DECODING FINANCIAL TRENDS: AN ANALYSIS OF WORLD BANK FINANCIAL INDICATORS

DESCRIPTION & PURPOSES

The evolution of financial markets and businesses over time can reveal much about the future direction of a country. For instance, these trends can indicate which countries may be more susceptible to significant layoffs or which are poised to welcome new businesses entering the market. When considered together, various financial indicators paint a comprehensive picture of each country's market dynamics, aiding in the prediction of economic momentum and major market trends.

The World Bank serves as a premier resource for a vast range of economic indicators. The following link provides access to all of these indicators along with detailed explanations: World Bank Indicators.

In this analysis, data will be accessed through the World Bank API. For more information on the API, please refer to the API documentation. The focus is exclusively on market-related indicators over a 10-year period (2012 to 2022), with the objective of offering a general overview of the financial landscape across different countries.

- Canada
- China
- France
- Italy
- Qatar
- South Africa
- United States

While the indicators chosen for the analysis are:

- CM.MKT.LCAP.GD.ZS: Market_Capitalization
- CM.MKT.TRAD.GD.ZS: Market_Liquidity
- CM.MKT.TRNR: Turnover_Ratio
- CM.MKT.LDOM.NO: Listed_Companies
- CM.MKT.INDX.ZG: SP500 GlobIndex

Prior to begin the analysis, let's load the packages needed.

```
In [61]: #import packages for data cleaning, collecting and analysis
         import pandas as pd
         import numpy as np
         import requests
         import wbdata
         import os
         #ARIMA, HW & accuracy measures
         from statsmodels.tsa.stattools import adfuller
         from statsmodels.tsa.arima.model import ARIMA
         from statsmodels.tsa.statespace.sarimax import SARIMAX
         from statsmodels.tsa.holtwinters import ExponentialSmoothing
         from statsmodels.graphics.tsaplots import plot acf, plot pacf
         from statsmodels.tsa.stattools import adfuller, acf, pacf
         from sklearn import metrics
         from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_s
         #packages for plotting
         from IPython.display import display
         import seaborn as sns
         from plotly.subplots import make subplots
         import matplotlib.pyplot as plt
         import plotly.io as pio
```

```
In [2]: #function to save static plots
        # Create the img directory if it doesn't exist
        if not os.path.exists('img'):
            os.makedirs('img')
        def save_plotly_figures(fig, filename):
            Saves a Plotly figure to the img folder.
            Parameters:
            - fig: The Plotly figure to save.
            - filename: The name of the file to save as (without extension).
            file_path = os.path.join('img', f"{filename}.html")
            pio.write_html(fig, file_path) # Save as HTML file
            print(f"Figure saved as: {file path}")
        #function to save interactive plots
        def save_plotly_figure(fig, filename, format='html'):
            Save a Plotly figure as an HTML file or an image.
            Parameters:
            fig : plotly.graph objs.Figure
                The Plotly figure to save.
            filename : str
                The name of the file to save (without extension).
```

```
format : str, optional
    The format to save the figure ('html' or 'png', 'jpeg', 'webp', '
    Default is 'html'.

if format == 'html':
    pio.write_html(fig, file=filename + '.html', auto_open=False)
    print(f"Figure saved as {filename}.html")

elif format in ['png', 'jpeg', 'webp', 'svg', 'pdf']:
    pio.write_image(fig, filename + '.' + format)
    print(f"Figure saved as {filename}.{format}")

else:
    raise ValueError("Invalid format. Choose 'html' or one of 'png',
```

DATA COLLECTION & CLEANING & MANIPULATION

The first thing to do is to retrieve and load data from the WB website. To make thing easier, we will define countries, map the indicators by giving them an understandable name and set the time range (2012 - 2022). After that, it is possible to build a dataframe containing all the indicators for each countries by accessing the WV API. This df will then be unstacked, to let it be more readable.

```
In [3]: #listing the Country API codes
        countries = ["US",
                       "CA", #canada
                       "IT", #italia
                       "FR", #france
                       "CN", #china
                       "QA", #gatar
                       "ZA" #South Africa
        #set up the indicators needed
        #giving them a clear defintion
        indicators = {"CM.MKT.LCAP.GD.ZS": "Market_Capitalization",
                      "CM.MKT.TRAD.GD.ZS": "Market Liquidity",
                      "CM.MKT.TRNR": "Turnover_Ratio",
                      "CM.MKT.LDOM.NO": "Listed_Companies",
                      "CM.MKT.INDX.ZG": "SP500_GlobIndex"
        #create a tuples for the dates we are interested into
        dates = ("2012-01-01", "2022-01-01")
        #grab indicators above for countires above and load into data frame
        df = wbdata.get_dataframe(indicators, country=countries, parse_dates=True
        #df is "pivoted", pandas' unstack fucntion helps reshape it into somethin
        dfu = df.unstack(level=0)
        #show the df
        dfu
```

