STAT 210

Applied Statistics and Data Analysis: Homework 2 - Solution

Due on Sept. 18/2022

Question 1

You will need the file Human_data.txt. Place this file on your working environment.

(a) Read the file Human_data.txt and store this in an object called human. Before reading the data, check whether the file has a header. If it does, use the appropriate argument in the read function to include the header. Look at the structure of human using the function str.

```
human <- read.table('Human_data.txt', header = T)
str(human)</pre>
```

```
'data.frame':
                    500 obs. of 10 variables:
   $ Index
                    : int
                           1 2 3 4 5 6 7 8 9 10 ...
                           "M" "F" "M" "F" ...
##
   $ Gender
                    : chr
## $ age
                           22 33 46 24 37 31 38 38 21 31 ...
                    : int
                           "Nothing" "Nothing" "Work" "student" ...
##
  $ Ocupation
                    : chr
## $ Head_size
                           34.4 28 27 24.8 30.1 26.6 25.6 25.6 27.6 23.6 ...
                    : num
##
   $ Height_cm
                           206 163 162 156 173 ...
                    : num
##
  $ Weight_kg
                           105.3 71.3 94.7 56 103.3 ...
                    : num
  $ Salary
                           0 0 19268 2034 14829 10586 11272 13048 2068 12326 ...
                    : int
   $ blood_type
                           4 4 4 3 2 3 4 2 1 3 ...
                    : int
                           95.2 83.5 92.7 95.8 114.1 ...
   $ Sugar_in_blood: num
```

We see that the file has 500 observations of 10 variables, two of which are character variables while the rest are numeric.

(b) The body mass index (BMI) is defined as a person's weight in kilograms divided by the square of height in meters. Add a column named bmi to the data frame with the value of this index for each subject. Count how many subjects have BMI above 30.

There are several ways of adding a variable bmi to the data frame human. One is to use the function within to create the new variable

```
human <- within(human, {bmi = Weight_kg/(Height_cm/100)^2})
str(human)</pre>
```

```
'data.frame':
                    500 obs. of 11 variables:
##
   $ Index
                    : int
                           1 2 3 4 5 6 7 8 9 10
##
   $ Gender
                           "M" "F" "M" "F" ...
                    : chr
  $ age
                           22 33 46 24 37 31 38 38 21 31 ...
                    : int
                           "Nothing" "Nothing" "Work" "student" ...
##
  $ Ocupation
                    : chr
##
   $ Head_size
                           34.4 28 27 24.8 30.1 26.6 25.6 25.6 27.6 23.6 ...
                    : num
                           206 163 162 156 173 ...
##
   $ Height_cm
                    : num
   $ Weight_kg
                           105.3 71.3 94.7 56 103.3 ...
                    : num
                           0 0 19268 2034 14829 10586 11272 13048 2068 12326 ...
   $ Salary
                    : int
```

```
## $ blood_type : int 4 4 4 3 2 3 4 2 1 3 ...
## $ Sugar_in_blood: num 95.2 83.5 92.7 95.8 114.1 ...
## $ bmi : num 24.9 26.9 35.9 23 34.6 ...
```

Another is to define a new variable inside the file human using the \$ notation:

```
human$bmi <- human$Weight_kg/(human$Height_cm/100)^2</pre>
```

A third way is to use the function transform

```
human <- transform(human, bmi = Weight_kg/(Height_cm/100)^2)</pre>
```

Now we count how many subjects have bmi greater than 30.

```
sum(human$bmi>30)
```

```
## [1] 108
```

There are 108 subjects out of 500 with bmi above 30.

(c) Calculate mean and standard deviation for bmi according to Gender. Compare these results and comment. Boxplot bmi against Gender and comment.

