## Space data processing: making sense of experimental data Exam, May 24, 2016

1. You have experimental data about a dynamical process. What do you start with to study the regularities of process?

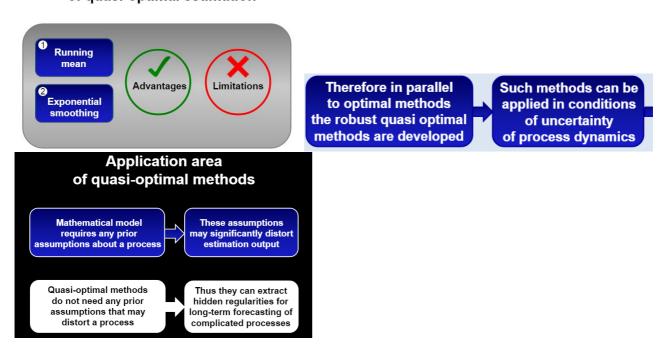
Regularities (cycle, min, max etc)

Changes in dynamics of a process leads to great increase of forecasting errors

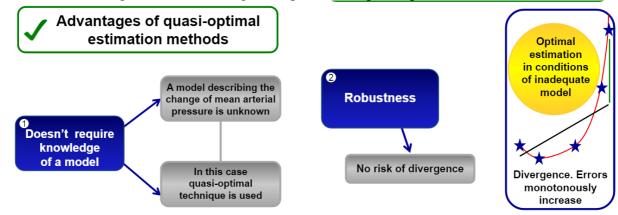
To extract regularities that will allow long-term forecasting we need to smooth data

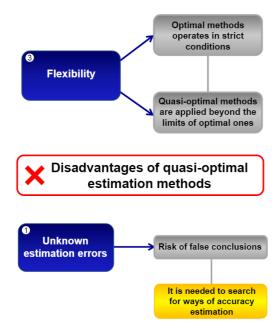
- Try to find characteristics of dynamic process, such as trajectory (there will be big estimation error if parabolic line would be considered as linear) than optimal method if dynamic is known
- 2. What is the difference between optimal and quasi-optimal estimation methods? In optimal method characteristics of dynamic process is known, more accurate predictions.

The most popular methods of quasi-optimal estimation

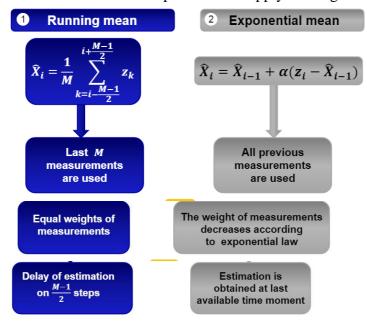


3. Describe advantages and disadvantages of optimal and quasi-optimal estimation methods.





- 4. How do you analyze the reliability of obtained estimation results and potential success of processing? (?)
- 5. Which conditions are more preferable to apply running mean than exponential mean?



In running mean in order to smooth data we need to wait following measurements and if it is months or years it is inconvenient to wait, than we will not have smoothing of last points.

For exponential mean, the graph is shifted to the right, because only previous measurements were taken in account, in running mean, there is no shift.

Errors for running mean is greater than in exponential.

It is critical to choose M and alfa for those methods. If process is almost constant than it is necessary to reduce as much noise as possible, in this case big window M is suitable. For

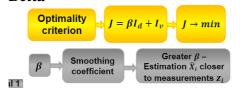
exponential, it is needed small alfa, because the smaller it is the less we rely on next measurements, to this noise.

6. What are results of running mean if the width of running window is the same or greater than period of variations?

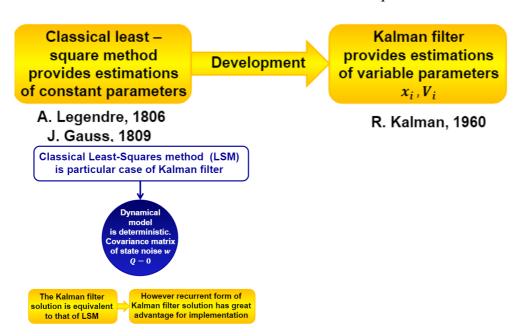
If running mean applied for width of running mean equal to period of variations, than process is completely distorted. Graph is linear.

If it is greater, than inverse oscillation occurs.

- 7. Processing methods are based on finding a balance between the maximal noise reduction and the minimal distortion of true process. Which parameters determine this balance?
  - A. In Kalman filter Ki
  - B. In running mean M
  - C. In exponential mean alfa
  - D. In smoothing algorithm based on complex minimization of deviation and variability indicator? **Betta**



8. What is the main difference between classical least-square method and Kalman filter?

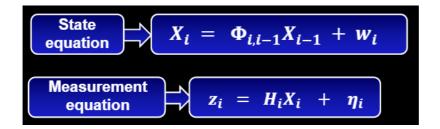


9. How a theoretical model of process can be adjusted on the basis of available experimental data? How errors of measurements can be estimated?

Through state space model

Motion model

$$x_i = x_{i-1} + V_{i-1}T + \frac{a_{i-1}T^2}{2}$$
 $V_i = V_{i-1} + a_{i-1}T$ 



- 10. Is it possible to estimate directly unmeasured parameters using (**not sure**)
  - A. Classical least-square method? NO



B. Kalman filter? - YES

$$v_i = z_i - 2z_{i-1} + z_{i-2}$$

$$\rho_i = z_i - 3z_{i-2} + 2z_{i-3}$$

- C. Quasi-optimal estimation methods? **NO** (measurements constantly is needed)
- 11. How to estimate the accuracy of forecast *m* steps ahead using Kalman filter?

Extrapolation 12 steps ahead 
$$\boxed{X_{12,1} = \ \Phi_{12,1} X_{1,1}} \boxed{\Phi_{12,1} = \Phi_{12,11} \Phi_{11,10} + \cdots \Phi_{3,2} \Phi_{2,1}}$$

- 12. Does Extended Kalman filter provide optimal estimation? Why? Under which conditions it comes to divergence even if all the parameters are known?
- 13. Which methods considered in the course can be widely applied in
  - A. Navigation?
  - B. Space weather?
  - C. Biomedicine (running mean)
- 14. What is the most important thing you learned in this course?