0ut[3]: Market_Ca

country	Canada	China France		Italy	Qatar	South Africa
date						
2012- 01-01	112.667433	43.334455	67.377418	23.087545	NaN	208.959959
2013- 01-01	114.471175	41.263836	81.834493	28.734086	76.776551	235.182091
2014- 01-01	116.041579	57.323049	73.036475	27.165117	90.125175	244.998287
2015- 01-01	102.370079	74.022199	85.615244	NaN	88.139297	212.265471
2016- 01-01	130.466597	65.169892	87.306014	NaN	102.037608	293.993489
2017- 01-01	143.522053	70.762953	105.940446	NaN	81.074346	322.710975
2018- 01-01	112.320751	45.519408	84.772010	NaN	88.934165	213.523690
2019- 01-01	138.158155	60.010722	NaN	NaN	90.746482	271.322876
2020- 01-01	159.538505	83.585104	NaN	NaN	114.529616	310.835168
2021- 01-01	162.599382	81.016127	NaN	NaN	103.043192	272.067355
2022- 01-01	126.983151	64.139833	NaN	NaN	70.736830	289.127168

11 rows × 35 columns

Since there may be the necessity to analyze just a single indicator, let's build a dataframe for each one of them.

```
dfu["Turnover_Ratio"]
)
#listed Company
ListComp = pd.DataFrame(
    dfu["Listed_Companies"]
)
#listed Company
SP500Index = pd.DataFrame(
    dfu["SP500_GlobIndex"]
)
```

Having cleaned data is fundamental to get sound results. Since the study comprehend several dfs, let's set up a function to clean the data. This function, named clean(df, df_name), will (consequently):

- · check the date is the index
- check data type
- count the null values (NaN)
- replace the null-values with 0 (to avoid issues while modeling)
- round the decimal to 2
- save the cleaned dataframe with the name provided in "df_name" in the out_folder

```
In [5]: #build a function that check data types, counts the null value, replace t
        def clean(df, df name) :
            #check the index (should be the date)
            print("The Index should be the date:")
            print(df.index)
            #check the data type
            print("Variables are of type:")
            print(df.dtypes)
            #count the nulls values
            print("Null values for each column:")
            print(df.isnull().sum())
            #replace the null with 0
            df = df.fillna(value = 0)
            #round the decimals to 2
            df = df.round(2)
            #save the updated df as csv with the name provided in "df name"
            df.to_csv(f"out_data/{df_name}.csv", index = True)
            return df
```

Let's clean all the df for each indicators. Remember that those cleaned df are saved in the out_data folder.

```
In [6]: clean(mrkCap, "mrkCap")
   clean(mrkLiq, "mrkLiq")
   clean(TurnRatio, "TurnRatio")
   clean(ListComp, "ListComp")
   clean(SP500Index, "SP500Index")
```

```
The Index should be the date:
DatetimeIndex(['2012-01-01', '2013-01-01', '2014-01-01', '2015-01-01',
                '2016-01-01', '2017-01-01', '2018-01-01', '2019-01-01', '2020-01-01', '2021-01-01', '2022-01-01'],
               dtype='datetime64[ns]', name='date', freq=None)
Variables are of type:
country
Canada
                  float64
                  float64
China
France
                  float64
                  float64
Italv
Qatar
                  float64
South Africa
                  float64
United States
                  float64
dtype: object
Null values for each column:
country
Canada
                  0
China
                  0
                  4
France
Italy
                  8
Qatar
                  1
South Africa
United States
dtype: int64
The Index should be the date:
DatetimeIndex(['2012-01-01', '2013-01-01', '2014-01-01', '2015-01-01', '2016-01-01', '2017-01-01', '2018-01-01', '2019-01-01',
                '2020-01-01', '2021-01-01', '2022-01-01'],
               dtype='datetime64[ns]', name='date', freq=None)
Variables are of type:
country
Canada
                  float64
China
                  float64
                  float64
France
Italy
                  float64
0atar
                  float64
South Africa
                  float64
United States
                  float64
dtype: object
Null values for each column:
country
Canada
                  0
China
                  0
                  7
France
Italy
                  8
                  0
Qatar
South Africa
                  0
United States
dtype: int64
The Index should be the date:
DatetimeIndex(['2012-01-01', '2013-01-01', '2014-01-01', '2015-01-01',
                 '2016-01-01', '2017-01-01', '2018-01-01', '2019-01-01',
```

```
'2020-01-01', '2021-01-01', '2022-01-01'],
               dtype='datetime64[ns]', name='date', freq=None)
Variables are of type:
country
Canada
                   float64
China
                   float64
France
                   float64
                   float64
Italy
Qatar
                   float64
                   float64
South Africa
United States
                  float64
dtype: object
Null values for each column:
country
Canada
                   0
China
                   0
France
                   7
Italy
                   8
Qatar
                   1
South Africa
                   0
United States
                   5
dtype: int64
The Index should be the date:
DatetimeIndex(['2012-01-01', '2013-01-01', '2014-01-01', '2015-01-01',
                '2016-01-01', '2017-01-01', '2018-01-01', '2019-01-01', '2020-01-01', '2021-01-01', '2022-01-01'],
               dtype='datetime64[ns]', name='date', freg=None)
Variables are of type:
country
Canada
                   float64
China
                   float64
France
                   float64
                   float64
Italy
                   float64
0atar
South Africa
                  float64
United States
                  float64
dtype: object
Null values for each column:
country
Canada
                   0
China
                   0
France
                   4
Italv
                   8
0atar
                   3
South Africa
United States
                   0
dtype: int64
The Index should be the date:
DatetimeIndex(['2012-01-01', '2013-01-01', '2014-01-01', '2015-01-01', '2016-01-01', '2017-01-01', '2018-01-01', '2019-01-01',
                 '2020-01-01', '2021-01-01', '2022-01-01'],
               dtype='datetime64[ns]', name='date', freq=None)
Variables are of type:
country
```

