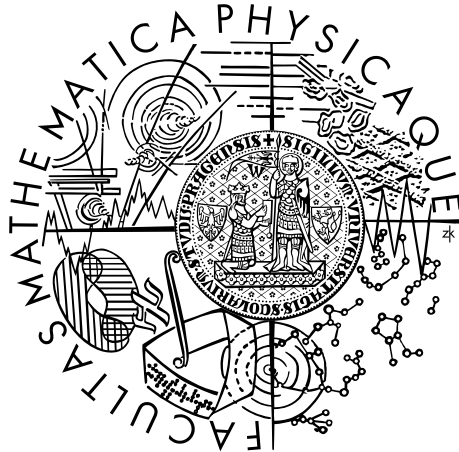Charles University in Prague

Faculty of Mathematics and Physics

BACHELOR THESIS

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Graph Based SLAM on NDT Maps

Name of the department

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Title: Graph Based SLAM on NDT Maps

Author: Lukáš Jelínek

Department: Name of the department

Supervisor: Supervisor's Name, department

Abstract: Abstract.

Dedication.

Contents

Introduction

Humanity has envisioned many tasks which could be carried out by robots including transportation, health care, save and rescue and many more. Robots of current world can efficiently operate only in very limited conditions. To solve problems of the future we need fast and reliable algorithms for our robots. Big question in field of mobile robotics is how to efficiently localize robot and create map as precise as possible. This problem is often referred to as Simultaneous localization and mapping (SLAM) problem.

Good localization is crucial part of any good navigation software. Generated map plays important role in path planning and multi-robot coordination. SLAM algorithm should relay mostly on robots internal sensors like, e.g., sonars, cameras, wheel encoders. Using Global positioning system (GPS) is only possible in outdoor environment. Precision of this localization is very often not good enough to successfully navigate robot.

In last decade many high quality SLAM algorithms where presented. Solution to full problem of map building and robot positioning is usually done by combining algorithms for map representation, sensor measurement registration and position estimation. This work solves full SLAM problem by combination of Normal distributions transform (NDT) map building process and scan registration with well developed research branch of graph-based SLAM optimizing engines. To achieve this combination this work presents extended implementation of NDT mapping process and new way of robust scan-matching on NDT map. Implementation is done in Robot operating system (ROS) to make it easy to test, use and improve.

This work has following structure. First chapter analyze full SLAM on NDT maps. Second chapter provides more information about algorithms used in this work. Third chapter describes whole system of NDT SLAM. Fourth chapter makes focus on implementation details behind the algorithms. In the last chapter we wrap up results of this algorithm and compare it to existing ROS implementations.

1. NDT SLAM problem analysis

Solving full SLAM problems requires combining algorithms for position estimation, mapping and measurement data registration. Solution to mapping and localization starts with initial data from sensors. Every solution to full SLAM requires different input data. Standard is to expect odometry information about relative movement of robot and some measurements of environment for map building. SLAM problems were first studied with only sonar measurement and odometry from wheel encoders. Sonars were later replaced by more sophisticated laser scanners. An odometry got more exact with use of Integrated Measurement Unit (IMU). Alternatively, full SLAM problem is also solved with use of camera images for both odometry and map building. Visual methods are very popular mostly in 3D mapping of environment.

Types of SLAMs based on lasers is still wildly used in real life applications. More research was done in 2D variant. It is generally less computationally expensive to perform 2D SLAM. This is mostly because full solution needs to include data registration process. It is used for variety of tasks e.g., map building, odometry estimation, unique feature detection.... Some techniques used in registration are described in section 1.4.

Every solution also needs to output some type of map, which should be used for navigation and planning of robot. Every solution again uses different mapping technique. The map can be represented as a set of unique landmarks or as a set of measurements integrated together. Some of these integration methods are presented in section 1.3

Lastly we need to estimate position of robot based on our data and created map. First we need to define what it is position of robot and how we will represent it.

1.1 SLAM problem definition

Successfully solving SLAM problem means to find location of robot in every time step and be able to create map at that time-stamp. In real world we deal with robot's sensors which have always some inherited noise. This means we are not able to fully say exact position of robot. This is main reason why to use probabilistic definition of problem. Robot moves through unknown space along trajectory expressed as variables $\mathbf{x}_{1:T} = \{\mathbf{x}_1, ..., \mathbf{x}_T\}$. While moving robot is taking odometry measurements $\mathbf{u}_{1:T} = \{\mathbf{u}_1, ..., \mathbf{u}_T\}$ and perception of environment $\mathbf{z}_{1:T} = \{\mathbf{z}_1, ..., \mathbf{z}_T\}$ Solving SLAM than means finding out probability of the robot's trajectory $\mathbf{x}_{1:T}$ and a map $\mathbf{m}$ of local environment given all the measurements and initial pose $\mathbf{x}_0$:

$$p(\mathbf{x}_{1:T}, \mathbf{m} \mid \mathbf{z}_{1:T}, \mathbf{u}_{1:T}, \mathbf{x}_0) \tag{1.1}$$

Odometry is represented in 2D by triple (x, y, θ) or by three dimensional transformation matrix. Initial pose can be interpreted as origin of coordinate system for global map.

1.2 SLAM's position estimation categories

Over the past decade reaserch has developed three distinctive categories of SLAM position estimation.

First category is Extended Kallman Filter (EKF) variant. It is based on Kalman filters (KF). The KF assume that probability density functions are Gaussian distributions and system is linear. The EKF solves problems with non-linearity of robot pose model. Performance of EKF strongly depends on quality of statistical model for noise in sensors and odometry. Unfortunately, these models are usually not available. A set of comparative tests for convergence and inconsistencies of EKF is in work of [HD07].

Another category is based on Particle filters (PF). Current state of the robot is represented by set of weighted particles. This brings advantage of representing uncertainty through multi-modal distributions and dealing with non-Gaussian noise. [MTKW02] proposed computationally efficient method based on PF called FastSLAM. It uses particles to represent posterior probability of motion. In addition, each particle also holds K Kallman filters representing landmark positions. It was demonstrated that it is possible to calculate high precision maps utilizing FastSLAM. Inspired by FastSlam, a method based on Rao-Blackwellized Particle Filter is proposed in [GSB07]. Derivations of this approach are still actively used in robotics today.

Last category is based on modeling state of the system by constructing robot's state graph and optimizing to find final robot position. In this graph nodes represent robots possible pose and edges its relative movement. Nodes may also hold information about current stae of map or laser measurements. This representation was first time used in work of [LM97]. This technique was later improved by [OLT06]. They have presented efficient optimization approach based on the scholastic gradient descent. It was able to correct even large graphs. Later multiple authors improved SLAM optimization by adding hierarchies to large graphs or adding robustness to optimization process. Graph based model of SLAM offers a lot of flexibility for improvements and can be reasonably fast even on large graphs. More details about graph generation and optimization is in section 2.1.

1.3 Map representation

Successful solving SLAM problem should output map of the unknown environment. This map needs to be stored for local path planning and obstacle avoidance. It is also needed for scan registration. Algorithms for avoiding obstacles very often need precise map. Map should keep low memory consumption, because robots very often have limited access to memory. Scan registration algorithms usually might benefit from maps with high precision.

Point-cloud is map representation which stores all measured points. This is very precise representation. All input data is still in its raw form. We are not loosing any information. Scan-matching algorithms e.g. Iterative closest point (ICP) is working on top of this datastructure. It is very easy to convert from this model to different type of map if needed. Problematic is memory consumption. If robot runs for long period with higher frequency of data production, it is likely that robot will run out of memory.
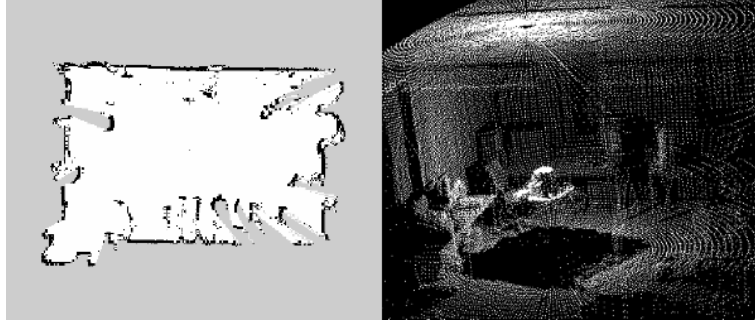
Figure 1.1: On the left is visualization of occupancy grid. On the right is visualized point cloud of a room.

Occupancy map is grid based type. It consists of grid with cells. In every cell we have just one value describing probability that this cell is occupied. Value becomes higher with more incoming data measurements. It has constant memory consumption with respect to time of robot's run-time. It is possible to use this representation for map to map registration process. This model is also possible to represent empty spaces (low probability). This feature is used by many path planning and obstacle avoidance algorithms. That is why, occupancy maps are main output format for SLAM algorithms in ROS. It is important to select good resolution of grid. Finer grid offers better detail but higher memory consumption.

Quad-tree is a tree data structure. Each node of the tree has exactly four children. Nodes are decomposing space into sub-areas. Every node has its threshold. When it is reached, cell subdivides into four smaller cells. This process dynamically change resolution of the grid. This way we get higher precision in places where it matters more. Maximal precision is usually bounded by minimal size of leaf nodes.

NDT representation uses grid based datastructure. Each cell has normal distribution parameters calculated based on inserted points. This model offers constant memory consumption over time. In comparison, NDT has better representation of inner points than octree (3D case of quad-tree). This was proven as convenient by [SAS$^+$13]. They have shown that coarser NDT grid can have similar results in precision of space representation than finer octree map. Standard NDT representation has deeper explanation in section 2.2.1. NDT maps can also include information about occupancy. This extension called NDT-Occupancy mapping (NDT-OM) will be presented in 2.2.2. In addition to occupancy, this method also add a way how to remove dynamic objects from map. This is important feature if SLAM should work in dynamic environment.
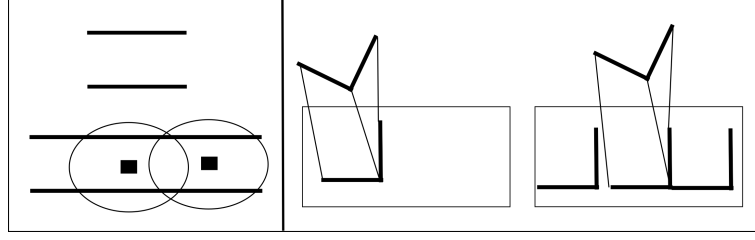
Figure 1.2: Local and global ambiguities in scan registrations. On the left is local ambiguity. On the right is global ambiguity with two maps. First map is original map without all information about environment. Second map is reality with all features. Registration wrongly associated matching based on information only from first map.

