# DECISION FIELD THEORY

A Dynamic Connectionist Model of Decision Making

### PREFERENTIAL CHOICE

- Large number of alternatives and attributes
- Example: Three cars
  - Three alternatives
  - Two attributes; Economy and Quality
  - Consider three choice effects; Attraction, Similarity, and Compromise

## MULTIALTERNATIVE PREFERENTIAL CHOICE

The Basics



### MAIN FINDINGS

Similarity Effect

Attraction Effect

Compromise Effect

 $Pr(A | \{A,B\}) > Pr(B | \{A,B\})$ 

 $Pr(A | \{A,B\}) < Pr(B | \{A,B\})$ 

 $Pr(A | \{A,B\}) > Pr(B | \{A,B\})$ 

BUT

BUT

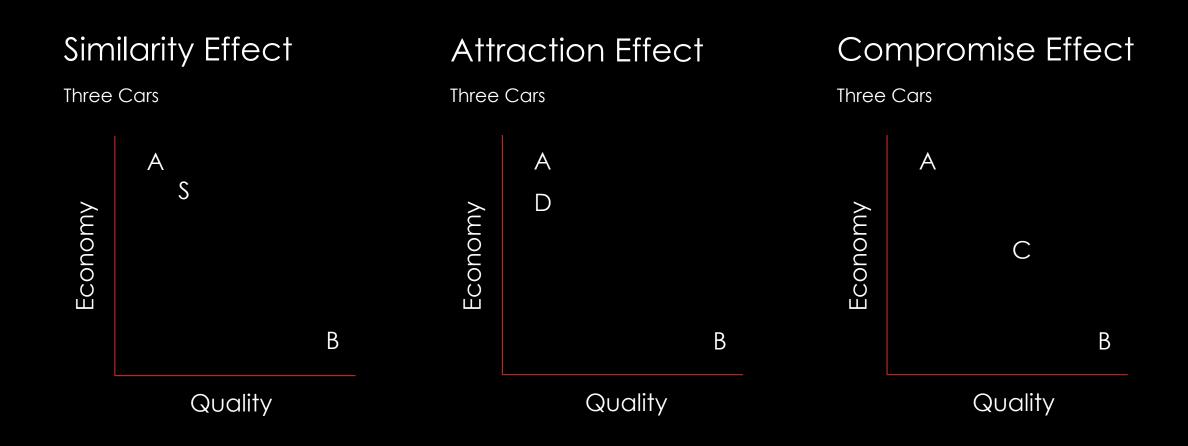
BUT

 $Pr(A | \{A,B,S\}) < Pr(B | \{A,B,S\})$ 

 $Pr(A | \{A,B,D\}) > Pr(B | \{A,B,D\})$ 

 $Pr(A | \{A,B,C\}) \approx Pr(B | \{A,B,C\})$ 

# MAIN FINDINGS (CONT)



**Valences**: At any moment in time, each alternative in the choice set is associated with a valence value.

Component 1: Personal evaluation

Component 2: Attention weight

Component 3: Contrast comparison

• 
$$V(t) = [v_i(t), ..., v_n(t)]'$$

#### **Component 1**

- $m_{ij}$
- $\mathbf{M}_{j} = [m_{i}, \dots, m_{n}]'$
- $\mathbf{M} = [\mathbf{M}_j | \dots | \mathbf{M}_n]$

#### **Component 2**

- $W_j(t)$
- $w_i$
- $\mathbf{W}(t) = [W_j(t), ..., W_n(t)]'$
- **MW**(*t*)

#### **Component 3**

• 
$$v_i(t) = W_j(t)m_{ij} + \dots + W_n(t)m_{in} - \frac{\left[ (W_j(t)m_{hj} + \dots + W_n(t)m_{hn}) + \dots + (W_j(t)m_{gj} + \dots + W_n(t)m_{gn}) \right]}{n}$$

• Process represented by defining a contrast matrix, denoted  ${f C}.$ 

#### **Matrix Product Form**

• V(t) = CMW(t)

**Valences:** Example: Three cars

• 
$$\mathbf{V}(t) = [v_A(t), v_B(t), v_C(t)]'$$

#### Component 1

• 
$$\mathbf{M}_{\mathrm{E}} = [m_{\mathrm{AE}}, m_{\mathrm{BE}}, m_{\mathrm{CE}}]'$$

• 
$$\mathbf{M}_{\mathbf{Q}} = [m_{\mathrm{AQ}}, m_{\mathrm{BQ}}, m_{\mathrm{CQ}}]'$$

• 
$$\mathbf{M} = [\mathbf{M}_{\mathbf{E}} | \mathbf{M}_{\mathbf{Q}}]$$

#### **Component 2**

• 
$$\mathbf{W}(t) = [W_{\mathrm{E}}(t)W_{\mathrm{Q}}(t)]'$$

#### **Component 3**

• 
$$v_{\rm A}(t) = W_{\rm E}(t)m_{\rm AE} + W_{\rm Q}(t)m_{\rm AQ} - \frac{[(W_{\rm E}(t)m_{\rm BE}+W_{\rm Q}(t)m_{\rm BQ})+(W_{\rm E}(t)m_{\rm CE}+W_{\rm Q}(t)m_{\rm CQ})]}{[(W_{\rm E}(t)m_{\rm BE}+W_{\rm Q}(t)m_{\rm BQ})+(W_{\rm E}(t)m_{\rm CE}+W_{\rm Q}(t)m_{\rm CQ})]}$$

• 
$$\mathbf{C} = \begin{bmatrix} \mathbf{1} & -1/2 & -1/2 \\ -1/2 & \mathbf{1} & -1/2 \\ -1/2 & -1/2 & \mathbf{1} \end{bmatrix}$$

#### **Matrix Product Form**

• 
$$V(t) = CMW(t)$$

**Preferences**: At any moment in time, each alternative in the choice set is associated with a preference strength.

- $P_i(t)$
- P(0) = 0
- $\mathbf{P}(t) = [P_i(t), \dots, P_n(t)]$

• 
$$P(t+1) = SP(t) + V(t+1)$$

**Feedback Matrix**: The feedback matrix **S** contains the self-connections and interconnections among the choice alternatives.

- *S*<sub>ii</sub>
- $S_{ij}$  for  $i \neq j$

• 
$$S_{ij} = F[d(A_i, A_j)]$$

• 
$$\mathbf{S} = \begin{bmatrix} 0.95 & -0.09 & -0.001 \\ -0.09 & 0.95 & -0.003 \\ -0.001 & -0.003 & 0.95 \end{bmatrix}$$

Parameters: Altogether there are four sets of parameters that need to be specified to derive predictions.

• w

• M

•  $\epsilon(t)$ 

• S

### SOURCES

- Roe, R. M., Busemeyer, J. R., & Townsend, J. T. (2001). Multialternative decision field theory: A dynamic connectionst model of decision making. Psychological review, 108(2), 370.
- Jessup, R. (2019). Personal interview with L Stevens.