Canada	float64				
China	float64				
France	float64				
Italy	float64				
Qatar	float64				
South Africa	float64				
United States	float64				
dtype: object					
Null values for	each column:				
country					
Canada	0				
China	0				
France	0				
Italy	0				
Qatar	0				
South Africa	0				
United States	0				
dtvpe: int64					

Out[6]:

	country	Canada	China	France	Italy	Qatar	South Africa	United States
	date							
2	2012-01-01	5.99	17.17	15.23	11.03	-1.86	15.75	13.41
2	2013-01-01	2.98	7.26	17.99	23.06	23.97	-7.45	29.60
2	014-01-01	-2.14	3.03	-0.54	-12.02	23.00	3.86	11.39
2	2015-01-01	-26.17	-6.01	8.53	3.20	-18.65	-26.62	-0.73
2	016-01-01	22.56	-2.02	4.86	-13.00	2.19	17.62	9.54
2	2017-01-01	13.75	46.03	9.26	29.77	-16.77	30.62	19.42
2	018-01-01	-19.38	-20.52	-10.95	-20.95	22.22	-25.89	-6.24
2	019-01-01	25.32	19.26	26.37	24.54	-1.90	8.55	28.88
	2020-01- 01	4.48	27.87	-7.14	2.68	-4.04	-7.02	16.26
2	2021-01-01	22.68	-20.65	28.85	14.87	12.23	5.44	26.89
	2022-01- 01	-14.80	-23.62	-9.50	-19.40	-11.26	-7.15	-19.44

The cleaned dfs are the ones that we are going to analyze. Let's load them all.

```
In [7]: mrkCapclean = pd.read_csv("out_data/mrkcap.csv")
    mrkLiqclean = pd.read_csv("out_data/mrkLiq.csv")
    TurnRatioclean = pd.read_csv("out_data/TurnRatio.csv")
    ListCompclean = pd.read_csv("out_data/ListComp.csv")
    SP500Indexclean = pd.read_csv("out_data/SP500Index.csv")
```

All these dfs should now be ready to be analyzed. Let's double check that they have been properly loaded by printin the mrkCapclean df.

```
In [8]: print("Double check that data are loaded:")
print(mrkCapclean)
```

Double check that data are loaded:

```
date Canada China
                              France
                                      Italy
                                              Qatar
                                                     South Africa
0
    2012-01-01 112.67 43.33
                               67.38
                                      23.09
                                               0.00
                                                           208.96
1
   2013-01-01 114.47 41.26
                               81.83
                                      28.73
                                              76.78
                                                           235.18
2
   2014-01-01 116.04
                       57.32
                               73.04
                                     27.17
                                              90.13
                                                           245.00
3
   2015-01-01
               102.37
                       74.02
                               85.62
                                              88.14
                                       0.00
                                                           212.27
4
   2016-01-01 130.47
                       65.17
                               87.31
                                             102.04
                                                           293.99
                                       0.00
5
   2017-01-01
               143.52
                       70.76
                              105.94
                                       0.00
                                              81.07
                                                           322.71
6
              112.32 45.52
                               84.77
                                              88.93
                                                           213.52
   2018-01-01
                                       0.00
7
   2019-01-01 138.16 60.01
                                0.00
                                       0.00
                                              90.75
                                                           271.32
8
   2020-01-01
               159.54 83.59
                                0.00
                                       0.00
                                             114.53
                                                           310.84
9
   2021-01-01 162.60 81.02
                                0.00
                                       0.00
                                             103.04
                                                           272.07
10
   2022-01-01
               126.98 64.14
                                              70.74
                                                           289.13
                                0.00
                                       0.00
```

```
United States
0
            114.85
1
            142.38
2
            149.54
3
            137.02
4
            145.45
5
            163.78
6
            147.34
7
            158.38
8
            194.95
9
            205.77
10
            156.53
```

As noticeable, the df are stored in a wide format. It may be come in handy to have them also in a long format. The function widetolong(df, varname) does exactly this by:

- · resetting the index
- melting the dataframe to adjust the column into the new format
- renaming the columns