1.4 Registration

Scan registration is one of the key concepts in full SLAM solution. Algorithm can use scan matching between two scans to determine transformation. It tells how far robot moved between scans. Two scans might not offer enough information for successful registration. Imagine a robot which is standing in the corner of a room with sensor facing the wall. Scan from this robot has only information from very limited field of view and this might lead to matching errors. Therefore, it is usually necessary to combine individual scans to operate with more data.

One of the algorithms which uses this process is called incremental scanmatching. It takes arriving scan and tries to match it against the map built from previous measurements. By doing so it can very well be used instead of robots odometry in SLAM's graph creation. Algorithms which are possible to work in incremental scan-matching on top of NDT maps are mentioned in sections 2.3.1 and 2.3.2. Other often used approach is the ICP, which is described in 2.3.3. All these algorithms use optimization methods, e.g. Newton's method. Good initial guess is needed in order to guarantee converge to the right solution.

Another example of usage scan registration in graph based SLAM is for testing generated loop closures. Loop closures are edges which close the loop (create cycle) of robot's movement in graph. Details about loop closure generation are in section 2.1.2. Measurements from nodes which play role in loop closure are scan matched. By doing this we are trying to proof if two nodes are really overlapping. The Biggest problem with this registration is that we have no valid prior information about positions of these nodes. These two scans might be perfectly aligned or they can be from completely different parts of the world. Registration needs to robustly estimate the transformation. In case of misleading closure algorithm should reject it. One scan matcher capable of robust transformation calculation is mentioned in 2.3.4.

Even robust scan-matchers can fail to correctly identify loop closures. These registration mismatches can be divided into two categories.

The First category is local ambiguity. Good example of it is when robot moves in long corridor as seen in figure 1.2 on the left. Environment does not have many distinctive features and algorithm selected one of three possible correct options.

The second category is global ambiguity. This ambiguity usually happens when algorithm do not have enough information about whole environment. Lim-

ited size of scans and environment with similar indistinguishable elements can resolve in wrong association. One example can be seen in figure 1.2 on the right.

1.5 Graph-based SLAM on NDT maps

After initial research we have noticed that there is big potential in using NDT maps for introducing full SLAM solution. NDT maps have good memory consumption they can hold occupancy information and reject dynamic objects with use of NDT-OM extension 2.2.2. Registration algorithms for alignment with initial guess on top of NDT grids already exists. Graph based pose estimation currently represent very flexible way how to find robots position. It is also possible to extend to work on large scale maps. It also has topological information about robot movement which can be beneficial.

Additionally, in the work of [SSAL13b], authors described that scan matching based on NDT registration can provide very good result in mapping process with use of NDT-OM. They have proven this by mapping large area with only use of global map solely created by modified method of incremental scan matching. They have noted that even though results are very accurate, there is need for solution with loop closure mechanism to improve results. In this work, they have mapped real life factory datasets with dynamic entities. NDT-OM proven to be reliable way of removing dynamic objects and updating map.

Loop closures can be created in graph based SLAM and additionally tested by robust scan matcher. In order to use NDT maps this work presents robust registration method for loop closure alignment 3.5.

It was also necessary to find solution how to represent the map. In previous works there was always one global NDT map. Iterative scan matching than used this map for more precise alignment. In our work we use graph pose estimation which is making changes to the based on graph optimization. We present a way how to represent the map which can be updated 3.3.

Incremental scan matching on NDT grids was proven to get good results. Therefore, it should be included in this work as well and combine it with rest of proposed system 3.2.

Lastly, it needs to be implemented in a way that on-line processing of real datasets is possible. It needs to have standard ROS interface commonly found in other SLAM. It should use standard libraries available in ROS.

Final result of this works should be implementation of 2D graph based SLAM on NDT maps with easy use inside of ROS ecosystem.

2. Used algorithms and key concepts

This section offers basic introduction to multiple state-of-the-art algorithms used in this work. It starts with explanation of graph-based SLAM variant. Next section 2.2 describes NDT based map representations. Section 2.3 is dedicated to NDT based registration algorithms. We also include basic introduction to ICP and Correlative registration algorithm.

2.1 Graph-based SLAM

A graph-based SLAM solves SLAM pose estimation problem by constructing graph representation. This graph is commonly called a pose graph. Nodes of the graph represent potential poses of robot at certain time stamp T. Therefore, nodes are representing our trajectory $\{\mathbf{x}_1, ..., \mathbf{x}_T\}$. Nodes also hold state of the current map. Edges in the graph represent possible spatial transformation between nodes. Edge is generated out of noisy sensor data. Therefore, we need to model uncertainty of this movement. It is represented by probability distribution and included in the edge. Generation of constrains is done by algorithm's front-end. It creates them either from odometry $\mathbf{u}_T$ or by measurement data $\mathbf{z}_T$ registration. Once the graph is completed ,it is optimized by algorithms back-end. Result of this process is the most likely position of all nodes in the graph.

2.1.1 Pose graph creation

Process of graph creation operates in SLAM's front-end. First step is to receive robot's movement. This transformation may come from wheels' encoders, visual odometry from camera or IMU. Front-end also receives a covariance of the transformation based on noise model of source sensor. From transformation and covariance we can create an edge for the graph. This edge type is usually called odometry edge. Consecutive odometry measurements creates long chain of edges in graph.

Nodes represent current robot position. Therefore, they should have some initial estimate. This initial guess may come from concatenation of transformations in odometry edges. Another method is to use propagation of transformation through minimum spanning tree constructed out of full graph.

Second type, represents edges from nodes to landmarks. A landmark is and unique descriptors of the place. When landmark is detected, front-end creates node representing this place and landmark edge connecting it with graph. Edge carries transformation between current node and landmark. If landmark already exists than created edge might help to optimize correct pose estimate of other nodes.

Third common type of edges are loop closure edges. These edges usually connect two nodes, which share same perception of the world. Aligning these perceptions yields virtual transformation between these nodes. A covariance needs to be provided from alignment process and depends on used technique. Loop closure

edge usually exists if we have revisited same place again. This is crucial information for SLAM's back-end. Based on it optimalization finds out if odometry edges reliably represent reality and adjust pose estimates.

2.1.2   Loop closure creation

First step of correct loop closure creation is to identify all nodes ,which might have overlapping measurements. Given pose a we find all nodes $b_1...b_n$ from graph whose sensor measurements overlap pose a. This could be determined by finding relative position of nodes a and b_i. One possible method how to determine is to use Dijkstra projection mentioned in [Ols09a]. Dijkstra projection starts at node a and concatenate covariances and transformation along the minimum uncertainty path. This path is selected based on determinant of covariance matrix. Small covariance matrix has lower determinant than covariance matrix with large numbers. Minimum uncertainty selection guaranties that algorithm will get to the target b_i with maximum precision. Concatenation of covariances is done based on equation:

$$P_{a+b} = J_a P_a J_a^T + J_b P_b J_b^T \tag{2.1}$$

$$J_a = \begin{pmatrix} 1 & 0 & -x\sin\theta - y\cos\theta \\ 0 & 1 & x\cos\theta - y\sin\theta \\ 0 & 0 & 1 \end{pmatrix} J_b = \begin{pmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \tag{2.2}$$

where P_a is acumulated covariance, P_b is aditional covariance, Jaccobian J_a use parameters from transformation $(x, y, \theta)_a$ and J_b from $(x, y, \theta)_b$ Concatenation of transformations is defined as:

$$\begin{pmatrix} x \\ y \end{pmatrix}_{a+b} = \begin{pmatrix} x \\ y \end{pmatrix}_a + R(\theta_a) \begin{pmatrix} x \\ y \end{pmatrix}_b \tag{2.3}$$

$$\theta_{a+b} = \theta_a + \theta_b \tag{2.4}$$

where $R(\theta_a)$ is rotation matrix created from angle θ_a.

After successful generation of overlapping nodes, every potential pair needs to be tested by registration algorithm. This algorithm needs to be robust enough to reject as many incorrect pairs as possible. If matching is possible it should align measurements and return best transformation. More about this type of algorithms can be found in section 1.4.

Even the best registration algorithm may fail and return erroneous measurement. Loop closure process needs to reject these errors. One solution is to use method proposed by [Ols09a]. In this approach we first group loop closure edges into groups based on their topological distance from each other. Later we validate every cluster against internal inconsistencies. Edges marked as inconsistent are deleted from system.

Other option is to use robust optimization engines, witch can identify outliers in the form of error edges. Comparison of known outliers rejection methods was done by [SP13].

2.1.3 Optimization

Back-end receives graph with odometry edges and loop closure edges. The main task of back-end is to optimize this graph and return the most likely position of nodes. Popular method of optimization is to use the Gauss-Newton or the Levenberg-Marquardt algorithms.

To utilize these methods we first need to define our error function. We will use notation similar to one presented in section 1.1. Let $\mathbf{x} = (\mathbf{x}_1, ..., \mathbf{x}_T)^T$ be a vector of graph's nodes positions. Let $z_{i,j}$ to be a registration algorithm transformation between nodes x_i and x_j. Let $\Omega_{i,j}$ be a information matrix of this transformation (information matrix is an inverse of covariance). Lastly let $\hat{z}_{i,j}$ be a estimate of registration transform received from initial configurations of nodes i and j.

The log-likelihood of measurement $z_{i,j}$ is than defined as:

$$l_{i,j} = (\hat{z}_{i,j} - z_{i,j})^T \Omega_{i,j} (\hat{z}_{i,j} - z_{i,j}) \tag{2.5}$$

where $(\hat{z}_{i,j} - z_{i,j})$ is a difference between expected measurement and real measurement. Now we can define out error function as

$$F(\mathbf{x}_{1,T}) = \sum_{<i,j>\in G} (\hat{z}_{i,j} - z_{i,j})^T \Omega_{i,j} (\hat{z}_{i,j} - z_{i,j}) \tag{2.6}$$

Our goal is to calculate such a $\mathbf{x}$ that this function is minimal. More formaly we wan to find solution to

$$\bar{x}_{1,T} = argmin_{\mathbf{x}} \ F(\mathbf{x}) \tag{2.7}$$

Information on how to minimize this function, calculate derivatives and how to exploit structure of the problem to get significant speed gains continue in reading in this tutorial [GKSB10].