A convenient function for calculating mean and standard deviation is tapply

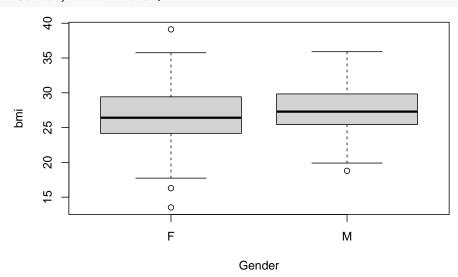
tapply(human\$bmi, human\$Gender, mean)

```
## F M
## 26.60612 27.68282
tapply(human$bmi, human$Gender, sd)
```

```
## F M
## 3.888583 3.253710
```

We see that females have a lower mean value for BMI but the standard deviation is bigger, so the distribution is more spread. This is also apparent form the boxplots:

boxplot(bmi ~ Gender, data = human)



The median for males is higher and the range of values and the box width are shorter than for females.

(d) Using subset, create a new data frame from human with the variables Head_size, Height_cm, Weight_kg for subjects with age between 30 and 50 (both inclusive) and head size bigger than 26. Call this new data frame human1.

(e) Use the function apply twice to calculate the mean and standard deviation for each of the three variables in human1. Call the vectors you obtain human.mean and human.sd.

```
(human.mean <- apply(human1, 2, mean))
## Head_size Height_cm Weight_kg
## 29.06995 173.72069 83.62611
(human.sd <- apply(human1, 2, sd))
## Head_size Height_cm Weight_kg
## 1.844911 11.261780 15.266648</pre>
```

(f) Use the function sweep twice, first to subtract the mean for each variable to the values in human1 and then to divide by the standard deviation. Store the result in a data frame named human.std.

```
human.cen <- sweep(human1, 2, human.mean)
human.std <- sweep(human.cen,2,human.sd,'/')</pre>
```

(g) The previous procedure is known as *standardization*. The resulting columns in the human.std should now have mean zero and variance equal to one. Verify this using apply.

```
apply(human.std, 2, mean)
## Head_size Height_cm Weight_kg
```

Observe that the values we obtain are not exactly zero. This is due to rounding off errors in the calculations. To get a neater result, we can use the function round that rounds off the results to a given accuracy level, in our case 10^{-14} :

```
round(apply(human.std, 2, mean),14)

## Head_size Height_cm Weight_kg
## 0 0 0
apply(human.std, 2, sd)

## Head_size Height_cm Weight_kg
## 1 1 1
```

Question 2

6.606647e-16 6.125368e-16 3.787337e-16

For this question you will use again the file human that you created in the first question.

(a) Use the function split on the file human with second argument Gender and store the result in an object called human2. Describe this object.

```
human2 <- split(human,human$Gender)
str(human2)</pre>
```

```
## List of 2
    $ F:'data.frame':
                        272 obs. of 11 variables:
##
     ..$ Index
                       : int [1:272] 2 4 5 6 7 8 9 10 13 15 ...
                       : chr [1:272] "F" "F" "F" "F" ...
##
     ..$ Gender
##
     ..$ age
                       : int [1:272] 33 24 37 31 38 38 21 31 49 33 ...
     ..$ Ocupation
                       : chr [1:272] "Nothing" "student" "Work" "Work" ...
##
     ..$ Head size
                       : num [1:272] 28 24.8 30.1 26.6 25.6 25.6 27.6 23.6 30.1 25.4 ...
##
     ..$ Height cm
                       : num [1:272] 163 156 173 158 152 ...
##
##
     ..$ Weight kg
                       : num [1:272] 71.3 56 103.3 47 46.5 ...
                        : int [1:272] 0 2034 14829 10586 11272 13048 2068 12326 0 17270 ...
##
     ..$ Salary
##
     ..$ blood_type
                       : int [1:272] 4 3 2 3 4 2 1 3 2 1 ...
     ..$ Sugar_in_blood: num [1:272] 83.5 95.8 114.1 95.1 82.7 ...
##
     ..$ bmi
##
                        : num [1:272] 26.9 23 34.6 18.9 20.1 ...
    $ M:'data.frame':
##
                        228 obs. of 11 variables:
##
     ..$ Index
                       : int [1:228] 1 3 11 12 14 16 17 18 19 20 ...
                       : chr [1:228] "M" "M" "M" "M" ...
##
     ..$ Gender
##
     ..$ age
                       : int [1:228] 22 46 19 38 57 35 29 52 54 41 ...
##
     ..$ Ocupation
                       : chr [1:228] "Nothing" "Work" "student" "Work"
##
     ..$ Head size
                       : num [1:228] 34.4 27 32.3 27.9 27.7 28.7 30.8 29.5 28 26.3 ...
##
     ..$ Height cm
                       : num [1:228] 206 162 190 165 167 ...
##
     ..$ Weight_kg
                       : num [1:228] 105.3 94.7 109.6 98 75.4 ...
##
     ..$ Salary
                       : int [1:228] 0 19268 2493 10900 19709 14521 16198 10961 0 12904 ...
##
     ..$ blood_type
                       : int [1:228] 4 4 2 4 1 4 2 1 3 4 ...
     ..$ Sugar in blood: num [1:228] 95.2 92.7 95.7 106.2 96 ...
##
     ..$ bmi
                        : num [1:228] 24.9 35.9 30.3 35.9 27.1 ...
##
```