By applying this function to all dfs, all dfs will become long-dfs.

```
In [10]: mrkCaplong = widetolong(mrkCapclean, "mrk_cap")
```

```
mrkLiqlong = widetolong(mrkLiqclean, "mrk_liq")
TurnRatiolong = widetolong(TurnRatioclean, "turnover_ratio")
ListComplong = widetolong(ListCompclean, "listed_comp")
SP500Indexlong = widetolong(SP500Indexclean, "SP500_index")
```

To be sure that the transformation has been performed properly, let's print one df as a try.

```
In [11]: print("Checking the long df has been saved properly:")
    print(mrkCaplong)
```

```
Checking the long df has been saved properly:
         date
                       state mrk_cap
0
   2012-01-01
                      Canada
                              112.67
1
   2013-01-01
                     Canada
                              114.47
                     Canada 116.04
   2014-01-01
   2015-01-01
                             102.37
3
                     Canada
   2016-01-01
                     Canada
                              130.47
72 2018-01-01 United States
                             147.34
73 2019-01-01 United States
                             158.38
74 2020-01-01 United States
                              194.95
75 2021-01-01 United States
                              205.77
76 2022-01-01 United States
                              156.53
```

[77 rows x 3 columns]

Finally, let's merge all the long dfs to get a single dataframe where each column corresponds to a single indicator.

```
In [12]: #create a list with allo the long dfs
df_list = [mrkCaplong, mrkLiqlong, TurnRatiolong, ListComplong, SP500Inde

#perform the merge
final_df = df_list[0] #start with the first df
for df in df_list[1:]:
    final_df = pd.merge(final_df, df, on = ["date", "state"], how = "inne

#display the result
final_df
```

Out[12]:		date	state	mrk_cap	mrk_liq	turnover_ratio	listed_comp	SP500_index
	0	2012- 01-01	Canada	112.67	73.73	65.44	3874.0	5.99
	1	2013- 01-01	Canada	114.47	71.68	62.62	3810.0	2.98
	2	2014- 01-01	Canada	116.04	74.42	64.15	3691.0	-2.14
	3	2015- 01-01	Canada	102.37	70.42	68.80	3501.0	-26.17
	4	2016- 01-01	Canada	130.47	75.48	57.55	3368.0	22.56
	•••	•••	•••		•••			
	72	2018- 01-01	United States	147.34	237.52	0.00	4013.0	-6.24
	73	2019- 01-01	United States	158.38	168.87	0.00	3910.0	28.88
	74	2020- 01-01	United States	194.95	192.69	0.00	4104.0	16.26
	75	2021- 01-01	United States	205.77	194.43	0.00	4774.0	26.89
	76	2022- 01-01	United States	156.53	172.14	0.00	4642.0	-19.44

77 rows × 7 columns

Another cleaning phase's fundamental part is checking that each column has the same amount of observation. Let's do that.

In [13]:	<pre>final_df.count()</pre>							
Out[13]:	date	77						
	state	77						
	mrk_cap	77						
	mrk_liq	77						
	turnover_ratio	77						
	listed_comp	77						
	SP500_index	77						
	dtype: int64							

That's a good news: the amount of obs is the same for every column. Now let's count how many missing values there are for each single indicator.

Remember that, after the cleaning phase above, missing data are represented by 0s. As such, we need a function that counts the 0s in each column. Let's build that.

```
In [14]: def count_zeros(df, column_name):
    # Group by 'state' and count how many times 0 appears in the specifie
    return df.groupby('state')[column_name].apply(lambda x: (x == 0).sum()
```

Finally, check missing data for all indicators. Results may give interesting insights.

```
In [15]: #count the 0s in each column of the final df
    print(count_zeros(final_df, "mrk_cap"))
    print(count_zeros(final_df, "mrk_liq"))
    print(count_zeros(final_df, "turnover_ratio"))
    print(count_zeros(final_df, "listed_comp"))
    print(count_zeros(final_df, "SP500_index"))
```

```
state
Canada
                  0
China
                  0
France
                  4
Italy
                  8
0atar
South Africa
United States
Name: mrk_cap, dtype: int64
state
Canada
                  0
China
                  0
France
                  7
                  8
Italy
Qatar
                  0
South Africa
United States
Name: mrk_liq, dtype: int64
state
Canada
China
                  0
France
                  7
Italy
                  8
Qatar
                  1
South Africa
United States
                  5
Name: turnover_ratio, dtype: int64
state
Canada
                  0
China
                  0
France
                  4
                  8
Italy
                  3
Qatar
South Africa
United States
Name: listed_comp, dtype: int64
state
Canada
China
                  0
                  0
France
Italy
Qatar
South Africa
United States
```

Name: SP500_index, dtype: int64

As evident, France and Italy are the countries with the greatest amount of 0s (i.e NaN). The natural question now is: why so?

