

SEIFERT THESIS

BY

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THESIS

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Abstract

Abstract.

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Chapter 1

Introduction

1.1 Energy

In modern society, the usefulness and convenience supplied by advancing technologies has allowed quality of life to increase drastically over time. Within these advancing technologies, ranging from air conditioning to food production, there is a common thread of energy requirement. To cool the air, energy is required in order to compress, pressurize, and cool the refrigerant. To produce food, energy is required to pump water, create fertilizer, and operate heavy machinery. Thus, the importance of energy is significant in maintaining and developing quality of life for society.

However, energy is not free, and it takes effort to harvest and convert energy into usable forms. For wind power, this means building large turbines which can be turned by the wind. For solar power, this means building solar panels, which convert photons from the sun into electrical energy. However, for most large-scale electrical generation needs, it is more efficient for the conversion aspect to use boiling water to turn a turbine, which then generates electricity, as can be seen in Figure 1.1. Regardless of how it is generated, electricity can then be transported or stored to be used by people for any variety of purpose.

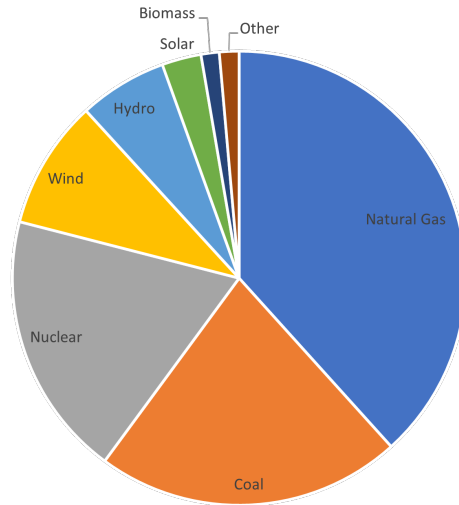


Figure 1.1: Energy generation in the United States in 2021 from the US Energy Information Administration CITE <https://www.eia.gov/electricity/monthly/>.

Figure 1.1 shows the portion of energy generation. From this figure, it can be seen that the methods which dominate energy contribution are natural gas, coal, and nuclear. Of the various methods to generate electricity, desirable characteristics would be safety, efficiency, consistency, availability, and economics. Nuclear energy is strong in these characteristics, though there is an economic problem due to high up-front costs, which are on the order of \$10 billion for a 1GW nuclear power plant [14].

1.2 Nuclear Energy

Part of the reason nuclear energy has high up-front costs is because the nuclear industry is highly safety conscious and has many regulations in place in order to minimize risks. Although this mindset increases costs, the effort has paid dividends, which is apparent when viewing the deaths associated with different energy generation methods, shown in Table 1.1 [10].

Table 1.1: Mortality rates for each energy source in deaths per billion kWh produced (recreated from [10]).

Energy Source	Mortality Rate (deaths per billion kWh)
Coal (Global Average)	100
Biofuel/Biomass	24
Coal (U.S.)	15
Oil	36
Natural Gas	4
Hydro (Global Average)	1.4
Solar (Rooftop)	0.44
Wind	0.15
Nuclear (Global Average)	0.04

Even though the up-front costs are high, nuclear power plants are licensed to operate for 40 years and can get extensions to extend that time by 10-20 years [9]. This means that nuclear plants are a very long term investment. An investment at this time scale is difficult to make for a private industry though, as there is less risk when investing in cheaper plants, such as natural gas.

In order to address the economic issue of nuclear power plants, there are many different approaches which are implemented. One of these is to build smaller, cheaper nuclear plants which are then more affordable and have less up-front cost. Another approach is from the regulation perspective, and involves either taxing negative externalities more harshly or subsidizing carbon-free energy sources. There is also the approach of developing new generation IV reactor designs [22].

1.3 Molten Salt Reactors

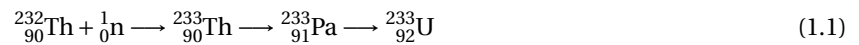
One of the new generation IV reactor designs is the molten salt reactor, or MSR [22]. The MSR potentially offers a lower cost of electricity when compared to coal and pressurized water reactors, which are a large portion of the nuclear fleet [27]. The liquid fueled MSR design is significantly different from the current light water reactor, or LWR, designs which dominate the nuclear fleet currently in use. Light water reactors include boiling water reactors (BWRs) and pressurized water reactors (PWRs), both of which are well understood reactor designs currently

implemented. These LWRs use a solid fuel containing uranium-235 with a water coolant, which also serves as a moderator to slow down the neutrons to thermal energies. This fuel generates heat as the fissile uranium-235 fissions. After some lengthy amount of depletion, it can be reshuffled or removed from the reactor to be placed into a cooling pool.

Molten salt reactors, instead of a solid fuel, can use a liquid fuel composed of a molten salt mixed with some fissile isotope, such as uranium-235. Using a liquid fuel allows for online reprocessing, which is a continuous process which can involve adding fresh fuel to the system as well as chemically removing undesirable products which are generated through fission. The system also allows for batchwise reprocessing, which is a process which occurs in discrete steps, such as salt disposal. Typically, most reprocessing involved in an MSR is continuously performed while the reactor is online.

The usefulness of reprocessing, particularly online reprocessing, is that the reactor does not need excess reactivity in order to continue operating for a long period of time. In a typical LWR, burnable poisons and control rods are used to lower reactivity initially so the reactor can burn longer. In a liquid fueled MSR, the parasitic absorbers, such as xenon-135, can be removed from the reactor. Additionally, fresh fuel salt can be added to the reactor in order to maintain stable operation.