2.2 NDT mapping algorithms

2.2.1 NDT grid

NDT grid representation was first time used by [BS03] in their scan registration process. Central idea was to convert laser scan into grid with cells containing normal distributions. Points in space from laser scanner are first separated into corresponding cells. From points in single cell we approximate normal distribution (μ_i, P_i) by calculating mean and covariance:

$$\mu_i = \frac{1}{n} \sum_{k=1}^{n} x_k \tag{2.8}$$

$$P_i = \frac{1}{n-1} \sum_{k=1}^{n} (x_k - \mu_i)(x_k - \mu_i)^t \tag{2.9}$$

NDT grid was than used for registration.Originally proposed grid could be updated with new laser scans only by keeping used points and recalculating all cells again. This has changed with proposed recursive covariance update step by [SAS$^+$13]. Their update step offers way how to fuse in new measurements. First it calculate normal distributions for added points. In second step, it merges old covariances with new one.

Consider two sets of measurement $\{x_i\}_{i=1}^{m}$ and $\{y_i\}_{i=1}^{n}$ than formula for mean calculation is in equation (2.11). Recursive update for covariance (RCU) is in equation (2.14)

$$T_x = \sum_{i=1}^{m} x_i \quad T_y = \sum_{i=1}^{n} y_i \quad T_{x \oplus y} = T_x + T_y \tag{2.10}$$

$$\mu_{x \oplus y} = \frac{1}{m+n} T_{x \oplus y} \tag{2.11}$$

$$S_x = \sum_{i=1}^{m} (x_i - \frac{1}{m} T_x)(x_i - \frac{1}{m} T_x)^T \quad S_y = \sum_{i=1}^{n} (y_i - \frac{1}{n} T_y)(y_i - \frac{1}{n} T_y)^T \tag{2.12}$$

$$S_{x \oplus y} = S_x + S_y + \frac{m}{n(m+n)} (\frac{n}{m} T_x - T_{x \oplus y})(\frac{n}{m} T_x - T_{x \oplus y})^T \tag{2.13}$$

$$P_{x \oplus y} = \frac{1}{m+n-1} S_{x \oplus y} \tag{2.14}$$

Proof and further explanation for these equations can be found in work of [SAS$^+$13] and later improved in [SSAL13a].

In addition to fusing in new laser measurements we can also easily generated coarser grid by merging cells from higher resolution grid to grid with lower resolution. This mechanism is useful in path planning where we can plan on coarser grid which could be faster. Also, we can use multi-level scan matching approaches, which will be discussed in next section 2.3. Small disadvantage of this method is that we need to keep number of points used in every cell.

It is worth noting that in continual integration of scans calculated mean and covariance grow unbounded with increasing number of points added. This could lead to numerical instabilities. Second problem is that cell's distribution contains measurements from all scans. This is problem in dynamic environment where some objects might disappear. These problems are solved by restricting maximal number of points in cell with parameter M

$$N_{x \oplus y} = \begin{cases} n + m, & n + m < M \\ M, & n + m \geq M \end{cases} \tag{2.15}$$

Parameter M modifies how fast we let RCU replace old measurements by new one. Small value of M makes adaptation faster and big M keeps weight of older data higher. This cause to have new data making smaller impact on result of process.

2.2.2   NDT-OM extension

NDT grids offers good compromise between space and precision, but it lacks information about occupied space and unoccupied space. This is crucial for planning algorithms. This functionality was added to NDT by [SAS$^+$13] and later improved by same authors in later work [SSAL13a]. Every cell in NDT-OM is represented with parameters $c_i = \{\mu_i, p_i, N_i, p_i\}$, where μ_i and P_i are parameters of estimated normal distribution, N_i is number of points in cell and p_i is probability of the cell being occupied.

Calculation of occupancy parameter is done by ray-tracing. Consider that we have current map m_x. We have calculated new NDT map m_y from incoming distance measurements. Both maps needs to be in the same coordinate system. Ray-tracing starts at current robot position in map m_x. End point of ray-tracing is value of mean from one of the cells in new map m_y. Program visits every cell along the line and updates covariance. It is important to visit every cell just once. When is ray-tracing over we merge in all cells from m_y into m_x with RCU update rule.

The main idea in occupancy update calculation is that not all cells are occupied fully. Normal distribution usually occupies only part of the cell. A ray tracing through this cell might not intersect bounds of normal distribution at all. In order to consistently update occupancy the update value should not be a constant. Better option is to choose a function describing difference between map m_y and m_x. This function with explanation might be found in [SSAL13a].
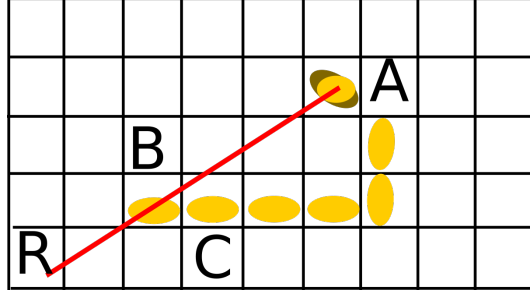
Figure 2.1: Image describing raytracing update. Yellow elipses represent normal distributions. Letter R represent robot position and red line ray tracing line. RCU will be applied to the cell marked A. A distribution in cell marked with letter B will get updated as unoccupied. Cell C will stay without any update.

2.3 Registration algorithms

2.3.1 NDT registration

NDT registration process was first time explained by [BS03]. They have explained how to make 2D registration between older scan (target scan) and newer scan (source scan). Target scan was converted to NDT grid by technique mentioned in section 2.2.1. Result of registration should be transformation defined in 2D:

$$T : \begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix} \tag{2.16}$$

where $(t_x, t_y)^T$ represents translation and θ represents rotation. Transformation is used for transforming source scan. At the beginning of program parameters of transformation are initialized either by zero or from initial guess. For each point of transformed scan cost function is computed This function is defined as:

$$score(\mathbf{p}) = \sum_i \exp(-\frac{1}{2}((T(x_i, \mathbf{p}) - \mu_i)^T P_i^{-1}(T(x_i, \mathbf{p}) - \mu_i)) \tag{2.17}$$

where $\mathbf{p} = (t_x, t_y, \theta)$ are parameters of transformation, $N(\mu_i, P_i)$ are parameters of normal distribution where point x is transformed by transformation T. Goal of the NDT scan-matching is to find parameters $\mathbf{p}$ which maximize this function. This maximization problem is changed to minimization problem by searching for minimal value of -score. Newton's algorithm finds minimizing parameters in p by iteratively solving equation

$$H\Delta p = -g \tag{2.18}$$

Representation of hessian, gradient and all derivations might be found in work of [Mag09]. Magnusson also introduced new scaling parameters into score function in order to reject possible outliers. probability distribution function (PDF) inside of cells of target NDT grid may not be always from normal distribution. In practice any representation which approximates structure of the element is valid. Outliers are points far from the mean of distribution and cause unbounded growth of PDF.

At the beginning, algorithm created discrete NDT grid out of target scan. This introduces discretization problems. These problems are cause by points

generating PDF which are larger than their cells. In the original work of [BS03] this was solved by creating 4 target grids where each grid is translated by half of the cell size in single direction. This process made this algorithm inefficient. Introduction to multi-layer NDT grid structure, presented by [UT11], solved this problem. Multi-layer approach consists of several grids with different resolution. Grids are ordered from coarser grid to finer grid. Algorithm starts with coarse grid and estimates parameters of transformation. Calculated transformation is used as initial guess at lower level. This principle practically eliminated need for four overlapping grids. It also offered better convergence time and increase to robustness. Algorithm is able to converge when matched scans are farther away. Good configuration is 4 layers with cell sizes 2, 1, 0.5 and 0.25 meters.

Another improvement to algorithm is usage of concept of linked cells. In practical registration very often part of the source scan lie far from any target cells. This causes only small portion of points contribute to score function. It can cause algorithm failure or just increase time of convergence. Linked cells prevent this by providing cells in target scan, which are close to the point from source scan. Implementation of this technique is possible with use of kD-tree with means of all cells as input points. Every point or source scan finds k-nearest cells and execute score calculation on them.

Algorithm 1 NDT algortihms with muilti layer and linked cell enhancements

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Require: source scan, target scan, parameters (x, y, θ) of initial transformation, cell resolution for each layer
 1: **function** NDTREGISTRATION($scan_s$, $scan_t$, p_{init},$resolutions$)
 2:      $\mathbf{p} \leftarrow p_{init}$
 3:      **for all** res from $resolutions$ **do**
 4:          $ndt_t \leftarrow$createNDTGrid(res,$scan_t$)   ▷ described in section 2.2.1
 5:          transform each point $x_i \in scan_{trans}$ with $T(x_i, \mathbf{p})$
 6:          $\mathbf{p} \leftarrow$ computeSingleGrid($scan_{trans}$, ndt_t, $\mathbf{p}$)
 7:      **end for**
 8:      **return** calculated parameters $\mathbf{p}$ of transformation
 9: **end function**

2.3.2 D2D-NDT registration

Distribution to distribution (D2D)-NDT is variant of NDT registration algorithm proposed by [SMAL12]. It is extension of original algorithm presented in section 2.3.1. Instead of using only one grid for target scan. This aproach uses two grids. One for source scan and second for target grid. Algorithm than minimize the sum of L_2 distances between pairs of PDF's from both grids. Formally, transformation between two sets of cells X and Y is defined as:

$$f(\mathbf{p}) = \sum_{i=1,j=1}^{n_X,n_Y} -d_1 \exp\left(-\frac{d_2}{2}\mu_{ij}^T(R^T P_i R + P_j)^{-1}\mu_{ij}\right) \qquad (2.19)$$

$$\mu_{ij} = R\mu_i + t - \mu_j \qquad (2.20)$$

where $\mathbf{p} = (t_x, t_y, \theta)$; $X(\mu_i, P_i)$ and $Y(\mu_j, P_j)$ are PDF's of individual cells in pair; a pair (R, t) represents rotation matrix from parameter θ and translation

Algorithm 2 Computing transformation on with single target NDT grid and source point cloud

---

Require: source scan, target NDT grid, parameters (x, y, θ) of initial transformation

  1: **function** COMPUTESINGLEGRID($scan_s$, ndt_t, p_{init})
  2:      **while** not converged **do**
  3:          $\mathbf{p} \leftarrow p_{init}$
  4:          $(score, g, H) \leftarrow (0, 0, 0)$
  5:          **for all** points $x_i \in scan_{trans}$ **do**
  6:              $\bar{x}_i \leftarrow T(x_i, \mathbf{p})$
  7:              $cells \leftarrow$ find k-closest cells to $\bar{x}_i$
  8:              **for all** cells $c_i \in cells$ **do**
  9:                  {based on [Mag09]}
10:                  $(score, g, H) \leftarrow (score, g, H) +$ calcNewtonParameters(c_i, $\bar{x}_i$)
11:              **end for**
12:          **end for**
13:          solve $H\Delta p = -g$
14:          $\mathbf{p} \leftarrow \mathbf{p} + \Delta p$
15:      **end while**
16:      **return p**
17: **end function**

---

vector $t = (t_x, t_y)$. Regulation parameters d1 and d2 are set to values $d_1 = 1$ and $d_2 = 0.05$. Equation 2.20 represents difference in means where mean u_i is transformed to new position.