Let's try to zoom-in by focusing just on these two countries to see if we can spot some shared patterns. Keep in mind that both of them are European Countires (and EU members too).

```
In [16]: #Italy
  italy = final_df[final_df["state"] == "Italy"]
  italy
```

Out[16]:		date	state	mrk_cap	mrk_liq	turnover_ratio	listed_comp	SP500_index
	33	2012- 01-01	Italy	23.09	37.50	162.42	303.0	11.03
	34	2013- 01-01	Italy	28.73	35.95	125.11	285.0	23.06
	35	2014- 01-01	Italy	27.17	95.08	350.01	290.0	-12.02
	36	2015- 01-01	Italy	0.00	0.00	0.00	0.0	3.20
	37	2016- 01-01	Italy	0.00	0.00	0.00	0.0	-13.00
	38	2017- 01-01	Italy	0.00	0.00	0.00	0.0	29.77
	39	2018- 01-01	Italy	0.00	0.00	0.00	0.0	-20.95
	40	2019- 01-01	Italy	0.00	0.00	0.00	0.0	24.54
	41	2020- 01-01	Italy	0.00	0.00	0.00	0.0	2.68
	42	2021- 01-01	Italy	0.00	0.00	0.00	0.0	14.87
	43	2022- 01-01	Italy	0.00	0.00	0.00	0.0	-19.40

```
In [17]: #france
    france = final_df[final_df["state"] == "France"]
    france
```

Out[17]:

	date	state	mrk_cap	mrk_liq	turnover_ratio	listed_comp	SP500_index
22	2012- 01-01	France	67.38	40.04	59.42	562.0	15.23
23	2013- 01-01	France	81.83	39.32	48.04	500.0	17.99
24	2014- 01-01	France	73.04	40.92	56.02	495.0	-0.54
25	2015- 01-01	France	85.62	54.46	63.61	490.0	8.53
26	2016- 01-01	France	87.31	0.00	0.00	485.0	4.86
27	2017- 01-01	France	105.94	0.00	0.00	465.0	9.26
28	2018- 01-01	France	84.77	0.00	0.00	457.0	-10.95
29	2019- 01-01	France	0.00	0.00	0.00	0.0	26.37
30	2020- 01-01	France	0.00	0.00	0.00	0.0	-7.14
31	2021- 01-01	France	0.00	0.00	0.00	0.0	28.85
32	2022- 01-01	France	0.00	0.00	0.00	0.0	-9.50

Speaking about Italy, the pattern is clear: from 2015 there are no more available data for each indicator except the SP500_Index.

Turning to France, instead, there is not a single year when data become not available. What it is interesting is that listed companies and market capitalzion stop to be available in the same year. The same is for market liquidity and the turnover ration. Still, the only indicator that has no missing data is the SP500_index.

When there are so many missing data, the first thing to do is to check that the API loaded the information correctly. After manually browsing the WB official website, we discovered that this data is still not available there. That is our main interest: be sure that no mistakes were done during the import.

To make thing easier, we are not going to consider these two Countries in our analysis. Since available data are a few, they will not add many information to our study.

On the other hand, it would be interesting to delve more in profundity on the reasons why these countries stopped discolsing data on those specific years. Could it be due

> to a new EU regulation? An Internal law? A change in the goverment? We will leave these question for law and politics experts.

Seeing that, let's exclude both Italy and France from our df. As such, the df is narrowed down to: Canada, China, Qatar, South Africa, United States.

```
In [18]: #drop Italy and France from the df
         #drop all the rows containing Italy
         noIt = final_df.drop(final_df[final_df['state'] == 'Italy'].index)
         #drop all the rows containing France
         mrkdf = noIt.drop(noIt[noIt['state'] == 'France'].index)
         #resetting the index to avoid miscounting
         mrkdf = mrkdf.reset_index()
         #drop the column index
         mrkdf = mrkdf.drop(columns = "index")
         #print the df to check it
         mrkdf
```

Out[18]:		date	state	mrk_cap	mrk_liq	turnover_ratio	listed_comp	SP500_index
	0	2012- 01-01	Canada	112.67	73.73	65.44	3874.0	5.99
	1	2013- 01-01	Canada	114.47	71.68	62.62	3810.0	2.98
	2	2014- 01-01	Canada	116.04	74.42	64.15	3691.0	-2.14
	3	2015- 01-01	Canada	102.37	70.42	68.80	3501.0	-26.17
	4	2016- 01-01	Canada	130.47	75.48	57.55	3368.0	22.56
	5	2017- 01-01	Canada	143.52	77.62	54.08	3278.0	13.75
	6	2018- 01-01	Canada	112.32	79.62	70.88	3330.0	-19.38
	7	2019- 01-01	Canada	138.16	82.16	59.46	3358.0	25.32
	8	2020- 01-01	Canada	159.54	118.02	73.98	3922.0	4.48
	9	2021- 01-01	Canada	162.60	109.09	67.09	3455.0	22.68
	10	2022- 01-01	Canada	126.98	104.06	81.95	3534.0	-14.80
	11	2012- 01-01	China	43.33	58.92	135.97	2494.0	17.17
	12	2013-	China	41.26	80.41	194.88	2489.0	7.26

