

# Spatial reallocation of areal data

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11, March 2019

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# Introduction

Geographical information  
systems and maps

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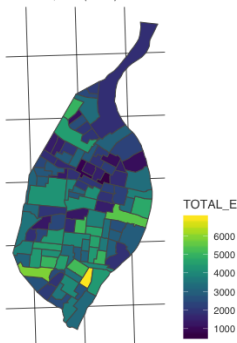
- Spatial interpolation(or Reallocation)is the process of using points with known values to estimate values at other unknown points;
- **Aim:** Spatial interpolation is used to combine information from one data set to another;
- The basic role of spatial interpolation is to fill in the missing data for those areas where real world observations are not available.

The areal interpolation problem can be 2 types.

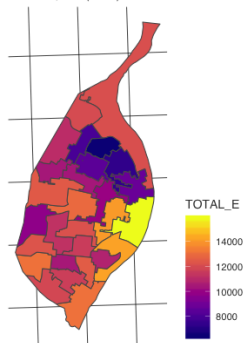
- Aggregation type: if sources are much smaller in size than targets, then a target value is recovered by aggregating sources that will fall inside this target and possibly a few border intersections;
- Disaggregation type: It is the reverse case of the previous one; In this case, a given target will contain intersections of itself with possible several sources.
- We focus on the disaggregation type.

## When do we need to spatially reallocate data?

(A) Total Population per Tract  
St. Louis, MO (2017)



(B) Total Population per Ward  
St. Louis, MO (2017)



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Throughout this work, we are going to:

- Describe 3 class of methods of spatial reallocation:
  - An elementary method: Areal weighing,
  - Dasymetric weighing techniques,
  - Regression techniques;
- Apply these methods on a data set and compare them.



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Throughout this work, we consider the following notations:

- $Y_A$ : target variable on the region  $A$ ;
- $|A|$ : the area of the region  $A$ ;
- $S$ : a set of source zones  $S_s, s = 1, \dots, S$ ;
- $T$ : a set of target zones  $T_t$ , with  $t = 1, \dots, T$ ;
- $A_{s,t} = S_s \cap T_t$ : the intersection zones;
- For simplicity, we set:
  - $Y_{S_s} := Y_s$ ,
  - $Y_{T_t} := Y_t$ ,
  - $Y_{A_{s,t}} := Y_{s,t}$ .

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- **Extensive:** The variable  $Y$  is extensive if its value for a target zone  $t$  is equal to the sum of its value for each zone  $s$  which intersects.

$$Y_t = \sum_s Y_{s,t}$$

- **Intensive:** if its value for a target zone is a weighted average of its value for the intersections zones, often the weights will be the areas involved:

$$Y_t = \frac{\sum_s Y_{s,t} A_{s,t}}{\sum_s A_{s,t}}$$

(e.g. percentage, proportion, ratio)

There are 2 mains properties to

## Homogeneity

- An extensive variable is homogeneous in a given zone  $A$  if it is evenly distributed within  $A$ .
- An intensive variable is homogeneous in a given zone  $A$  when the variable is constant in each sub-zone of  $A$ .

# Properties: -Pycnophylactic Property

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- It ensures the preservation of the initial data;
- **statement:** The predicted value  $\hat{Y}_s$  on source  $S_s$  obtained by aggregating the predicted values on intersections with  $S_s$  should coincide with the observed value  $Y_s$  on  $S_s$ .

## Pycnophylactic Property

- For an Extensive variable:  $Y_{s,t} = \hat{Y}_{s,t}$
- For an Intensive variable :  $Y_{s,t} = \sum_{s': s' \cap t \neq \emptyset} w_{s',t} \hat{Y}_{s',t}$

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# Areal weighting interpolation: How does it work?

