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CPSC 335 Project 1: Lawnmower

Alternating Algorithm:

int numOfSwap	-> 1 tu
disk Sort = unsorted	-> 1 tu
for i = 0 in sorted.size() / 2 do	-> (n / 2) tu
for j = i in sorted.size() do	-> (n - 1) tu
if (LIGHT Disk is not followed by DARK Disk) do	-> 4 tu
swap LIGHT and DARK	-> 1 tu
numOfSwap++	-> 1 tu
return sorted and numOfSwap	

This is the pseudocode for the alternate algorithm, and it shows that the worst time complexity for this would be $O(n^2)$

By calculating every step of the pseudocode, we can figure out the time complexity is $1 + 1 + ((n / 2) * (n - 1) * (4 + 1 + 1))$, and if we simplified this equation we would end up with

$$6\frac{n^2}{2} - 6\frac{n}{2} + 2$$

Handwritten mathematical derivation showing the simplification of the time complexity expression using the Limit Theorem:

$$\frac{6n^2}{2} - \frac{6n}{2} + 2 \in O(n^2)$$

Limit Theorem

$$\lim_{n \rightarrow \infty} \frac{6n^2 - 6n + 2}{2n^2} \leftarrow \text{ignore}$$
$$\frac{d}{dn} \frac{12n - 6}{4n} \Rightarrow \frac{12}{4} = 3 \neq \infty$$
$$\frac{6n^2}{2} - \frac{6n}{2} + 2 \in O(n^2)$$

Lawnmower Algorithm:

Int numOfSwaps

-> 1 tu

disk Sort = unsorted

-> 1 tu

for i = 0 in sorted.size() - 1 do

-> (n - 1) tu

for j in i to sorted.size() - 1 do

-> (n - 1) tu

if (LIGHT Disk is not followed by DARK Disk) do

-> 4 tu

Swap LIGHT and DARK

-> 1 tu

numOfSwap++

-> 1 tu

return sorted and numOfSwap

This is the pseudocode for the Lawnmower algorithm, and it shows that the worst time complexity for this would be $O(n^2)$

By calculating every step of the pseudocode, we can figure out the time complexity is $1 + 1 + ((n - 1) * (n - 1) * (4 + 1 + 1))$, and if we simplified this equation we would end up with $6n^2 - 8n + 8$

Limit Theorem:

$$6n^2 - 8n + 8 \in O(n^2)$$

L.T.

$$\lim_{n \rightarrow \infty} \frac{6n^2 - 8n + 8}{n^2}$$

$$\lim_{n \rightarrow \infty} 6 - \lim_{n \rightarrow \infty} \frac{8}{n} + \lim_{n \rightarrow \infty} \frac{8}{n^2} = 6 \neq \infty$$

$6n^2 - 8n + 8 \in O(n^2)$

README.md — ~/Documents/LMCF-Project1 — Atom

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disks.hpp README.md

```
1 # LMCF-Project1
2 Group Members:
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16 -----
17
18 This project contains the lawnmower and the alternate algorithm.
19
```

~/Documents/LMCF-Project1/README.md 19:1 LF UTF-8 GitHub Markdown main Fetch GitHub Git (0)

```
[tuffix@vclvm011104-225-174 LMCF-Project1]$ g++ -std=c++11 -Wall disks_test.cpp
[tuffix@vclvm011104-225-174 LMCF-Project1]$ ./a.out
disk_state still works: passed, score 1/1
sorted_disks still works: passed, score 1/1
disk_state::is_initialized: passed, score 3/3
disk_state::is_sorted: passed, score 3/3
alternate, n=4: passed, score 1/1
alternate, n=3: passed, score 1/1
alternate, other values: passed, score 1/1
lawnmower, n=4: passed, score 1/1
lawnmower, n=3: passed, score 1/1
lawnmower, other values: passed, score 1/1
TOTAL SCORE = 14 / 14
```