	01-01						
13	2014- 01-01	China	57.32	114.16	199.16	2613.0	3.03
14	2015- 01-01	China	74.02	355.52	480.29	2827.0	-6.01
15	2016- 01-01	China	65.17	162.86	249.91	3052.0	-2.02
16	2017- 01-01	China	70.76	139.91	197.71	3485.0	46.03
17	2018- 01-01	China	45.52	94.07	206.65	3584.0	-20.52
18	2019- 01-01	China	60.01	127.80	212.96	12730.0	19.26
19	2020- 01-01	China	83.59	215.03	257.26	12341.0	27.87
20	2021- 01-01	China	81.02	226.48	279.55	11629.0	-20.65
21	2022- 01-01	China	64.14	181.54	283.04	11497.0	-23.62
22	2012- 01-01	Qatar	0.00	10.39	0.00	42.0	-1.86
23	2013- 01-01	Qatar	76.78	10.35	13.48	42.0	23.97
24	2014- 01-01	Qatar	90.13	26.54	29.45	43.0	23.00
25	2015- 01-01	Qatar	88.14	14.93	16.94	43.0	-18.65
26	2016- 01-01	Qatar	102.04	12.49	12.65	44.0	2.19
27	2017- 01-01	Qatar	81.07	11.38	14.03	45.0	-16.77
28	2018- 01-01	Qatar	88.93	10.35	11.64	46.0	22.22
29	2019- 01-01	Qatar	90.75	7.56	8.34	47.0	-1.90
30	2020- 01-01	Qatar	114.53	16.05	14.01	0.0	-4.04
31	2021- 01-01	Qatar	103.04	17.28	16.77	0.0	12.23
32	2022- 01-01	Qatar	70.74	18.72	26.46	0.0	-11.26