Optimization of this function is done in similar way to 2.3.1 by utilizing Newtons method and solving $H\Delta\mathbf{p} = -g$. Derivations for calculation of hessian and gradient are presented in work of [SMAL12].

This algorithm is also possible to improve by iterating over multiple layers with different resolutions similar to NDT registration in previous section.

In comparison, with NDT registration this algorithm needs only NDT grids for registration. Point cloud can be thrown away after successful creation of grid. This allow saving memory and efficiently represent maps in SLAM. In addition, D2D is almost ten times faster than standard NDT registration on same dataset. This was proven in comparative study from [MVS+15]. The main cause of this speed up is smaller number of calls for score calculation. In point to distribution (P2D)-NDT mentioned in last section we need to calculate score for each point in source point cloud. In case of D2D we just calculate score function for each cell of source grid. This is done by generating only pairs between cell from source grid and closest cell from target cell. Closest cell can be easily found by using kD-tree with values of target grid's means.

2.3.3 ICP

The iterative closest point (ICP) algorithm was first introduced by [CM92] and it is still very popular method for registering point clouds. To briefly summaries algorithm: ICP iteratively refines position of two point clouds by optimizing the sum of square distances between corresponding pair of points from two clouds. This approach is usually called point-to-point registration. Class of algorithms based on ICP has developed many modifications. Surrvey of base type of ICP algorithms and their comparison on well designed datasets is in work of [PCSM13].

2.3.4 Correlative scan registration

Correlative scan registration is algorithm presented by [Ols09b]. This method was developed to robustly solve registration problem. It does not require any initial guess. Therefore, it is possible to use it for loop closure registration.

The algorithm requires two point clouds. Target point cloud is used for generation of fast look up table filled with bit values. It is created by separating points from target cloud into individual cells. Every cell which has some points in it is marked as occupied. After this step we have a table with value 1 in cells with some points and value 0 in cells without points. In next step we add sensor noise to the table. As a function of our noise we use radially symmetric kernel.

$$K_{i,j} = \exp\left(\frac{-1}{2}\left(\frac{\sqrt{(ir)^2 + (jr)^2}}{\sigma}\right)^2\right)\eta \qquad (2.21)$$

$$K = \begin{pmatrix} 2 & 14 & 2 \\ 14 & 100 & 14 \\ 2 & 14 & 2 \end{pmatrix} \qquad (2.22)$$

where $K_{i,j}$ is one element of kernel; $\sqrt{(ir)^2 + (jr)^2}$ is euclidean distance from center of the kernel to the element i, j with cell size parameter r. Standard deviation of sensor nose is abbreviated by σ and η is kernels max value.

The Kernel overlaps over every occupied cell in the table. If value of kernel is higher than value in table. Table is updated with the kernels value. Generated smoothing can be seen in figure 2.3.4.

This algorithm is avoiding initial guess by trying all possible rotations and translations of source cloud. Every point of transformed source cloud is mapped into certain cell of look up table. The total score of transformed cloud is sum of all mapped cells scores. Algorithm usually tries rotations and translations from selected range. Transformation with the best score is the most probable transformation.

This brute force process might take long time if we select small cell size to achieve good registration. To speed up this process we first need to avoid computationally expensive calculation of goniometric functions in transformation. This can be achieved by first generating all possible rotations of point cloud. For each rotation we try all translations from selected range with step size selected based on cell size of look up table.

Real speed improvements offers usage of two layer architecture of look up tables. The first table has coarse resolution. This table is used for initial estimation

									2	14	2
							2	14	14	14	100	14
	1	1	1	1			14	100	100	100	100	14
							2	14	14	14	14	2

Figure 2.2: Image on the left shows look up table before applying smoothing kernel. Image on the right is after application of kernel.

on the whole range of selected rotations and translations. The transformations with best score are used in the second round. From every good transformation is generated search space voxel. Origin of voxel is taken from transformation. Size of voxel is cell size from coarse table. Search voxels are evaluated on look up table with fine resolution. Search space is this time limited to search voxel and initial transformation is taken from origin of voxel. The best result is our solution. By this process computation time drops rapidly as show in work of [Ols09b].

3. NDT graph-SLAM overview

In this chapter we will present our solution to create 2D varian of graph based SLAM on NDT maps. This chapter starts with complete overview of algorithm. In next sections we explain how we have designed each part of the system.

3.1 System composition

Standard input of many SLAM algorithms is odometry. In our case we do not require any prior information about robot movements. Robot position estimation is done by fast incremental scan matching. The only mandatory input is a point cloud extracted from robot's measurement. Scan matcher calculates relative transformation based on received point cloud and incremental scan matcher's map. We will refer to this map as to the moving window. It is created by merging multiple old point clouds. More details will be provided in section 3.2.

Resulting transformation is used in the NDT frame creation process. NDT frame is small map which is created out of couple consecutive scans. Precise transformation is used to correctly merge these scans into single frame. This mini map is than used as a measurement information in a node of pose graph. Creating small NDT frames solves problem measurements with small number of points. Imagine situation where robot is standing close to the corner of the room. In this scenario incoming point clouds hold only small number of points, because field of view is narrow. Similar problem arise if robot uses sensor with limited field of view e.g. Kinect. To solve it we need to integrate multiple scans to get better outline of the world. More information about world also helps to reduce chance of ambiguous loop detections 1.4 because larger frames have higher chance to include more unique features. Additionally, we also want to utilize advantages of NDT-OM occupancy update rule. It is able to detect dynamic objects by ray-tracing and update map accordingly. This detection is done by merging multiple scans and re-observing same cell multiple times. More information about design choices behind NDT frames are in section 3.3.

After NDT frame generation phase, algorithms creates representing node in pose graph. Each two nodes are connected by odometry edge. Original odometry received from scan matching process was used to create NDT frames. In our abstraction, odometry is represented by transformation between origins of consecutive frames. In the next step, pose graph generates possible loop closure edges. To do so we need to traverse a graph with use of Dijkstra projection and apply our radius based metric described in section 3.4.

The potential matches need to be robustly aligned. Solution to this problem is the most difficult. We need algorithm which is able to perform 10s of registration per second. At the same time it needs to reject matches which are not from the same part of the environment. In addition, some errors caused by local and global ambiguities 1.4 are very difficult to avoid. We propose solution to these problems by improving version of D2D-NDT. In this adaptation, we utilize robust initial pose estimation from Correlative scan registration 2.3.4 and for finer alignment D2D-NDT 2.3.2. Full description is provided in 3.5.

Generated loop closure edges needs to be validated against possible outliers.
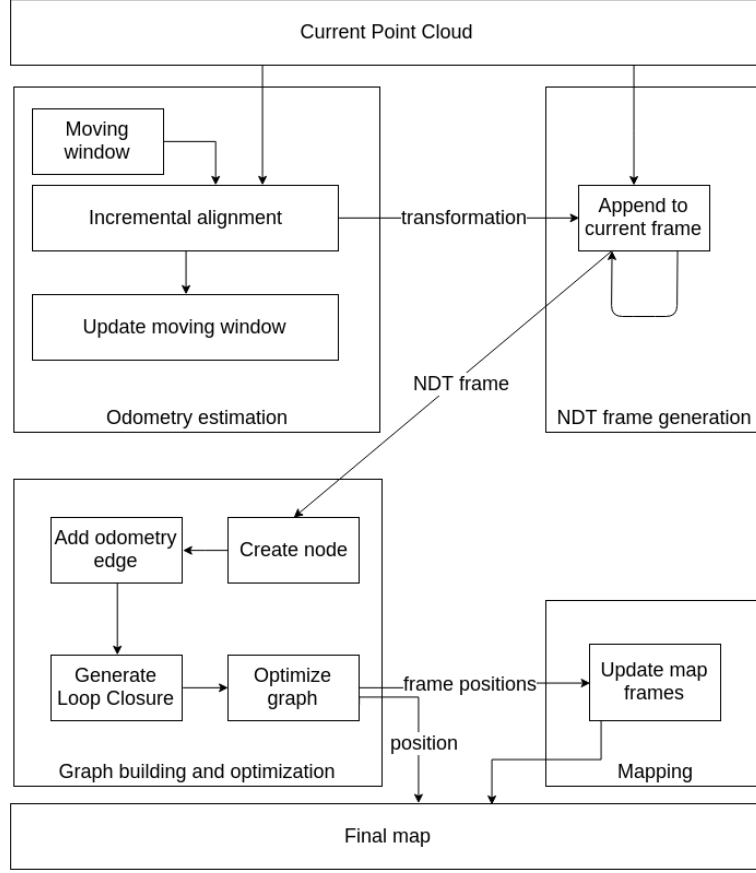
Figure 3.1: Diagram of graph based SLAM on NDT maps

In this matter we have decided to use robust optimization engine with switchable constrains. We have made decision based on comparative study by [SP13], where this method offered the best result in comparison to execution time. We need to minimize amount of time spent in optimization. Saved time can be used to validate more loop closure edges. Second important factor in optimization process is number of nodes and edges in graph. Computation time grows with increasing number of elements in the graph. We are limiting number of nodes by using NDT frames. Frames can be farther away from each other, because they accumulate multiple measurements.

Smaller number of nodes in graph also mean less work to NDT mapper. In case of successful loop closure we need to regenerate map based on new position of nodes in graph. In this version of algorithm we just simple iterate over all frames and merge them to the new map based on new origins. In the future NDT frames allow to only generate part of the map based on request from user. It could also be possible to dynamically load and save individual frames based on their need and save memory for long run of algorithm.

