# Lab 4: Intro to Machine Learning

Practice session covering topics discussed in Lecture 4

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#### **GOAL OF TODAY'S PRACTICE SESSION**

- Revisit PCA algorithm explored via MetaboAnalyst, to learn how we can compute it with R
- Understand some key elements of statistical Power Analysis
- Introduce how ML approaches deal with available data

The examples and datasets in this Lab session follow very closely two sources:

- 1. The tutorial on "Principal Component Analysis (PCA) in R" by: Statistics Globe
- 2. The materials in support of the "Core Statistics using R" course by: Martin van Rongen

#### **Topics discussed in Lecture #4**

#### **Lecture 4: topics**

- Introduction to MetaboAnalyst software
  - A useful R-based resources for metabolomics
- Elements of statistical Power Analysis

# RENVIRONMENT SET UP & DATA

#### **Needed R Packages**

- We will use functions from packages base, utils, and stats (pre-installed and pre-loaded)
- We may also use the packages below (specifying package::function for clarity).

```
4 library(here)
 5 library(dplyr)
6 library(skimr)
7 library(magrittr) # A Forward-Pipe Operator for R
8 library(readr)
11 library(ggplot2)
12 library(ggfortify) # Data Visualization Tools for Statistical Analysis Results
13 library(scatterplot3d) # 3D Scatter Plot
16 library(MASS)
17 library(factoextra) # Extract and Visualize the Results of Multivariate Data Analyses
18 library(FactoMineR) # Multivariate Exploratory Data Analysis and Data Mining
19 library(rstatix)
22 library(rsample)
23 library(broom)
```

### DATASETS for today

In this tutorial, we will use:

- the biopsy data attached to the MASS package.
- a few clean datasets used in the "Core Statistics using R" course by: Martin van Rongen

#### **Dataset on Breast Cancer Biopsy**

Name: Biopsy Data on Breast Cancer Patients

**Documentation**: See reference on the data downloaded and conditioned for R here https://cran.r-project.org/web/packages/MASS/MASS.pdf

**Sampling details**: This breast cancer database was obtained from the University of Wisconsin Hospitals, Madison from Dr. William H. Wolberg. He assessed biopsies of breast tumours for 699 patients up to 15 July 1992; each of nine attributes has been scored on a scale of 1 to 10, and the outcome is also known. The dataset contains the original Wisconsin breast cancer data with 699 observations on 11 variables.

#### Importing Dataset biopsy

The data can be interactively obtained form the MASS R package

```
1 # (after loading pckg)
2 # library(MASS)
3
4 # I can call
5 utils::data(biopsy)
```

#### biopsy variables with description

Variable	Туре	Description
ID	character	Sample ID
V1	integer 1 - 10	clump thickness
V2	integer 1 - 10	uniformity of cell size
V3	integer 1 - 10	uniformity of cell shape
V4	integer 1 - 10	marginal adhesion
V5	integer 1 - 10	single epithelial cell size
V6	integer 1 - 10	bare nuclei (16 values are missing)
V7	integer 1 - 10	bland chromatin
V8	integer 1 - 10	normal nucleoli
V9	integer 1 - 10	mitoses
class	factor	benign or malignant

#### biopsy variables exploration 1/2

The biopsy data contains 699 observations of 11 variables.

The dataset also contains a character variable: **ID**, and a factor variable: **class**, with two levels ("benign" and "malignant").

```
2 str(biopsy)
'data.frame':
             699 obs. of 11 variables:
            "1000025" "1002945" "1015425" "1016277" ...
$ ID
$ V1
       : int 5 5 3 6 4 8 1 2 2 4 ...
$ V2
       : int 1 4 1 8 1 10 1 1 1 2 ...
       : int 1 4 1 8 1 10 1 2 1 1 ...
$ V3
$ V4
       : int 1511381111...
$ V5
      : int 2 7 2 3 2 7 2 2 2 2 ...
$ V6
      : int 1 10 2 4 1 10 10 1 1 1 ...
$ V7
      : int 3 3 3 3 3 9 3 3 1 2 ...
$ V8
       : int 1 2 1 7 1 7 1 1 1 1 ...
$ V9
       : int 1 1 1 1 1 1 1 5 1 ...
$ class: Factor w/ 2 levels "benign", "malignant": 1 1 1 1 1 2 1 1 1 1 ...
```

#### biopsy variables exploration 2/2

There is also one incomplete variable V6

remember the package skimr for exploring a dataframe?

#### biopsy dataset manipulation

#### We will:

- exclude the non-numerical variables (ID and class) before conducting the PCA.
- exclude the individuals with missing values using the na.omit() or filter(complete.cases() functions.
- We can do both in 2 equivalent ways:

#### with base R (more compact)

```
1 # new (manipulated) dataset
2 data_biopsy <- na.omit(biopsy[,-c(1,1)])</pre>
```

#### with dplyr (more explicit)

```
1 # new (manipulated) dataset
2 data_biopsy <- biopsy %>%
3 # drop incomplete & non-integer cold
4 dplyr::select(-ID, -class) %>%
5 # drop incomplete observations (rows
6 dplyr::filter(complete.cases(.))
```

#### biopsy dataset manipulation

We obtained a new dataset with 9 variables and 683 observations (instead of the original 699).

```
1 # check reduced dataset
2 str(data_biopsy)
```

```
'data.frame': 683 obs. of 9 variables: $ V1: int 5 5 3 6 4 8 1 2 2 4 ...
$ V2: int 1 4 1 8 1 10 1 1 1 2 ...
$ V3: int 1 4 1 8 1 10 1 2 1 1 ...
$ V4: int 1 5 1 1 3 8 1 1 1 1 ...
$ V5: int 2 7 2 3 2 7 2 2 2 2 ...
$ V6: int 1 10 2 4 1 10 10 1 1 1 ...
$ V7: int 3 3 3 3 3 9 3 3 1 2 ...
$ V8: int 1 2 1 7 1 7 1 1 1 1 ...
$ V9: int 1 1 1 1 1 1 1 5 1 ...
```

# PCA: EXAMPLE of UNSUPERVISED ML ALGORITHM

Reducing high-dimensional data to a lower number of variables

#### **Calculate Principal Components**

The first step of PCA is to calculate the principal components. To accomplish this, we use the prcomp() function from the stats package.

