

Concrete Machine Learning

Deep User : 2020 Summer Program

A | Naïve Bayes Classifier

Naïve Bayes Classifier

Clustering algorithm

Supervised/Unsupervised learning

Strong & Simple

Labeling process

Bayesian probability theory base

The diagram shows the Naïve Bayes formula with arrows pointing from descriptive labels to the corresponding parts of the equation:

$$P(c|x) = \frac{P(x|c)P(c)}{P(x)}$$

- Likelihood** points to $P(x|c)$
- Class Prior Probability** points to $P(c)$
- Posterior Probability** points to $P(c|x)$
- Predictor Prior Probability** points to $P(x)$

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Main Purpose

Proceed with classification of objects as the group with the greatest **posterior probability**

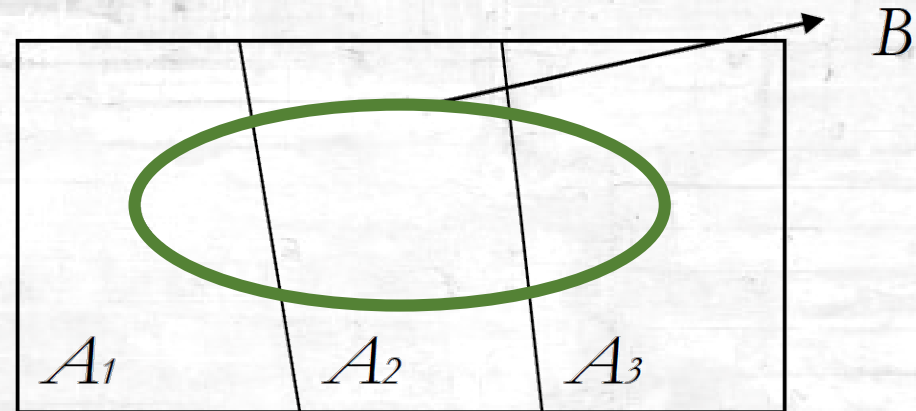
$$\text{posterior} = \frac{\text{prior} \times \text{likelihood}}{\text{evidence}}.$$

* posterior : 사후 확률, prior : 사전확률, likelihood : 우도, evidence : 관찰값

$$\hat{y} = \underset{k \in \{1, \dots, K\}}{\operatorname{argmax}} p(C_k) \prod_{i=1}^n p(x_i | C_k).$$

Assign classes with the highest post probability for k classes

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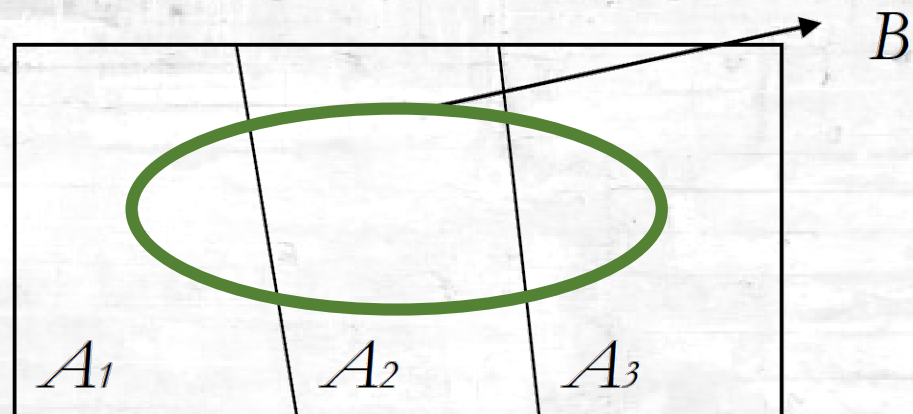


$$P(B) = P(A_1 \cap B) + P(A_2 \cap B) + P(A_3 \cap B)$$

$$P(B) = P(A_1)P(B|A_1) + P(A_2)P(B|A_2) + P(A_3)P(B|A_3) = \sum_{i=1}^3 P(A_i)P(B|A_i)$$

Law of Total Probability

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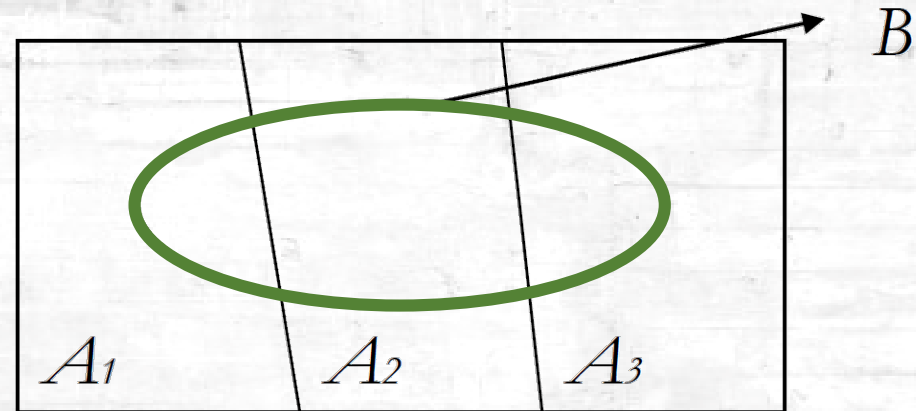
$$P(A_1), P(A_2), P(A_3).$$

