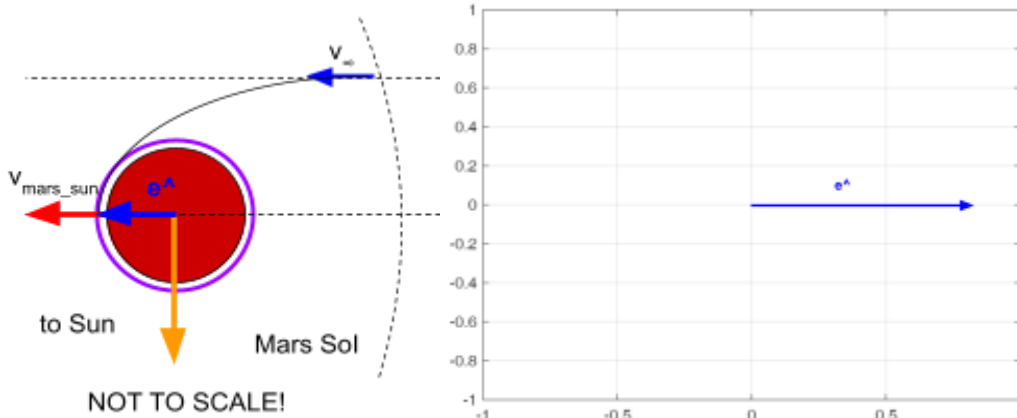


## Homework 6

**DUE: Mon 2025-11-24 @ 23:59 on Canvas**

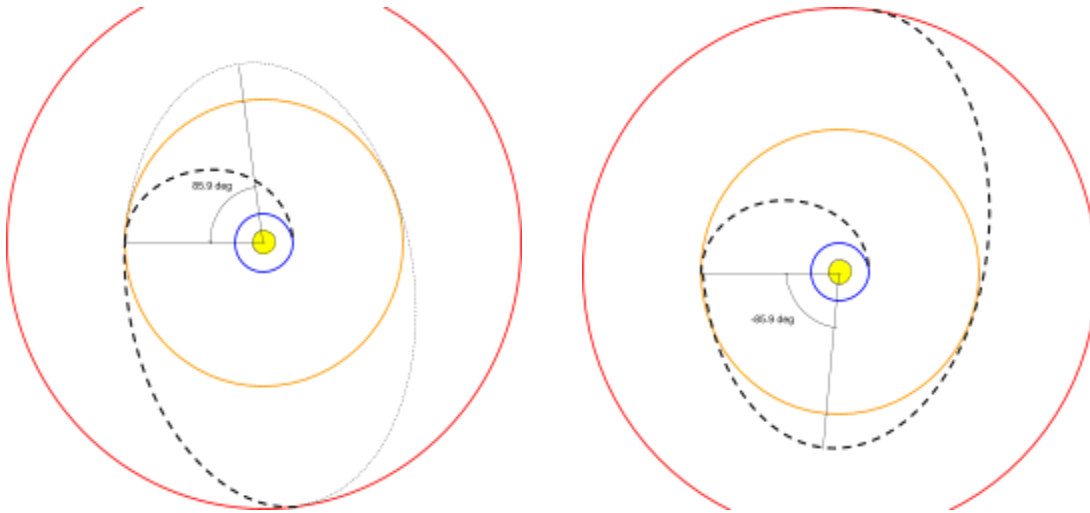
(PDF submissions only; can be pictures/scans as needed)

1. In HW5 P2 the arrival to Mars was presented (below) with arrival from “right to left”, which put the periapsis on the *left* side of the planet - meaning that the “origin” of the perifocal frame points left. Matlab/Python default to the “origin” pointing *right*.



- a. Create a 2D rotation matrix that would allow you to plot the standard output of your Matlab/Python functions but align it with the “arrival” picture, rather than in the default *right* direction.
- b. Make that same matrix into a 3D matrix, which correctly handles the 3rd dimension during the rotation.

At the end of HW5 P4, the transfer orbits to Saturn after the fly-by had a true anomaly of  $\pm 85.9^\circ$ , which means it was not aligned with the original transfer orbit:



- c. What are the 2 2D rotation matrices to rotate from the original transfer orbit axis? (provide numerical answers)
2. The elliptical orbit of an Earth satellite has the following orbital elements:
- |                          |  |
|--------------------------|--|
| $\Omega = 90^\circ$      | <i>right ascension of the ascending node</i> |
| $i = 90^\circ$           | <i>inclination</i>                           |
| $\omega = -45^\circ$     | <i>argument of perigee</i>                   |
| $r_p = 12000 \text{ km}$ | <i>radius of perigee</i>                     |
| $e = 0.5000$             | <i>eccentricity</i>                          |
| $\theta = 45^\circ$      | <i>true anomaly</i>                          |
- a. Carefully sketch the orbit (in 3D) in the geocentric reference frame XYZ. Clearly identify in your sketch the orbital parameters  $\Omega$ ,  $i$ ,  $\omega$ ,  $\theta$  and the position vector  $\mathbf{r}$ .
- b. What is the position vector  $\mathbf{r}$  in the geocentric reference frame? [*Partial answer:*  $|\mathbf{r}| = 13,298 \text{ km}$ ]
3. If we know  $\mathbf{r}$  and  $\mathbf{v}$  in the geocentric equatorial frame we can know everything about an orbit. Given:
- $$\mathbf{r} = 1000\mathbf{I}^\wedge + 2000\mathbf{J}^\wedge + 20000\mathbf{K}^\wedge \text{ (km)}$$
- $$\mathbf{v} = 3\mathbf{I}^\wedge + 3\mathbf{J}^\wedge - 0.3\mathbf{K}^\wedge \text{ (km/s)}$$
- calculate all the orbital parameters  $[\Omega, i, \omega, e, h, \theta]$  by coding Curtis Algorithm 4.2 into Matlab/Python and showing all your code and intermediate answers.  
[*Partial answer:*  $i=92.010^\circ$ ;  $e = 0.093685$ ]

4. A measurement taken from the UW Jacobson Observatory (Latitude:  $47.660503^\circ$ , Longitude:  $-122.309424^\circ$ , Altitude: 220.00 feet) when its local sidereal time is  $36.00^\circ$  makes the following observations of a space object (*Based on Curtis Problems 5.12 + 5.13*):

Azimuth:  $8.0000^\circ$

Azimuth rate:  $0.050000^\circ/\text{s}$ .

Elevation:  $24.000^\circ$

Elevation rate:  $0.02000^\circ/\text{s}$

Range: 8250.0 km

Range rate:  $-0.25000 \text{ km/s}$

- a. What are the  $\mathbf{r}$  &  $\mathbf{v}$  vectors (the state vector) in geocentric coordinates?

(Answer  $\mathbf{r} = [230.51 \ 1464.0 \ 12199] \text{ km}$

$\mathbf{v} = [-1.0662 \ 7.1295 \ 0.31939] \text{ km/s}$ )

- b. Calculate the orbital parameters  $[\Omega, i, \omega, e, h, \theta]$  of the satellite. (For your thoughts: what type of object could this be?)

(Partial Answer  $e = 0.61784, i = 87.902$ )

*Tip: use Curtis algorithms 5.4 and 4.2.*