This fresh fuel feed can include fissile isotopes, such as uranium-233 or uranium-235, fertile isotopes, such as uranium-238 or thorium-232, or some combination of both. Adding a fissile isotope to the reactor will allow for the reactor to continue fission when the isotope is fissioned by a neutron. For the fertile isotopes, the neutron must first be absorbed and the product decays, leading to a fissile isotope. This process can be seen in Equation (1.1), which is the breeding process used in the Molten Salt Breeder Reactor.



The half life of thorium-233 via beta decay is on the order of tens of minutes, while the half life of protactinium-233 via beta decay is roughly 27 days. Without reprocessing, the protactinium-233 remaining in the core for such a period of time would be more likely to interact with neutrons, impacting the breeding efficiency. The Molten Salt Breeder Reactor continuously chemically extracts the protactinium from the fuel salt, allowing it to decay in a separate tank. While it decays, another continuous chemical process strips uranium which is formed and brings the uranium back into the reactor, continuing the process.

1.4 Reprocessing Methods

For molten salt reactor reprocessing, the two different physical approaches are continuous and batchwise. Additionally, these reprocessing schemes can be online, while the reactor is operating, or offline, when the reactor is shutdown. Of particular importance for MSR behaviour is online reprocessing, which changes the fuel composition while the reactor is operating.

In order to model online reprocessing, there are two different computational methods which can be implemented. These methods are named continuous and batchwise reprocessing methods, the same naming convention as the physical processes which they represent. However, it is fairly common for MSR analysis works which implement a physically continuous reprocessing scheme to simulate this scheme using batchwise mathematical models.

Thus, this work seeks to investigate the continuous and batchwise computational reprocessing methods. This investigation involves effects of depletion step size, validity of batchwise methods approximating continuous methods, and different sub-methods within both batchwise and continuous methods which can be implemented.

Chapter 2

Literature Review

2.1 Molten Salt Reactors

Modeling and simulation of liquid fueled molten salt reactors (MSRs) differs from solid fueled reactors in two main areas. The first is in the fresh fuel feed and fission product removal streams used during operation in MSRs, called online reprocessing. Modeling an MSR without online reprocessing will cause very different results during depletion calculations due to the lack of fresh fuel and buildup of fission products. In order to simulate this reprocessing functionality, software can either use batchwise reprocessing or continuous reprocessing.

The second difference is in the movement of the fuel salt, which causes delayed neutron precursors (DNPs) to move in the core. Because the DNPs have different decay times before the delayed neutrons are born, the effect of the fuel movement on each group varies. However, the overall result is more delayed neutrons in less important regions, such as external piping, which means there is a reduced effective delayed neutron fraction in the core.

2.1.1 Online Reprocessing

The online reprocessing functionality of MSRs is simulated in different ways depending on the particular software used, and depending on the methods employed by that software. The two main ways to approach the online reprocessing problem is by either using batch-wise reprocessing or continuous reprocessing. For these approaches, the physical process may represent either approach, such as continuously removing protactinium from the core, but adding in the uranium it decays into only after some time has elapsed. Typically, however, a purely batchwise modeling approach will not fit the reprocessing design used by a reactor since online reprocessing is carried out continuously. An MSR using offline reprocessing, however, can be accurately represented using purely batchwise reprocessing.

Codes such as SaltProc and older versions of ChemTriton implement batchwise reprocessing by running the simulation, stopping, and then adding and removing materials [35, 8]. The process is then iterated. This method is useful because it is fairly straightforward to implement, easy to customize, and makes mass balancing of the core straightforward. Some issues with the batchwise approach are that using large time steps will make the results

more inaccurate, it has increased computational cost with smaller time steps, it has to rerun each time step for pre-reprocessing and post-reprocessing, and it is an approximation of the actual physical process of reprocessing. It is an approximation because, in online reprocessing of a reactor, the fission products are continuously removed while any feed flows are continuously fed into the reactor.

Codes such as Serpent2 and newer versions of ChemTriton implement continuous reprocessing by adding terms to the Bateman equation similar to an extra decay term, as can be seen in Equation (2.5) [4, 21]. The benefits of using continuous reprocessing are that the model is more physically accurate, it doesn't impact computational cost as much as a batchwise process, and it allows for larger time steps to be used. However, the maximum time step size cannot become too large, or the simulation will become less accurate. This is because the neutron spectrum and cross section data does not update to the new material compositions until a new depletion step begins.

Another aspect of online reprocessing that must be considered is mass balancing. For batchwise reprocessing, mass balancing can be solved in several different ways. One method is to have the net mass of the feed rate over some depletion step be equivalent to the mass removed over that same depletion step, which is the current approach used by SaltProc [35]. Alternatively, the volume of the system can be adjusted so that constant density is maintained in order to keep cross section data consistent [32]. Another approach is to move excess fuel salt into a bleed-off tank [32]. For continuous reprocessing, the depletion time steps can be much larger. This means that during the interval between steps, the mass will not be balanced. However, the same batchwise methods can be used with continuous reprocessing at new depletion steps. Implementing these approaches increases computational cost when performed in Serpent2. This is because using a single input script with depletion steps will cause each depletion step to be run once, but altering the input script by changing volumes or removing mass to a bleed-off tank will cause the time step to be run twice.

2.1.1.1 Batchwise Reprocessing

Batchwise reprocessing starts with some removal rate where $X\%$ of some element is removed from the fuel salt in the system over some time period T . Over a depletion step τ , $\gamma\%$ of the element's mass is removed, where γ corresponds to X according to Equation (2.1). The scaling term γ for the removal efficiency is a linear approximation based on the time step adjustment in Equation (2.1). If the time step used causes the removal fraction to be greater than 1, the amount removed remains at 100% so as to not have negative mass.