The function split creates a list whose components are obtained by dividing the original file according to the value of a factor. In our case the factor is Gender, with two values. Therefore, the list has two components, one for F and one for M. Each component is a data frame with the same variables as the original file.

(b) Using the data in human2 obtain a numerical summary (summary) for the variable Salary for males and females and compare.

```
summary(human2$F$Salary)
```

##

##

..\$ age

```
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                  Max.
##
         0
               2063
                       10660
                                        13364
                                                 44232
                                8849
summary(human2$M$Salary)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                  Max.
##
               2152
                       11178
                                9836
                                        14404
                                                 27354
```

We observe that all the values in the summary are higher for males, except for the maximum, which is much higher for females.

(c) Use again the function split on human but now you want to use two variables for splitting the data, Gender and Work. Look at the help for this function to find out how to do this. Call the resulting object human3. Describe the file human3.

```
human3 <- split(human,list(human$Ocupation, human$Gender))</pre>
str(human3)
## List of 6
    $ Nothing.F:'data.frame':
##
                                 61 obs. of 11 variables:
                        : int [1:61] 2 13 22 26 27 32 33 38 44 61 ...
##
     ..$ Index
     ..$ Gender
                        : chr [1:61] "F" "F" "F" "F" ...
```

: int [1:61] 33 49 20 24 21 26 24 38 26 31 ...

```
: chr [1:61] "Nothing" "Nothing" "Nothing" "Nothing" ...
##
     ..$ Ocupation
                       : num [1:61] 28 30.1 27.8 25.2 24.6 29.6 26.8 28.7 28.4 27.6 ...
##
     ..$ Head size
##
                      : num [1:61] 163 178 160 156 156 ...
     ..$ Height cm
##
                       : num [1:61] 71.3 109 83.9 64.6 58.7 96.9 74.8 91.1 88.3 84.9 ...
     ..$ Weight_kg
                       : int [1:61] 0 0 0 0 0 0 0 0 0 0 ...
##
     ..$ Salary
##
     ..$ blood type
                       : int [1:61] 4 2 3 3 4 3 4 3 1 4 ...
##
     ..$ Sugar in blood: num [1:61] 83.5 81.1 83 98.1 83.2 ...
                       : num [1:61] 26.9 34.3 32.9 26.4 24.2 ...
##
##
    $ student.F:'data.frame':
                                47 obs. of 11 variables:
                       : int [1:47] 4 9 47 55 62 103 122 126 129 141 ...
##
     ..$ Index
                       : chr [1:47] "F" "F" "F" "F" ...
##
     ..$ Gender
##
                       : int [1:47] 24 21 23 22 21 20 22 20 22 24 ...
     ..$ age
##
     ..$ Ocupation
                       : chr [1:47] "student" "student" "student" "student" ...
     ..$ Head_size : num [1:47] 24.8 27.6 23.5 26.5 24.9 27.9 29.9 22.7 26.8 29.6 ... 
..$ Height_cm : num [1:47] 156 164 145 159 155 ...
##
##
                       : num [1:47] 56 82.2 82.7 75.3 51.7 75.1 92.7 40.1 64.7 73.5 ...
##
     ..$ Weight_kg
##
     ..$ Salary
                       : int [1:47] 2034 2068 2271 2157 2415 2539 2345 2008 2064 2443 ...
                       : int [1:47] 3 1 3 1 4 3 1 4 2 2 ...
##
     ..$ blood_type
     ..$ Sugar_in_blood: num [1:47] 95.8 80.5 91.2 95.5 86.7 87.1 94.5 99 93.1 81.2 ...
##
     ..$ bmi
                       : num [1:47] 23 30.7 39.1 29.9 21.6 ...
##
##
   $ Work.F
               :'data.frame':
                                164 obs. of 11 variables:
##
     ..$ Index
                       : int [1:164] 5 6 7 8 10 15 21 24 31 36 ...
##
     ..$ Gender
                       : chr [1:164] "F" "F" "F" "F" ...
                       : int [1:164] 37 31 38 38 31 33 49 42 44 50 ...
##
     ..$ age