34 2013- South Africa 235.18 57.93 24.63 322.0 -7.45 35 2014- South Africa 245.00 64.45 26.31 322.0 3.86 36 2015- South O1-01 Africa 212.27 67.49 31.79 316.0 -26.62 37 2016- South Africa 293.99 124.37 38.37 303.0 17.62 38 2017- Africa 322.71 107.41 25.74 294.0 30.62 39 2018- South Africa 213.52 72.80 41.86 289.0 -25.89 40 2019- South Africa 271.32 73.16 33.13 274.0 8.55 41 2020- South Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- South Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- O1-01 Africa 142.38 196.95 138.33 4180.0 29.60 45 2013- United O1-01 States 149.54 221.36 148.03 4369.0 11.39 47 2016- United O1-01 States 145.45 223.73 94.72 4331.0 9.54 49 2017- United O1-01 States 145.45 223.73 94.72 4331.0 9.54 49 2017- United States 145.45 223.73 94.72 4331.0 9.54 49 2017- United O1-01 States 147.34 237.52 0.00 4013.0 -6.24 50 2018- United O1-01 States 147.34 237.52 0.00 4013.0 -6.24 50 2018- United O1-01 States 147.34 237.52 0.00 4013.0 -6.24 50 2018- United O1-01 States 158.38 168.87 0.00 3910.0 28.88							
34 01-01 Africa 235.18 57.93 24.63 322.0 -7.45 35 2014- O1-01 Africa Africa 245.00 64.45 26.31 322.0 3.86 36 2015- Africa 212.27 67.49 31.79 316.0 -26.62 37 2016- South Africa 293.99 124.37 38.37 303.0 17.62 38 2017- South Africa 322.71 107.41 25.74 294.0 30.62 39 2018- South Africa 213.52 72.80 41.86 289.0 -25.89 40 2019- South Africa 271.32 73.16 33.13 274.0 8.55 41 2020- South Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- O1-01 Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 States 142.38	33		208.96	52.22	24.99	338.0	15.75
35 01-01 Africa 245.00 64.45 26.31 322.0 3.86 36 2015- O1-01 South Africa 212.27 67.49 31.79 316.0 -26.62 37 2015- O1-01 Africa 293.99 124.37 38.37 303.0 17.62 38 2017- O1-01 Africa 322.71 107.41 25.74 294.0 30.62 39 2018- South O1-01 Africa 213.52 72.80 41.86 289.0 -25.89 40 2019- South O1-01 Africa 271.32 73.16 33.13 274.0 8.55 41 2020- South O1-01 Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- South O1-01 Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 States 142.38 196.95	34		235.18	57.93	24.63	322.0	-7.45
36 01-01 Africa 212.27 67.49 31.79 316.0 -26.62 37 2016- O1-01 South Africa 293.99 124.37 38.37 303.0 17.62 38 2017- O1-01 Africa Africa 322.71 107.41 25.74 294.0 30.62 39 2018- South O1-01 Africa 213.52 72.80 41.86 289.0 -25.89 40 2019- South O1-01 Africa 271.32 73.16 33.13 274.0 8.55 41 2020- South O1-01 Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- South O1-01 Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 States 114.85 199.03 173.29 4102.0 13.41 45 2013- United O1-01 States 142.38 <t< th=""><th>35</th><th></th><th>245.00</th><th>64.45</th><th>26.31</th><th>322.0</th><th>3.86</th></t<>	35		245.00	64.45	26.31	322.0	3.86
37 01-01 Africa 293.99 124.37 38.37 303.0 17.62 38 2017- 01-01 South Africa 322.71 107.41 25.74 294.0 30.62 39 2018- 01-01 South Africa Africa 213.52 72.80 41.86 289.0 -25.89 40 2019- O1-01 South Africa Africa 271.32 73.16 33.13 274.0 8.55 41 2020- O1-01 South Africa Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- O1-01 South Africa Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 United States 142.38 196.95 138.33 4180.0 29.60 45 2013- United O1-01 States 149.54 221.36 148.03 4369.0 11.39 47 2015- United O1-01 States <th>36</th> <th></th> <th>212.27</th> <th>67.49</th> <th>31.79</th> <th>316.0</th> <th>-26.62</th>	36		212.27	67.49	31.79	316.0	-26.62
38 01-01 Africa 322.71 107.41 25.74 294.0 30.62 39 2018- O1-01 Africa 213.52 72.80 41.86 289.0 -25.89 40 2019- O1-01 Africa 271.32 73.16 33.13 274.0 8.55 41 2020- South O1-01 Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- South O1-01 Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 States 114.85 199.03 173.29 4102.0 13.41 45 2013- O1-01 States 142.38 196.95 138.33 4180.0 29.60 46 2014- O1-01 States 149.54 221.36 148.03 4369.0 11.39 47 2015- O1-01 States 137.02 226.28 165.15 4381.0 -0.73 48 2016- O1-01 States 145.45 <th>37</th> <th></th> <th>293.99</th> <th>124.37</th> <th>38.37</th> <th>303.0</th> <th>17.62</th>	37		293.99	124.37	38.37	303.0	17.62
39 01-01 Africa 213.52 72.80 41.86 289.0 -28.89 40 2019- 01-01 South Africa 271.32 73.16 33.13 274.0 8.55 41 2020- 01-01 South Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- 01-01 Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 States 114.85 199.03 173.29 4102.0 13.41 45 2013- O1-01 States 142.38 196.95 138.33 4180.0 29.60 46 2014- O1-01 States 149.54 221.36 148.03 4369.0 11.39 47 2015- O1-01 United States 137.02 226.28 165.15 4381.0 -0.73 48 2016- O1-01 States 145.45 223.73	38		322.71	107.41	25.74	294.0	30.62
40 01-01 Africa 271.32 73.16 33.13 274.0 8.55 41 2020- 01-01 Africa Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- 01-01 South Africa 272.07 61.41 29.37 252.0 5.44 43 2022- 01-01 South Africa 289.13 57.76 26.69 237.0 -7.15 44 2012- 01-01 United States 114.85 199.03 173.29 4102.0 13.41 45 2013- 01-01 United States 142.38 196.95 138.33 4180.0 29.60 46 2014- 01-01 United O1-01 149.54 221.36 148.03 4369.0 11.39 47 2015- 01-01 United O1-01 137.02 226.28 165.15 4381.0 -0.73 48 2016- 01-01 States 145.45 223.73 94.72 4331.0 9.54 49 2017- 01-01 States 163.78 202.86 116.08 4336.0 19.42 50 01-01 Sta	39		213.52	72.80	41.86	289.0	-25.89
41 01-01 Africa 310.84 86.86 35.30 264.0 -7.02 42 2021- O1-01 South Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South O1-01 289.13 57.76 26.69 237.0 -7.15 44 2012- United O1-01 14.85 199.03 173.29 4102.0 13.41 45 2013- United O1-01 142.38 196.95 138.33 4180.0 29.60 46 2014- United O1-01 149.54 221.36 148.03 4369.0 11.39 47 2015- United O1-01 137.02 226.28 165.15 4381.0 -0.73 48 2016- United O1-01 145.45 223.73 94.72 4331.0 9.54 49 2017- United O1-01 163.78 202.86 116.08 4336.0 19.42 50 2018- United O1-01 147.34 237.52 0.00 4013.0 -6.24 51 2019- United O1-01 158.38 168.87 0.00 3910.0 28.88 52 2020-	40		271.32	73.16	33.13	274.0	8.55
42 01-01 Africa 272.07 61.41 29.37 252.0 5.44 43 2022- South Ol-01 289.13 57.76 26.69 237.0 -7.15 44 2012- United Ol-01 114.85 199.03 173.29 4102.0 13.41 45 2013- United Ol-01 142.38 196.95 138.33 4180.0 29.60 46 2014- United Ol-01 149.54 221.36 148.03 4369.0 11.39 47 2015- United Ol-01 137.02 226.28 165.15 4381.0 -0.73 48 2016- United Ol-01 145.45 223.73 94.72 4331.0 9.54 49 2017- United Ol-01 163.78 202.86 116.08 4336.0 19.42 50 2018- United Ol-01 15ates 147.34 237.52 0.00 4013.0 -6.24 51 2019- United Ol-01 158.38 168.87 0.00 3910.0 28.88 52 2020- United Ol-01 194.95 192.69 0.00 4104.0 16.36	41		310.84	86.86	35.30	264.0	-7.02
43 01-01 Africa 289.13 57.76 26.69 237.0 -7.15 44 2012-	42		272.07	61.41	29.37	252.0	5.44
44 01-01 States 114.85 199.03 173.29 4102.0 13.41 45 2013- 01-01 United States 142.38 196.95 138.33 4180.0 29.60 46 2014- 01-01 United States 149.54 221.36 148.03 4369.0 11.39 47 2015- 01-01 United States 137.02 226.28 165.15 4381.0 -0.73 48 2016- 01-01 United States 145.45 223.73 94.72 4331.0 9.54 49 2017- 01-01 United States 163.78 202.86 116.08 4336.0 19.42 50 2018- 01-01 United States 147.34 237.52 0.00 4013.0 -6.24 51 2019- 01-01 United States 158.38 168.87 0.00 3910.0 28.88 52 2020- United 194.95 192.69 0.00 4104.0 16.26	43		289.13	57.76	26.69	237.0	-7.15
45 01-01 States 142.38 196.95 138.33 4180.0 29.60 46 2014-	44		114.85	199.03	173.29	4102.0	13.41
46 01-01 States 149.54 221.36 148.03 4369.0 11.39 47 2015-	45		142.38	196.95	138.33	4180.0	29.60
47 01-01 States 137.02 226.28 165.15 4381.0 -0.73 48 2016- United 01-01 145.45 223.73 94.72 4331.0 9.54 49 2017- United 01-01 163.78 202.86 116.08 4336.0 19.42 50 2018- United 01-01 147.34 237.52 0.00 4013.0 -6.24 51 2019- United 01-01 158.38 168.87 0.00 3910.0 28.88 52 2020- United 20	46		149.54	221.36	148.03	4369.0	11.39
48 01-01 States 145.45 223.73 94.72 4331.0 9.54 49 2017- United 01-01 163.78 202.86 116.08 4336.0 19.42 50 2018- United 01-01 147.34 237.52 0.00 4013.0 -6.24 51 2019- United 01-01 158.38 168.87 0.00 3910.0 28.88 52 2020- United 194.95 192.69 0.00 4104.0 16.26	47		137.02	226.28	165.15	4381.0	-0.73
49 01-01 States 163.78 202.86 116.08 4336.0 19.42 50 2018-	48		145.45	223.73	94.72	4331.0	9.54
50 01-01 States 147.34 237.52 0.00 4013.0 -6.24 51 2019- United 01-01 States 158.38 168.87 0.00 3910.0 28.88 52 2020- United 194.95 193.69 0.00 4104.0 16.36	49		163.78	202.86	116.08	4336.0	19.42
51 01-01 States 158.38 168.87 0.00 3910.0 28.88 52 2020- United 194.95 192.69 0.00 4104.0 16.26	50		147.34	237.52	0.00	4013.0	-6.24
10/10h 10760 000 /10/10 1676	51		158.38	168.87	0.00	3910.0	28.88
	52		194.95	192.69	0.00	4104.0	16.26