An alternative approach is to establish a depletion time step τ such that the efficiency based time value T is a multiple of τ and only have the $X\%$ batchwise removal occur at the steps when τ is a multiple of T , thus removing the need for scaling.

$$\gamma = X \frac{\tau}{T} \quad (2.1)$$

For the Molten Salt Breeder Reactor (MSBR), SaltProc performs batchwise reprocessing every 3 days using a linear approximation of the cycle times given by Robertson et al in the ORNL report [33, 35]. The xenon and krypton removals in SaltProc use a gas separation system equation, while the protactinium uses a modeled liquid-liquid reductive extraction process. These efficiencies differ from the cycle time values, causing slight differences in those terms. The MSBR also has two varying feed inputs of ^{232}Th and ^{233}U .

Examples of the batchwise method used in SaltProc can be seen in Equations (2.2) and (2.3). Both examples show what the resulting mass removal per step, or γ , term should be for different cycle time values. The first shows a cycle time of 20s, which is shorter than the step time of 3 days. This results in a removal rate over 100%, which is set to 100%. The second shows a cycle time of 60 days, longer than the step size. This results in a 5% removal per step. An alternative approach to the second example, which is implemented in the earlier versions of SaltProc, is to perform no removal until 60 days have elapsed and then remove 100% of material.

$$X = 100\%, T = 20\text{s}, \tau = 3\text{d} \rightarrow \gamma > 100\% \rightarrow 100\% \quad (2.2)$$

$$X = 100\%, T = 60\text{d}, \tau = 3\text{d} \rightarrow \gamma = 5\% \quad (2.3)$$

2.1.1.2 Continuous Reprocessing

The continuous approach manipulates the Bateman equation by adding a reprocessing term, which contains a reprocessing constant and the concentration of the isotope. This is one of the methods used in Serpent2 continuous reprocessing, an extension developed by Aufiero et al [4]. Equation (2.4) shows the generic form of the Bateman equation, while Equation (2.5) shows the terms added to Equation (2.4), which are the reprocessing constants, λ_r . These terms represent removal of the current isotope as well as feed of the current isotope from other sources.

$$\begin{aligned} \frac{dN_j}{dt}_{base} = \sum_{i \neq j} [(\gamma_{i \rightarrow j} \sigma_{f,i} \Phi + \lambda_{i \rightarrow j} + \sigma_{i \rightarrow j} \Phi) N_i] \\ - (\lambda_j + \sigma_j \Phi) N_j \end{aligned} \quad (2.4)$$

$$\frac{dN_j}{dt}_{net} = \frac{dN_j}{dt}_{base} - \lambda_{r,j} N_j + \sum_{mat} \lambda_{r,i \rightarrow j} N_i \quad (2.5)$$

The symbols given in the equations are defined as follows from Equation [23]:

N_j is the atomic density of isotope j .

$\gamma_{i \rightarrow j}$ is the fractional fission product yield of j in the fission of isotope i .

$\sigma_{f,i}$ is the microscopic fission cross section of isotope i .

Φ is the spectrum-averaged scalar flux in the fuel region.

$\lambda_{i \rightarrow j}$ is the decay constant of decay $i \rightarrow j$.

$\sigma_{i \rightarrow j}$ is the microscopic transmutation cross section of reaction $i \rightarrow j$.

N_i is the atomic density of isotope i .

λ_j is the decay constant of isotope j .

$\lambda_{r,j}$ is the reprocessing constant for removal of isotope j .

σ_j is the microscopic total transmutation cross section of isotope j .

$\lambda_{r,i \rightarrow j}$ is the reprocessing constant for feed of material $i \rightarrow j$.

Equation (2.5) shows that the reprocessing removal has the same mathematical operation as the decay rate. Unlike decay, the isotopes removed by reprocessing instead are transferred to a different material, which operates as a feed for that material. This can be seen in the summation term, which sums over the different materials and moves them from material i to material j .

Serpent2 has three different settings for continuous reprocessing which alter the effect on the Bateman equations. The zeroth setting does not conserve mass, so it will not be discussed. The first setting, which adds a decay-like term to the Bateman equation, is shown in Equations (2.4) and (2.5). This approach of adding a decay-like term to the Bateman equation has been done with other codes [21, 34]. For this setting, three different approaches are implemented in order to compare their results.

The first approach is labeled the Cycle Time Decay (CTD) approach. It takes half the value of the cycle times and treats them as half life values. A similar method of treating removal periods for reprocessing can be seen in Brovchenko et al [11]. Equation (2.6) shows how this approach works with a cycle time of 20 seconds. The operation cuts the cycle time in half and then calculates the decay constant, or reprocessing constant, using the half life from the cycle time.

$$20s \rightarrow \tau = 10s \rightarrow \lambda_r = \frac{\ln(2)}{\tau} \approx 6.93E-2 \quad (2.6)$$

The next approach is labeled the SaltProc Cycle Rate (SPCR) approach. It takes the same efficiency rates used by SaltProc, which uses 3 day depletion steps for the MSBR, and directly converts those rates to continuous reprocessing rates. Taking the inverse of the cycle time is a common way to generate the removal rate [35, 29]. Equation (2.7) shows how this approach works with a cycle time of 20s. This operation uses the SaltProc value, which in this case becomes 100% removal over 3 days, converts it to be per second, and then converts that to the rate form usable in Serpent2.

$$20s \rightarrow \frac{1}{3d} \rightarrow X = \frac{4E-6}{1s} \rightarrow \lambda_r = \ln\left(\frac{1}{1-X}\right) \approx 4E-6 \quad (2.7)$$

This natural logarithm in this approach comes from the differential equation solution based on the removal rate provided. The method used to derive this equation can be seen in Equations (2.8), (2.9), and (2.10). These equations assume that the X term, or the fractional removal rate, is in units of per second.