 With argument "scale = TRUE" each variable in the biopsy data is scaled to have a mean of 0 and a standard deviation of 1 before calculating the principal components (just like option Autoscaling in MetaboAnalyst)

#### **Analyze Principal Components**

Let's check out the elements of our obtained biopsy\_pca object

• (All accessible via the \$ operator)

```
1 names(biopsy_pca)
[1] "sdev" "rotation" "center" "scale" "x"
```

"sdev" = the standard deviation of the principal components

"sdev"^2 = the variance of the principal components (eigenvalues of the covariance/correlation matrix)

"rotation" = the matrix of variable loadings (i.e., a matrix whose columns contain the eigenvectors).

"center" and "scale" = the means and standard deviations of the original variables before the transformation;

"x" = the principal component scores (after PCA the observations are expressed in principal component scores)

#### **Analyze Principal Components (cont.)**

We can see the summary of the analysis using the summary () function

- 1. The first row gives the **Standard deviation** of each component, which can also be retrieved via biopsy\_pca\$sdev.
- 2. The second row shows the **Proportion of Variance**, i.e. the percentage of explained variance.

```
1 summary(biopsy pca)
Importance of components:
                                  PC2
                          PC1
                                          PC3
                                                   PC4
                                                           PC5
                                                                   PC6
                                                                           PC7
Standard deviation
                       2.4289 0.88088 0.73434 0.67796 0.61667 0.54943 0.54259
Proportion of Variance 0.6555 0.08622 0.05992 0.05107 0.04225 0.03354 0.03271
Cumulative Proportion 0.6555 0.74172 0.80163 0.85270 0.89496 0.92850 0.96121
                           PC8
                                   PC9
Standard deviation
                       0.51062 0.29729
Proportion of Variance 0.02897 0.00982
Cumulative Proportion 0.99018 1.00000
```

#### **Proportion of Variance for components**

2. The row with **Proportion of Variance** can be either accessed from summary or calculated as follows:

```
1 # a) Extracting Proportion of Variance from summary
2 summary(biopsy_pca)$importance[2,]

PC1   PC2   PC3   PC4   PC5   PC6   PC7   PC8   PC9
0.65550 0.08622 0.05992 0.05107 0.04225 0.03354 0.03271 0.02897 0.00982

1 # b) (same thing)
2 round(biopsy_pca$sdev^2 / sum(biopsy_pca$sdev^2), digits = 5)

[1] 0.65550 0.08622 0.05992 0.05107 0.04225 0.03354 0.03271 0.02897 0.00982
```

The output suggests the **1st principal component** explains around 65% of the total variance, the **2nd principal component** explains about 9% of the variance, and this goes on with diminishing proportion for each component.

#### **Cumulative Proportion of variance for components**

3. The last row from the summary (biopsy\_pca), shows the Cumulative Proportion of variance, which calculates the cumulative sum of the Proportion of Variance.

```
1 # Extracting Cumulative Proportion from summary
2 summary(biopsy_pca)$importance[3,]

PC1 PC2 PC3 PC4 PC5 PC6 PC7 PC8 PC9
0.65550 0.74172 0.80163 0.85270 0.89496 0.92850 0.96121 0.99018 1.00000
```

Once you computed the PCA in R you must decide the number of components to retain based on the obtained results.

# VISUALIZING PCA OUTPUTS

#### Scree plot

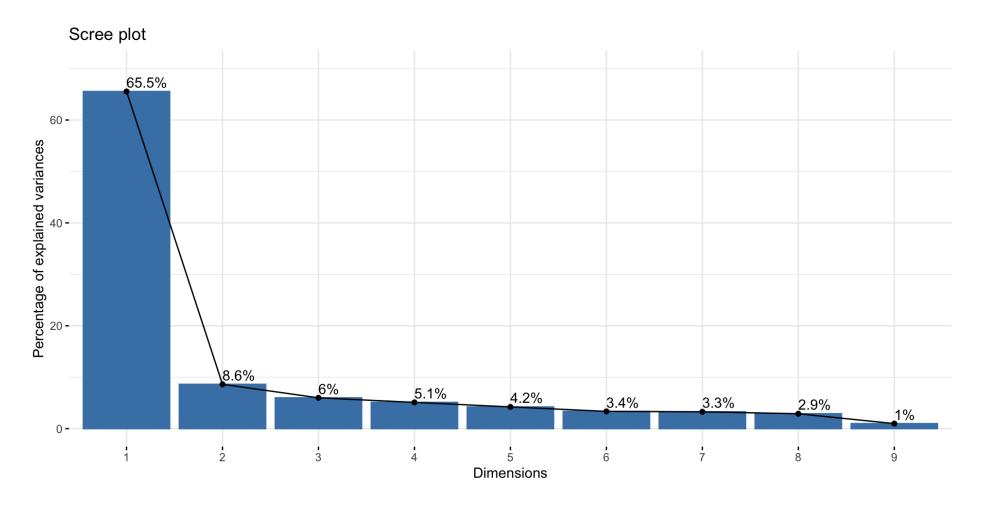
There are several ways to decide on the number of components to retain.

- One helpful option is visualizing the percentage of explained variance per principal component via a scree plot.
  - Plotting with the fviz\_eig() function from the factoextra package

Visualization is essential in the interpretation of PCA results. Based on the number of retained principal components, which is usually the first few, the observations expressed in component scores can be plotted in several ways.

#### **Scree plot**

The obtained **scree plot** simply visualizes the output of **summary(biopsy\_pca)**.



#### **Principal Component Scores**

After a PCA, the observations are expressed as **principal component scores**.

- 1. We can retrieve the principal component scores for each Variable by calling biopsy\_pca\$x, and store them in a new dataframe PC\_scores.
- 2. Next we draw a scatterplot of the observations expressed in terms of principal components

```
1 # Create new object with PC_scores
2 PC_scores <- as.data.frame(biopsy_pca$x)
3 head(PC_scores)</pre>
```

It is also important to visualize the observations along the new axes (principal components) to interpret the relations in the dataset:

#### **Principal Component Scores**

```
PC1
                       PC2
                                      PC3
                                                    PC4
                                                                   PC5
                                                                                 PC6
1 \quad 1.469095 \quad -0.10419679 \quad 0.56527102 \quad -0.03193593 \quad 0.15088743 \quad -0.05997679
2 - 1.440990 - 0.56972390 - 0.23642767 - 0.47779958 - 1.64188188 0.48268150
3 \quad 1.591311 \quad -0.07606412 \quad -0.04882192 \quad -0.09232038 \quad 0.05969539 \quad 0.27916615
4 - 1.478728 - 0.52806481 0.60260642 1.40979365 0.56032669 - 0.06298211
5 \quad 1.343877 \quad -0.09065261 \quad -0.02997533 \quad -0.33803588 \quad 0.10874960 \quad -0.43105416
6 -5.010654 -1.53379305 -0.46067165 0.29517264 -0.39155544 -0.11527442
          PC7
                       PC8
                                       PC9
1 - 0.3491471 0.4200360 0.005687222
2 1.1150819 0.3792992 -0.023409926
3 - 0.2325697 \quad 0.2096465 \quad -0.013361828
4 0.2109599 -1.6059184 -0.182642900
5 - 0.2596714 \quad 0.4463277 \quad 0.038791241
6 - 0.3842529 - 0.1489917 0.042953075
```

