When you see the words	This is what you think of doing
1. Find the area of the unbounded region represented by the integral $\int_{1}^{\infty} f(x)dx$ (sometimes called a horizontal improper integral).	Set up $\lim_{b\to\infty}\int_1^b f(x)\ dx$ to see if the area diverges or converges.
2. Find the area of a different unbounded region under $f(x)$ from $(a,b]$, where $\lim_{x \to a^r} f(x) = \infty$ or $-\infty$, where the area is represented by $\int_a^b f(x) dx$, (sometimes called a vertical improper)	Set up $\lim_{x \to a^+} \int_a^b f(x) dx$ to see if the area diverges or converges.
3. Given a f(x), find arc length of the function on the interval (a, f(a)) and (b,f(b)).	Use the integral: $L = \int_{a}^{b} \sqrt{1 + \left[f'(x)\right]^2} dx$.
4. Given a curve in parametric form where $x = f(t)$, $y = g(t)$, find the arc length of the curve on the interval $\begin{bmatrix} t_1, t_2 \end{bmatrix}$.	Use the integral: $L = \int_{t_1}^{t_2} \sqrt{\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2} dt$
5. Given $\frac{dy}{dx} = F(x, y) = xy$ and an initial point $(x_o, y_o) = (1, 1)$, find an approximate value for $f(1.2)$ and $\Delta x = 0.1$	Think about Euler's Method to draw tangent lines and approximate along the tangent lines. First calculate the slope at $(1,1)$ and write an equation of a tangent line to f at $(1,1)$. Use this line to approximate a new point at $x=1.1$ using $\Delta x=0.1$. This gives you a second point to repeat the procedure again. Write another tangent line with a new slope and approximate the value of $f(1.2)$ by moving along this second tangent line to the point $x=1.2$.
6. Given the differential equation of the form $\frac{dP}{dt} = kP\left(1 - \frac{P}{L}\right)$ for P as a function of t, where k and L are constants.	Separate the differentials, use partial fractions, integrate, use an initial condition to solve for the constant and end up with an equation of the form: $P = \frac{L}{1 + Ae^{-Mkt}}$

7. Given the differential equation $\frac{dP}{dt} = 12P - 4P^2$ where P is measuring the number an animal present on day 0. Find the value of P when the number of these animals is increasing the fastest.	7. First notice that $\frac{dP}{dt} = 12P - 4P^2$ is a parabola, so rewriting it in the form $\frac{dP}{dt} = kP\left(1 - \frac{P}{L}\right)$ or $\frac{dP}{dt} = 12P\left(1 - \frac{P}{3}\right)$ tells us that the $\frac{dP}{dt} = 0$ v when P=0 or P=3. The number of animals is increasing fastest at the midpoint of 0 and 3 or 1.5.
8. Given the differential equation $\frac{dP}{dt} = 1200P - 400P^2 \text{ where P is measuring the number an}$ animal present on day 0. Determine the $\lim_{n\to\infty} P(t)$.	Factoring $\frac{dP}{dt} = 1200P - 4P^2 = 1200P \left(1 - \frac{P}{300}\right)$ we can see that $\frac{dP}{dt} = 0$ when P=0 and P=300. Therefore, P=300 is the $\lim_{N \to \infty} P(t)$ since the grow increases between P = 0 and P = 300 but stops at P = 300.
9. Given that a line segment has endpoints of (1,2) and (5,10), write a set of parametric equations for the line that passes through these two points.	Determine the slope (m) of the line segment (m=2), write an equation for the line segment using point slope form (y=2(x-1)+2), and then rewrite this equation as parametric equations where $x(t)=t$ and $y(t)=2(t-1)+2$ or $y(t)=2t$. Select values for t from knowing that x or t starts at 1 and goes to 5 so $1 \le t \le 5$
10. Given the position function of two particles in parametric form, $x_1(t) = f(t)$, $y_1(t) = g(t)$ and $x_2(t) = h(t)$, $y_2(t) = k(t)$, determine if the particles intersect or collide.	For the paths to intersect $x_1(t_1) = x_2(t_2)$ and $y_1(t_1) = y_2(t_2)$. Solve these equations simultaneously to find the time when the paths intersect. For the particles to collide they must be at a point at the same time. Determine the times when each particle is at the given point. If the times match, the particles collide, otherwise their paths only cross.
11. Given a set of parametric equations where $x = f(t)$, $y = g(t)$, find $\frac{dy}{dx}$ or the slope of the tangent line.	Recall that $\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$

