

1、 If $f(x) = kx + b$, then

$$\begin{aligned}
 g_k(x) \equiv y_k &= f\left(\sum_j w_{kj} f\left(\sum_i w_{ji} x_i + w_{j0}\right) + w_{k0}\right) \\
 &= k_2 \left(\sum_j w_{kj} (k_1 (\sum_i w_{ji} x_i + w_{j0}) + b_1) + w_{k0}\right) + b_2 \\
 &= k_2 k_1 \sum_j \sum_i w_{kj} w_{ji} x_i + k_2 (\sum_j w_{kj} (k_1 x_i + b_1) + w_{k0}) + b_2 \\
 &= w_k x_i + b_k
 \end{aligned}$$

Thus, nonlinearity is not be achieved.

2、 (1) assume: $Z = W^T X$

If it use Gradient Descent update weight:

$$\begin{aligned}
 \frac{\partial E}{\partial W} &= \frac{\partial E}{\partial y} \frac{\partial y}{\partial Z} \frac{\partial Z}{\partial W} \\
 &= (y - g) y (1 - y) X
 \end{aligned}$$

Then $W = W - \lambda (y - g) y (1 - y) X$

(2) We know W, X, g, λ ,

and compute $y = s(W^T X)$,

Based on formula (1), $W = (0.5002, 1.0004, 1.0001)^T$