adjective	<i>big</i>
<i>JJR</i>	Adjective, comparative	<i>bigger</i>
<i>JJS</i>	Adjective, superlative	<i>biggest</i>
<i>LS</i>	List item marker	<i>1, One</i>
<i>MD</i>	Modal	<i>can, should</i>



# The Penn TreeBank tagset (2)

<i>NN</i>	Noun, singular or mass	<i>dog</i>
<i>NNS</i>	Noun, plural	<i>dogs</i>
<i>NNP</i>	Proper noun, sing.	<i>Edinburgh</i>
<i>NNPS</i>	Proper noun, plural	<i>Orkneys</i>
<i>PDT</i>	Predeterminer	<i>all, both</i>
<i>POS</i>	Possessive ending	<i>'s</i>
<i>PP</i>	Personal pronoun	<i>I, you, she</i>
<i>PP\$</i>	Possessive pronoun	<i>my, theirs</i>
<i>RB</i>	Adverb	<i>quickly</i>
<i>RBR</i>	Adverb, comparative	<i>faster</i>
<i>RBS</i>	Adverb, superlative	<i>fastest</i>

# the penn treebank tagset (3)

<i>RP</i>	Particle	<i>up, off</i>
<i>SYM</i>	Symbol	<i>+, %, &amp;</i>
<i>TO</i>	The word "to"	<i>to</i>
<i>UH</i>	Interjection	<i>oh, oops</i>
<i>VB</i>	verb, base form	<i>eat</i>
<i>VBD</i>	verb, past tense	<i>ate</i>
<i>VBG</i>	verb, gerund	<i>eating</i>
<i>VBN</i>	verb, past participle	<i>eaten</i>
<i>VBP</i>	Verb, non-3sg, pres	<i>eat</i>
<i>VBZ</i>	Verb, 3sg, pres	<i>eats</i>
<i>WDT</i>	Wh-determiner	<i>which, that</i>
<i>WP</i>	Wh-pronoun	<i>what, who</i>

# the Penn treebank tagset (4)

<b>WP\$</b>	Possessive-wh	<i>whose</i>
<b>WRB</b>	Wh-adverb	<i>how, where</i>
<b>\$</b>	Dollar sign	<i>\$</i>
<b>#</b>	Pound sign	<i>#</i>
<b>"</b>	Left quote	<i>' , "</i>
<b>"</b>	Right quote	<i>' , "</i>
<b>(</b>	Left parenthesis	<i>(</i>
<b>)</b>	Right parenthesis	<i>)</i>
<b>,</b>	Comma	<i>,</i>
<b>.</b>	Sentence-final punctuation	<i>. ! ?</i>
<b>:</b>	Mid-sentence punctuation	<i>: ; — ...</i>

# Part-of-speech tagging

PoS tagging is the process of assigning a single part-of-speech tag to each word (and punctuation marker) in some text.›

"/ The/DT guys/NNS that/WDT make/VBP traditional/JJ  
hardware/NN are/VBP really/RB being/VBG obsoleted/VBN  
by/IN microprocessor-based/JJ machines/NNS ./, "/ said/VBD  
Mr./NNP Benton/NNP ./.

# PoS Tagging

# Carrying out PoS tagging

- comparatively shallow form of processing
  - one tag per word
  - no larger structures created
- non-trivial
  - must resolve ambiguities
  - the same word can have different tags in different contexts

# PoS ambiguity

- In the Brown corpus:
  - **11.5% of word types and 40% of word tokens** are ambiguous with respect to POS tag i.e., could be labelled with multiple PoS tags
  - Why is the percentage of ambiguous word tokens higher than the percentage of ambiguous word types?
- Which of the words below are ambiguous with respect to PoS?

Word	PoS?	Word	PoS?
dream		desert	
the		rebel	
word		bravely	
green		over	

# Local vs global ambiguity

- Which words can have multiple PoS tags in the following sentence:

*Fruit flies like a banana*

- This is an example of **global** ambiguity.
  - There are different plausible tag sequences which can be assigned to the sentence
  - Often rare in real text. Why?
- Most words are only **locally** ambiguous. The intended PoS can be determined from the context

*Time always flies like an arrow*



# Evaluating taggers

- Compare output of a tagger with a human-labelled gold standard
  - assume that performance will be similar on other similar unlabelled text
- Measure accuracy: proportion of tags which are correct
  - could measure (average) precision of each class
- On well-formed text, best methods have accuracy of 96-97%
  - using the Penn Treebank tagset
  - average of one error every couple of sentences
- Inter-annotator agreement is also around 97% accurate

# Information sources for PoS tagging

What information can be used to determine the most likely PoS tag for a word token?

