CS 484: Introduction to Machine Learning

Spring 2021 Assignment 4

# Question 1 (40 Points)

In 2014, Allstate provided the data on Kaggle.com for the Allstate Purchase Prediction Challenge. The data contain transaction history for customers that ended up purchasing a policy. For each Customer ID, we know the quote history and the purchased coverage options.

The data is available on the Blackboard as **Purchase\_Likelihood.csv**.

1. It contains 665,249 observations on 97,009 unique Customer ID.
2. The nominal target variable is **insurance** that has these categories 0, 1, and 2
3. The nominal features are (categories are inside the parentheses):
4. **group\_size**. *How many people covered under the policy (1, 2, 3, or 4)*?
5. **homeowner**. *Whether the customer owns a home or not (0 = No, 1 = Yes)*?
6. **married\_couple**. *Does the customer group contain a married couple (0 = No, 1 = Yes)*?

You will train a Naïve Bayes model without any smoothing using all the observations in the **Purchase\_Likelihood.csv**. In other words, the Laplace/Lidstone alpha is zero. Please answer the following questions based on your model.

1. (5 points) Show in a table the frequency counts and the Class Probabilities of the target variable.

| insurance | 0 | 1 | 2 |
| --- | --- | --- | --- |
| Frequency Count | 143691 | 426067 | 95491 |
| Class Probability | 0.2159958151008 | 0.6404624433859 | 0.1435417415133 |

1. (5 points) Show the crosstabulation table of the target variable by the feature **group\_size**. The table contains the frequency counts.

| group\_size | insurance | | |
| --- | --- | --- | --- |
| 0 | 1 | 2 |
| 1 | 115460 | 329552 | 74293 |
| 2 | 25728 | 91065 | 19600 |
| 3 | 2282 | 5069 | 1505 |
| 4 | 221 | 381 | 93 |

1. (5 points) Show the crosstabulation table of the target variable by the feature **homeowner**. The table contains the frequency counts.

| homeowner | insurance | | |
| --- | --- | --- | --- |
| 0 | 1 | 2 |
| 0 | 78659 | 183130 | 46734 |
| 1 | 65032 | 242937 | 48757 |

1. (5 points) Show the crosstabulation table of the target variable by the feature **married\_couple**. The table contains the frequency counts.

| Married\_couple | insurance | | |
| --- | --- | --- | --- |
| 0 | 1 | 2 |
| 0 | 117110 | 333272 | 75310 |
| 1 | 26581 | 92795 | 20181 |

1. (5 points) Calculate the Cramer’s V statistics for the above three crosstabulations tables. Based on the Cramer’s V statistics, which feature has the strongest association with the target insurance?

| Feature | Cramer’s V |
| --- | --- |
| group\_size | 0.0271020140558 |
| homeowner | 0.0970864196478 |
| married\_couple | 0.0324216458352 |

* The feature **“homeowner”** has the strongest association with the target insurance because it has the highest Cramer’s V value.

1. (10 points) For each of the sixteen possible value combinations of the three features, calculate the predicted probabilities for insurance = 0, 1, 2 based on the Naïve Bayes model that includes features group\_size, homeowner, and married\_couple. List your answers in a table with proper labeling.

| group\_size | homeowner | married\_couple | Prob (insurance = 0) | Prob (insurance = 1) | Prob (insurance = 2) |
| --- | --- | --- | --- | --- | --- |
| 1 | 0 | 0 | 0.227037256 | 0.627592848 | 0.145369896 |
| 1 | 0 | 1 | 0.214390665 | 0.637466936 | 0.148142399 |
| 1 | 1 | 0 | 0.205587859 | 0.654127713 | 0.140284428 |
| 1 | 1 | 1 | 0.193842332 | 0.663414024 | 0.142743644 |
| 2 | 0 | 0 | 0.238441326 | 0.61446183 | 0.147096844 |
| 2 | 0 | 1 | 0.225341775 | 0.624634588 | 0.150023637 |
| 2 | 1 | 0 | 0.21628069 | 0.641527617 | 0.142191693 |
| 2 | 1 | 1 | 0.204078619 | 0.651127524 | 0.144793857 |
| 3 | 0 | 0 | 0.250201027 | 0.601083762 | 0.148715211 |
| 3 | 0 | 1 | 0.236653104 | 0.611545886 | 0.15180101 |
| 3 | 1 | 0 | 0.227342158 | 0.628651728 | 0.144006114 |
| 3 | 1 | 1 | 0.214684236 | 0.638559292 | 0.146756472 |
| 4 | 0 | 0 | 0.262307501 | 0.587474666 | 0.150217833 |
| 4 | 0 | 1 | 0.248317896 | 0.598215123 | 0.153466982 |
| 4 | 1 | 0 | 0.238767044 | 0.615512737 | 0.145720219 |
| 4 | 1 | 1 | 0.225655892 | 0.625720343 | 0.148623765 |

1. (5 points) Based on your model, determine the value combination of group\_size, homeowner, and married\_couple that will yield the maximum value for this odds Prob (insurance = 1) / Prob (insurance = 2)? What is that maximum odds value?