사전확률(prior probability)

$$P(B|A_1), P(B|A_2), P(B|A_3).$$

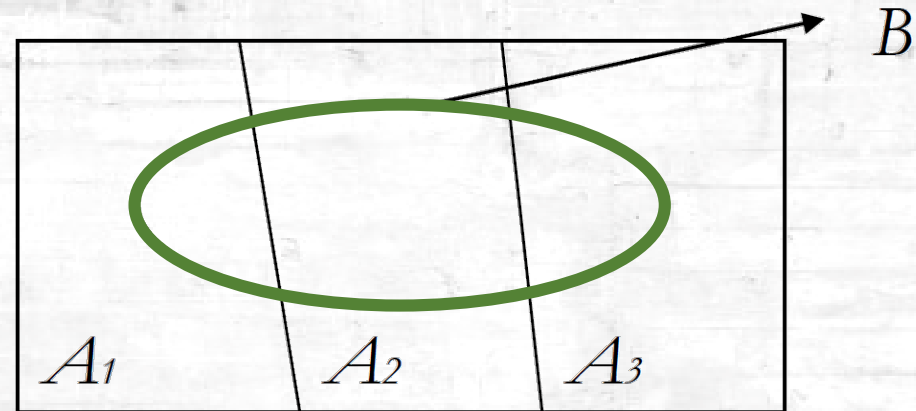
우도(likelihood probability)

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$$\begin{aligned} P(A_1|B) &= \frac{P(A_1)P(B|A_1)}{P(B)} \\ &= \frac{P(A_1)P(B|A_1)}{P(A_1)P(B|A_1) + P(A_2)P(B|A_2) + P(A_3)P(B|A_3)} \end{aligned}$$

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$$P(A_1|B)$$

사후확률(posterior probability)

Posterior probability is an updated version of prior probability

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: 쿠키가 들어 있는 그릇 두 개가 있다

첫번째 그릇에는 바닐라 쿠키 30개와 초콜렛 쿠키 10개가 들어있고, 두번째 그릇에는 두 가지 쿠키가 종류별로 20개씩 들어 있을 때

어떤 그릇인지 보지 않고 한 그릇에서 임의로 쿠키를 집었는데 바닐라 쿠키라면 이 때 '이 바닐라 쿠키가 그릇 1에서 나왔을 가능성'은 얼마일까요?

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$$P(H|D) = \frac{P(H)P(D|H)}{P(D)} = \frac{\frac{1}{2} \times \frac{3}{4}}{\frac{5}{8}} = \frac{3}{5}$$

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항목	가설1(그릇1)	가설2(그릇2)
사전확률 $P(H)$	$1/2$	$1/2$
우도 $P(D H)$	$3/4$	$1/2$
사전확률 × 우도	$3/8$	$1/4$
한정상수 $P(D)$	$5/8$	$5/8$
사후확률 $P(H D)$	$3/5$	$2/5$

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Document Classifier

$$P(c_1|d) = \frac{P(c_1, d)}{P(d)} = \frac{\frac{P(c_1, d)}{P(c_1)} \cdot P(c_1)}{P(d)} = \frac{P(d|c_1)P(c_1)}{P(d)}$$

$$P(c_2|d) = \frac{P(d|c_2)P(c_2)}{P(d)}$$

$$P(c_i|d) \propto P(d|c_i)P(c_i)$$

$$\begin{aligned} P(c_i|d) &= P(c_i|w_1, w_2) \\ &\propto P(w_1, w_2|c_i)P(c_i) \\ &\propto P(w_1, w_2|c_i) \end{aligned}$$

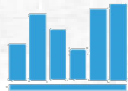
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Normalization Formula

$$X_{normalized} = \frac{(X - X_{minimum})}{(X_{maximum} - X_{minimum})}$$



Numpy.sum

Numpy.mean

Numpy.std

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Calculate the mean and standard deviation of train data each for label 1, label 2, label 3, feature 1, feature2, feature 3, feature4

the example of mean matrix of train data

	Feature1	Feature2	Feature3	Feature4
Label1	Mean	Mean	Mean	Mean
Label2	Mean	Mean	Mean	Mean
Label3	Mean	Mean	Mean	mean

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- Estimate the probability of feature vector each for class 1, class 2, class3
- Use Naive Bayesian theorem
 - $p(C_k|x) = \frac{p(C_k)p(x|C_k)}{p(x)}$
 - $p(x|C_k) = k_{th}$ - feature (observation)
 - $p(x)$ = normalization factor ($\sum_{k=1}^{class_num} p(C_k)p(x|C_k)$) (Never mind)
 - $p(C_k)$ = initial probability of class
- Use chain rule
 - $p(C_k)p(x_1 \text{ and } x_2 \text{ and } x_3|C_k) = p(C_k)p(x_1|C_k)p(x_2|C_k)p(x_3|C_k)$
- Use log scale
 - $\ln(p(C_k)p(x_1|C_k)p(x_2|C_k)p(x_3|C_k)) = \ln(p(C_k)) + \ln(p(x_1|C_k)) + \ln(p(x_2|C_k)) + \ln(p(x_3|C_k))$