## Principal Component Scores plot (adding label variable)

- 3. When data includes a factor variable, like in our case, it may be interesting to show the grouping on the plot as well.
- In such cases, the label variable class can be added to the PC set as follows.

```
1 # retrieve class variable
2 biopsy_no_na <- na.omit(biopsy)
3 # adding class grouping variable to PC_scores
4 PC_scores$Label <- biopsy_no_na$class</pre>
```

The visualization of the observation points (point cloud) could be in 2D or 3D.

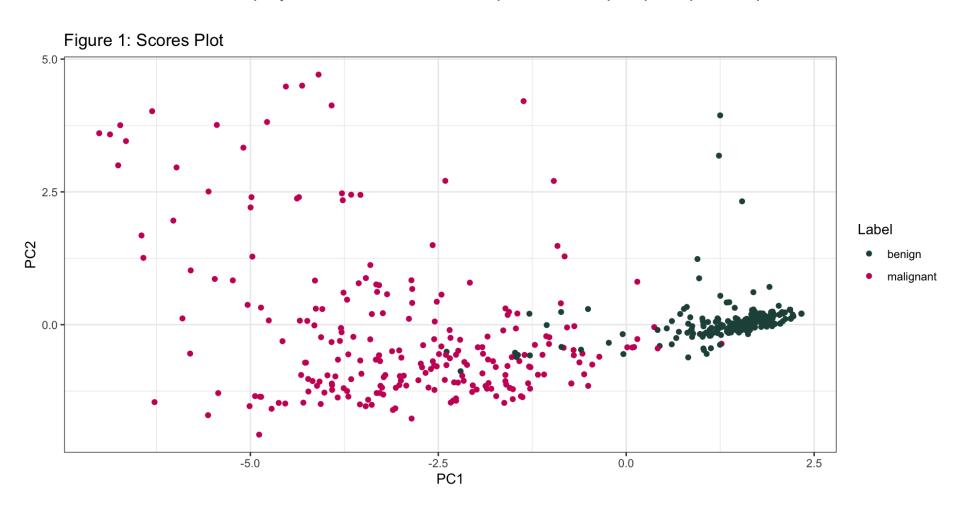
#### Principal Component Scores plot (2D)

The Scores Plot can be visualized via the ggplot2 package.

- grouping is indicated by argument the color = Label;
- geom\_point() is used for the point cloud.

#### Principal Component Scores plot (2D)

Figure 1 shows the observations projected into the new data space made up of principal components



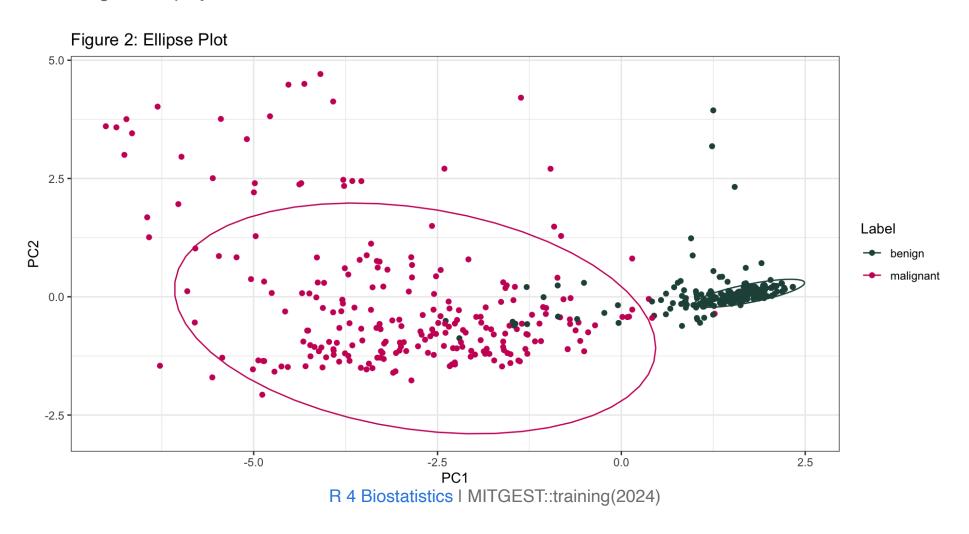
## Principal Component Scores (2D Ellipse Plot)

Confidence ellipses can also be added to a grouped scatter plot visualized after a PCA. We use the ggplot2 package.

- grouping is indicated by argument the color = Label;
- geom\_point() is used for the point cloud;
- the stat\_ellipse() function is called to add the ellipses per biopsy group.

## Principal Component Scores (2D Ellipse Plot)

Figure 2 shows the observations projected into the new data space made up of principal components, with 95% confidence regions displayed.



#### Principal Component Scores plot (3D)

A 3D scatterplot of observations shows the first **3 principal components' scores**.

- For this one, we need the scatterplot3d() function of the scatterplot3d package;
- The color argument assigned to the Label variable;
- To add a legend, we use the legend() function and specify its coordinates via the xyz.convert() function.

```
plot 3d <- with (PC scores,
                    scatterplot3d::scatterplot3d(PC scores$PC1,
                                                  PC scores$PC2,
                                                  PC scores$PC3,
                                                  color = as.numeric(Label),
                                                  pch = 19,
                                                  main = "Figure 3: 3D Scatter Plot",
                                                  xlab="PC1",
                                                  ylab="PC2",
                                                  zlab="PC3"))
14 legend(plot 3d$xyz.convert(0.5, 0.7, 0.5),
          pch = 19,
          yjust=-0.6,
          xiust=-0.9,
          legend = levels(PC scores$Label),
          col = seq along(levels(PC scores$Label)))
```

#### Principal Component Scores plot (3D)

Figure 3 shows the observations projected into the new 3D data space made up of principal components.