$$\frac{dN}{dt} = -\lambda_r N \quad (2.8)$$

$$N(t) = (1 - X)N_{cur} = N_{cur} e^{-\lambda_r} \quad (2.9)$$

$$-\ln(1 - X) = \lambda_r = \ln\left(\frac{1}{1 - X}\right) \quad (2.10)$$

The final approach is labeled the Cycle Rate (CR) approach. It takes the cycle times and uses a linear approximation to generate the efficiency rate directly. Equation (2.11) shows how this approach works using a cycle time of 20 seconds. This operation takes the cycle time, determines the efficiency rate for 100% removal over 20 seconds, and then uses that value to calculate the Serpent2 reprocessing constant.

$$20s \rightarrow X = \frac{1}{20s} \rightarrow \lambda_r = \ln\left(\frac{1}{1 - X}\right) \approx 5.12E-2 \quad (2.11)$$

The second continuous reprocessing setting used in Serpent2 removes a constant value from each isotopic Bateman equation for an element. This approach can be seen in Equation 2.12, where the C term represents the constant value being removed by continuous reprocessing.

$$\frac{dN_j}{dt} = \sum_{i \neq j} [(\gamma_{i \rightarrow j} \sigma_{f,i} \Phi + \lambda_{i \rightarrow j} + \sigma_{i \rightarrow j} \Phi) N_i] - (\lambda_j + \sigma_j \Phi) N_j - C \quad (2.12)$$

This approach has a flaw which can be directly demonstrated through an example if the reprocessing constants

are defined for an element and not for each isotope. Imagine an element exists with two isotopes A and B . There is a removal rate of 10% per second defined for the element. A batchwise process could remove 10% of each isotopes relative abundance after a second by using a one second time step, which is physical in terms of fractional removal. This can be seen directly in Table 2.1, where 10% of both isotopes and the net count are removed.

Table 2.1: Serpent2 Second Setting Approaches

Labels	Initial	Batch	Net	A	B	Null
A	1000	900	949.5	900	999	990
B	10	9	-40.5	-90	9	0
Net	1010	909	909	810	1008	990

For the continuous reprocessing, the first attempt might be to try and remove 10% of the net by splitting it amongst the isotopes evenly. The issue with this approach is immediately noticeable, which is that the concentration of isotope B becomes negative, as can be seen in the *Net* column. A logical next approach would be to try and make one of the isotopes exactly correct while bringing the other along with it, which can be seen in the A and B columns. The results of this approach are seen in the table, and it can be seen that only by looking at the isotope with the smallest concentration and using that to determine the amount to remove can the result be ensured to be non-negative. One final approach to consider is to set the smallest concentration to 0, and bring the other isotopes along. This approach can be seen in the *Null* column, and it also does not work very well.

2.1.2 DNP Movement

The movement of DNPs in liquid fueled molten salt reactors impacts the operation of the reactor directly since the decay of the precursors occurs at a different location compared to a static reactor [40, 3]. There are several effects which this movement can have on the reactor. Since the delayed neutron precursors move, there is a probability of decay in non-core regions of the reactor, meaning there are fewer delayed neutrons in the core. This results in a reduced effective delayed neutron fraction, which reduces controllability of the reactor. Additionally, since delayed neutrons have a softer spectrum than prompt neutrons, there is a difference in spectrum in a reactor which has no flow against a reactor which has a circulating fuel. In a solid fueled reactor, the flux and the concentration of delayed neutron precursors have the same profile. However, a moving fluid fuel causes the precursors to have a shifted profile based on the fluid flow rate, mixing, and decay rate of the precursors. This was shown very clearly by Jun Shi and Massimiliano Fratoni in their work, which can be seen in Figure 2.1.

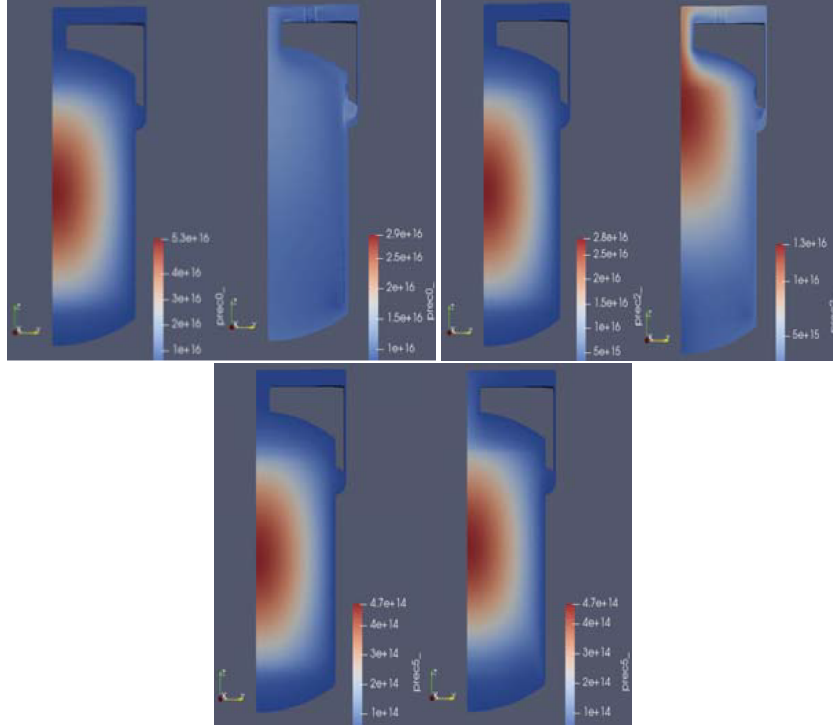


Figure 2.1: Plots of DNP concentrations in the molten salt reactor experiment [37]. The left side of each image shows concentration with no flow, while the right shows the concentration with a 1200 gallon per minute flow rate. Top Left) Longest lived DNP group. Top Right) Third longest lived DNP group. Bottom) Shortest lived DNP group.