##
     ..$ Ocupation
                       : chr [1:164] "Work" "Work" "Work" "Work" ...
##
     ..$ Head size
                       : num [1:164] 30.1 26.6 25.6 25.6 23.6 25.4 26.5 23.7 24.6 26.6 ...
                       : num [1:164] 173 158 152 153 149 ...
##
     ..$ Height_cm
##
     ..$ Weight_kg
                       : num [1:164] 103.3 47 46.5 64.6 52.1 ...
##
     ..$ Salary
                       : int [1:164] 14829 10586 11272 13048 12326 17270 11992 11996 12646 10412 ...
     ..$ blood_type : int [1:164] 2 3 4 2 3 1 1 4 3 2 ...
     ..$ Sugar_in_blood: num [1:164] 114.1 95.1 82.7 112 100.6 ...
##
     ..$ bmi
                       : num [1:164] 34.6 18.9 20.1 27.7 23.5 ...
##
##
   $ Nothing.M:'data.frame':
                                49 obs. of 11 variables:
##
     ..$ Index
                       : int [1:49] 1 19 23 34 42 43 46 52 60 106 ...
                       : chr [1:49] "M" "M" "M" "M" ...
     ..$ Gender
##
##
     ..$ age
                       : int [1:49] 22 54 37 20 45 36 34 52 59 45 ...
     ..$ Ocupation : chr [1:49] "Nothing" "Nothing" "Nothing" "Nothing" ...
##
##
     ..$ Head_size
                      : num [1:49] 34.4 28 30.1 28.6 28.2 32.9 28.9 28.7 27.5 30.5 ...
                       : num [1:49] 206 173 182 177 163 ...
##
     ..$ Height_cm
##
     ..$ Weight_kg
                       : num [1:49] 105.3 69.1 92.4 74.9 56.6 ...
                       : int [1:49] 0 0 0 0 0 0 0 0 0 0 ...
##
     ..$ Salary
     ..$ blood_type
                       : int [1:49] 4 3 1 3 1 2 1 3 3 3 ...
##
##
     ..$ Sugar in blood: num [1:49] 95.2 99.4 93.3 88 90.9 ...
##
     ..$ bmi
                       : num [1:49] 24.9 23.2 28 23.8 21.3 ...
##
   $ student.M:'data.frame':
                                28 obs. of 11 variables:
                       : int [1:28] 11 63 94 108 110 111 124 128 155 163 ...
##
     ..$ Index
                       : chr [1:28] "M" "M" "M" "M" ...
##
     ..$ Gender
##
     ..$ age
                       : int [1:28] 19 18 24 24 21 20 19 22 22 21 ...
                       : chr [1:28] "student" "student" "student" "student" ...
##
     ..$ Ocupation
##
                       : num [1:28] 32.3 31.6 29.4 28 26 28.9 30.8 31.5 31.3 31.3 ...
     ..$ Head_size
     ..$ Height_cm
                       : num [1:28] 190 190 174 174 165 ...
##
##
     ..$ Weight_kg
                      : num [1:28] 109.6 110.2 81.5 80.4 89.3 ...
                       : int [1:28] 2493 2739 2028 2083 2063 2263 2427 3402 2152 2269 ...
##
     ..$ Salary
                       : int [1:28] 2 4 2 1 2 3 3 4 1 1 ...
##
     ..$ blood_type
```

```
##
     ..$ Sugar in blood: num [1:28] 95.7 80.9 108.7 108.8 91.3 ...
                        : num [1:28] 30.3 30.6 27 26.7 32.8 ...
##
     ..$ bmi
                                 151 obs. of
##
    $ Work.M
               :'data.frame':
                                             11 variables:
##
     ..$ Index
                        : int [1:151] 3 12 14 16 17 18 20 25 28 29 ...
##
     ..$ Gender
                       : chr [1:151] "M" "M" "M" "M"
                       : int [1:151] 46 38 57 35 29 52 41 45 55 50 ...
##
     ..$ age
                       : chr [1:151] "Work" "Work" "Work" "Work" ...
##
     ..$ Ocupation
                       : num [1:151] 27 27.9 27.7 28.7 30.8 29.5 26.3 30.2 28.1 30.4 ...
##
     ..$ Head size
##
     ..$ Height cm
                       : num [1:151] 162 165 167 172 182 ...
##
     ..$ Weight_kg
                       : num [1:151] 94.7 98 75.4 55.7 90.1 95.9 58.8 96.2 90.1 88.6 ...
##
     ..$ Salary
                       : int [1:151] 19268 10900 19709 14521 16198 10961 12904 17219 10406 16740 ...
     ..$ blood_type
                       : int [1:151] 4 4 1 4 2 1 4 3 4 2 ...
##
##
     ..$ Sugar_in_blood: num [1:151] 92.7 106.2 96 92.3 101 ...
                        : num [1:151] 35.9 35.9 27.1 18.8 27.1 ...
##
     ..$ bmi
```