- **Input:** A set of source zones;
- **Idea:** Allocate a set of source zones  $S$  into a set of target zones  $T$ ;
- We distinguish 2 cases for computing the intersection zone prediction;

## Extensive variable

It is based on the homogeneity assumption stated as follows;

- **Assumption 1:** For each sub-region  $s$  (with  $s \cap t \neq \emptyset$ ), the estimated value of  $Y$  in  $A_{s,t}$  is:

$$\hat{Y}_{s,t} = \frac{|A_{s,t}|}{|S_s|} Y_s$$

- The target zone prediction is:

$$\hat{Y}_t = \sum_{s: s \cap t \neq \emptyset} \frac{|A_{s,t}|}{|S_s|} Y_s$$



# Areal weighting interpolation: second case

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## Intensive variable

- **Assumption 2:**  $Y$  is uniform on the source zones:

$$\hat{Y}_{s,t} = Y_s$$

- The target zone prediction is:

$$\hat{Y}_t = \sum_{s: s \cap t \neq \emptyset} \frac{|A_{s,t}|}{|T_t|} Y_s$$

where  $\hat{Y}_{s,t}$  is the estimated value for the intersection zones  
and  $\hat{Y}_t$  is the the estimated value for the target zone.

# Areal weighting interpolation: Pros and Cons

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## Pros

- It is the simplest technique used for areal interpolation;
- It can be used for extensive or intensive variable;
- It satisfies the pycnophylactic property;

## Con

- But, it does not require additional auxiliary information;
- Hence, we cannot make use of external knowledge about the data with this method.

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# Dasymetric weighting: Overview

Geographical data science  
and statistics

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- **Objective:** Extension and improvement of the areal weighting methods.
- **Idea:** It uses other relevant and available information  $X$  to distribute  $Y$  accordingly.

## Notes:

- This method is adapted to the case of both intensive and extensive variable  $Y$ .
- This method also satisfies the pycnophylactic property.

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# Ordinary dasymetric weighting

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- **Assumption:** auxiliary information is known at intersection level and it has quantitative nature.

Case of an extensive target variable with an extensive auxiliary variable  $X$ :

■

$$\hat{Y}_t = \sum_{s: s \cap t \neq \emptyset} \frac{X_{s,t}}{X_s} Y_s$$

- This formulae extend the formulae of the areal weighting interpolation by substituting  $X$  for the area

Case of an intensive target variable with weights given by  $\omega_A = \frac{Z_A}{Z_\Omega}$  for a given variable  $Z$  and an extensive auxiliary variable  $X$ :

- We define two variables  $\tilde{Y}_A = Z_A Y_A$  and  $\tilde{X}_A = \frac{X_A}{Z_A}$
- The formula is obtained using the correspondence intensive-to-extension

$$\hat{Y}_t = \sum_{s: s \cap t \neq \emptyset} \frac{X_{s,t}}{X_s} \frac{Z_s}{Z_t} Y_s$$

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- Input: a set of source zones and a categorical ancillary data set—control zone
- Idea: In order to provide a more accurate depiction of how the demographic data is distributed, we redistribute the data to a set of target zones formed from the intersection of the source and ancillary zones. e.g. redistribute the population based on levels of urbanization.
- Assumptions:
  - 1 Auxiliary information is known at intersection level and it has qualitative nature.
  - 2 The count density is uniform throughout control zones.
  - 3 Intersection units are nested within control zones (not restrictive)

# Dasymetric weighting with control zones

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## ■ Method:

- 1 Estimates these densities  $D_c$  for control zone  $c$  by sampling a subset of the total source zones using:

$$\hat{D}_c = \frac{\sum_{s \in c} Y_s}{\sum_{s \in c} |S_s|}$$

- 2 The intersection zone prediction is given by:

$$\hat{Y}_{s,t} = \frac{|A_{s,t}| \hat{D}_{(s,t)}}{\sum_{t': s \cap t' \neq \emptyset} |A_{t',s}| \hat{D}_{c(t',s)}} Y_s$$

- Advantage: The method is guided by use of ancillary land-use data, in contrast to the use of simple areal weighting.
- Limitation: The accuracy of dasymetric maps is highly dependent on the data being used as inputs.