12. A path of a particle is described with a set of parametric equations $x = f(t)$, $y = g(t)$. Find the equation of the tangent line when $t = to$.	Determine the point where the particle is $(x(t_o), y(t_o))$. Then find the slope of the graph at the time $t=t_o$ by calculating $\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}\Big _{t=t_o}$. Then write the equation of the line in point-slope form.
13. A path of a particle is described with a set of parametric equations $x = f(t)$, $y = g(t)$.	a. Determine the times when $\frac{dx}{dt} = 0$ and $\frac{dy}{dt} \neq 0$.
a. Find all values of t where the particle's path is vertical.	b. Determine the times when
b. Find all values of t where the particle's path is horizontal.	$\frac{dy}{dt} = 0 \text{ and } \frac{dx}{dt} \neq 0 .$
14. Given a set of parametric equations where $x = f(t)$, $y = g(t)$, find $\frac{d^2y}{dx^2}$	First find $\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$ then calculate $\frac{d}{dx} \left[\frac{dy}{dx} \right] = \frac{\frac{d}{dt} \left[\frac{dy}{dx} \right]}{\frac{dx}{dt}}$.
15. Given the position vector of a particle moving in the plane is $r(t) = \langle x(t), y(t) \rangle$. Find the velocity vector.	Recall that the velocity vector is $v(t) = \langle x'(t), y'(t) \rangle$ which means that you must differential $x(t)$ and $y(t)$ respect to t and then write a vector.
16. The position vector of a particle moving in the plane is	Recall that the acceleration vector is
$r(t) = \langle x(t), y(t) \rangle$. Find the acceleration vector.	$a(t) = \langle x''(t), y''(t) \rangle$ which means that you must differential x'(t) and y'(t) respect to t and then write a vector.
17. The position vector of a particle moving in the plane is $r(t) = \langle x(t), y(t) \rangle$. Find the speed of the particle at a moment	Recall that speed is the magnitude of the velocity vector and is found by calculating
at time $t = a$.	$\left v(a)\right = \left \left\langle x'(a), y'(a)\right\rangle\right = \sqrt{\left(x'(a)\right)^2 + \left(y'(a)\right)^2}$
18. Given the velocity vector $v(t) = \langle x'(t), y'(t) \rangle$	Recall that the position vector is
and position vector at $t = 0$ as $\langle X(0), Y(0) \rangle$, find the position vector at time $t = a$.	$\left\langle x(0) + \int_0^a x'(t)dt, y(0) + \int_0^a y'(t)dt \right\rangle$