From these images, it can be seen that for the long shortest lived DNPs, the movement of the fuel does not have any significant impact upon the DNP distribution when compared to static fuel. This is reasonable since the precursors do not live for very long in this group, so they do not have much chance to travel. For the intermediate DNP group, there is a clear shift in the direction of the fuel flow, which causes more precursors to produce delayed neutrons in the less important piping and upper plenum regions. The longest lived DNP group seems to be spread almost equally throughout the entire reactor, which means that those delayed neutrons are contributing significantly less to the overall neutron economy. This reduces the overall effective delayed neutron fraction since the delayed neutrons are in less important regions. This directly affects the controllability of the reactor through the reactor period, which is heavily dependent upon the delayed neutrons.

2.2 Depletion

Depletion is the process of burning the fuel and simulating the changes to the materials this causes in the system. Depletion requires specific information to run properly, such as decay constants, fission yields, and fission and transmutation cross section data. The fission and transmutation cross section data can come from a transport

calculation, while the other data can be read from a data library [23]. Additionally, running depletion involves solving the Bateman equations, a generic version of which can be seen in Equation 2.4.

There are several different approaches to solving these equations, such as the Transmutation Trajectory Analysis (TTA) method and the Chebyshev Rational Approximation Method (CRAM). These are the two different methods used in Serpent2, and are both built into Serpent2 [24]. Other codes may use external software to compute depletion, such as REM used by MCNP and ORIGEN-S used by KENO-VI [4]. Another code, aside from Serpent2, that contains built-in depletion solvers is ERANOS [4].

The purpose behind solving these equations and having depletion models is to generate an accurate representation of the composition of the target materials during reactor operation. This is important in determining how long the reactor can run, how the safety of the reactor develops over time, and how operation may have to change to adjust to the new reactor state. For molten salt reactors, depletion also allows for information regarding fresh fuel feed rate and fission product removal rates, as well as how variations of those parameters can affect reactor performance and behaviour.

2.3 The Molten Salt Breeder Reactor

The molten salt breeder reactor (MSBR) is a useful design to analyze for several reasons. Because it is a molten salt reactor, online reprocessing is used within the design. In addition, it contains an inner and outer zone, each of which has different neutronic behaviour [33]. More specifically, the inner zone has a softer spectrum, a higher fission rate, and a 13% fuel-to-graphite ratio [30]. The outer zone has a harder spectrum, a higher breeding rate, and a 37% fuel-to-graphite ratio. The inner and outer zones prove to be an issue when accurately modeling using a unit-cell or one-region approach, as those models are unable to capture the different characteristics of each region [35]. The differences in the regions can also be seen in Figure 2.2, which allows for the difference in the fuel-to-graphite ratio to be visually noticeable.

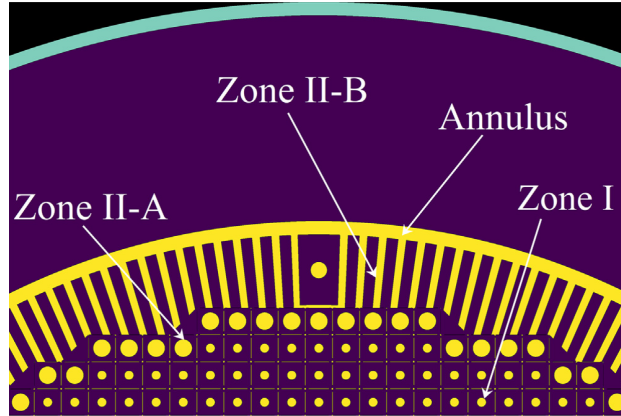


Figure 2.2: MSBR core axial slice showing the different regions from [35]. Zones II-A and II-B are where the spectrum is harder and there is increased breeding. Zone I is where there is more fission and a softer spectrum. The yellow is fuel salt, the purple is graphite, and the cyan is the reactor vessel.

Table 2.2 has general information on the MSBR, while Table 2.3 has specific information on the distribution of the fuel salt during operation. It can be seen in Table 2.2 that the salt inventory cycle time is 10 days, which means that for the entire salt inventory to be cycled takes 10 days. However, the loop cycle time is 11 seconds [33].

Table 2.2: MSBR General Data [33]

Component	Data
Thermal Capacity	2250 MW _{th}
Vessel Inner Diameter	6.77 m
Core Height	3.96 m
Vessel Pressure	0.52 MPa
Inner Salt Fraction	0.13
Outer Salt Fraction	0.37
Maximum Flow Velocity	2.6 $\frac{m}{s}$
Fuel Salt (Vessel)	30.4 m ³
Fuel Salt (Primary System)	48.7 m ³
Thorium Inventory	68,100 kg
Breeding Ratio	1.06
Processing Rate	1 gpm
Salt Inventory Cycle Time	10 days
Salt Components	⁷ LiF–BeF ₂ –ThF ₄ –UF ₄
Salt Composition	71.7-16-12-0.3 mole %

Table 2.3 shows that the salt inventory in the core is approximately 19 m³ due to each core zone. However, SaltProc uses the volume of the primary system for its calculation [35]. This is because the other parts of the MSBR outside of the core are not modeled, but the geometry implemented in Serpent2 uses the correct dimensions. This allows cross sections to remain as if the correct volume were implemented, but also allows the depletion results to be closer to the expected result if the fuel salt were fully utilized.