Combining these parts together creates whole graph base SLAM algorithm on NDT maps.

3.2 Moving window

Moving window is a special type of NDT grid. It uses all features of NDT-OM including occupancy update and dynamic object rejection. Main idea behind moving window is to offer small map which can be used by incremental scan-matcher in order to efficiently align incoming scans against longer history. In standard incremental scanmatching approaches we need to know whole map. Information from whole map is used to correct small errors when revisiting same place. A problem with this method arise when alignment fails. In this case wrongly aligned scan is merged into the map. This creates single environment feature multiple times in the map. This can be wrongly understood by next registration and error might be never corrected. NDT-OM can solve some of degeneration be cleaning occupied cells which are on the way between robot position and new measurement. In order for this mechanism to work next alignment scan needs to converge to original correct position. This is very unlikely with already corrupted mapmand standard NDT technics for registrations, which can end up in local optima during scan refinement step.

In our system, we do not need to know whole map of environment because loops closures errors are fixed by graph optimization. We need incremental scan-matcher to provide us good local estimate of robot movement. For this purpose we only need to know the part of environment occupied by current scan. It strongly depends on the type of sensor and environment. In our setup, robot operated in indoor environment with laser sensor ranging up to 20m in long corridors. In this scenario window size of 20m should incorporate all information which can help in scan registration. If it is possible to select smaller window size based on environment structure this adds to additional speed and memory efficiency.

The mowing window also needs to follow movement of the robot to incorporate new measurements. This can be done in two ways. First we might rotate window based on exact changes of robot global position. By doing this we need to transfer whole window after each small movement of robot. This approach tries to transform every single normal distribution inside grid in every step of algorithm. Transformed cell's distribution may suddenly overlap multiple fields. We would need to develop mechanism how to split original distributions into multiple cells. Better way is to keep windows orientation fixed and only translate window based on robot's movement. This prevents rotation of distributions in cells, but still suffer from same spiting problem. Solution to this problem is by moving window only in multiples of the grid. This does not affect parameters of normal distribution inside of original grid in order to move whole window. After movement some cells may get out of the scope of current window. These cells are destroyed. This also helps to reduce accumulated error in the window by deleting old corrupted measurement.

To minimize any alignment issues we decided to perform fast scan matching. This means process most of the data from laser. High frequency scan matching does not need initial guess because valid result is reasonably close to inital position of source and target measurements. Registration algorithm capable of this performance needs to work in order of milliseconds. Two algorithms developed for fine registration on top of NDT grid are P2D-NDT and D2D-NDT. We have decided to use standard D2D algorithm, because it offers ten times better run

time than P2D. Comparative study by [MVS$^+$15] shows that even though P2D is usually more precise it needs significantly more computation time. Skipping multiple measurements from sensor may cause that we will not be able to robustly estimate transformation and whole process can converge to local minimum.

Algorithm 3 Moving window processing loop

Require: point cloud X, move window's NDT grid M, transformation T_o to the origin of moving window, transformation T_r unused from move in last call of function, transformation P last known absolute pose of moving window.

1: **function** CALCULATETRANSFORM(X)
2: $\quad X_o \leftarrow$ transformPointCloud(X,$T_o * T_r$)
3: $\quad N_o \leftarrow$ createNDTGrid(X_o)
4: $\quad T_{ox} \leftarrow$ alignD2D(N_o,M)
5: $\quad M$.mergeIn(X_o,T_{ox}) ▷ applies transformation on point cloud and merge it into moving window
6: $\quad T_{diff} \leftarrow P^{-1} * (T_o * T_{ox})$
7: $\quad P \leftarrow T_o * T_{ox}$ $\qquad\qquad$ ▷ update of absolute pose of window for next call
8: $\quad T_r \leftarrow M$.moveWindow(T_{ox})
9: $\quad$ **return** T_{diff}
10: **end function**

---

add visualization of running window

3.3   NDT frame creation

NDT frame is created by merging multiple point clouds based on transformation received from odometry estimation. Important question is how many scans should we combine ? This algorithm uses consecutive addition of transformation as in equation 2.3. Afterwards, it calculates total displacement done by robot. If it is more than threshold we close down old NDT frame and start to add scans into new empty frame. A new frame is assigned its coordinate system based on current robot position. Every new scan is transformed into coordinate system of current open frame and merged in. Closed frame is sent to pose graph generation where it is transformed into graph's node.

Selection of good displacement value is important for run of whole algorithm. Small value will create many nodes in pose graph. Every node will reflect only small portion of environment. This will make loop closure computationally expensive by need to evaluate too many possible loop closure nodes. At the same time loop closing algorithm will work with only limited information. This may cause bigger number of local and global ambiguities in registration. A large value of displacement will generate fewer nodes with more information in each node. This is less computationally dependent. On the other hand it creates ambiguous environment inside of NDT frame. Loop closure registration may not correctly deduct which part of the same environment in the frame is correct for registering. This forces registration algorithm to correctly identify this situation and solve it. At the same, it wastes optimizer potential for rejection of ambiguous alignments based on topological information of whole environment.

3.4   Loop closure detection

Loop closure detection is done on top of pose graph. Loop detector can use current positions of pose graph's nodes and relative transformations stored in odometry and loop closure edges. With this information we need to find all nodes which can with current node create loop closure edge. The process starts by Dijkstra projection in section 2.1.2 from current node. During this process algorithm also calculates relative displacement along edges. Sum of displacements is used as parameter for rejection of nodes which are too close to our current position. These nodes are certainly overlapping with our start node and therefore it is not necessary to check them again. All the nodes passing previous test are used in one of two rejection models.

First model tests all nodes against selected radius. Second mechanism is using cumulative transformation and covariance calculated by Dijkstra projection. In validating if two nodes overlap we use same metric as presented by [Ols09a].

$$\Delta c = (c_b - c_a) \tag{3.1}$$

$$s = \max(0, \|\Delta c\| - r_a - r_b)\frac{\Delta c}{\|\Delta c\|} \tag{3.2}$$

$$mahl = s^T P_{a,b}^{-1} s \tag{3.3}$$

where c_a and c_b are centroids of start and currently compared NDT grids; r_a and r_b are radii of respective NDT grids and $P_{a,b}^{-1}$ is inverse of accumulated covariance.

Selected nodes are registered by robust D2D. Those matches with high score are inserted into the graph. Edges added by this mechanism may still include some errors or ambiguities. Rejection of these edges is done in optimizer.

3.5   Robust D2D-NDT registration

Construction of robust D2D registration needs to be fast and precise. In addition, it needs to have a mechanism how to reject invalid association. It also needs to use only information present in NDT grids because loop closure mechanism is working only with this data. We knew that D2D can offer quick a reliable registration on NDT grids with good initial guess. Correlative scan matching algorithm 2.3.4 can provide registration without knowledge of initial guess but in standard version is not possible to operate on top of NDT grids. The time performance of this algorithm is also slower than D2D. To solve these problems we have developed modified version of correlative algorithm which can work on top of NDT grids.

3.5.1   Adaptation of correlative registration

We have started with base algorithm described in section 2.3.4. For our needs it is sufficient when this algorithm provides only rough initial guess. For this reason we use only one layer architecture. Our single grid has cell size double of original size of NDT grid. One reason is faster execution time. In first part of algorithm we need to go over large search space. Mainly because we cannot expect any prior information from graph. Larger grid size limits number of translation because we always try translations in multiple of cell size as mentioned in 2.3.4.

Secondly, we need to transfer original NDT grid into reasonable point cloud. In our implementation we have decided to recreate point cloud out of grid by taking mean from every cell with distribution. Colection of these means makes our mean cloud. In addition, we use information about how many points were used to create normal distribution. This information is used in our algorithm as weight for every mean value. Original algorithm uses two point clouds.

First is called target cloud and is used for creation of look up table. This table is created by projecting all points to individual cells. When is cell occupied by at least one point it is marked with value 1. In our scenario we use cloud of means from target grid to construct look up table. Use of means is more robust to outliers than original look up table from point cloud. Original implementation marked occupied every cell regardless on number of points mapped into it. Our grids needs at least 4 points to create normal distribution. This is limiting influence of single point spread in space and also emphasizing dominant structures in environment. Target grid conversion to mean cloud does not loose any information in comparison to original cloud. This is because look up table and traget grid are aligned. On top of that double step size of look up table makes four cells from target NDT contribute to single look up cell.

Second source cloud is used for scoring on top of look up table. Every point of point-cloud contributes to total score based on value from look up cell it belongs to. In our case single point represents information about mean center of multiple points. In order to keep all information, algorithm maps mean into correct cell in look up table. By doing this mean only contributed once. Fortunately a score

generated by mean can be scaled with use of weight associated with mean. This makes weighted mean point contribute same amount to system as standard points from point cloud. Score function is defined as:

$$score(T, C) = \frac{1}{d} \sum_{p \in C} v(T, p) w(p) \qquad (3.4)$$

where T is transformation which should be applied to point p of cloud C. A function $v(T, p)$ applies transformation T to point p maps it to look up table and return score value for single point. A function $w(p)$ return weight of current mean point. Scaling factor d is defined as

$$d = m \sum_{p \in C_t} w(p) \qquad (3.5)$$

where m is the maximal value one point can receive from look up table after application of smoothing kernel in equation 2.21; C_t represents target point cloud.

Last problem with conversion of source cloud to mean cloud is to handle discretization errors. These errors happen when we need to transform NDT grid. In this situation one original PDF may overlap multiple cells. A original point cloud would contribute into multiple cells. Our mean formulation would contribute only to one cell based on mean location. To minimize this effect, we map every mean value into the taget look up table which has double cell size in comparison with source NDT. This process is similar to multi layer discretization removal in multi layer NDT registration [UT11]. Target look up table also include smoothing kernel, which assign some value to cells surrounding occupied cell in table. This also makes mean which could potentially slip out of occupied cell's boundaries contribute into the total score.

By executing these approximations, we were able to create version of correlative estimate on top of NDT grids. Coarser resolution improved performance and allowed us search larger search space. Approximation of input cloud into means reduced number of point we need to test in every iteration of algorithm loop. This effectively lowered number of look up table calls, which speeds up whole process. In addition, mean cloud removes outliers from points spread in space.