- Word identity (the likelihood of a tag given the word)
- Adjacent PoS tags (the likelihood of a sequence of tags)

# Word identities

- A word may have different possible PoS tags
- But they are not all equally likely
- **Entropy** can be used to measure the uncertainty in the tag distribution
  - 50:50 is high entropy (high uncertainty)
  - 90:10 is low entropy (low uncertainty)
  - See the lab
- Tag distributions for words are often low entropy:
  - one tag is far more likely than the other possibilities

# A unigram Pos tagger

- Choose the most likely tag for each word

$$\text{tag}(w) = \underset{t}{\operatorname{argmax}} P(t|w)$$

- Use labelled training data to estimate these probabilities

$$P(t|w) = \frac{\text{number of occurrences of } w \text{ tagged as } t}{\text{number of occurrences of } w}$$

- Always chooses same tag for a word regardless of context
- Usually results in a tagger with about 90% accuracy

# Beyond unigram PoS tagging

- Which of these look like a possible tag sequence in well-formed English?
  - DET DET JJR NN NNS VBD
  - DET NNS VBD DET JJR NN
  - VBD JJR NNS DET NN DET
- How can we incorporate information about likely tag sequences into a tagger?
  - Hidden Markov Models (HMMs)

# Part 2: Hidden Markov Models

# Consider this example

“Every night I dream the same dream.”

- What PoS tag would you associate with each token in the sentence above?
- Which word type(s) are ambiguous with respect to PoS tag?
- How do you know the correct tag?

# The PoS tagging problem

- Input: a sequence of words  $w_1^n$ :

$$w_1^n = (w_1, w_2, \dots, w_n)$$

- Output: a sequence of tags  $t_1^n$ :

$$t_1^n = (t_1, t_2, \dots, t_n)$$

- In particular, find the most probable PoS tag sequence  $\hat{t}_1^n$ :

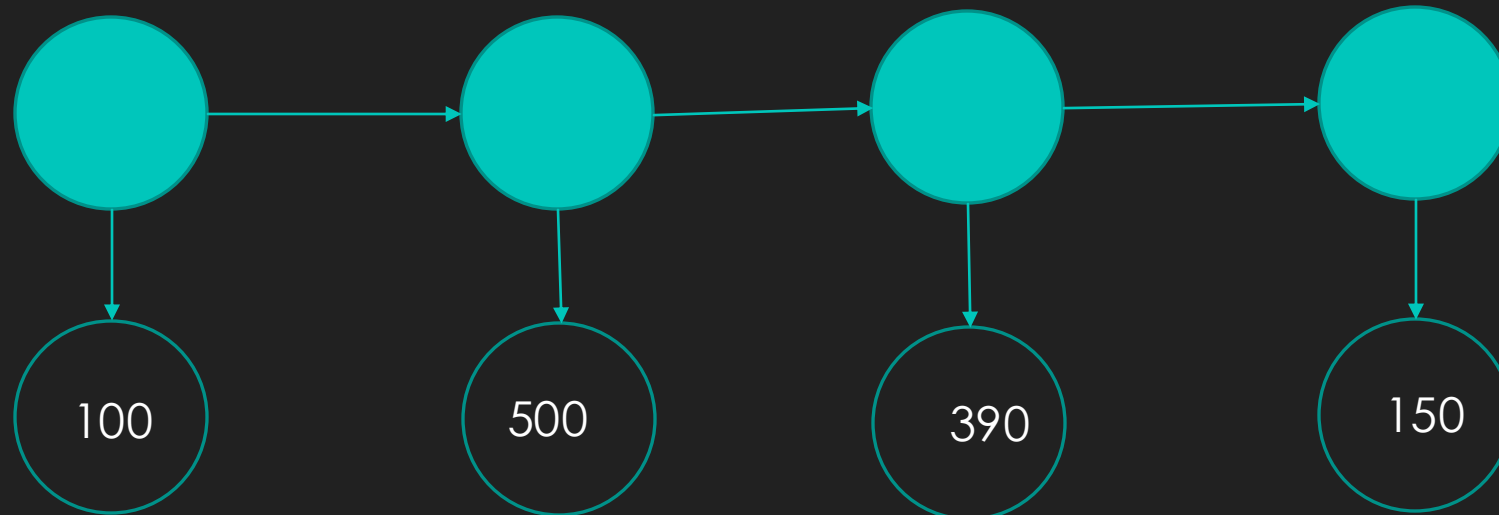
$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n)$$