PC1

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Figure 3: 3D Scatter Plot

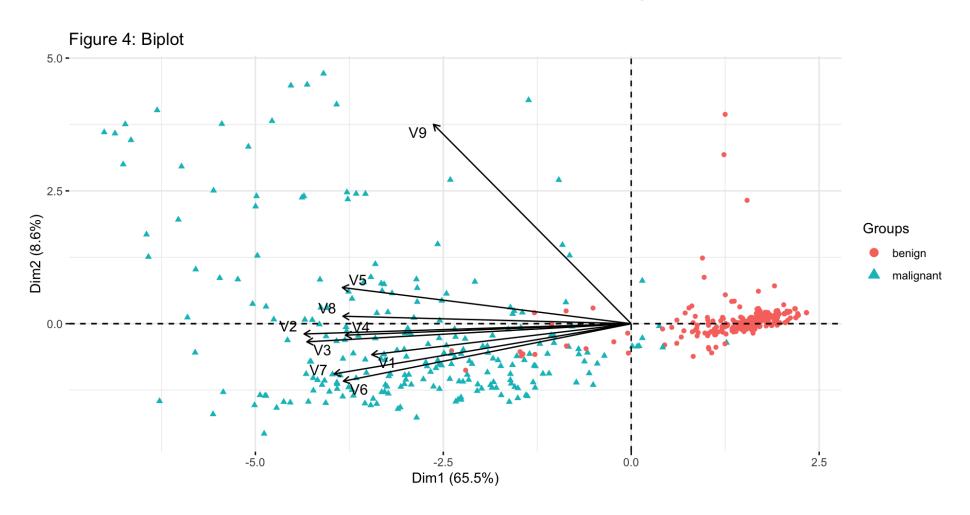
#### Biplot: principal components v. original variables

Next, we create another special type of scatterplot (a **biplot**) to understand the relationship between the principal components and the original variables. In the **biplot** each of the observations is projected onto a scatterplot that uses the *first and second principal components as the axes*.

- For this plot, we use the fviz\_pca\_biplot() function from the factoextra package
  - We will specify the color for the variables, or rather, for the "loading vectors"
  - The habillage argument allows to highlight with color the grouping by class

#### Biplot: principal components v. original variables

The axes show the principal component scores, and the vectors are the loading vectors



#### Interpreting biplot output

Biplots have two key elements: **scores** (the 2 axes) and **loadings** (the vectors). As in the scores plot, each point represents an observation projected in the space of principal components where:

- Biopsies of the same class are located closer to each other, which indicates that they
  have similar scores referred to the 2 main principal components;
- The **loading vectors** show strength and direction of association of original variables with new PC variables.

As expected from PCA, the single PC1 accounts for variance in almost all original variables, while V9 has the major projection along PC2.

#### Interpreting biplot output (cont.)

```
1 scores <- biopsy_pca$x
2
3 loadings <- biopsy_pca$rotation
4 # excerpt of first 2 components
5 loadings[ ,1:2]

PC1 PC2
V1 -0.3020626 -0.14080053
V2 -0.3807930 -0.04664031
V3 -0.3775825 -0.08242247
V4 -0.3327236 -0.05209438</pre>
```

#### **POWER ANALYSIS**

In this section, we will use:

- the NHANES clinical data, we already analysed in Lab # 3
- a few, tidy "fish-related" datasets @ 🎉 🤏 📞 📚 that we will load on the go
  - Source: the materials of the "Core Statistics using R" by: Martin van Rongen

# Sample Size determination in Inferential statistics

"OK, so how big of a sample do I need?"

...the 1,000,000 \$ question"!

### Purpose and challenges of Power Analysis

- Power analysis helps with the key question **How many observations/subjects do I need for my experiment?** (= n)
  - Too small of a sample size can under detect the effect of interest in your experiment
  - **Too large** of a sample size may lead to unnecessary wasting of resources
  - We strive to have just the sufficient number of observations needed to have a good chance of detecting the effect researched. (Even more so in a very time-consuming or expensive experiment.)
- When should we do power analysis?
  - (Ideally), before the experiment: a priori power analysis allows to determine the necessary sample size n of a test, given a desired  $\alpha$  level, a desired power level  $(1 \beta)$ , and the size of the effect to be detected (a measure of difference between  $H_0$  and  $H_1$ )
  - In reality, sometimes you can only do post-hoc power analysis after the experiment, so the sample size n is already given.
    - $\circ$  In this case, given n,  $\alpha$ , and a specified effect size, the analysis will return the power (  $1-\beta$ ) of the test, or  $\beta$  (i.e. the probability of Type II error = incorrectly retaining  $H_o$ ).

### Required inputs to define the sample size n

- $\bullet$  A specified **effect size** (i.e. the minimum deviation from  $H_o$  that you hope to detect for a meaningful result)
  - The larger the effect size, the easier it is to detect an effect and require fewer obs
- As standarddeviation gets bigger, it is harder to detect a significant difference, so you'll need a bigger sample size.
- α is the significance level of the test (i.e. the probability of incorrectly rejecting the null hypothesis (a false positive).
  - Understanding if the test is one-tailed (difference has a direction) or two-tailed
- $\beta$  is the probability of accepting the null hypothesis, even though it is false (a false negative), when the real difference is equal to the minimum effect size.
  - $1 \beta$  is the **power of a test** is the probability of correctly rejecting the null hypothesis (getting a significant result) when the real difference is equal to the minimum effect size.
    - a power of 80% (equivalent to a beta of 20%) is probably the most common, while some people use 50% or 90%

# Specifying effect size

So (since  $\alpha$  and  $1-\beta$  are normally set) the key piece of information we need is the **effect size**, which is essentially a function of the difference between the means of the null and alternative hypotheses over the variation (standard deviation) in the data.

The tricky part is that effect size is related to biological/practical significance rather than statistical significance

How should you estimate a meaningful Effect Size?

