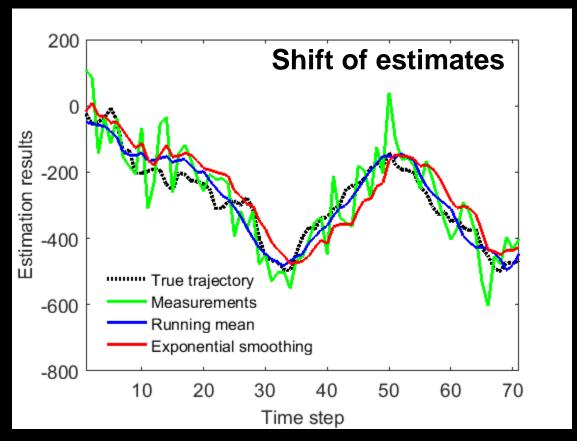


"Space Data Processing: Making Sense of Experimental Data"

Laboratory work 3 Shot discussion

Tatiana Podladchikova Rupert Gerzer Term 4, March 28 – May 27, 2016 t.podladchikova@skoltech.ru

Shift of estimates in exponential smoothing



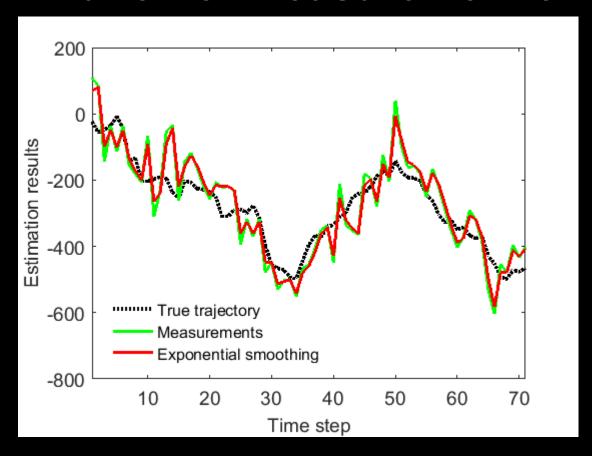
Optimal smoothing constant $\alpha = 0.25$

Equal component of estimation error related with measurement errors

Size of running mean window

M = 7

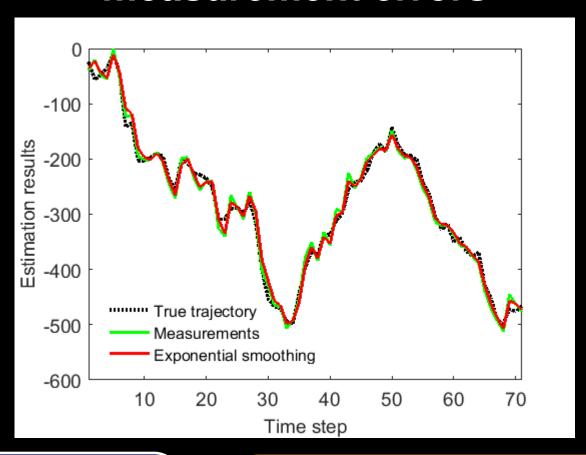
No filtration of measurement errors



Non-optimal smoothing constant $\alpha = 0.8$

No shift of estimates, but no filtration of measurement errors

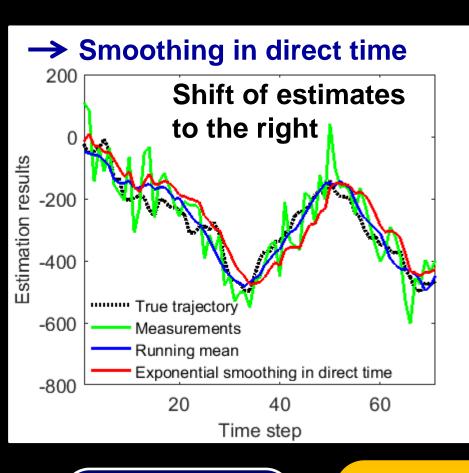
Smoothing in conditions of small measurement errors



Optimal smoothing constant $\alpha = 0.81$

Small measurement errors - small estimation problems

Shift of estimates in exponential smoothing



Smoothing in backward time

Shift of estimates by exponential smoothing in backward time?

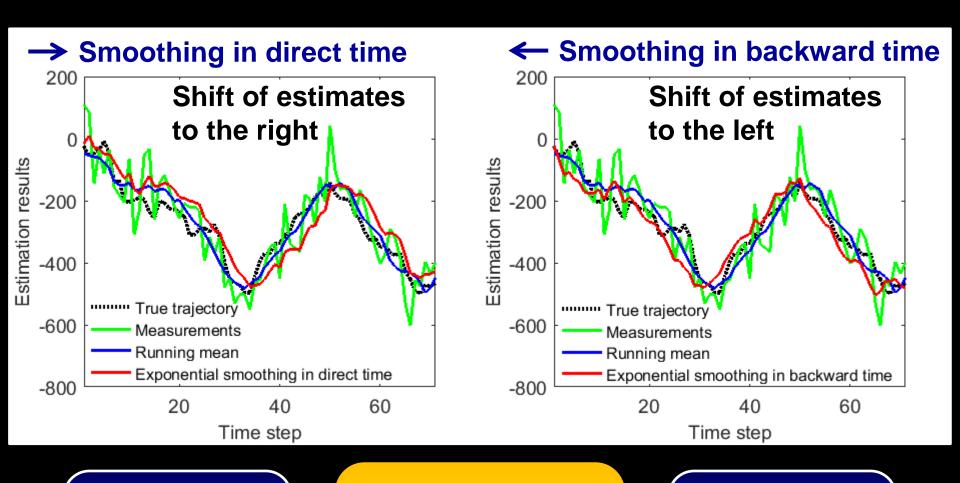
Optimal smoothing constant $\alpha = 0.25$