## Table 1:

| group\_size | homeowner | married\_couple | Prob (insurance = 0) | Prob (insurance = 1) | Prob (insurance = 2) | Odd Value (Prob (insurance = 1)/Prob (insurance = 2)) |
| --- | --- | --- | --- | --- | --- | --- |
| 1 | 0 | 0 | 0.227037256 | 0.627592848 | 0.145369896 | 4.317213292 |
| 1 | 0 | 1 | 0.214390665 | 0.637466936 | 0.148142399 | 4.303068801 |
| 1 | 1 | 0 | 0.205587859 | 0.654127713 | 0.140284428 | 4.662867606 |
| 1 | 1 | 1 | 0.193842332 | 0.663414024 | 0.142743644 | 4.647590647 |
| 2 | 0 | 0 | 0.238441326 | 0.61446183 | 0.147096844 | 4.177260451 |
| 2 | 0 | 1 | 0.225341775 | 0.624634588 | 0.150023637 | 4.163574487 |
| 2 | 1 | 0 | 0.21628069 | 0.641527617 | 0.142191693 | 4.511709549 |
| 2 | 1 | 1 | 0.204078619 | 0.651127524 | 0.144793857 | 4.49692783 |
| 3 | 0 | 0 | 0.250201027 | 0.601083762 | 0.148715211 | 4.041844517 |
| 3 | 0 | 1 | 0.236653104 | 0.611545886 | 0.15180101 | 4.028602216 |
| 3 | 1 | 0 | 0.227342158 | 0.628651728 | 0.144006114 | 4.365451644 |
| 3 | 1 | 1 | 0.214684236 | 0.638559292 | 0.146756472 | 4.351149109 |
| 4 | 0 | 0 | 0.262307501 | 0.587474666 | 0.150217833 | 3.910818415 |
| 4 | 0 | 1 | 0.248317896 | 0.598215123 | 0.153466982 | 3.898005396 |
| 4 | 1 | 0 | 0.238767044 | 0.615512737 | 0.145720219 | 4.223935041 |
| 4 | 1 | 1 | 0.225655892 | 0.625720343 | 0.148623765 | 4.210096157 |

## Table 2:

|  |  |
| --- | --- |
| group\_size | 1 |
| homeowner | 1 |
| married\_couple | 0 |
| Prob (insurance = 0) | 0.205587859 |
| Prob (insurance = 1) | 0.654127713 |
| Prob (insurance = 2) | 0.140284428 |
| Odd Value (Prob (insurance = 1)/Prob (insurance = 2)) | 4.662867606 |

* The value combination of group\_size, homeowner, and married\_couple that will yield the maximum value for this odds Prob (insurance = 1) / Prob (insurance = 2) is **4.662867606** at the combination **(group\_size = 1, homeowner = 1, married\_couple = 0).**
* The maximum odds value is **4.662867606**.

# Question 2 (60 points)

The **SpiralWithCluster.csv** contains four variables.

|  |  |  |  |
| --- | --- | --- | --- |
| **Name** | **Description** | **Measurement Level** | **Role** |
| Id | Case Identifier | Nominal | Identifier |
| X | x-coordinate | Interval | Feature |
| Y | y-coordinate | Interval | Feature |
| SpectralCluster | Cluster Identifier | Binary | Target |

Please use the Support Vector Machine (SVM) algorithm to classify SpectralCluster. You will use the sklearn.svm.SVC function with the following specifications.

1. The linear kernel
2. The decision function shape is One Over Rest (OVR)
3. No limit on the number of iterations
4. The random seed is 20210325

Please answer the following questions based on your model.

1. (5 points) What is the equation of the separating hyperplane in the Slope-Intercept form? Please state the coefficients up to seven decimal places.

## Ans:

The following data are found:

Intercept: [0.003345]

Co-efficient: [[0.05333512 0.32868383]]

Now, the equation of the separating hyperplane in the Slope-Intercept form is given as,

1. (5 points) What is the misclassification rate?

## Ans:

The misclassification rate is **0.5.**

1. (10 points) Please plot the y-coordinate against the x-coordinate in a scatterplot. Please color-code the points using the predicted SpectralCluster (0 = Red and 1 = Blue). Besides, plot the hyperplane as a dotted line to the graph. To obtain the full credits, you should properly label the axes, the legend, and the chart title. Also, please add grid lines to the axes.

