

Outline for paper

1. Desire for parallelizing multiplication
 - a. Further optimize fast multiplication algorithms
 - i. Downsides of long multiplication
 1. Big O is slow $O(n^2)$
 - ii. Karatsuba's algorithm
 1. First major improvement to multiplication
 2. Splitting up factor into smaller parts
 3. Significant big O decrease
 - iii. Brief mention of Toom-Cook and Fourier transform (FFT algorithm)
 - b. Large Numbers are typically used for
 - i. Cryptography (generating really large numbers)
 - ii. Cosmology (measuring really large astronomical values)
 - iii. Important for solving some math problems where large numbers need to be checked, such as primes and $3n+1$ conjecture
2. Difficulty of parallelizing multiplication
 - a. Splitting up factors
 - i. Must divide string first (use of hex)
 - b. Bit shifting
 - i. Takes up some of the cost that would be otherwise be saved from calculating individual partial sums
3. How we did our naive pthread program
 - a. Use of the GNU library
 - i. `Mpz_t` struct
 1. Can store an extremely large integers
 - b. Give each task a part of one factor
 - i. Calculate the substring
 - c. Global of other factor
 - i. `mpz_t_init_set_str`
 - d. Compute partial sum
 - i. `Mpz_mult`
 - e. Bit shift over correct number of bits
 - i. `Mpz_mult_2exp` function
 - f. Add all values together(in mutex)
 - i. `Mpz_add`
 - g. Timing results (how it compares at various values)

Sources

1. GNU Library documentation <https://gmplib.org/gmp-man-6.2.1.pdf> , specifically sections on fast multiplication algorithms