- · Use preliminary information in the form of pilot study
- Use background information in the form of similar studies in the literature
- (With no prior information), make an estimated guess on the effect size expected (see guidelines next)

Most R functions for sample size only allow you to enter effect size as input

# Specifying effect size: general guidelines

As a general indicative reference, below are the "Cohen's Standard Effect Sizes" (from statistician Jacob Cohen who came up with a rough set of numerical measures for "small", "medium" and "large" effect sizes that are still in use today)

Test	Effect Size	Small	Medium	Large
<ul> <li>All t-tests:</li> <li>one-sample t-test</li> <li>independent samples t-test</li> <li>paired samples t-test</li> </ul>	Cohen's d	0.20	0.50	0.80
Difference between many means (ANOVA)	Cohen's f	0.10	0.25	0.40
Chi-squared test	Cohen's w	0.10	0.30	0.50
Pearson's correlation coefficient	Pearson's p	0.10	0.30	0.50
Linear Regression (entire model)	Cohen's <b>f<sup>2</sup></b>	0.02	0.15	0.35

# The pwr package

The pwr package (develoed by Stéphane Champely), implements power analysis as outlined by Cohen (1988). The key arguments of the function pwr.t.test are 4 quantities, plus 2 for the test description:

- 1. n =sample size
- 2. d = effect size (based on Cohen's)
- 3. sig.level = the desired significance level
- The significance level ( $\alpha$ ) defaults to 0.05. Therefore, to calculate the significance level, given an effect size, sample size, and power ( $1 \beta$ ), use the option "siglevel=NULL".
- 4. power = the desired power
- 5. type = the type of t-test you will eventually be carrying out (one of two sample, one sample or paired)
- 6. alternative = the type of alternative hypothesis you want to test (one of two sided, less or greater)
- The core idea behind its functions is that **you enter 3 of the 4 quantities** (effect size, sample size, significance level, power) **and the 4th is calculated**.

# One Sample Mean: EXE data

GOAL: Imagine this is a *pilot study*, in which we tested fish is (on average) different form 20 cm in length.

The guanapo\_data dataset contains information on fish lengths from the Guanapo river pilot

```
2 fishlength data <- readr::read csv(here::here("practice", "data input", "04 datasets",
                                                           "fishlength.csv"),
                                          show col types = FALSE)
            guanapo data <- fishlength data %>%
              dplyr::filter(river == "Guanapo")
        11 names(guanapo data)
[1] "id"
            "river" "length"
          1 mean H1 <- mean(guanapo data$length) # 18.29655
          2 mean H1
[1] 18.29655
          1 sd sample <- sd(quanapo data$length) # 2.584636
          2 sd sample
[11 2.584636
```

## One Sample Mean t-test: EXAMPLE cont.

Let's compute the one sample t-test with stats::t.test against a hypothetical average fish length (mean\_ $H_o=20$ )

```
One Sample t-test

data: guanapo_data$length

t = -3.5492, df = 28, p-value = 0.001387

alternative hypothesis: true mean is not equal to 20

95 percent confidence interval:

17.31341 19.27969

sample estimates:

mean of x

18.29655
```

 There appear to be a statistically significant result here: the mean length of the fish appears to be different from 20 cm.

QUESTION: In a new study of the same fish, what sample size n would you need to get a comparable result?

#### One Sample Mean t-test: POWER ANALYSIS (n)

- We input Cohen's d (after calculating it manually) following: effect size  $\approx \frac{\text{Mean}_{H_1} \text{Mean}_{H_0}}{\text{Std Dev}}$
- We use pwr::pwr.t.test to calculate the minimum sample size n required:

```
One-sample t test power calculation

n = 20.07483
d = 0.6590669
sig.level = 0.05
power = 0.8
alternative = two.sided
```

We would need n = 21 (rounding up) observations for an experiment (e.g. in different river) to detect an effect size as the pilot study at a 5% significance level and 80% power.

#### One Sample Mean t-test: POWER ANALYSIS, stricter conditions

What if we wanted the results to be even more stringent?

• e.g. require higher significance level (0.01) and power (0.90) with the same effect?

```
One-sample t test power calculation

n = 37.62974
d = 0.6590669
sig.level = 0.01
power = 0.9
alternative = two.sided
```

This time, we would need n = 38 observations for an experiment to detect the same effect size at the stricter level of significance and power.

# Two Independent Samples: EXE data

Let's look at the entire fishlength\_data with the lengths of fish from 2 separate rivers.

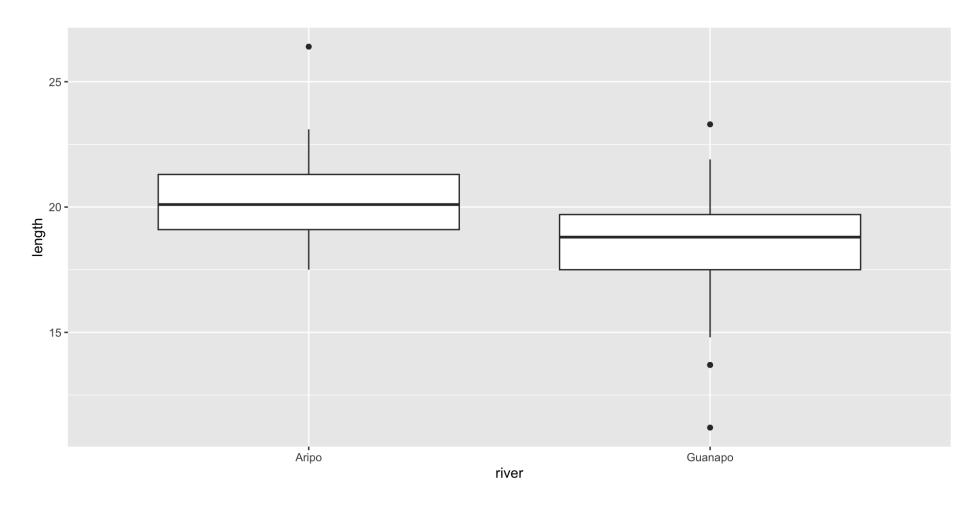
```
2 fishlength data %>%
               dplyr::group by (river) %>%
               dplyr::summarise (N = n(),
                                 mean len = mean(length),
                                 sd len = sd(length))
# A tibble: 2 \times 4
  river
              N mean len sd len
          <int>
                   <dbl> <dbl>
  <chr>
1 Aripo
                    20.3
                           1.78
             29
                    18.3 2.58
2 Guanapo
```

Visualize quickly the 2 samples (rivers) with a boxplot

```
1 # visualize the data
2 fishlength_data %>%
3    ggplot(aes(x = river, y = length)) +
4    geom_boxplot()
```

# Two Independent Samples: EXE data

The fish in the 2 samples appear to have different mean length



# Two Independent Samples: t-test

Let's confirm it with a two sample t-test against  $m{H_0}$ : The two population means are equal

The t-test analysis confirms that the difference is significant.

QUESTION: Can we use this information to design a more efficient experiment? I.e. run an experiment powerful enough to pick up the same observed difference in means but with **fewer observations**?

