

Homework_2:

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Part_1:

a) if $w=0$, $y_w=1$, else : $y_w=0$ so:

$$- \sum_{w \in Vocab} y_w \log(\hat{y}_w) = -y_o \log(\hat{y}_o) = -\log(\hat{y}_o)$$

b)

$$\begin{aligned} \frac{\partial J}{\partial v_c} &= \frac{\partial \left(-\log \frac{\exp(u_o^T v_c)}{\sum_{w \in Vocab} \exp(u_w^T v_c)} \right)}{\partial v_c} \\ \frac{\partial J}{\partial v_c} &= \frac{\partial(-u_o^T v_c)}{\partial v_c} - \frac{\partial(-\log(\sum_{w \in Vocab} \exp(u_w^T v_c)))}{\partial v_c} \\ \frac{\partial J}{\partial v_c} &= -u_o + \frac{1}{\sum_{w \in Vocab} \exp(u_w^T v_c)} \cdot \sum_{i \in Vocab} \exp(u_i^T v_c) u_i \\ \frac{\partial J}{\partial v_c} &= U(\hat{y} - y) \end{aligned}$$

c) if $w=0$, we have:

$$\begin{aligned} \frac{\partial J}{\partial u_w} &= \frac{\partial \left(-\log \frac{\exp(u_o^T v_c)}{\sum_{w \in Vocab} \exp(u_w^T v_c)} \right)}{\partial u_o} \\ \frac{\partial J}{\partial u_w} &= -v_c + \frac{\exp(u_o^T v_c) \cdot v_c}{\sum_{w \in Vocab} \exp(u_w^T v_c)} \\ \frac{\partial J}{\partial u_w} &= (-y + \hat{y}) v_c \end{aligned}$$

if $w \neq 0$, $y = 0$, so we have:

$$\frac{\partial J}{\partial u_w} = \hat{y}v_c$$

d) in sigmoid fuction: $y'=y(1-y)$, so:

$$\sigma'(x) = \sigma(x)(1 - \sigma(x))$$