University of Padova

Master Degree in *Computer Science* a.y. 2017/2018

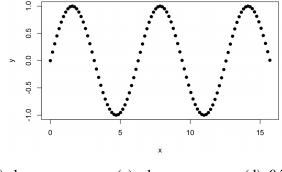
Data Mining

Teacher: Annamaria Guolo

Written assessment: June, 6, 2018

INSTRUCTIONS: The examination takes 1 hour. You are asked to reply using these papers. In case you need other papers, you can use them but they will not be corrected. Do not use pencil. Do not use corrector tape.

	Name:	Surname:		Enrolment number:		
_	tions with multiple choic one response is the correct		e right respons	se. Wrong or missing replies take 0 points.		
1)	1) The comparison between two linear models can be performed through the F statistic					
ŕ	•	never	*	arge sample size		
2)) Type I error is					
ŕ	(a) the rejection of H_0 wh (c) always smaller than 0.			tion of H_0 when it is false e previous responses is true		
3)	A confidence interval for on n observations	a covariate in the linear regression model based				
	(a) has a smaller width as(c) does not depend on n	n decreases		ger width as n increases he previous responses is true		
4)	4) The following plot suggests that the correlation between X and Y is					
		÷ - V				



- **(a)** 0
- (b) 1
- (c) -1
- (d) 0.7
- 5) Incorrelation between X and Y suggests that in the linear regression model $Y = \beta_0 + \beta_1 X + \varepsilon$
 - (a) the estimate of β_0 is 0
- **(b)** the p-value associated to X is close to 1

- (c) $R^2 = 0.3$
- (d) the residual standard error is 0.5

Exercise.

Consider the dataset about the information of 120 houses on sale. Data include the following information:

- Lprice: Natural logarithm of the asking price (in thousands of dollars)
- State: Location of the house in US (CA, NJ, NY, PA)
- Size: Area of all rooms (in thousand square feet)
- Beds: Number of bedrooms
- Baths: Number of bathrooms
- a) We estimate a linear regression model to explain the relationship between the logarithm of the price and some characteristics of the house. This is the output from R

```
Call:
lm(formula = Lprice ~ Size + State)
Residuals:
    Min
                   Median
                                3Q
              1Q
                                       Max
-1.77915 -0.27947 -0.03962 0.29892 1.69701
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 4.84306 0.13469 35.957 < 2e-16 ***
                       0.04409 11.888 < 2e-16 ***
Size
            0.52416
           -0.13825
StateNJ
                       0.13835 -0.999 0.319735
           -0.01309
                       0.13842 -0.095 0.924802
StateNY
StatePA
           -0.47680
                       0.13860 -3.440 0.000811 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 0.5358 on 115 degrees of freedom
Multiple R-squared: 0.5864,
                              Adjusted R-squared: 0.572
F-statistic: 40.76 on 4 and 115 DF, p-value: < 2.2e-16
```

a.1) Write the expression of the estimated model. Describe how R handles the qualitative variable State and which level is the baseline level.

a.2) Discuss the output of the model paying attention to i) the significance of the coefficients, ii) the possibility to simplify the model, iii) the accuracy of the model using R^2 .

) Which kind of information about the residuals is provided in the output? Why is this information useful?					
a.4) Predict the price (on the original scale) for a house of 2 thousand square for compare it to that of an equal-size house located in NJ.	feet located in CA and				
a.5) Compute a confidence interval at nominal level 0.95 for the coefficients Explain assumptions if any.	s associated to Size.				
The extension of the model including the number of beds and bathrooms prov following page	rides the output in the				
b.1) Does it make sense to maintain the new variables in the model? Can be Why and how?	the model simplified?				

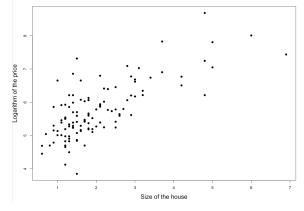
b)

Call: lm(formula = Lprice ~ Size + State + Beds + Baths) Residuals: Min **1Q** Median **3Q** Max -1.76421 -0.27840 -0.06076 0.28479 1.70864 Coefficients: Estimate Std. Error t value Pr(>|t|) (Intercept) 0.17534 27.190 < 2e-16 *** 4.76738 Size 0.39523 0.07576 5.217 8.33e-07 *** StateNJ -0.06764 0.14116 -0.479 0.632752 **StateNY** 0.03983 0.13761 0.289 0.772750 StatePA -0.47654 0.13629 -3.497 0.000675 *** Beds -0.05569 0.06198 -0.899 0.370801 Baths 0.21060 2.491 0.014204 * 0.08456 Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1 Residual standard error: 0.5262 on 113 degrees of freedom Multiple R-squared: 0.6079, Adjusted R-squared: 0.5871

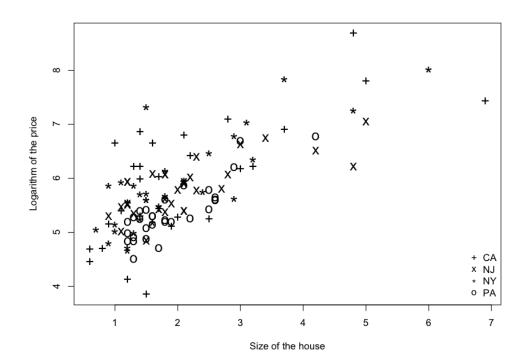
b.2) Compare the two models using statistic F, explaining the hypothesis test and discussing the result. Consider the significance level equal to 0.05.

F-statistic: 29.2 on 6 and 113 DF, p-value: < 2.2e-16

c) The following plot shows the distribution of the logarithm of the price versus that of Size. Does the plot provide any information useful to improve the model?



d) The following plot shows the distribution of the logarithm of the price versus that of Size by distinguishing the State. Does the plot suggest an interaction between the two covariates useful to improve on the fitting of the model? Why?



Useful information

Quantiles of a standard Normal distribution

$$z_{0.01} = -2.33$$
 $z_{0.025} = -1.96$ $z_{0.05} = -1.64$ $z_{0.95} = 1.64$ $z_{0.975} = 1.96$ $z_{0.99} = 2.33$

Quantiles of F distribution

$$F_{0.025;2,113} = 0.0025 \ F_{0.025;113,2} = 0.262 \ F_{0.05;2,113} = 0.051$$

$$F_{0.05;1,113} = 0.0039 \ F_{0.95;2,113} = 3.077 \ F_{0.95;1,113} = 3.925$$