19. Given $V(t) = \langle x'(t), y'(t) \rangle$ determine when the particle is stopped.	You must consider both x'(t) and y'(t). You need to determine when both x'(t) and y'(t) equal zero.
20. Given $V(t) = \langle x'(t), y'(t) \rangle$ find the slope of the tangent line to the vector at t_1 .	You must calculator $\frac{dy}{dx} = \frac{y'(t)}{x'(t)}$ and evaluate this expression at t_1 .
21. Given a particle moves along a function $y = 3x^2 + 1$, the rate of change of x or $\frac{dx}{dt} = 3t$ for t>0 and x(0)=1. Find the particle's position at time t = 3.	Find the change in the x direction or $x(3) = x_o + \int_0^3 x'(t)dt = 1 + \int_0^3 (3x^2 + 1) dt = 31$. Determine the y coordinate using the function $y = f(x) = 3(31^2) + 1 = 2884$. Write the coordinate: (31, 2884)
22. Find the slope of the tangent line to the polar curve $r = f(\theta)$.	Recall that $x = r \cos \theta, y = r \sin \theta \Rightarrow \frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}}$
23. Given a polar curve $r = f(\theta)$, find horizontal tangents to curve.	Recall that $x = r \cos \theta$, $y = r \sin \theta$ and then find where $r \sin \theta = 0$ and where $r \cos \theta \neq 0$
24. Find vertical tangents to a polar curve $r = f(\theta)$.	Recall that $x = r \cos \theta$, $y = r \sin \theta$ and then find where $r \cos \theta = 0$ and where $r \sin \theta \neq 0$
25. Find the area inside one of the petals on the flower described by $r = 2\cos(3\theta)$.	Recall that one petal can be traced by $-\frac{\pi}{6} \le \theta \le \frac{\pi}{6}$ and the area can be found by calculating the integral

26. Find the area outside r_1 (θ) but inside	First find the points of intersection $\theta = a$ and $\theta = b$ and then
$r_2(\theta)$.	integrate $\int_{a}^{b} \frac{1}{2} (r_2(\theta) - r_1(\theta))^2 d\theta$
	Recall the $x = r \cos \theta$ and $y = r \sin \theta$ to convert from polar
27. Find the arc length of a function $r_1(\theta)$ from $\theta = a \ and \ \theta = b$.	form to parametric form. Then use the integral for arc length with parametric equations. Perform the integral $\int_{a}^{b} \sqrt{\left(\frac{dx}{d\theta}\right)^{2} + \left(\frac{dt}{d\theta}\right)^{2}} d\theta$
2 1 1 1	Notice that the sum is a geometric series where
28. Find the sum $\frac{3}{2} + \frac{1}{2} + \frac{1}{6} + \frac{1}{216} + \cdots$	$a = \frac{3}{2}$ and $r = \frac{1}{3}$ so the sum is given by
	$\frac{a}{1-r} = \frac{\frac{3}{2}}{1-\frac{1}{3}} = 1\frac{1}{2}$
29. Determine if the series $\frac{1}{2} + \frac{2}{3} + \frac{3}{4} + \dots + \frac{n}{n+1} + \dots$	Think about the nth term in this series: $\frac{n}{n+1}$. By the nth term
converges or diverges	test, since $\lim_{n\to\infty} \frac{n}{n-1} = 1 \neq 0$ the series diverges.
30. Determine if the series $\sum_{n=1}^{\infty} \frac{3}{n+1}$ converges or diverges	Think about using the integral test. $\int_{1}^{\infty} \frac{3}{x+1} dx = \lim_{b \to \infty} \int_{1}^{b} \frac{3}{x+1} dx$
	$= \lim_{b \to \infty} \ln \frac{b+1}{2} = \infty$ Therefore, the series diverges since the integral diverges.

31. Determine if the series $\sum_{n=1}^{\infty} \frac{1}{x^{\frac{3}{2}}}$ converges or diverges.	One test you might think of using is the p-series test. Since $p = \frac{3}{2} > 0$ converges.
32. Determine if the series $\sum_{n=1}^{\infty} \frac{1+\sin x}{x^2}$ converges or diverges.	Since the series $\sum_{n=1}^{\infty} \frac{2}{x^2}$ converges and $0 < \frac{1 + \sin x}{x^2} \le \frac{2}{x^2}$ the series converges by the comparison test.
33. Determine if the series $\sum_{n=1}^{\infty} \frac{3^n}{4^n + 1}$ converges or diverges.	Using the ratio test, $\lim_{n \to \infty} \frac{\frac{3^{n+1}}{4^{n+1} + 1}}{\frac{3^n}{4^n + 1}} = \frac{3}{4^{n+1} + 1} (4^n + 1) < \frac{3}{4^{n+1}} (4^n) = \frac{3}{4} < 1$ So the series converges.
34. Determine if the series $\sum_{n=1}^{\infty} (-1)^{n-1} \frac{1}{n}$ converges or diverges.	Using the alternating series test, since each term $\frac{1}{n}$ decreases as n approaches infinity and converges to 0, then the alternating series converges.
35. Write a series for $X \cos X$ where n is an integer	Recall that $\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$ and then multiply through by x.
36. Write a series for $ln(1+3x)$ centered at $x=0$.	Recall that $\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots + (-1)^{n-1} \frac{x^n}{n} + \dots$ Substitute 3x for x.