# Hidden Markov Models (HMMs)

A sequence of **observations** is generated by a sequence of **hidden states**.

*Can we infer the most likely sequence of hidden states from the observations*

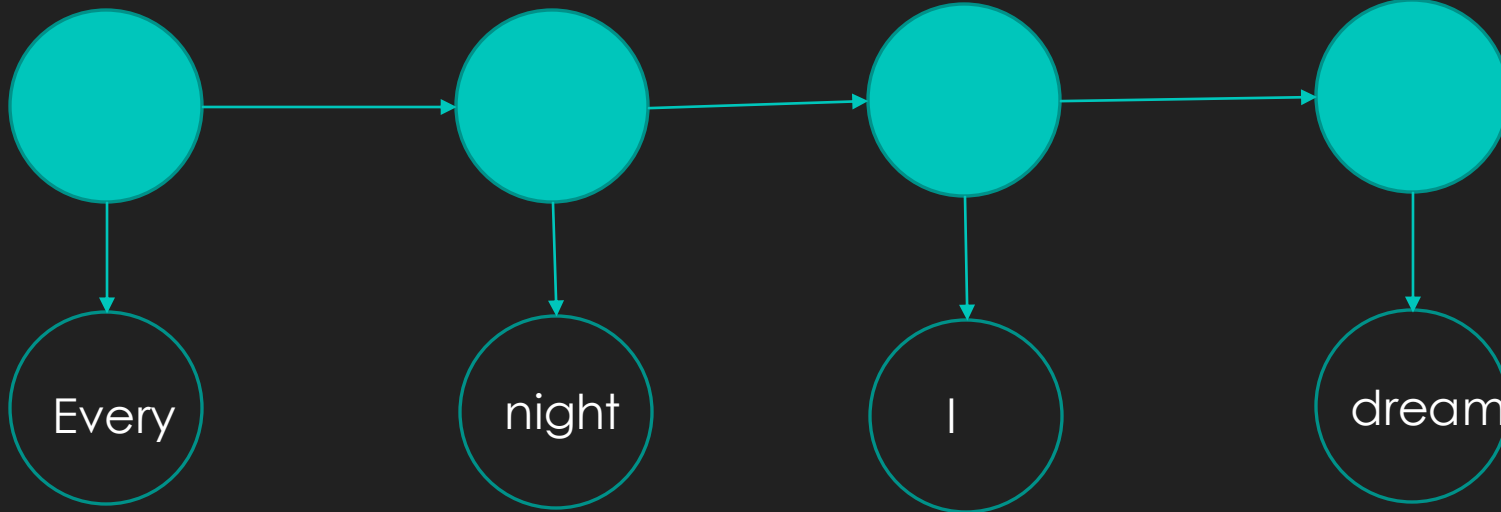


**Markov Assumption:**  
current state  
depends only on  
previous state

**Output Assumption:**  
current output  
depends only on  
current state

# HMMs for PoS Tagging

POS tags  
are the  
hidden  
states

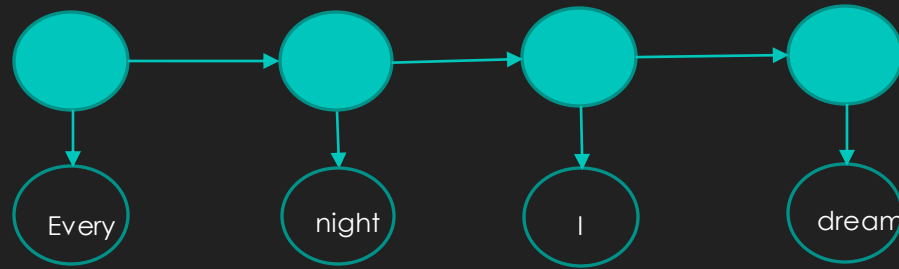


Words are  
the  
observations

**Markov assumption:**  
current POS tag  
depends only on  
single previous tag

**Output assumption:**  
word depends only  
on current POS tag

# Encoding the assumptions probabilistically



**Markov assumption:** current POS tag depends only on single previous tag

$$P(t_i | t_1^{i-1}) = P(t_i | t_{i-1})$$

**Output assumption:** word depends only on current POS tag

$$P(w_1^n | t_1^n) = \prod_i^n P(w_i | t_i)$$

# Parameters for an HMM

To define a HMM tagger, we need to specify:

- **Emission** or **observation** probabilities:
  - $P(w|t)$  for each word  $w$  and tag  $t$
- **Transition** or **bigram** probabilities:
  - $P(t_j|t_i)$  for each pair of tags  $t_i$  and  $t_j$

These probabilities can be:

- calculated directly from POS-tagged corpora (supervised approach)
- learnt from untagged corpora (unsupervised approach) using Expectation Maximisation (EM)

# Calculating emission probabilities

- For each possible tag, we need to count the number of occurrences of each word.

train

```
[('Pierre', 'NNP'),  
 ('Vinken', 'NNP'),  
 (',', ','),  
 ('61', 'CD'),  
 ('years', 'NNS'),  
 ('old', 'JJ'),  
 (',', ','),  
 ('will', 'MD'),  
 ('join', 'VB'),  
 ('the', 'DT'),  
 ('board', 'NN'),  
 ('as', 'IN'),  
 ('a', 'DT'),  
 ('nonexecutive', 'JJ'),  
 ('director', 'NN'),  
 ('Nov.', 'NNP'),  
 ('29', 'CD'),  
 (',', ',')]
```

```
def calculate_emissions(trainlist):  
    #trainlist is a list of (word,tag) pairs  
    emissions={}  
    for word,tag in trainlist:  
        current=emissions.get(tag,{})  
        current[word]=current.get(word,0)+1  
        emissions[tag]=current  
    return {tag:{word:value/sum(worddist.values()) for word,value in worddist.items()}  
            for tag,worddist in emissions.items()}
```

```
: calculate_emissions(train)
```

```
: {'NNP': {'Pierre': 6.613100552193897e-05,  
          'Vinken': 2.204366850731299e-05,  
          'Nov.': 0.0026231965523702454,  
          'Mr.': 0.04412040251738694,  
          'Elsevier': 1.1021834253656494e-05,  
          'N.V.': 0.0001432838452975344,  
          'Dutch': 8.817467402925195e-05,
```

# Calculating transition probabilities

- For each possible tag, we need to count the number of occurrences of each previous tag.

```
train
```

```
[('Pierre', 'NNP'),  
 ('Vinken', 'NNP'),  
 ('', ' '),  
 ('61', 'CD'),  
 ('years', 'NNS'),  
 ('old', 'JJ'),  
 ('', ' '),  
 ('will', 'MD'),  
 ('join', 'VB'),  
 ('the', 'DT'),  
 ('board', 'NN'),  
 ('as', 'IN'),  
 ('a', 'DT'),  
 ('nonexecutive', 'JJ'),  
 ('director', 'NN'),  
 ('Nov.', 'NNP'),  
 ('29', 'CD'),  
 ('', ' ')]
```

```
: def calculate_transitions(trainlist):  
    transitions={}  
    previous="start"  
    for _, tag in trainlist:  
        current=transitions.get(previous,{})  
        current[tag]=current.get(tag,0)+1  
        transitions[tag]=current  
        previous =tag  
    return {previous:{tag:value/sum(tagdist.values()) for tag,value in tagdist.items()}  
            for previous,tagdist in transitions.items()}
```

```
: calculate_transitions(train)
```

```
: {'NNP': {'NNP': 0.09662176841190528,  
          ' ': 0.05123470200593816,  
          'CD': 0.0383040898305879,  
          'NNS': 0.06321111977269726,  
          'JJ': 0.06465412582586803,  
          'MD': 0.010335331177876321,  
          'VB': 0.02326265242573224,  
          'DT': 0.02326265242573224,  
          'IN': 0.02326265242573224,  
          'NN': 0.02326265242573224,  
          'MD': 0.010335331177876321,  
          'JJ': 0.06465412582586803,  
          'NNS': 0.06321111977269726,  
          'CD': 0.0383040898305879,  
          ' ': 0.05123470200593816,  
          'NNP': 0.09662176841190528}}
```