Equal component of estimation error related with measurement errors

Size of running mean window

M = 7

Shift of estimates in exponential smoothing

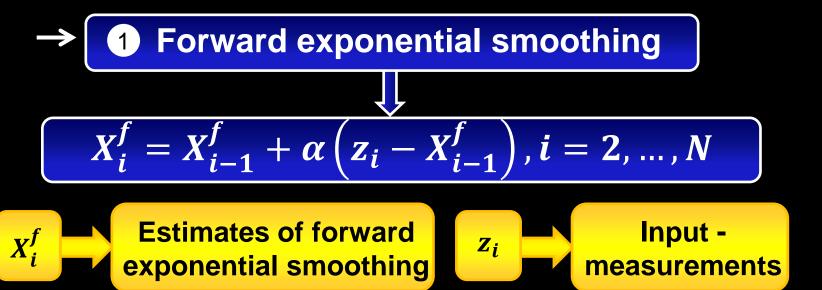


Optimal smoothing constant $\alpha = 0.25$

Equal component of estimation error related with measurement errors

Size of running mean window M = 7

Forward – backward exponential smoothing



Forward – backward exponential smoothing



$$X_{i}^{f} = X_{i-1}^{f} + \alpha \left(z_{i} - X_{i-1}^{f} \right), i = 2, ..., N$$

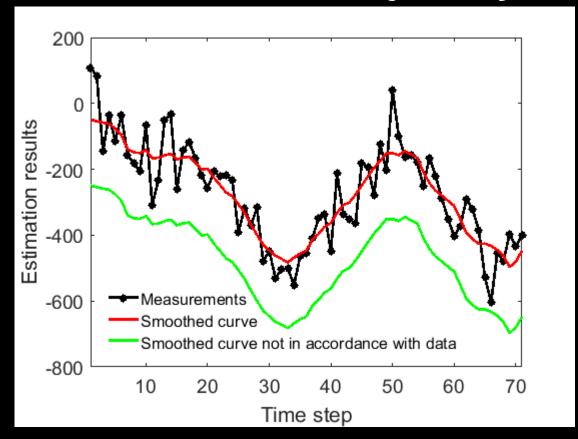
Input - measurements

2 Backward exponential smoothing

$$X_i^b = X_{i+1}^b + lpha\left(X_i^f - X_{i+1}^b
ight)$$
 , $\mathbf{i} = \mathsf{N}-1$, \ldots , 1

 $X_N^b = X_N^f$

How to verify the effectiveness of smoothing when true trajectory is unknown?



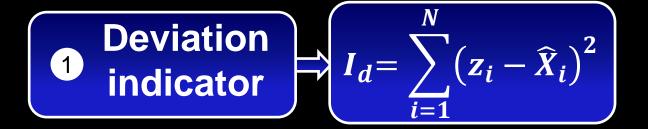
Requirement of estimation to be close to measurements

$$I_d = \sum_{i=1}^{N} (z_i - \widehat{X}_i)^2$$

 $oldsymbol{z_i}$ - measurements

 \widehat{X}_i - estimation

How to verify the effectiveness of smoothing when true trajectory is unknown?

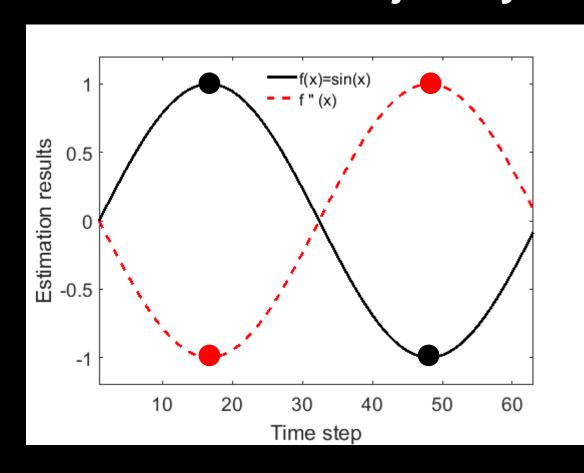




Not enough to use only deviation indicator.

Additional criterion is needed

How to verify the effectiveness of smoothing when true trajectory is unknown?



Absolute value of second derivative is maximal at points of the greatest "variability" of curve

Maximal rate of change of the process

$$I_{v} = \sum_{j=1}^{N-2} (\widehat{X}_{j+2} - 2\widehat{X}_{j+1} + \widehat{X}_{j})^{2}$$

 \widehat{X}_i - estimation