The file human3 is a list with six components, each of which is a data frame. The components correspond to the combination of two genders and three ocupation status.

(d) Using the data in human3 obtain numerical summaries for the variable Salary for males and females that work and compare.

```
summary(human3$Work.F$Salary)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                  Max.
##
     10011
              11130
                      12772
                               13960
                                        15696
                                                 44232
summary(human3$Work.M$Salary)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                  Max.
##
     10012
              11245
                      12904
                               14386
                                        16163
                                                 27354
```

Except for the maxima which have the same values as before, the values for the other parameters are closer than when we looked at the complete data set.

(e) The function cut divides the range of values of a continuous variable into intervals and creates a factor according to which interval they fall. You have to use this function to divide the range of salaries in the file human into three intervals, according to the following scheme: between 2000 and 8000 it is low, between 8000 and 18000 it is medium, and more than 18000 it is high. Call the resulting factor sal. Use the function table to count how many subjects fall in each category.

```
sal <- cut(human$Salary,c(2000,8000, 18000, 45000), labels = c('low','medium','high'))
table(sal)

## sal
## low medium high
## 75 272 43</pre>
```

(f) Using the factor sal and the variable Gender, split the file human and call the resulting file human4. Using this file, obtain numerical summaries for the variable Salary for males and females that have a high salary and compare.

```
human4 <- split(human, list(sal, human$Gender))</pre>
str(human4)
## List of 6
##
    $ low.F
              :'data.frame':
                                 47 obs. of 11 variables:
##
     ..$ Index
                        : int [1:47] 4 9 47 55 62 103 122 126 129 141 ...
                                     "F" "F" "F" "F" ...
##
                        : chr [1:47]
     ..$ Gender
##
     ..$ age
                        : int [1:47] 24 21 23 22 21 20 22 20 22 24 ...
     ..$ Ocupation
                        : chr [1:47] "student" "student" "student" "student" ...
##
```

```
: num [1:47] 24.8 27.6 23.5 26.5 24.9 27.9 29.9 22.7 26.8 29.6 ...
##
     ..$ Head size
                       : num [1:47] 156 164 145 159 155 ...
##
     ..$ Height_cm
     ..$ Weight_kg
##
                       : num [1:47] 56 82.2 82.7 75.3 51.7 75.1 92.7 40.1 64.7 73.5 ...
##
                       : int [1:47] 2034 2068 2271 2157 2415 2539 2345 2008 2064 2443 ...
     ..$ Salary
     ..$ blood_type
                       : int [1:47] 3 1 3 1 4 3 1 4 2 2 ...
##
##
     ..$ Sugar in blood: num [1:47] 95.8 80.5 91.2 95.5 86.7 87.1 94.5 99 93.1 81.2 ...