# Forward Algorithm

- calculates the probability of a word sequence given a tag sequence

$$P(w_1^n | t_1^n) = \prod_i^n P(w_i | t_i)$$

remember the output  
assumption: the current word  
only depends on the current  
tag

w	P(w   N)	P(w   V)
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

$$\begin{aligned} &P(\text{flies like flowers} | N \ V \ N) \\ &= P(\text{flies} | N) \cdot P(\text{like} | V) \cdot P(\text{flowers} | N) \\ &= 0.025 \times 0.034 \times 0.05 = 0.0000425 \end{aligned}$$

# Tagging as decoding

How do we use a HMM to find the most likely tag sequence?

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n)$$

Apply Bayes' Rule

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \frac{P(w_1^n | t_1^n) P(t_1^n)}{P(w_1^n)}$$

Drop the denominator

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(w_1^n | t_1^n) P(t_1^n)$$



# Simplifying assumptions

Assume output independence: current observation depends only on current state

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \prod_i^n P(w_i | t_i) P(t_1^n)$$

Make the bigram or first order Markov assumption: current state depends only on the single previous state

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \prod_i^n P(w_i | t_i) P(t_i | t_{i-1})$$

emission probabilities

transition probabilities

# Decoding

- Given a tag sequence and a word sequence, we can estimate the probability that the word sequence was generated by that tag sequence

$$P(t_1^n | w_1^n) \propto \prod_i^n P(w_i | t_i) P(t_i | t_{i-1})$$

- So given two possible tag sequences we can choose between them

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \prod_i^n P(w_i | t_i) P(t_i | t_{i-1})$$

# Decoding example

- Which is the most likely tag sequence for “flies like flowers”?
  - NVN
  - VNN

w	$P(w   N)$	$P(w   V)$
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

	N	V	start
N	$P(N   N) = 0.13$	$P(V   N) = 0.43$	$P(\text{start}   N) = 0$
V	$P(N   V) = 0.35$	$P(V   V) = 0.05$	$P(\text{start}   V) = 0$
start	$P(N   \text{start}) = 0.29$	$P(V   \text{start}) = 0.32$	$P(\text{start}   \text{start}) = 0$

# $P(N \ V \ N \mid \text{flies like flowers})$

w	$P(w \mid N)$	$P(w \mid V)$
flies	<b>0.025</b>	0.015
like	0.012	<b>0.034</b>
flowers	<b>0.05</b>	0.005

	N	V	start
N	$P(N \mid N) = 0.13$	<b><math>P(V \mid N) = 0.43</math></b>	$P(\text{start} \mid N) = 0$
V	<b><math>P(N \mid V) = 0.35</math></b>	$P(V \mid V) = 0.05$	$P(\text{start} \mid V) = 0$
start	<b><math>P(N \mid \text{start}) = 0.29</math></b>	$P(V \mid \text{start}) = 0.32$	$P(\text{start} \mid \text{start}) = 0$

$$P(\text{flies like flowers} \mid N \ V \ N) = P(\text{flies} \mid N) \times P(\text{like} \mid V) \times P(\text{flowers} \mid N) \\ = 0.025 \times 0.034 \times 0.05 = 0.0000425$$

$$P(N \ V \ N) = P(N \mid \text{start}) \times P(V \mid N) \times P(N \mid V) = 0.29 \times 0.43 \times 0.35 = 0.043645$$

$$P(N \ V \ N \mid \text{flies like flowers}) = 0.0000425 \times 0.043645 = 0.0000018549125$$

# $P(V\ N\ N \mid \text{Flies like flowers})$

w	$P(w \mid N)$	$P(w \mid V)$
flies	0.025	<b>0.015</b>
like	<b>0.012</b>	0.034
flowers	<b>0.05</b>	0.005