37. If $f(x) = 2 + x + \frac{1}{2}x^2 + \frac{1}{4}x^3 + \dots$ represents a T	Notice that $f(x)$ is a geometric series with $a = 2$ and $r = \frac{1}{2}x$ so
Taylor Polynomials about $x = 0$, find $f(-2)$	the sum of the series can be written as $\frac{a}{}$ or
	the sum of the series can be written as $\frac{a}{1-r}$ or $ \frac{2}{1-\frac{1}{2}x} = \frac{2}{1-\frac{1}{2}(-2)} = 1 $
	$1 - \frac{1}{2}x$ $1 - \frac{1}{2}(-2)$
	2
38. Write the nth degree Taylor Polynomial for $f(x)$ at $x = c$.	$(r-c)^2$
	$T_n(x) = f(c) + f'(c)(x-c) + f''(c)\frac{(x-c)}{2!}$
	$T_{n}(x) = f(c) + f'(c)(x-c) + f''(c)\frac{(x-c)^{2}}{2!} + \dots + f^{(n)}(c)\frac{(x-c)^{n}}{n!} + \dots$
	$+\cdots+f^{(n)}(c)\frac{(n-1)!}{n!}+\cdots$
39. Given a Taylor series, find the Lagrange form of the remainder for the 4 th term.	This error is no greater than the value of the 5^{th} term at some
the remainder for the 4 term.	value of a between x and c. $R_n(x) = \frac{f^{(n+1)}(a)}{(n+1)!}(x-c)^{n+1}$
40 Let S_4 be the sum of the first 4 terms of an alternating series	You should recognize this as the error for the 4 th term of an
for f(x). Approximate	alternating series which is no greater than the absolute value of the 5 th term.
$ f(x)-S_4 $.	
41. Given the polynomials	$f(x) = e^x$
$f(x) = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$, what is f(x)?	
$(x) = 1 + x + \frac{1}{2!} + \frac{1}{3!} + \dots$, what is $f(x)$?	
42. Given the polynomial	
$f(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots + \frac{(-1)^n x^{2n+1}}{(2n+1)!} + \dots, \text{ what is}$	$f(x) = \sin(x)$
f(x)?	
43. Given the polynomial	
$f(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots + \frac{(-1)^{11} x^{2n}}{(2n)!} + \dots,$	$f(x) = \cos(x)$
what is $f(x)$?	

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44. Find the interval of convergence of a series.	Apply the ratio test to find the interval and then test convergence at the endpoints.
45. Find $\lim_{x \to a} \frac{f(x)}{g(x)}$	Check to see if you can use L'Hopital's Rule. Check to see if $f(a) = g(a) = 0$ or $f(a) = g(a) = \infty$. If this is true, then $\lim_{x \to a} \frac{f(x)}{g(x)} = \frac{f'(a)}{g'(a)}$. You may have to repeat these steps.
46. Find $\int \frac{dx}{x^2 + x - 12}$	Use partial fraction to set up two integrals: $\int \frac{A}{x+4} dx + \int \frac{B}{x-3} dx$. Solve for A and B and then complete the integration. $\int \frac{-\frac{1}{7}}{x+4} dx + \int \frac{\frac{1}{7}}{x-3} dx = \frac{1}{7} \ln \left \frac{x-3}{x+4} \right + C$