Table 2.3: MSBR Primary System Salt Inventory [33]

Region	Volume [m ³]
Fuel Salt (Primary System)	48.7
Reactor	-
Core Zone I	8.2
Core Zone II	10.8
Plenums, Inlets, Outlets	6.2
Annulus	3.8
Reflectors	1.4
Primary Heat Exchangers	-
Tubes	7.6
Inlets, Outlets	0.8
Pump Bowls	5.2
Piping (including drain line)	4.1
Off-gas bypass loop	0.3
Tank heels and miscellaneous	0.3

Table 2.4: MSBR Online Reprocessing Cycle Times [33]

Reprocessing Group	Element(s)	Cycle Time (Full Power)
Rare Earths	Y, La, Ce, Pr, Nd, Pm, Sm, Gd	50 days
Rare Earths	Eu	500 days
Noble Metals	Se, Nb, Mo, Tc, Ru, Rh, Pd, Ag, Sb, Te	20 seconds
Seminoble Metals	Zr, Cd, In, Sn	200 days
Gases	Kr, Xe	20 seconds
Volatile Fluorides	Br, I	60 days
Discard	Rb, Sr, Cs, Ba	3435 days
Salt Discard	Th, Li, Be, F	3435 days
Protactinium	Pa	3 days
Higher Nuclides	Np, Pu	16 years

Shown in Table 2.4 are the cycle times for different elements in the MSBR. According to Robertson et al, the protactinium and rare earth processing has the largest impact on neutronics and performance [33].

The fuel processing of the MSBR is defined to operate continuously with processing methods [33]. For protactinium removal, fluorination is first used to remove uranium before protactinium isolation. Next is countercurrent bismuth with lithium and thorium for stripping any remaining uranium and the protactinium. This is followed by hydrofluorination to separate the uranium and protactinium. This process can be seen in Figure 2.3. For a 10 day protactinium cycle time, a fuel salt flow rate of 0.88 gallons per minute (gpm) is used. The processed salt is processed for rare earth fission products before being fed back into the reactor.

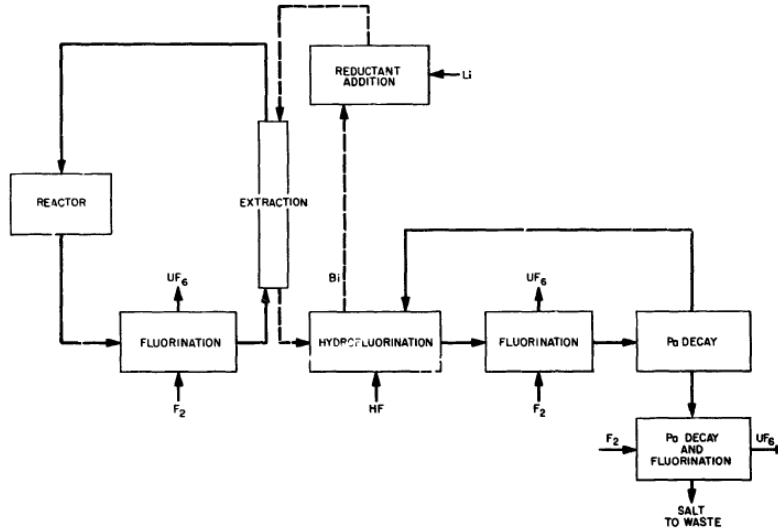


Figure 2.3: MSBR protactinium processing scheme from Robertson et al [33].

Rare earth fission product removal is performed using the metal-transfer process, which uses lithium chloride and bismuth containing a reductant. More specifically, bismuth containing a reductant of thorium and lithium is used to strip the rare earth fission products from the fuel salt. The rare earth fission products are then transported to the lithium chloride acceptor salt, though lithium bromide or a mix of both could be used. Figure 2.4 shows this process, and Figure 2.5 shows the protactinium and rare earth processing schemes together.

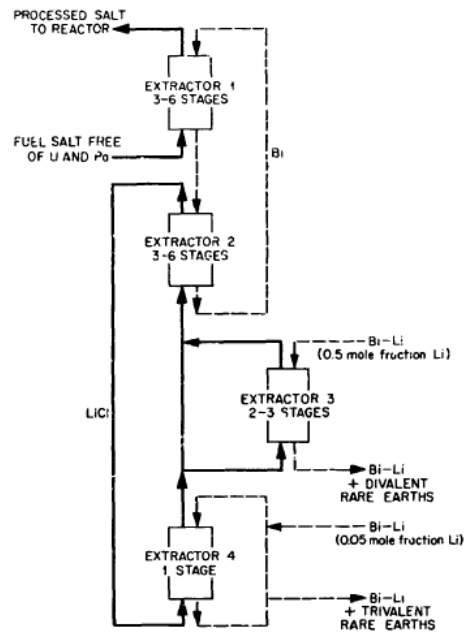


Figure 2.4: MSBR rare earth processing scheme from Robertson et al [33].

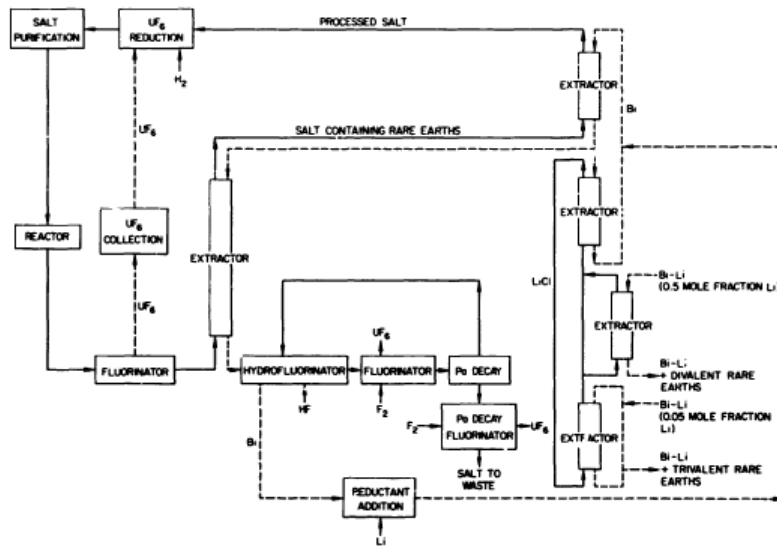


Figure 2.5: Combined MSBR rare earth and protactinium processing schemes from Robertson et al [33].