##
                       : num [1:47] 23 30.7 39.1 29.9 21.6 ...
                                147 obs. of 11 variables:
##
    $ medium.F:'data.frame':
##
     ..$ Index
                       : int [1:147] 5 6 7 8 10 15 21 24 31 36 ...
                       : chr [1:147] "F" "F" "F" "F" ...
##
     ..$ Gender
##
     ..$ age
                       : int [1:147] 37 31 38 38 31 33 49 42 44 50 ...
##
                       : chr [1:147] "Work" "Work" "Work" "Work" ...
     ..$ Ocupation
##
                       : num [1:147] 30.1 26.6 25.6 25.6 23.6 25.4 26.5 23.7 24.6 26.6 ...
     ..$ Head_size
##
     ..$ Height_cm
                       : num [1:147] 173 158 152 153 149 ...
                       : num [1:147] 103.3 47 46.5 64.6 52.1 ...
##
     ..$ Weight_kg
                       : int [1:147] 14829 10586 11272 13048 12326 17270 11992 11996 12646 10412 \dots
##
     ..$ Salary
##
     ..$ blood_type
                       : int [1:147] 2 3 4 2 3 1 1 4 3 2 ...
     ..$ Sugar in blood: num [1:147] 114.1 95.1 82.7 112 100.6 ...
##
                       : num [1:147] 34.6 18.9 20.1 27.7 23.5 ...
##
     ..$ bmi
                                17 obs. of 11 variables:
   $ high.F :'data.frame':
##
##
    ..$ Index
                       : int [1:17] 50 65 85 88 95 116 168 221 245 299 ...
                       : chr [1:17] "F" "F" "F" "F" ...
##
     ..$ Gender
##
                       : int [1:17] 48 36 53 54 43 31 46 40 26 45 ...
     ..$ age
                       : chr [1:17] "Work" "Work" "Work" "Work" ...
##
     ..$ Ocupation
##
                       : num [1:17] 24.9 26.9 30.3 28.1 25.9 30.3 26.6 30.7 24.5 24.1 ...
     ..$ Head size
##
     ..$ Height_cm
                       : num [1:17] 145 158 186 160 158 ...
##
     ..$ Weight_kg
                       : num [1:17] 56.6 61.4 85.5 66.2 69.1 75.1 62.7 87.2 71.4 48.1 ...
##
     ..$ Salary
                       : int [1:17] 20360 23772 18025 21671 26658 18568 18372 20351 20065 21314 \dots
##
     ..$ blood_type
                     : int [1:17] 1 2 4 3 3 2 3 4 2 1 ...
     ..$ Sugar_in_blood: num [1:17] 101.1 81.6 94.5 96.8 97 ...
                       : num [1:17] 26.9 24.6 24.6 25.8 27.6 ...
##
     ..$ bmi
##
   $ low.M
            :'data.frame':
                                28 obs. of 11 variables:
##
     ..$ Index
                       : int [1:28] 11 63 94 108 110 111 124 128 155 163 ...
                       : chr [1:28] "M" "M" "M" "M" ...
##
     ..$ Gender
                       : int [1:28] 19 18 24 24 21 20 19 22 22 21 ...
##
     ..$ age
     ..$ Ocupation : chr [1:28] "student" "student" "student" "student" ...
..$ Head_size : num [1:28] 32.3 31.6 29.4 28 26 28.9 30.8 31.5 31.3 31.3 ...
##
##
##
     ..$ Height_cm
                       : num [1:28] 190 190 174 174 165 ...
                       : num [1:28] 109.6 110.2 81.5 80.4 89.3 ...
##
     ..$ Weight_kg
##
                       : int [1:28] 2493 2739 2028 2083 2063 2263 2427 3402 2152 2269 ...
     ..$ Salary
     ..$ blood_type
##
                       : int [1:28] 2 4 2 1 2 3 3 4 1 1 ...
     ..$ Sugar_in_blood: num [1:28] 95.7 80.9 108.7 108.8 91.3 ...
