

# Homework 1

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## Part 1

### 1.

Assume  $f(x)$  is a linear function, i.e.  $f(x) = kx + b$ . Then

$$\begin{aligned}g_k(X) \equiv y_k &= f\left(\sum_j w_{kj} f\left(\sum_i w_{ji} x_i + w_{jo}\right) + w_{ko}\right) \\g_k(X) \equiv y_k &= f\left(\sum_j w_{kj} f\left(\sum_i w_{ji} x_i + w_{jo}\right) + w_{ko}\right) \\&= k\left(\sum_j w_{kj} f\left(\sum_i w_{ji} x_i + w_{jo}\right) + w_{ko}\right) + b \\&= k\left(\sum_j w_{kj} \left(k\left(\sum_i w_{ji} x_i + w_{jo}\right) + b\right) + w_{ko}\right) + b \\&= k^2 \sum_i \sum_j w_{kj} w_{ji} x_i + k\left(\sum_j w_{kj} (kw_{jo} + b) + w_{ko}\right) + b\end{aligned}$$

Which is still a linear function of  $X$ .

### 2.

#### (1)

Let  $z = W^T X$

$$\begin{aligned}\frac{\partial E}{\partial W} &= \frac{\partial E}{\partial y} \frac{\partial y}{\partial z} \frac{\partial z}{\partial W} \\&= (y - g)y(1 - y)X\end{aligned}$$

$$W' = W - \lambda \frac{\partial E}{\partial W} = W - \lambda(y - g)y(1 - y)X$$

#### (2)

$$y = f(W^T X) = 0.953$$

$$\frac{\partial E}{\partial W} = -0.002[1, 2, 0.5]^T$$

$$W' = W - \lambda \frac{\partial E}{\partial W} = 0.5002, 1.0004, 1.0001$$