To strip gaseous fission products, a bubble generator introduces sparging gas in 15 to 20 mil bubbles. 10 percent of the flow is redirected to the bypass loop which contains a gas separator. This gas separator strips the fission products with approximately 100 percent efficiency. The off-gas system also includes an approximately 2 hour holdup during which noble metals deposit on the fuelsalt drain tank surface. Figure 2.6 shows this process, beginning with the number per time, or flux, of the noble gasses in the salt migrating to the graphite voids and helium sparging bubbles. This is followed by the volume holdup into more processing to handle the noble metal fission product cleanup.

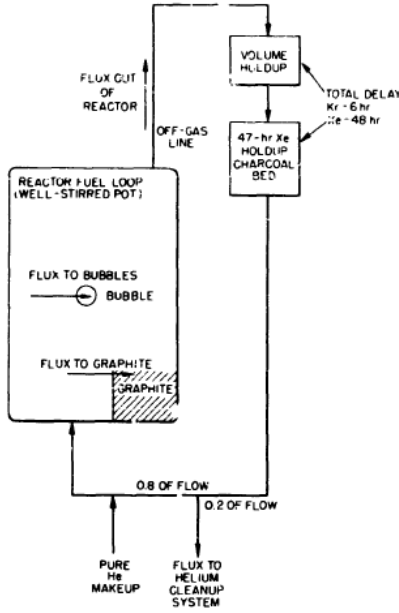


Figure 2.6: MSBR noble metal flux and off-gas system from Robertson et al [33].

Periodic discard of salt at a rate of 0.1 cubic feet per day occurs due to buildup of non-volatile fluorides during fluorination accumulating in the decay tank, such as from zirconium and corrosion product nickel.

2.4 MSR Modeling Approaches

For modeling of MSRs, there are generally two different models which are used. The first is a model which takes a given fuel composition and analyzes the performance of the reactor given that fuel composition. This may include focus on aspects such as DNP movement [15, 37] or reactor dynamics [39, 12, 5, 13, 38].

The second type of model is one which depletes the fuel. Because the online reprocessing of an MSR has such large effects on its fuel composition, depletion models of MSRs typically incorporate online reprocessing. These models can also account for other factors, such as DNP movement, as shown by Zhou et al [42]. The movement of DNP can have a noticeable effect on reactor performance by affecting neutron energy spectra and distribution of delayed neutrons [7]. Most, however, focus primarily on depletion and do not consider the DNP movement during depletion, as can be seen in Table 2.5. In order to handle spatial dependence of fuel salt without modeling the piping of the core, models can use the scaled flux method [6].

For all of the continuous reprocessing models given in Table 2.5, all of them use the "fictitious decay constant" approach, which is shown in Equation (2.5). For the batchwise models, they typically use the approach shown in Equation (2.1) and remove a fraction at each depletion step rather than bulk removal at certain steps.

The "Reprocessing" column of Table 2.5 shows the mathematical approach taken to the online reprocessing of

the work, and does not necessarily represent the reactor reprocessing approach. However, since online reprocessing is considered in the table, offline batchwise reprocessing is not included, such as in the work by Zou et al [44].

Table 2.5: Molten Salt Reactor Models with Online Reprocessing

Index	Reprocessing	Model	Reactor	DNP	Ref.
1	Batchwise	Full 3D	MSBR	No	[35]
2	Continuous	Full 3D	MSFR	No	[4]
3	Batchwise	Full 3D	MSBR	No	[30]
4	Batchwise	Unit Cell	MSBR	No	[8]
4*	Continuous	Unit Cell	N/A	No	[21]
5	Batchwise	Unit Cell	DMSR	No	[2]
6	Continuous	Full 3D	MSBR	Yes	[42]
7	Batchwise	Full 3D	MSBR	No	[29]
8	Batchwise	Full 3D	MOSART	No	[36]
9	Continuous	Unit Cell	ADNA	No	[34]
10	Mixed	2D Slice	MSFR	No	[16]
11	Continuous	Full 3D	MSFR	No	[43]
12	Batchwise	Full 3D	Toy	No	[32]
13	Mixed	2D Slice	N/A	Yes	[19]
14	Mixed	Full 3D	TMSR	No	[26]
15	Mixed	Unit Cell	Toy	Yes	[28]
16	Continuous	Full 3D	N/A	No	[41]

The first entry in Table 2.5 is SaltProc's MSBR example, which uses Serpent2, a full 3D core, 3 day time steps, and runs for 60 years. The batchwise reprocessing in SaltProc includes both the removal and feed processes.

The second entry is by Aufiero et al, and displays the Serpent2 newly developed continuous reprocessing functionality. A full 3D simplified core layout of the molten salt fast reactor (MSFR) is used, and continuous

reprocessing is used to operate the removal and feed processes. It evaluates the model at various scales, from steady state uranium concentrations at over 60 years to radiotoxicity over 10^8 years. The step sizes vary as well, though not specifically mentioned, appearing very small at BOC and expanding to around 10 years at SS for one of the figures presented.

The third entry by Park et al is very similar to the MSBR example in SaltProc, with the primary difference being MCNP6 is used for transportation calculations instead of Serpent2. The depletion was performed using CINDER90 and custom Python scripts. Another difference is that SaltProc uses adjusted values for the removal efficiency rates of xenon, krypton, and protactinium, while the work by Park et al uses the cycle time values from Robertson et al [33]. This model uses 3 day time steps and models the fuel composition over 20 years.

The fourth entry is for ChemTriton, a tool designed for SCALE to perform online reprocessing of MSRs. It contains work on multiple reactors, such as the MSBR and the MSRE. The tool iteratively runs SCALE/TRITON over small time steps to simulate continuous reprocessing. For the MSBR case, 3 day time steps are used, similar to SaltProc and Park et al. The reason for not using shorter time steps is that using shorter time steps increases computational cost while also providing very little improvements to calculated eigenvalue and fuel cycle metrics, discussed by Betzler et al as well as by Powers et al [31].