3.5.2 Algorithm overview

With coarse initial guess estimate we can constrict whole algorithm. First step is to run on pair of grids correlative estimation algorithm. This offers us the best initial guess it could find in selected search space. In this step we have used coarse look up table. This means that we are still possible almost two NDT cell away from right solution. To get right alignment we run D2D algorithm. Multi layer definition of D2D can converge to right solution if there is one. Problem arise if two matched grids are from diffrent locations and do not share same environment features e.g lines, corners. In this case correlation registration finds the best possible solution, which means that it rotates grid in a way that maximalize score. D2D than tryist to find best alignment and usually falss to first local minimum it can find. To solve these situations we propose solution validation process. Example of bad alignment is in figure 3.2.

3.5.3 Solution validation

Robust alignment offers us the best transformation between source and target NDT grid. This alignment can fail and do not offer successful registration at all. We need to validate if this registration succeeded or failed. In this algorithm we again use correlative scan matcher. In this case we use cell size of target look up table matching cell size of NDT target grid. We map every point from mean source cloud into look up table and receive total score based on contributions of each weighted mean point. In this case discretization is helping us provide better results. In case that some means stay out of target grid it means that registration was less successful which result in lower score. This method is able to reject scans based on their overlap. This method is not able to distinguish wrong alignment in case that two scans look similar but originate in two different parts of environment.

Algorithm 4 Robust D2D registration algorithm

Require: source NDT grid G_s and target NDT grid G_t. Resolution of NDT grids r. Validation threshold v

1: **function** ALIGN(G_s, G_t, r)
2:     transformation T is identity
3:     (T,$score$) $\leftarrow$ correlativeEstimater(G_s, G_t,T, $2 * r$)
4:     $T \leftarrow$ alignD2D(G_s, G_t,T)
5:     (T,$score$) $\leftarrow$ correlativeEstimater(G_s, G_t,T, r)
6:     **if** $score \geq v$ **then**
7:         **return** (T,$true$)
8:     **else**
9:         **return** (T,$false$)
10:    **end if**
11:    **return** T
12: **end function**
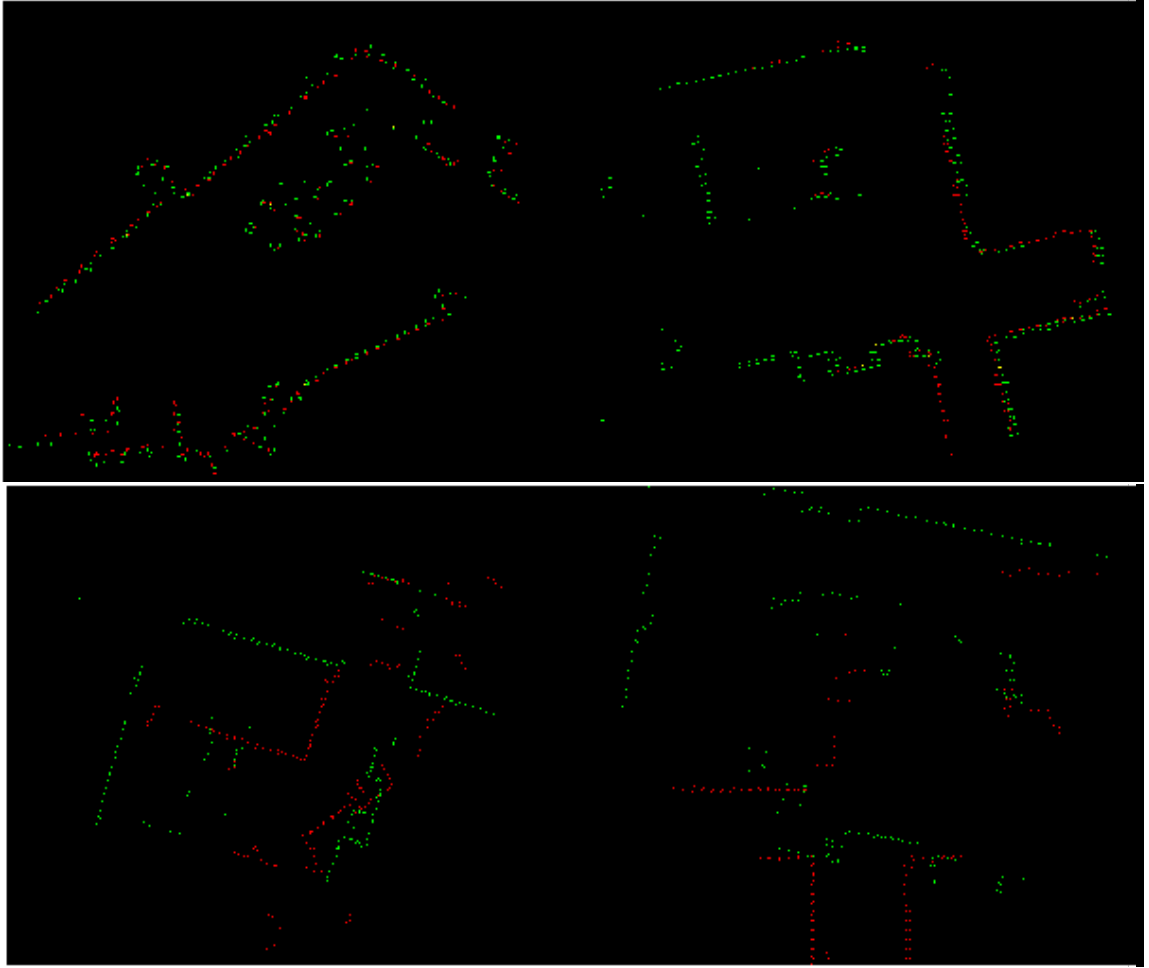
Figure 3.2: Images with alignment. Red dost represent target scan and green dots source scan. The first row shows valid alignment marked with high score. Second row shows two alignments which were rejected by validation.

4. Implementation and API

4.1 Used libraries

4.2 NDTGrid2D

4.2.1 VoxelGrid

4.3 Registration algorithms

4.4 NDTCell

4.5 Algorithm API

4.6 Graph SLAM API

4.7 ROS API

5. Comparison to SLAM implementation in ROS

In this chapter we will demonstrate functionality of our algorithm. We compare it with two well known SLAM approaches implemented in ROS. We also explain what parameters are needed to fully use potential of this algorithm. Whole experiment is conducted by running prerecorded data files from PR2 robot operating in Massachusetts Institute of Technology (MIT) Sata Center [FJKL13]. We have selected this dataset because laser scanner provides sufficient number of points to produce NDT fields with normal distribution. It is also recorded in form of "bag file" which is standard format in ROS. It is also very challenging dataset where at least some algorithms are failing.

5.1   MIT dataset details

This dataset offers fine laser data with 1130 points per scan. The sensor's field of view is 260 degrees. The 2D laser scans have maximum range of 60 m with publishing frequency around 20 Hz. The dataset was recorded on multiple floors of the Sata Center. This means that robot enters an elevator and is transported to different floors. Therefore, we have selected only data sets which stay on the same floor. Our experiments were conducted on the second floor with bags recorded from different robot's path.

We have selected two datasets which we think showcase well possibilities of this algorithm. First dataset runs in small loop inside of one room. This is challenging because robot needs to correct its position multiple time. It is also computationally difficult for loop closure mechanism. In every iteration it needs to compare its position with all previous measured data. Iterative movement at the same place can also demonstrate robustness of incremental scan matcher again any shift caused by registration error.

Second dataset starts in the long corridor and moves in direction towards room from the first selected dataset. It again do multiple loops and then it moves through corridor to new room. It maps this room and returns through the same corridor. In this type of setup odometry information or incremental scan matching cam accumulate error over long corridor and last room, which should be visible on the returning trip. This tests loop closure mechanism over long distance.

In the figure 5.1 is a map of used datasets built with NDT-OM with transformation between scan originating in ground truth measurements provided with dataset.
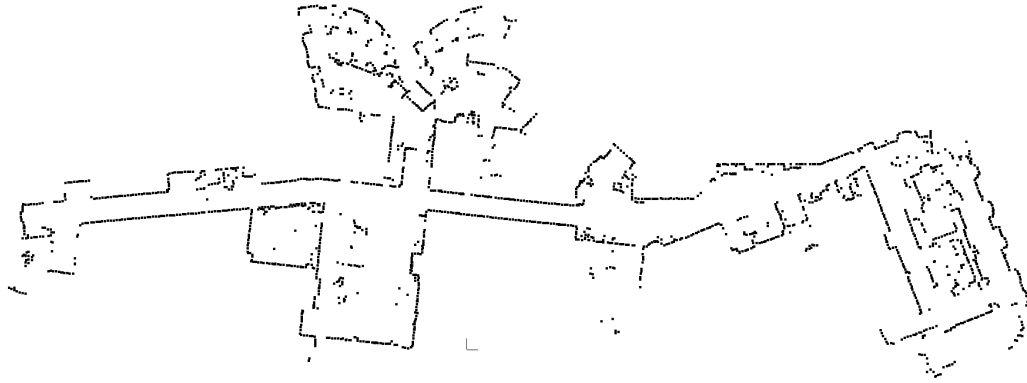
Figure 5.1: The NDT map generated out of selected datasets with use of ground truth odometry information.

5.2 ROS SLAM algorithm overview

5.2.1 Gmapping

5.2.2 Hector

5.3 NDT-GraphSLAM

In all our experiments we have used our SLAM algorithms as was described in section 3.1. We have decided to set moving window size to max range of the sensor which is 60 m in our dataset. We have also set fixed values for radius search for loop detection to 20m. We selected this value so we can test as many loop closures as possible. During our mapping and localization test we also record all loop closure measurements. These are saved to the disk as point cloud file (.pcd). We also save results of loop closure registration with resulting score for evaluation of loop closure algorithm based on changing parameters. Files from experiments are available in attachments of this work. Initial value for loop closure registration threshold was set to 0.6. Every loop registration with score higher than this value will be inserted into the graph as loop closure edge.

5.3.1 NDT frame generation frequency

In this experiment we wanted to test what is optimal euclidean distance between two consecutive NDT frames. We use same representation of frames as mentioned in section 3.3. Based on design of the system this parameter should influence quality loop closure detection and evaluation. In order to test this parameter we have decided to test it on second dataset with distances 1m 2m and 4 meters.