	N	V	start
N	<b><math>P(N \mid N) = 0.13</math></b>	$P(V \mid N) = 0.43$	$P(\text{start} \mid N) = 0$
V	<b><math>P(N \mid V) = 0.35</math></b>	$P(V \mid V) = 0.05$	$P(\text{start} \mid V) = 0$
start	$P(N \mid \text{start}) = 0.29$	<b><math>P(V \mid \text{start}) = 0.32</math></b>	$P(\text{start} \mid \text{start}) = 0$

$$P(\text{flies like flowers} \mid V\ N\ N) = 0.015 \times 0.012 \times 0.05 = \mathbf{0.00009}$$

$$P(V\ N\ N) = P(V \mid \text{start}) \times P(N \mid V) \times P(N \mid N) = 0.32 \times 0.35 \times 0.13 = \mathbf{0.01456}$$

$$P(V\ N\ N \mid \text{flies like flowers}) = \mathbf{0.00009} \times \mathbf{0.01456} = 0.0000013104$$

So which is the most likely tag sequence given the word sequence?

# Finding the most likely tag sequence

- Brute force?
- Number of possible tag sequences =  $k^n$ 
  - where  $k = |\text{tagset}|$ ,  $n = |\text{word tokens}|$
- With a tagset of size 2 and a sentence of length 3 there are:  $2^3 = 8$  possible tag sequences
  - possible to try every one
- With a tagset of size 10 and a sentence of length 8 there are:
  - $10^8 = 100\,000\,000$  possible tag sequences
  - it would take just over 1 day to check all possible tag sequence at the rate of 1000 per second
- With a tagset of size 45 and a sentence of length 15 ....

# Viterbi Algorithm

- finds the best tag sequence without enumerating all possibilities
- exploits HMM assumptions
  - probability of next state only depends on current state
  - probability of current output only depends on current state
- classic example of dynamic programming
  - recursively decompose problem into smaller problems
  - keep track of (tabulate) solutions to sub-problems

# Viterbi sub-problems

- For an input sequence  $w_1^n$
- A sub-problem corresponds to a pair  $(i, t)$  where:
- $i$  is the position in the sequence,  $i < n$
- $t$  is the current PoS tag

*flies like flowers*

$i=1$ , store best path where  
 $t_1=N$   
 $t_1=V$



# Viterbi sub-problems

- For an input sequence  $w_1^n$
- A sub-problem corresponds to a pair  $(i, t)$  where:
- $i$  is the position in the sequence,  $i < n$
- $t$  is the current PoS tag

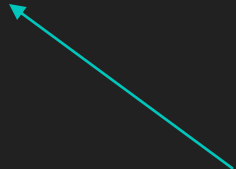
*flies like flowers*

$i=2$ , store best path where  
 $t_2=N$   
 $t_2=V$

# Viterbi sub-problems

- For an input sequence  $w_1^n$
- A sub-problem corresponds to a pair  $(i,t)$  where:
- $i$  is the position in the sequence,  $i < n$
- $t$  is the current PoS tag

*flies like flowers*



$i=3$ , store best path  
 $t_3=N$   
 $t_3=V$

# Viterbi initialisation

*flies like flowers*

i=1, store best path where  
 $t_1=N$   
 $t_1=V$

Subproblem 1:  $t_1 = N$

$$V(1, N) = P(t_1 = N) = P(\text{flies}|N) \times P(N|\text{start}) \\ = 0.025 \times 0.29 = 0.00725$$

Subproblem 2:  $t_1 = V$

$$V(1, V) = P(t_1 V) = P(\text{flies}|V) \times P(V|\text{start}) \\ = 0.015 \times 0.32 = 0.0048$$

w	P(w   N)	P(w   V)
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

	N	V	start
N	$P(N   N) = 0.13$	$P(V   N)=0.43$	$P(\text{start}   N)=0$
V	$P(N   V)= 0.35$	$P(V   V)=0.05$	$P(\text{start}   V)=0$
start	$P(N   \text{start})=0.29$	$P(V   \text{start})=0.32$	$P(\text{start}   \text{start})=0$

# Recursive Step

- For each subsequent position  $i \in \{2, \dots, n\}$  and each tag,  $t$

$$V(i, t) = \max_{t' \in T} (V(i - 1, t') \times P(t|t') \times P(w_i|t))$$

- For each possible previous tag  $t'$ , what's the probability of the current tag being  $t$ ?
- Which of these is highest? If the current tag is  $t$  then the previous tag must have been the one which gave the highest probability