##
##
                       : num [1:28] 30.3 30.6 27 26.7 32.8 ...
##
   $ medium.M:'data.frame':
                                125 obs. of 11 variables:
##
     ..$ Index
                       : int [1:125] 12 16 17 18 20 25 28 29 35 37 ...
                       : chr [1:125] "M" "M" "M" "M" ...
##
     ..$ Gender
##
                       : int [1:125] 38 35 29 52 41 45 55 50 52 28 ...
     ..$ age
##
     ..$ Ocupation
                       : chr [1:125] "Work" "Work" "Work" "Work" ...
                       : num [1:125] 27.9 28.7 30.8 29.5 26.3 30.2 28.1 30.4 31.5 32.5 ...
##
     ..$ Head_size
##
     ..$ Height_cm
                       : num [1:125] 165 172 182 180 163 ...
                       : num [1:125] 98 55.7 90.1 95.9 58.8 ...
##
     ..$ Weight_kg
                       : int [1:125] 10900 14521 16198 10961 12904 17219 10406 16740 10170 10540 ...
##
     ..$ Salary
     ..$ blood_type : int [1:125] 4 4 2 1 4 3 4 2 1 1 ...
##
##
     ..$ Sugar_in_blood: num [1:125] 106.2 92.3 101 95.9 85.9 ...
```

```
##
     ..$ bmi
                        : num [1:125] 35.9 18.8 27.1 29.4 22.2 ...
##
    $ high.M
             :'data.frame':
                                 26 obs. of 11 variables:
##
     ..$ Index
                        : int [1:26] 3 14 30 57 70 87 93 98 158 165 ...
                        : chr [1:26]
                                     "M" "M" "M" "M" ...
##
     ..$ Gender
##
     ..$ age
                             [1:26] 46 57 37 44 34 50 60 48 58 52 ...
     ..$ Ocupation
                                     "Work" "Work" "Work" "Work" ...
##
                        : chr [1:26]
##
     ..$ Head size
                        : num [1:26] 27 27.7 32 27.7 27.9 27.7 31.5 25.7 30 27.9 ...
     ..$ Height_cm
                              [1:26] 162 167 189 171 174 ...
##
                        : num
     ..$ Weight_kg
##
                        : num [1:26] 94.7 75.4 100.8 92 92.3 ...
                        : int [1:26] 19268 19709 23514 18945 22760 21741 18905 20455 26258 21811 ...
##
     ..$ Salary
##
     ..$ blood_type
                        : int [1:26] 4 1 2 1 1 1 1 1 4 4 ...
     ..$ Sugar_in_blood: num [1:26] 92.7 96 81.5 83.9 81 ...
##
                        : num [1:26] 35.9 27.1 28.3 31.6 30.5 ...
##
summary(human4$high.F$Salary)
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                               Max.
##
     18025
             18678
                      20351
                              22980
                                      21671
                                               44232
summary(human4$high.M$Salary)
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
```

In this final comparison, the only important change is that the average value for female salary is now above the male salary while the other parameters remain below, except for the maximum value which we already know corresponds to a female. The reason for this change is the effect of two large female salaries on a set of reduced size. See the boxplots below.

27354

24252

18905

19930

21776

22272

##