One meter range has generated frame every 1 meter of robot's trajectory. This has created high amount of nodes with small map representation of environment inside. For mapping purposes this created nice map because there was small odometry error inside of frame. Error may be caused by wrong odometry estimate from moving window. This can be observed in the first picture of figure 5.2. Its also important to note that it has generated the biggest amount of loop
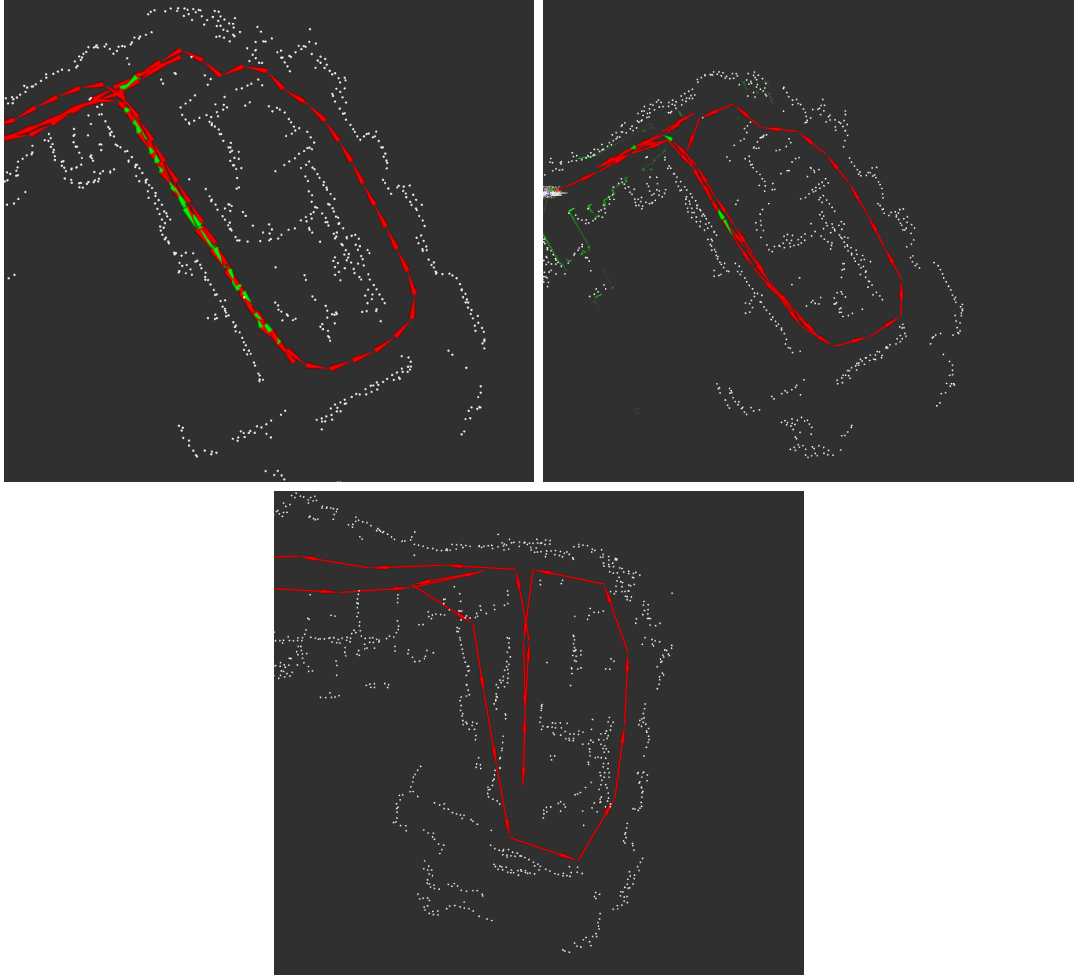
Figure 5.2: Comparison of effect of different frequency of frame creation. From left pictures of 1m, 2m and 4 meter distance between frames. Red arrows represent odometry edges, green edges are loop closure edges, white dost represent final map representation in form of point cloud of means

closure edges. This mainly thanks to fact that it is easier for two frames get high overlapping score from robust D2D if they have no errors inside. On the other hand it is more probable that these scans will have problems with ambiguities. This has happened in total 4 times in the second dataset with registration threshold set to 0.6.

The second variant with two meters long distance between frames offered optimal results. It has not generated fewer nodes than the first variant. Loop closure edges added to graph were able to repair errors from odometry estimation and still keep decent readability of map.

The third variant failed to find loop closures. Every frame had data with heavy noise inside. This caused that non of the loop closing tests received score more than 0.1.

ased on these results we have decided to use fixed distance of 2 meters between two frames in the next tests.

	correct	error	total
[0.7,1]	21	0	21
[0.6, 0.7)	33	1	34
[0.5, 0.6)]	18	26	44
[0.4, 0.5)]	13	28	31

Figure 5.3: Number of correct and incorrect registrations in score groups

5.3.2 Robust D2D score threshold

In a previous section we have use fixed registration threshold to value 0.6. In this section we will test if this is really optimal value. This test is executed by first setting threshold to value 0.6. Then running whole dataset. All measurement data received from all loop closure registration are sorted based on score value into groups. The first group has score range from 0.4 to 0.49. The second group from 0.5 to 0.59. The third group starts at 0.6 and ends in 0.69. Last group include all loop closures with higher value. We will look at number of edges in each category which are false positive. False positive edges are usually created on failure of algorithm to register correctly frames. The other reason might be ambiguity in the environment. We want to minimize number of incorrect edges in our graph. Result of this experiment is in 5.3.

Based on result we can conclude that algorithm is able to securely identify valid loop closure on this dataset if score is above 0.6. One error in this category was caused by ambiguity in long corridor. This error is not possible to correct by usual registration algorithms. Other two categories equally include more errors than correct results. Errors can be divided into two types. Some incorrect registrations are caused by matching unrelated places. These places are different but it is possible to match them in a way which yields good score. Score assigned by matcher is usually lower than 0.55. Some errors are also registration failures. In this type of error mostly depends on the structure ambiguity inside of the frame. This happens if two frames include same area but each has dominant number of cells mapping different feature of environment. This ambiguity makes robust estimator connect these two parts. This increases score in these likely part to higher levels. On the other hand parts of the frame not matching each other lower the score.

This experiment also confirmed that score setup for our algorithm strongly depends on character of size of NDT frames. It also proven that if we take loop closures with high score value we can construct graph with limited number of registration errors and ambiguities.

5.3.3 Iterative mapping of room

This dataset represents single. Room in order to fully map this robot multiple time moved around the room. Every movement had some error. This well demonstrates coordination of moving window with loop closure mechanism. Whole room has fitted inside the moving window and registration provided robust transformation for NDT frame building process. Loop closures were correctly identified all above threshold 0.6. Distance between frames is 2m as discussed previously. Map is compact and without any defects.
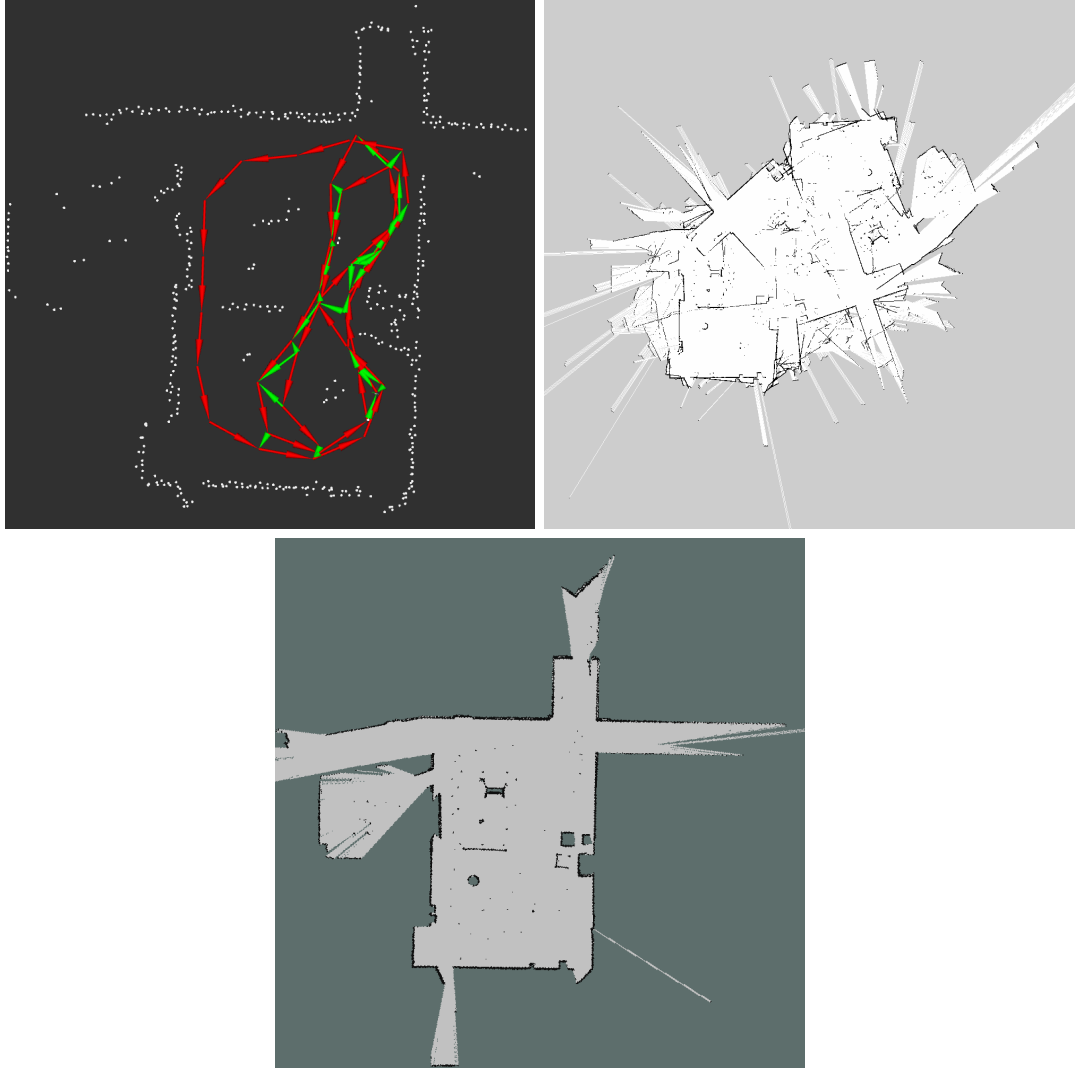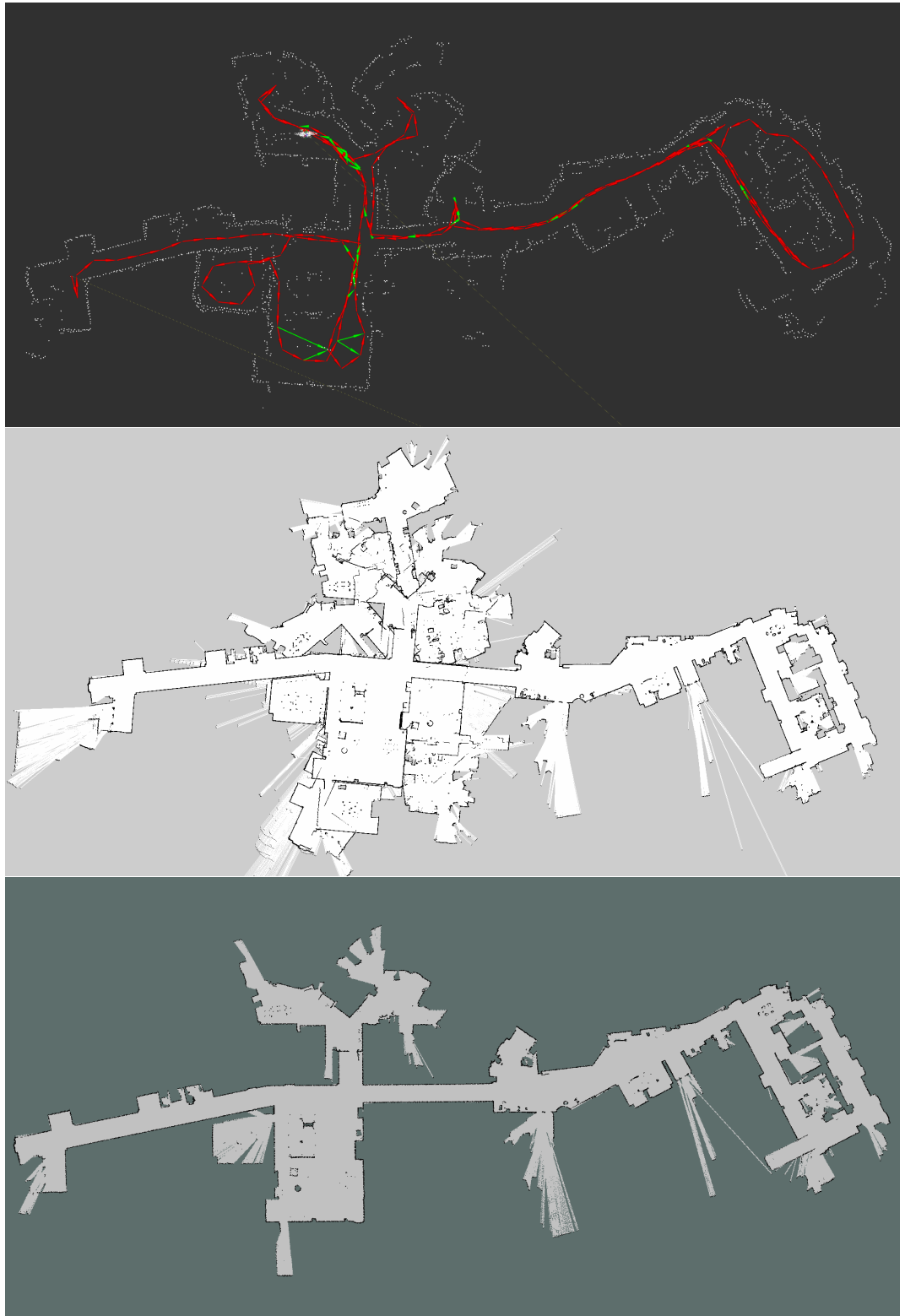
Figure 5.4: Map of the room mapped by our NDT aproach, hector mapper and gmapping. Visualization of our aproach includes visualization of pose graph with red odometric edges and green loop closure edges. White spots represent means of each cell's normal distribution.