# Step 2

*flies like flowers*

i=2, store best path where  
 $t_2=N$   
 $t_2=V$

Subproblem 1: **V(2,N)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_2 = N) = V(1, N) \times P(N|N) \times P(\text{like}|N)$$

$$P(t_2 = N) = 0.00725 \times 0.13 \times 0.012 = 0.00001131$$

- **If it was V:**

$$P(t_2 = N) = V(1, V) \times P(N|V) \times P(\text{like}|N)$$

$$P(t_2 = N) = 0.0048 \times 0.35 \times 0.012 = 0.00002016$$

- Which is higher?
- So  $V(2,N) = ??$

w	P(w   N)	P(w   V)
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

	N	V	start
N	$P(N   N) = 0.13$	$P(V   N)=0.43$	$P(\text{start}   N)=0$
V	$P(N   V)= 0.35$	$P(V   V)=0.05$	$P(\text{start}   V)=0$
start	$P(N   \text{start})=0.29$	$P(V   \text{start})=0.32$	$P(\text{start}   \text{start})=0$

# Step 2

*flies like flowers*

i=2, store best path where  
 $t_2=N$   
 $t_2=V$

Subproblem 2: **V(2,V)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_2 = V) = V(1, N) \times P(V|N) \times P(\text{like}|V) = ??$$

- **If it was V:**

$$P(t_2 = V) = V(1, V) \times P(V|V) \times P(\text{like}|V) = ??$$

- Which is higher?
- So  $V(2, V) = ??$

w	P(w   N)	P(w   V)
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

	N	V	start
N	$P(N   N) = 0.13$	$P(V   N) = 0.43$	$P(\text{start}   N) = 0$
V	$P(N   V) = 0.35$	$P(V   V) = 0.05$	$P(\text{start}   V) = 0$
start	$P(N   \text{start}) = 0.29$	$P(V   \text{start}) = 0.32$	$P(\text{start}   \text{start}) = 0$

# Step 3

*flies like flowers*

i=3, store best path where  
 $t_3=N$   
 $t_3=V$

w	P(w   N)	P(w   V)
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

Subproblem 1: **V(3,N)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_3 = N) = V(2, N) \times P(N|N) \times P(flowers|N) = ??$$

- **If it was V:**

$$P(t_3 = N) = V(2, V) \times P(N|V) \times P(flowers|N) = ??$$

- Which is higher?
- So  $V(3, N) = ??$

	N	V	start
N	$P(N   N) = 0.13$	$P(V   N)=0.43$	$P(start   N)=0$
V	$P(N   V)= 0.35$	$P(V   V)=0.05$	$P(start   V)=0$
start	$P(N   start)=0.29$	$P(V   start)=0.32$	$P(start   start)=0$

# Step 3

*flies like flowers*

i=3, store best path where  
 $t_3=N$   
 $t_3=V$

Subproblem 2: **V(3,V)**

The previous tag could have been N or V

- **If it was N:**

$$P(t_3 = V) = V(2, N) \times P(V|N) \times P(\text{flowers}|V) = ??$$

- **If it was V:**

$$P(t_3 = V) = V(2, V) \times P(V|V) \times P(\text{flowers}|V) = ??$$

- Which is higher?
- So  $V(3, V) = ??$

w	P(w   N)	P(w   V)
flies	0.025	0.015
like	0.012	0.034
flowers	0.05	0.005

	N	V	start
N	$P(N   N) = 0.13$	$P(V   N) = 0.43$	$P(\text{start}   N) = 0$
V	$P(N   V) = 0.35$	$P(V   V) = 0.05$	$P(\text{start}   V) = 0$
start	$P(N   \text{start}) = 0.29$	$P(V   \text{start}) = 0.32$	$P(\text{start}   \text{start}) = 0$



# Efficiency of Viterbi


- Number of sub-problems =  $k \times n$
- In each sub-problem, we have to consider  $k$  previous sub-problems
- So complexity =  $k^2 \times n$
- In toy example, worse than  $k^n$ 
  - $12 > 8$
- But with 10 tags and a sentence of length 8
  - $800 \ll 100000000$
- With 45 tags and sentences of length 15
  - $30375 \ll \text{????}$

# Next time

- Another sequence labelling problem
  - Named entity recognition

# Making progress

- There is 1 associated notebook this week:

 part 1: Lab\_8\_1.ipynb