ChemTriton has been updated after TRITON implemented new tools for continuous material feeds and removals. The work discusses in depth how the removal rates for isotopes can be calculated using a well mixed approximation and accounting for non-modeled piping by introducing a correcting decay factor. Although it does not account for DNP movement, it does account for neutron important regions without having to model the piping regions.

The fifth entry by Ahmad et al analyzes single fluid and two fluid denatured molten salt reactors (DMSRs). This work uses MCNP5 and ORIGEN2 as the codes to perform transport and depletion over 30 years. Although the steps at which fuel is adjusted is at 5 year intervals, the burnup intervals are actually set to 6 months. The reason such large steps were used is because the work analyzes proliferation and resource requirements for the reactors. This means that the neutronics and safety parameters were not as important, and so the model did not have to be as precise in that regard. Additionally, only gaseous fission products or fission products which are removed via sparging are included in the reprocessing scheme, no other chemical extraction takes place. This is because the authors wanted the system to be as simple as possible. ORIGEN provides continuous reprocessing capability, however for this work it would not have been necessary since the authors wanted to use a simpler approach for the model [17].

The sixth entry by Zhou et al is for FAMOS (Fuel cycle Analysis code for Molten Salt reactors). This code uses OpenMC to generate homogenized cross section data followed by the DIF3D diffusion solver along with extensions to model DNP movement, thermal hydraulics, depletion, and continuous reprocessing. Their work also analyzes

the molten salt fast reactor over 200 operational years. The depletion step size is not specifically given in the work, but from analysis of the plots, small time steps seem to have been used at the beginning of cycle and then larger time steps of 100 days are then used for the rest of the steps.

The seventh entry by Nuttin et al analyzes the MSBR using a slightly simplified geometry with MCNP. The reprocessing approach used here is also the same as the approach used in SaltProc, which is to take the inverse of the cycle time to determine the removal rate. Depletion is performed in this work by coupling MCNP to an evolution program and the NJOY code. However, this work uses 10 day steps instead of 3 day steps that SaltProc uses. It also runs for 100 years instead of 20.

The eighth entry by Sheu et al analyzes the Molten Salt Actinide Recycler & Transmuter (MOSART) reactor and uses custom scripts to implement batchwise reprocessing. The codes used are SCALE6 for transport and TRITON for depletion. The step sizes used include 15, 30, and 60 days, in which the authors found that 30 days gave the best results in terms of accuracy and run time balancing for the 30 year simulation.

The ninth entry by Rodriguez-Vieitez analyzes the Accelerator-Driven Neutron Applications (ADNA) Tier-1 reactor using MCNP. Although the model used does implement continuous reprocessing in the Bateman equation, it is not used for the purpose of fuel cycle analysis and depletion. Rather, the work iteratively works towards the equilibrium fuel composition in order to analyze the effect of varying different reactor parameters, such as geometry.

The tenth entry by Fiorina et al is on the Molten Salt Fast Reactor (MSFR) and uses a modified version of the ERANOS-based EQL3D procedure. This model makes use of continuous reprocessing for non-soluble fission products, but uses batchwise reprocessing for soluble fission products. The batchwise reprocessing was incorporated for simplicity in the model. The time steps used are shorter at beginning of cycle and extend out to 30 year steps for a 200 year depletion. Additionally, the radiotoxicity analysis extends out to 1 million years.

The eleventh entry by Zhuang et al discusses an OpenMC extension called OpenMCB-MSR to implement continuous reprocessing in an analysis of the MSFR. The depletion step sizes used are not specified in the work, though with continuous reprocessing step sizes could have been set to above single digit days and still maintained high precision.

The twelfth entry by Ridley and Chvala use batchwise reprocessing on a toy MSR using Serpent2 and a python library. The feed rates were set to fluctuate in order to maintain criticality while also accounting for density imbalance in Serpent2 by increasing the volume of the material. The full core 3D model was then analyzed using 7 day depletion steps for 10 years.

The thirteenth entry is on the Reactor Optimum Design (ROD) code, which allows users to use continuous or batchwise reprocessing for the MSR model. ROD operates by taking a one or two dimensional input and determining the equilibrium fuel composition. This is a useful code for determining a prediction of a model, but is less precise

than more modern codes which offer more detailed geometry and other features.

The fourteenth entry by Merle-Lucotte et al covers depletion of the Thorium Molten Salt Reactor (TMSR) using MCNP4 [18] for transport and REM for material evolution. Continuous reprocessing is used for gaseous fission product extraction, while the other fission products are processed with batchwise reprocessing.

The fifteenth entry by Nagy et al uses a toy model to go through different reprocessing schemes based on the MSBR and MOSART reprocessing designs [33, 20]. SCALE-5 [1] is used for neutron transport and ORIGEN-S is used for depletion. To account for DNPs, the authors make a few approximation which lead to reducing the calculated eigenvalues by 90 pcm. Depletion steps are performed every 5 days, during which continuous reprocessing was implemented for either only gaseous fission product removal or more, depending on the reprocessing scheme chosen. Additionally, the batchwise reprocessing was performed by altering the binary output of ORIGEN, as is performed for the feed fuel and more, depending on the reprocessing scheme chosen.

The sixteenth entry by Xia et al demonstrates the MOlten salt reactor specific DEpletion Code (MODEC). This code uses continuous reprocessing, and has been used to analyze the Molten Chloride salt Fast Reactor (MCFR) by Liaoyuan et al [25]. The MCFR analysis uses SCALE6.1 for transport and MODEC for depletion.

Appendix

Appendix.

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