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# Regression with auxiliary information at target level

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- Translate the target variable from source to intersection level  
(  $Y_s \rightarrow Y_{s,t}$  )
- Requires auxiliary information at target level  $X_T$
- Distinguish two cases:

## Extensive variable (count data)

- **Assumption 1:**

$$Y_{s,t} \sim \mathcal{P}(\mu_{s,t})$$

## Intensive variable (shares or ratios)

- **Assumption 1:**

$$Y_{s,t} \sim \mathcal{N}\left(\mu_{s,t}, \frac{\sigma^2}{n_{s,t}}\right)$$

- we assume:

$$\text{Cov}(Y_{s,t}, Y_s) = \sigma^2 / n_s$$

# Regression: How to estimate the model? 1

## (case of an intensive target variable)

- We have the relation between X and Y at target level:

$$E[Y_T|X] = \mu_T = X_T\beta$$

- Given the aggregation equation:

$$\mu_s = \sum_t \frac{n_{s,t}}{n_s} \mu_{s,t}$$

- Given the uniformity at target assumption:

$$\mu_t = \mu_{st}$$

- And the weight matrix W whose elements are given by:

$$w_{s,t} = \frac{n_{s,t}}{n_s}$$

# Regression: How to estimate the model? 2

## (case of an intensive target variable)

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- We get the following regression equation:

$$\mu_S = WX_T\beta \quad \text{with} \quad \mu_S = Y_S$$

- From this equation it is easy to estimate beta using weighted least squares
  - Weights are given by  $n_s$  (usually population)
- Use the model to obtain  $\hat{\mu}_t$  as a predictor for  $Y_t$ :

$$\hat{\mu}_t = X_T\hat{\beta}$$

- (For an extensive target one has to use Poisson regression and adapt the aggregation equation and the weight matrix.)

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The interpolation problem is cast as a missing data problem

- E-step: the algorithm compute an expected values of the intersection values of the target variable given the model and the source values.
  - $\mu_{s,t}$  at first iteration it can be estimated by areal weighting
- M-step: the previous values obtained are considered as i.i.d observation from  $\mathcal{P}(\hat{\mu}_{s,t})$  in case of extensive variable or  $\mathcal{N}(\hat{\mu}_{s,t})$  for intensive
  - we maximize those value and get a new expectation.

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# Regression with control zone

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- Assumption: means on controls zone are uniform  $\mu_{s,c} = \mu_t$   
The homogeneity are on controls ( $C \leq T$ )
- We have also the relation between  $Y$  and  $X$  at controls level:

$$\mu_C = X_C \beta$$

- And the aggregation equation:

$$\mu_s = \sum_c \frac{n_{s,c}}{n_s} \mu_{s,c}$$

- We get :

$$\mu_C = X_C \beta$$

$$\mu_s = W X_C \beta$$

with  $w_{s,c} = \frac{n_{s,c}}{n_s}$  element of  $W$

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# Regression with control zones 2

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- We obtain  $\hat{\mu}_C$  as above :

$$\hat{\mu}_C = X_C \hat{\beta}$$

and a predictor of  $Y_t$  by this relation:

$$\hat{Y}_t = \sum_c \frac{n_{c,t}}{n_c} \hat{\mu}_c$$

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- Now, we move on to the application part to apply each of the method we just described.
- For this purpose, let us describe the data used:
  - We use socio-demographic variables given by USA' census (2016):
  - incomepercap(GDP) as extensive variable, car numbers as intensive variable.
  - population on county
  - medianage, popmale, popfemale , popwhite , popblack, popasia, medianincome,unemployed,laborforce, incomepercap, ginicoef, cars, bartenders , as auxiliary's information on state.

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# Absolute Error

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Spatial econometrics

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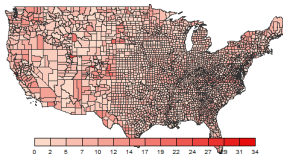
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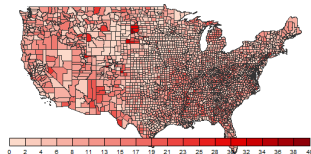
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Absolute errors of AIW methode



(Income per capita)

Absolute errors of regression methode



(per capita income)

# Absolute Error

Researcher's name  
Researcher's name

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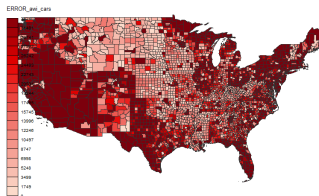
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Absolute errors of DAX method



(number of the cars)

Thanks for your attention!