## Ans:

The scatterplot is given as:

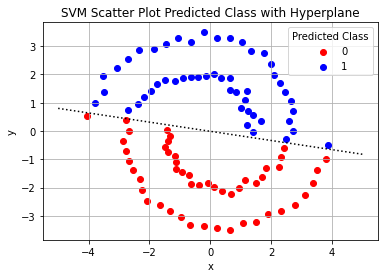


Figure 1

1. (10 points) Please express the data in polar coordinates. Please plot the theta-coordinate against the radius-coordinate in a scatterplot. Please color-code the points using the SpectralCluster variable (0 = Red and 1 = Blue). To obtain the full credits, you should properly label the axes, the legend, and the chart title. Also, please add grid lines to the axes.

## Ans:

The scatterplot is given as:

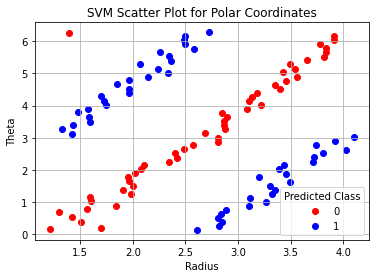


Figure 2

1. (10 points) You should expect to see three distinct strips of points and a single point. Since the SpectralCluster variable has two values, you will create another variable, named Group, and use it as the new target variable. Use your method to generate this Group variable. However, the Group variable must have four values. Value 0 for the single point on the upper left corner of the chart in (d), values 1, 2, and 3 for the next three strips of points.  
     
   Please plot the theta-coordinate against the radius-coordinate in a scatterplot. Please color-code the points using the new Group target variable (0 = Red, 1 = Blue, 2 = Green, 3 = Black). To obtain the full credits, you should properly label the axes, the legend, and the chart title. Also, grid lines should be added to the axes.

## Ans:

The scatterplot is given as:

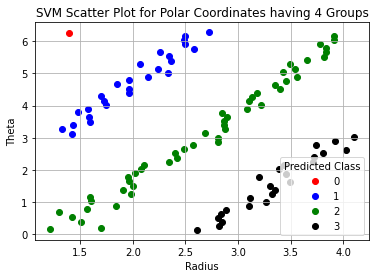


Figure 3

1. (10 points) Since the graph in (e) has four separate but neighboring segments, we will apply the Support Vector Machine algorithm differently. Instead of applying SVM once on a multi-class target variable, you will SVM three times, each on a pair of groups.

SVM 0: Group 0 versus Group 1  
SVM 1: Group 1 versus Group 2  
SVM 2: Group 2 versus Group 3  
Please give the equations of the three hyperplanes.

## Ans:

### SVM 0 (Group 0 versus Group 1):

The following data are found:

Intercept: [1.46912508]

Co-efficient: [[ 0.93378415 -0.45380249]]

Now, the equation of the separating hyperplane in the Slope-Intercept form is given as,

### SVM 1 (Group 1 versus Group 2):

The following data are found:

Intercept: [-0.87689426]

Co-efficient: [[ 1.89209533 -0.89613249]]

Now, the equation of the separating hyperplane in the Slope-Intercept form is given as,

### SVM 2 (Group 2 versus Group 3):

The following data are found:

Intercept: [-4.13284488]

Co-efficient: [[ 2.01258355 -0.83756164]]

Now, the equation of the separating hyperplane in the Slope-Intercept form is given as,

1. (5 points) Please plot the theta-coordinate against the radius-coordinate in a scatterplot. Please color-code the points using the new Group target variable (0 = Red, 1 = Blue, 2 = Green, 3 = Black). Please add the hyperplanes to the graph. To obtain the full credits, you should properly label the axes, the legend, and the chart title. Also, grid lines should be added to the axes.

## Ans:

The scatterplot is given as:

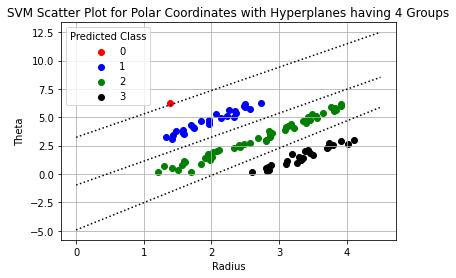


Figure 4

1. (5 points) Convert the observations along with the hyperplanes from the polar coordinates back to the Cartesian coordinates. Please plot the y-coordinate against the x-coordinate in a scatterplot. Please color-code the points using the SpectralCluster (0 = Red and 1 = Blue). Besides, plot the hyper-curves as dotted lines to the graph. To obtain the full credits, you should properly label the axes, the legend, and the chart title. Also, grid lines should be added to the axes.  
     
   Based on your graph, which hypercurve do you think is not needed?

## Ans:

The scatterplot is given as:

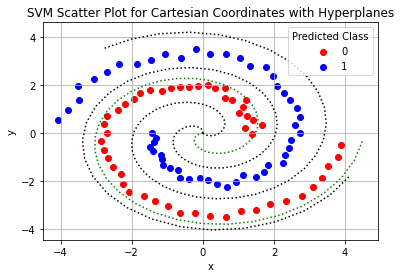


Figure 5

* The hyper curve marked in **“green”** is not needed as it does not separate two classes, whereas the hyper curve marked in black sperate the classes.