#### **Two Independent Samples: POWER ANALYSIS 1/2**

- 1. Let's work out exactly the **effect size** of this study by estimating Cohen's d using this data.
- (We use a function from the package rstatix::cohens\_d to estimate Cohen's
   d)

The effsize column contains the information that we want, in this case 0.94

#### Two Independent Samples: POWER ANALYSIS 2/2 (n)

2. Actually answer the question about **how many fish** we really need to catch in the future

```
1 # run power analysis
2 pwr::pwr.t.test(d = 0.94, power = 0.8, sig.level = 0.05,
3 type = "two.sample", alternative = "two.sided")
```

```
Two-sample t test power calculation

n = 18.77618
d = 0.94
sig.level = 0.05
power = 0.8
alternative = two.sided

NOTE: n is number in *each* group
```

The n output (= 19 observations per group) -as opposed to 39 + 29- would be sufficient if we wanted to confidently detect the difference observed in the previous study

# Two Paired Samples: EXE data

The cortisol\_data dataset contains information about cortisol levels measured on 20 participants in the morning and evening

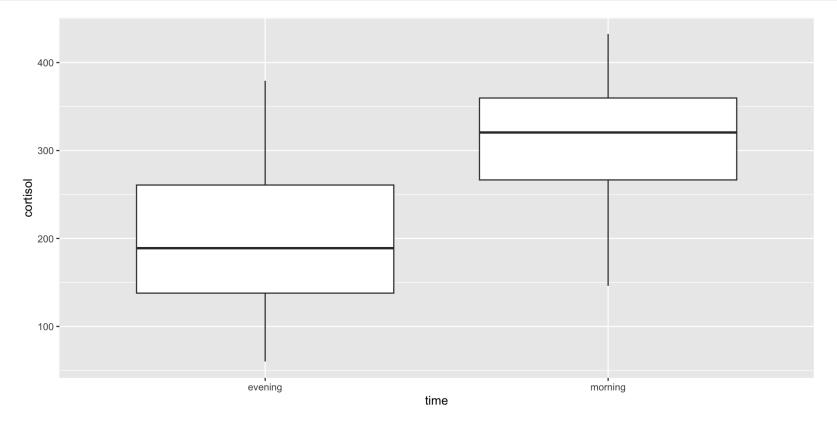
```
1 cortisol_data %>%
2  dplyr::group_by (time) %>%
3  dplyr::summarise (
4  N = n(),
5  mean_cort = mean(cortisol),
6  sd_cort = sd(cortisol))
# A tibble: 2 × 4
```

Notice the difference in the paired sample means is quite large

# **Two Paired Samples t-test: visualization**

Visualize quickly the 2 paired samples (morning and evening) with a boxplot

```
1 # visualize the data
2 cortisol_data %>%
3    ggplot(aes(x = time, y = cortisol)) +
4    geom_boxplot()
```



The cortisol levels in the 2 paired amples appear quite different

## Two Paired Samples: POWER ANALYSIS (d)

GOAL: Flipping the question, if we know the given n (20 patients observed twice): How big should the effect size be to be detected at power of 0.8 and significance level 0.05?

We use pwr::pwr.t.test, with the argument specification type = "paired", but this time
to estimate the effect size

```
Paired t test power calculation

n = 20
d = 0.6604413
sig.level = 0.05
power = 0.8
alternative = two.sided

NOTE: n is number of *pairs*
```

The functions returns the effect size (Cohen's metric): d = 0.6604413. So, with this experimental design we would be able to detect a **medium-large effect size**.

#### Two Paired Samples t-test: POWER ANALYSIS on given n

Looking instead at the actual sample data, what would be the observed effect size?

To compute "observed d" we can use the function rstatix::cohens\_d

```
1 d <- cortisol data %>%
               rstatix::cohens d(cortisol ~ time, paired = TRUE)
          5 d
# A tibble: 1 \times 7
                   group2 effsize
                                             n2 magnitude
                                       n1
           group1
  . y .
                             <dbl> <int> <int> <ord>
* <chr>
           <chr>
                   <chr>
1 cortisol evening morning -1.16
                                             20 large
                                       20
```

The obtained d (-1.16) is extremely large, so we likely have more participants in this study than actually needed given such a large effect.

#### Two Paired Samples t-test: POWER ANALYSIS gives sufficient n

Let's re-compute the power analysis, but leave n as the unknown quantity, given the effect size (d) we have observed

```
Paired t test power calculation

n = 7.960846
d = 1.16
sig.level = 0.05
power = 0.8
alternative = two.sided

NOTE: n is number of *pairs*
```

As a matter of fact, n = 8 pairs of observations would have sufficed in this study, given the size of effect we were trying to detect.

# One-way ANOVA test: EXE data

The mussels\_data dataset contains information about the length of the *anterior adductor muscle scar* in the mussel Mytilus trossulus across five locations around the world!

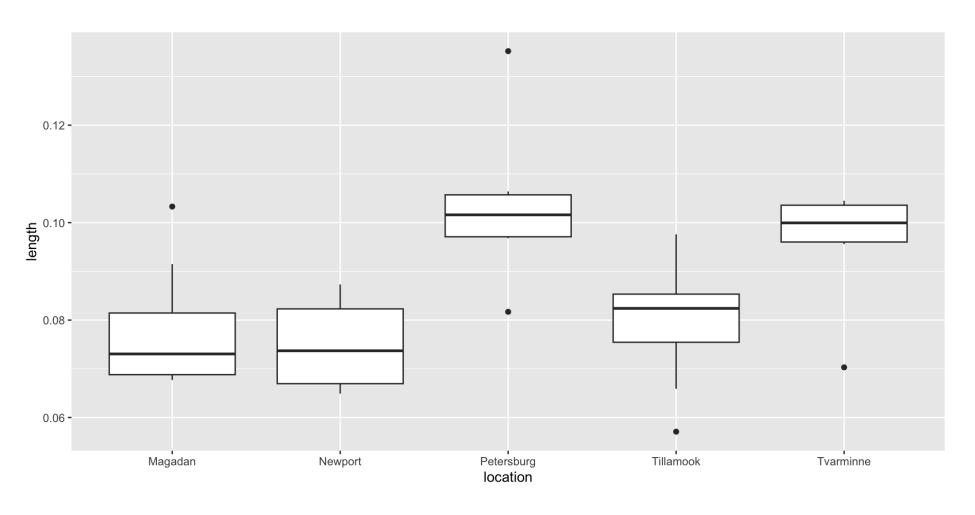
```
mussels data <- read.csv(file = here::here("practice", "data input", "04 datasets",</pre>
                                                    "mussels.csv"),
                                      header = TRUE, # 1st line is the name of the variables
                                      sep = ",", # which is the field separator character.
                                      na.strings = c("?","NA" ), # specific MISSING values
                                      row.names = NULL)
         10 names(mussels data)
[1] "length"
              "location"
          1 stats <- mussels data %>%
              dplyr::group by (location) %>%
              dplyr::summarise (
              N = n(),
               mean len = mean(length),
                sd len = sd(length))
          8 stats
# A tibble: 5 \times 4
 location
                N mean len sd len
  <chr>
            <int> <dbl>
                             <dbl>
                8 0.0780 0.0129
1 Magadan
2 Newport
                8 0.0748 0.00860
3 Petersburg 7 0.103 0.0162
4 Tillamook
               10 0.0802 0.0120
5 Tvarminne
                6 0.0957 0.0130
```

