University of Padova

Master Degree in *Computer Science* a.y. 2017/2018

Data Mining

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INSTRUCTIONS: The examination takes 1 hour. You are asked to reply using these papers. In case you

need other papers, you can use them but they will not be corrected. Do not use pencil. Do not use corrector tape. Name: Surname: Enrolment number: **Questions with multiple choice.** Only one response is the correct one. Mark the right response. Wrong or missing replies take 0 points. 1) The hypotheses on the errors in the simple linear regression model $Y = \beta_0 + \beta_1 X + \varepsilon$ include (c) increasing variance (a) normality (b) mean equal to one (d) correlation with X2) In a linear regression model, one factor X with 3 levels gives rise to a number of dummy variables (indicators) equal to (a) 3 (b) 4 (c) 2 (d) it depends on the response Y3) In a linear regression model, which one of the following values for a p-value indicates the lack of association between response Y and covariate X? **(b)** 0.83 (a) 0.05 (c) 0.003 (d) it depends on the sample size 4) Does the term spurious correlation refer to a nonsensical relationship between two variables? (c) it depends on the sample size (b) yes (d) it depends on the variances of the variables

5) The residual deviance

(c) always increases

(a) increases as R^2 increases

(b) increases as the total deviance increases

(d) none of the previous choices

Exercise.

Consider the data about the annual income of 130 subjects. Data include the following information:

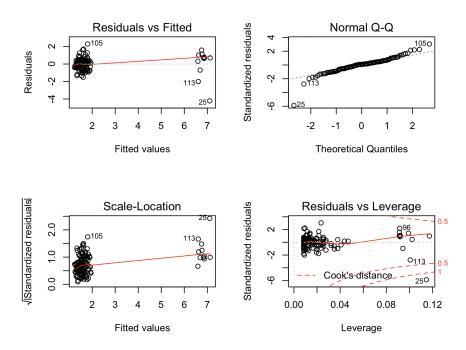
- earnings: the natural logarithm of the annual personal earnings (originally measured in 10,000\$)
- age: age (years)
- gender: female/male
- celebrity: is the subject a celebrity? yes/no
- a) We estimate a linear regression model to explain the relationship between the logarithm of annual earnings and the age and the gender. This is the output from R

```
Call:
lm(formula = y \sim age + celebrity)
Residuals:
   Min
            1Q Median
                            30
                                   Max
-4.2149 -0.3808 0.0656 0.3533 2.2920
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.916326
                      0.257670
                                  3.556 0.000529 ***
                                  2.593 0.010625 *
            0.016109
                       0.006212
                      0.246481 21.841 < 2e-16 ***
celebrityyes 5.383492
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Residual standard error: 0.7625 on 127 degrees of freedom
Multiple R-squared: 0.7916,
  Adjusted R-squared: 0.7883
F-statistic: 241.2 on 2 and 127 DF, p-value: < 2.2e-16
```

a.1) Write the expression of the estimated model. Describe how R handles the qualitative variable discipline and which level is the baseline level.

a.2) Discuss the output of the model paying attention to i) the significance of the coefficients, ii) the possibility to simplify the model, iii) the accuracy of the model using R^2 .

a.3) The following plot represents the residuals analysis of the fitted model. Comment on the plot and discuss whether the model is accurate, or whether the residuals suggest any modification of the model, or explaining whether there is indication of additional analyses.



a.4) Explain what the quantity *Multiple R-squared* in the output represents and how it is computed.

b) The extension of the model including variable gender provides the following output

```
lm(formula = y \sim age + gender + celebrity)
Residuals:
            10 Median
   Min
                            3Q
-4.0746 -0.2930 0.0539 0.3309 2.1673
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
                                         0.0030 **
(Intercept) 0.789541
                      0.260858
                                  3.027
                                         0.0126 *
            0.015519
                       0.006132
                                2.531
gendermale 0.283988
                       0.132281
                                 2.147
                                         0.0337 *
celebrityyes 5.399540
                      0.243167 22.205 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 0.7519 on 126 degrees of freedom
Multiple R-squared: 0.799,
 Adjusted R-squared: 0.7942
F-statistic: 166.9 on 3 and 126 DF, p-value: < 2.2e-16
```

b.1) Does it make sense to maintain the interaction in the model? Can we simplify the model? Why?

b.2) The comparison of the two models using function anova() provides the following output. Comment the output, explaining what it represents and what we can conclude from it.

```
Analysis of Variance Table
```

```
Model 1: y ~ age + celebrity

Model 2: y ~ age + gender + celebrity

Res.Df RSS Df Sum of Sq F Pr(>F)

1 127 73.840

2 126 71.234 1 2.6057 4.609 0.03372 *

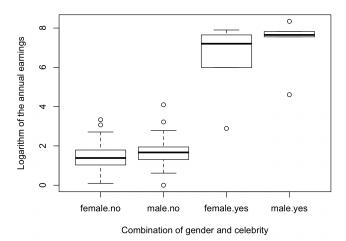
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Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

b.3) Using the best model, provide a confidence	interval at level 0.95 for the coeffi	cient associated
to age. Explain assumptions, if any.		

b.4) Using the last model, predict the earnings (on the original scale) for a 30-years old famous male and then the earnings (on the original scale) for a non-famous 30-years old male.

c) The following plot shows the distribution of earnings for different levels of gender and celebrity



c.1) Does the plot suggest to add an interaction between the two covariates in the model? Why?

we see that if we fix "no" there is no net difference between the medians for male and female, the same happens if we fix yes. If we fix female and male we do see the same pattern considering female.no-female.yes and male.no-male.yes (they look like two straight lines). These two consideration suggest that there are not interactions. By the way a more detailed analysis must be followed in order to be sure about it.

Useful information

Quantiles of a standard Normal distribution

$$z_{0.01} = -2.33 \ z_{0.025} = -1.96 \ z_{0.05} = -1.64 \ z_{0.95} = 1.64 \ z_{0.975} = 1.96 \ z_{0.99} = 2.33$$

Quantiles of F distribution

$$F_{0.025;1,127} = 0.00099 \ F_{0.05;1,127} = 0.0039 \ F_{0.975;1,127} = 5.146 \ F_{0.95;1,127} = 3.9163$$