

# Planning Review

## Combinatorial Planning

- Road map, or graph-based

Ex)

- Visibility graphs
- Voronoi diagrams
- Exact cell decomposition
- Approximate cell decomp.

Pros:

- elegant and complete
- find the solution or report NONE

Cons:

- quickly becomes intractable
- curse of dimensionality

## Sample-based planning

- does not characterize  $C_{free}$  &  $C_{obs}$
- only has collision detection algorithm

Ex) PRM (Probabilistic Road Maps)  
RRT

- Tractable, less computationally intensive
- Not complete

## Potential Field methods

- not graph-based

Field:  $U(q) = U_{\text{attractive}}(q) + U_{\text{repulsive}}(q)$

$$\vec{F}(q) = -\vec{\nabla} U(q) \quad \leftarrow \text{Gradient descent vector field}$$

- problem: local minima
  - use local-minima free navigation from

## Search

- sequence of actions (a path) that leads to desirable state, (a goal)

Types:

uninformed: no information about domain, can only expand nodes

- breadth-first, uniform cost, depth-first, bidirectional

Informed: further information about domain through heuristics

- A\*, greedy best-first, D\*

Performance: measured by

- Completeness
- Optimality
- Time complexity
- Space complexity

## D\* Search:

- unknown, partially known, or dynamic environments, the replanned path may be blocked
- planned path may be blocked or need to replan
- incrementally repair path keeping its modifications local around robot pose
- D\*, D\* Lite, Field D\*

## Collision avoidance

Ex | Dynamic window approaches  
Neuron Diagram Navigation  
Vector Field Histogram +  
Extended Potential Fields

## Markov Decision Process

- uncertainty about actions
- transition model  $T(a, s_i, s_{i+1})$  Markov Property

- Definitions of Problem:

States:  $S$

Actions:  $A$

initial state:  $s_0$

Transition:  $T(a, s_i, s_{i+1})$

Reward:  $R(s)$

we want to find optimal policy

$$\pi^*(s) = \arg \max_a E[V^*(s)]$$

$$\text{where } V^*(s) = E\left[\sum_{k=0}^{\infty} R(s_k) \mid \pi\right]$$

$$= R(s) + V^*(s')$$