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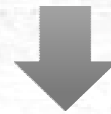
ESTIMATION OF PROBABILITY DISTRIBUTION

	Probability of class1	Probability of class2	Probability of class3
Feature vector1	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$
Feature vector2	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$
Feature vector3	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$
Feature vector4	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$

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ESTIMATION OF PROBABILITY DISTRIBUTION

	Probability of class1	Probability of class2	Probability of class3
Feature vector1	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$
Feature vector2	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$
Feature vector3	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$
Feature vector4	$\ln(p(C_1)p(x_1 C_1)p(x_2 C_1)p(x_3 C_1)p(x_4 C_1))$	$\ln(p(C_2)p(x_1 C_2)p(x_2 C_2)p(x_3 C_2)p(x_4 C_2))$	$\ln(p(C_3)p(x_1 C_3)p(x_2 C_3)p(x_3 C_3)p(x_4 C_3))$



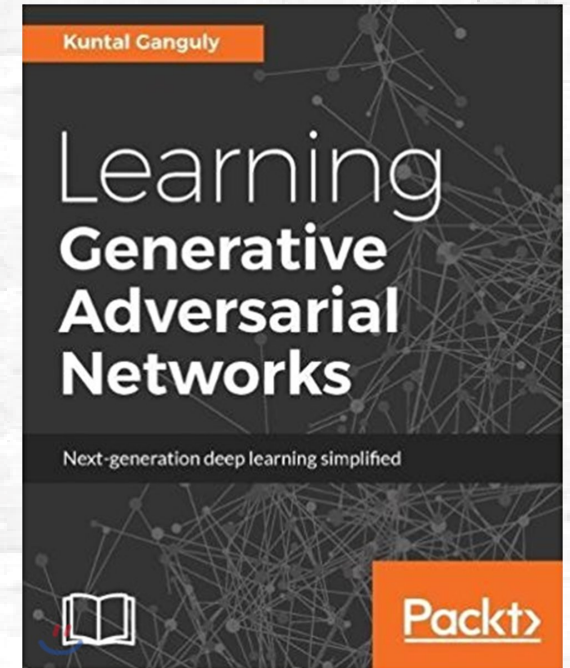
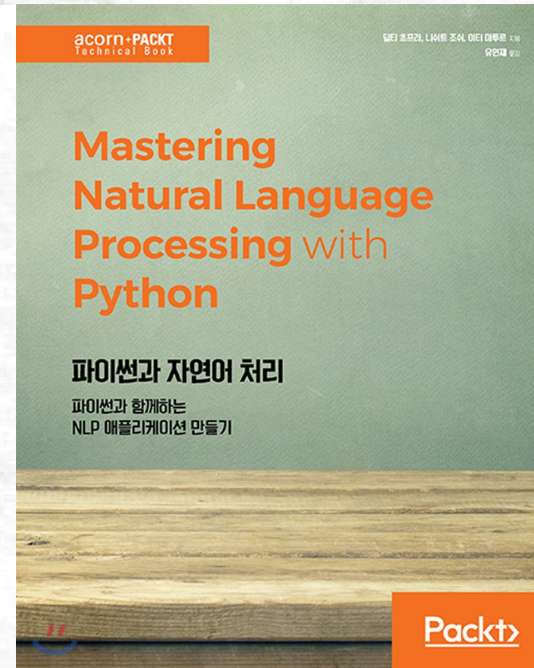
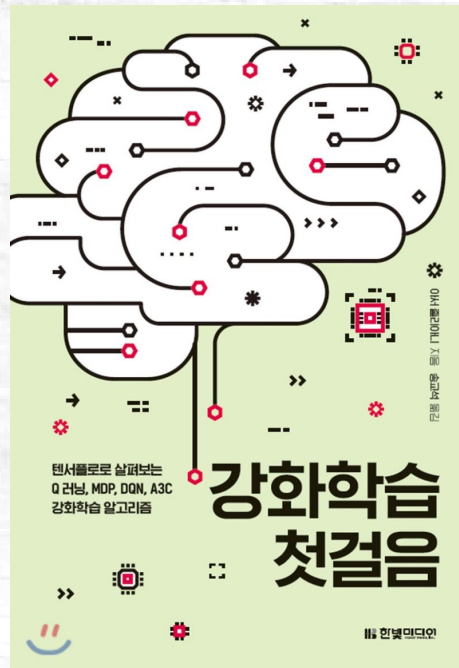
Estimation class	
Feature vector1	1
Feature vector2	2
Feature vector3	3
Feature vector4	1

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After build all of function, you can see below result from python console when you compile "main_app.py" (or yielded 90% accuracy due to shuffling data)

```
accuracy is 97.95918367346938% !!  
the number of correct data is 48 of 49 !!
```

```
In [22]:
```

DeepUser

Naïve Bayes Classifier

THANKS