# **One-way ANOVA test: visualization**

There appears to be a noticeable difference in length at average measurements *at least* between some of the locations

```
1 # Visualize the data with a boxplot
2 mussels_data %>%
3    ggplot(aes(x = location, y = length)) +
4    geom_boxplot()
```

# **One-way ANOVA test: visualization**



# One-way ANOVA test: EXAMPLE cont.

Assuming we verified the required assumptions, let's run the ANOVA test to confirm the visual intuition

With the stats::aov followed by the command summary

• A one-way ANOVA test confirms that the mean lengths of muscle scar differed significantly between locations (F = 7.121, with df = [4, 34], and p = 0.000281).

#### One-way ANOVA test: POWER ANALYSIS (effect)

In ANOVA it may be tricky to decide what kind of effect size we are looking for:

- if we care about an overall significance test, the sample size needed is a function of the standard deviation of the group means
- if we're interested in the comparisons of means, there are other ways of expressing the effect size (e.g. a difference between the smallest and largest means)

Here let's consider an overall test in which we could reasonably collect the same n. of observations in each group

```
1  n_loc <- nrow(stats)
2
3  means_by_loc <- c(0.0780, 0.0748, 0.103, 0.0802, 0.0957)
4  overall_mean <- mean(means_by_loc)
5  sd_by_loc <- c(0.0129, 0.00860, 0.0162, 0.0120, 0.0130)
6  overall_sd <- mean(sd_by_loc)</pre>
```

#### One-way ANOVA test: POWER ANALYSIS (effect)

```
1 # Effect Size f formula
2 Cohen_f = sqrt( sum( (1/n_loc) * (means_by_loc - overall_mean)^2) ) /overall_sd
3 Cohen_f # EXTREMELY BIG
```

[1] 0.877622

Balanced one-way analysis of variance power calculation

```
k = 5
n = 4.166759
f = 0.877622
sig.level = 0.05
power = 0.8
```

NOTE: n is number in each group

The n output ( = 5 observations per group) -as opposed to >6 per group- would be sufficient if we wanted to confidently detect the difference observed in the previous study

#### Linear Regression with grouped data: EXE data

The ideas covered before apply also to **linear models**, although here:

- we use pwr.f2.test() to do the power calculation
- the effect sizes ( $f^2$ ) is based on  $R^2$

$$f^2 = \frac{R^2}{1 - R^2}$$

#### Linear Regression with grouped data: EXE data

```
Call:
lm(formula = length ~ location, data = mussels data)
Residuals:
     Min
                10 Median
                                           Max
-0.025400 -0.007956 0.000100 0.007000 0.031757
Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                   0.078012 0.004454 17.517 < 2e-16 ***
(Intercept)
                  -0.003213 0.006298 -0.510 0.61331
locationNewport
locationPetersburg 0.025430 0.006519 3.901 0.00043 ***
locationTillamook 0.002187 0.005975 0.366 0.71656
locationTvarminne
                             0.006803 2.600 0.01370 *
                 0.017687
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.0126 on 34 degrees of freedom
Multiple R-squared: 0.4559, Adjusted R-squared: 0.3918
```

#### Linear Regression with grouped data: POWER ANALYSIS

From the linear model we get that the  $R^2$  value is 0.4559 and we can use this to calculate Cohen's  $f^2$  value using the formula

```
1  # Extract R squared
2  R_2 <- summary(lm_mussels)$r.squared
3  # compute f squared
4  f_2 <- R_2 / (1 - R_2)
5  f_2</pre>
[1] 0.837767
```

Our model has 5 parameters (because we have 5 groups) and so the numerator degrees of freedom u will be 4 (5–1=4).

Hence, we carry out the power analysis with the function pwr.f2.test:

Multiple regression power calculation

```
u = 4
v = 14.62182
f2 = 0.8378974
sig.level = 0.05
power = 0.8
```

#### Linear Regression with grouped data: POWER ANALYSIS interpret.

Recall that, in the F statistic evaluating the model,

- **u** the df for the numerator:  $df_{between} = k 1 = 5 1 = 4$
- v the df for the denominator:  $df_{within} = n k = ?$ 
  - so n = v + 5

Multiple regression power calculation

```
u = 4
v = 14.62182
f2 = 0.8378974
sig.level = 0.05
power = 0.8
```

This tells us that the denominator degrees of freedom  $\mathbf{v}$  should be 15 (14.62 rounded up), and this means that we would only need 20 observations  $\mathbf{n} = \mathbf{v+5}$  in total across all 5 groups to detect this effect size

# SAMPLE SPLITTING IN MACHINE LEARNING

Embracing a different philosophical approach...

#### 2 different approaches with different takes on empirical data

(Simplifying a little)

#### Inferential statistics

- GOAL: Convincingly explain
- APPROACH: Strong emphasis on defining assumptions (about variables distributions) and/or hypotheses on the relationship between them
- DATA:
  - The collection strategy is designed ex-ante, according to the experiment goal
  - Usually, ALL AVAILABLE DATA are used to estimate effect of interest (as sampling was designed to be representative of a population).