Hector mapping has not converged into correct output. It was not able to cope with rotations of the robot in this dataset. We have also tested slowing down dataset with rate 0.6. This has not helped as well.

The gmapping offers solution with similar quality to our result.

5.3.4 Long corridors

Long corridor dataset was selected because it maps two main rooms plus it adds mapping of top part of the map. This part with its irregular shapes proven to be very difficult mostly for hector mapping. It has failed mapping process as you can see on the middle image in figure 5.5. The gmapping algorithm offered accurate result.

Our approach has recovered main shape of the map correctly. Small difference is in noisiness of the walls. Our algorithm has higher noise. Main reason is different mapping model. The gmapping and hector mapping are both using extremely fine map with resolution 0.05m. Our approach is using coarser 0.25m grid for visualization. Our map is coarser but still covers and represent free space correctly without noise. Coarser grid has also advantage in path planning or ray-tracing which is faster. Finer grids often needs to be converted into lower resolutions to work with them efficiently.

Second difference is length of the corridors. Our approach has shortened length of corridors. This happened because of data ambiguity. Robot passing through these corridors do not see the end of hall. This makes him observe only two straight walls on the right and on the left. Without prior information about robot movement, this is correctly understood as robot standing still without movement. The way our algorithm deals with this type of errors is by closing loop closure when returning on the same place through different path. In this case robot used same trajectory, which lead to same error only in the opposite direction. The only other solution how to sove this problem is to integrate movement of robot into moving window incremental scan matching. Resulting cooridor than look like in figure 5.6.

Figure 5.5: Map of the corridors mapped by our NDT approach, hector mapper and gmapping. Visualization of our approach includes visualization of pose graph with red odometric edges and green loop closure edges. White spots represent means of each cell's normal distribution.
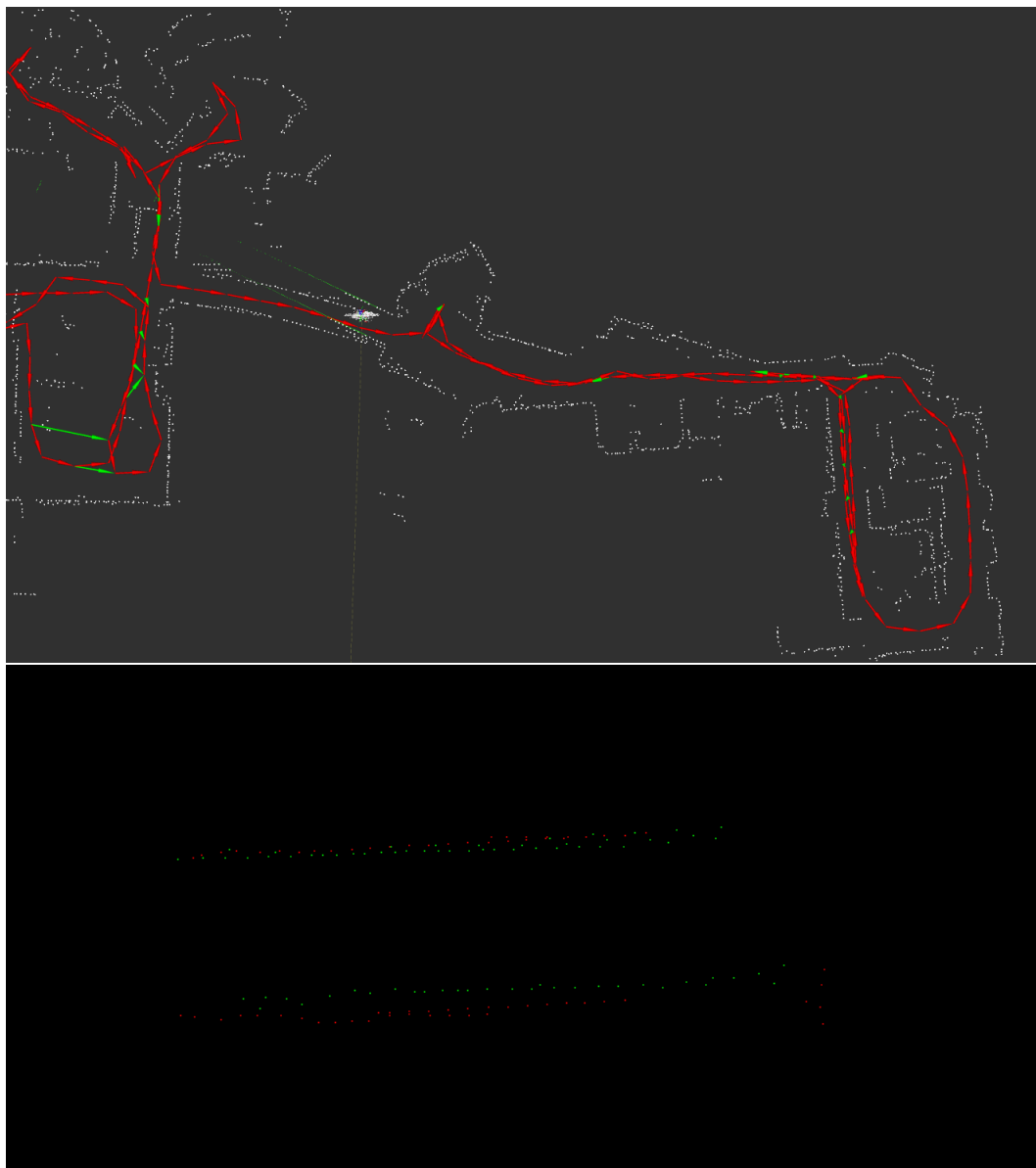
Figure 5.6: Top picture shows portion of map with corridor when incremental scan matcher may use initial guess from odometry. Bottom picture shows ambiguous registration in corridor area.

Conclusion

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List of Figures

List of Abbreviations

D2D Distribution to distribution. 15, 16, 19, 21, 24–26

EKF Extended Kallman Filter. 5

GPS Global positioning system. 3

ICP Iterative closest point. 5, 7, 9, 17

IMU Integrated Measurement Unit. 4, 9

KF Kalman filters. 5

NDT Normal distributions transform. 3, 6–9, 12–16, 19–26

NDT-OM NDT-Occupancy mapping. 6–8, 13, 19, 21

P2D point to distribution. 16, 21, 22

PDF probability distribution function. 14, 15, 25

PF Particle filters. 5

RCU Recursive update for covariance. 12, 14, 33

ROS Robot operating system. 3, 8

SLAM Simultaneous localization and mapping. 3–10, 16, 19, 20

Attachments