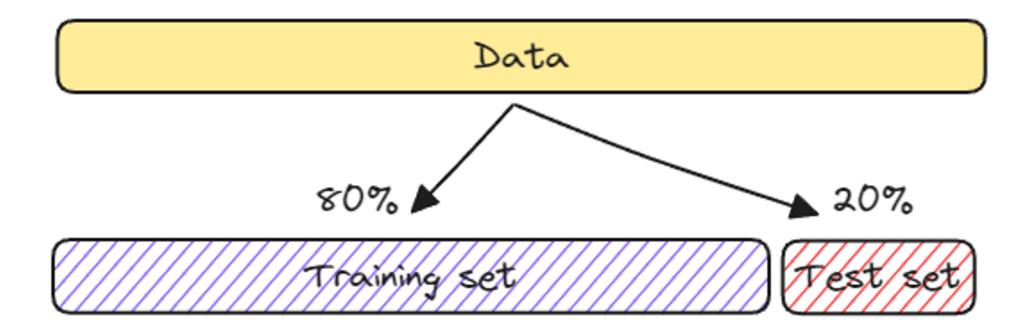
#### **Machine Learning**

- GOAL: Accurately predict
- APPROACH: Focus on labeling observations or uncovering ("learn") a pattern, without worrying about explaining them
- DATA:
  - Data drives the search for patterns, but there is a huge risk of "overfitting" models (too specific to initial data!)
  - It is critical to SPLIT THE DATA (usually 75% for training and 25% for testing the algorithms) leaving aside a sub-sample to test the model with unseen new data

# Data Splitting in ML approaches

Consistent with the ML approach (learning from (data) examples), it is critical to split the available data to obtain:

- 1. 60-80% → training sample for fitting a model and making prediction on the training data itself
- 2. 20-40% -> testing sample for evaluating the performance of the selected model(s) and test it works on new data too
- Since in ML we don't claim to know what works in advance, it is essential to "test" a candidate predictive model on fresh new data and see if it holds



# Introducing R (metapackage) tidymodels for modeling and ML

The package tidymodels (much like the tidyverse) is an ecosystem of packages meant to enable a wide variety of approaches for modeling and statistical analysis.

 One package in this system is rsample is one of its building blocks for resampling data



#### Revisiting NHANES for a quick demonstration of predictive modeling

Let's re-load a dataset from Lab # 3 (the NHANES dataset) for a quick demonstration of data splitting in an ML predictive modeling scenario

- We can try predicting BMI from age (in years), PhysActive, and gender, using linear regression model (which is a Supervised ML algorithm)
- (we already saved this dataset)

# Splitting the dataset into training and testing samples

- With this approach, it is best practice to "hold back" some data for testing to get a better estimate of how models will perform on new data
- We can easily specify training and testing sets using rsample's function initial\_split

```
1 # ensure we always get the same result when sampling (for convenience )
2 set.seed(12345)
3
4 nhanes_split <- nhanes %>%
5 # define the training proportion as 75%
6 rsample::initial_split(prop = 0.75,
7 # ensuring both sets are balanced in gender
8 strata = Gender)
9
10 # resulting datasets
11 nhanes_train <- rsample::training(nhanes_split)
12 dim(nhanes_train)</pre>
```

[1] 374 77

```
1 nhanes_test <- rsample::testing(nhanes_split)
2 dim(nhanes_test)</pre>
```

# Fitting a linear model on the training data

In this case the **regression models** serves for predicting numeric, continuous quantities

```
2 lin mod <- lm(BMI ~ Age + Gender + PhysActive, data = nhanes train)</pre>
          4 summary(lin mod)
Call:
lm(formula = BMI ~ Age + Gender + PhysActive, data = nhanes train)
Residuals:
   Min
            10 Median
                            30
                                  Max
-12.685 -4.674 -1.419 4.257 38.016
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
             30.14217 1.30426 23.110 < 2e-16 ***
(Intercept)
             0.01429 0.02198 0.650 0.51596
Age
Gendermale
             -0.72960 0.72176 -1.011 0.31275
PhysActiveYes -2.26539
                      0.73620 -3.077 0.00225 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.903 on 367 degrees of freedom
  (3 observations deleted due to missingness)
Multiple R-squared: 0.03416, Adjusted R-squared: 0.02626
F-statistic: 4.327 on 3 and 367 DF, p-value: 0.005155
```

## Predicting BMI estimates for new data set

Using the above model, we can predict the BMI for different individuals (those left in the testing data)

- with the function predict, where we specify the argument newdata = nhanes\_test)
- adding the prediction interval (the 95% CI), which gives uncertainty around a single value of the prediction

#### **Evaluating the predictive performance in testing data**

The ultimate goal of holding data back from the model training process was to **evaluate** its predictive performance on new data.

A common measure used is the RMSE (Root Mean Square Error) = a measure of the distance between observed values and predicted values in the testing dataset

```
1 # Computing the Root Mean Square Error
2 RMSE_test <- sqrt(mean((nhanes_test$BMI - predict(lin_mod, nhanes_test))^2, na.rm = T))
3 RMSE_test # 6.170518</pre>
```

[1] 6.170518

The RMSE (= 6.170518) tells us, (roughly speaking) by how much, on average, the new observed BMI values differ from those predicted by our model

## ... and what about RMSE in training data?

Let's see the RMSE in the training dataset (for comparison)

```
1 RMSE_train <- sqrt(mean((nhanes_train$BMI - predict(lin_mod, nhanes_train))^2, na.rm = T))
2 RMSE_train # 6.866044

[1] 6.866044

1 # R squared is also quite low
2 summary(lin_mod)$r.squared # R^2 0.0341589</pre>
[1] 0.0341589
```

This is not what expected (9), since RMSE on the training data is slightly bigger that in the testing data!

A possible explanation is that out model is underfitting in the first place (model's  $\mathbb{R}^2$  was quite low too), so we should definitely try different models...

# WRAPPING UP TODAY'S KEY MESSAGE

# Recap of the workshop's content

#### **TOPICS WE COVERED**

- 1. Motivated the choice of learning/using **R for scientific quantitative analysis**, and lay out some fundamental concepts in biostatistics with concrete R coding examples.
- 2. Consolidated understanding of **inferential statistic**, through R coding examples conducted on real biostatistics research data.
- 3. Discussed the **relationship between any two variables**, and introduce a widely used analytical tool: **regression**.
- 4. Presented a popular ML technique for dimensionality reduction (**PCA**), performed both with MetaboAnalyst and R.
- 5. Introduction to **power analysis** to define the correct sample size for hypotheses testing and discussion of how ML approaches deal with available data.

# **Final thoughts**

- While the workshop only allowed for a synthetic overview of fundamental ideas, it
  hopefully provided a solid foundation on the most common statistical analysis you will
  likely run in your daily work:
  - Thorough understanding of the input data and the data collection process
  - Univariate and bivariate exploratory analysis (accompanied by visual intuition) to form hypothesis
  - Upon verifying the assumptions, we fit data to hypothesized model(s)
  - Assessment of the model performance (R<sup>2</sup>, Adj. R<sup>2</sup>, F Statistic, etc.)
- You should now have a solid grasp on the R language to keep using and exploring the huge potential of this programming ecosystem
- We only scratched the surface in terms of ML classification and prediction models, but
  we got a hang of the fundamental steps and some useful tools that might serve us
  also in more advanced analysis