53	2021- 01-01	United States	205.77	194.43	0.00	4774.0	26.89
54	2022- 01-01	United States	156.53	172.14	0.00	4642.0	-19.44

We drop the SP500_index column too. That's to make the df "slimmer" and fitter to our purposes. We will consider SP500_Index later on to perform a more detailed analysis for all the Countries (i.e taking into consideration France and Italy). That's to make the df "slimmer".

In [19]: mrkdf = mrkdf.drop(columns = "SP500_index")
mrkdf

	mrk	df					
Out[19]:		date	state	mrk_cap	mrk_liq	turnover_ratio	listed_comp
	0	2012-01-01	Canada	112.67	73.73	65.44	3874.0
	1	2013-01-01	Canada	114.47	71.68	62.62	3810.0
	2	2014-01-01	Canada	116.04	74.42	64.15	3691.0
	3	2015-01-01	Canada	102.37	70.42	68.80	3501.0
	4	2016-01-01	Canada	130.47	75.48	57.55	3368.0
	5	2017-01-01	Canada	143.52	77.62	54.08	3278.0
	6	2018-01-01	Canada	112.32	79.62	70.88	3330.0
	7	2019-01-01	Canada	138.16	82.16	59.46	3358.0
	8	2020-01-01	Canada	159.54	118.02	73.98	3922.0
	9	2021-01-01	Canada	162.60	109.09	67.09	3455.0
	10	2022-01-01	Canada	126.98	104.06	81.95	3534.0
	11	2012-01-01	China	43.33	58.92	135.97	2494.0
	12	2013-01-01	China	41.26	80.41	194.88	2489.0
	13	2014-01-01	China	57.32	114.16	199.16	2613.0
	14	2015-01-01	China	74.02	355.52	480.29	2827.0
	15	2016-01-01	China	65.17	162.86	249.91	3052.0
	16	2017-01-01	China	70.76	139.91	197.71	3485.0
	17	2018-01-01	China	45.52	94.07	206.65	3584.0
	18	2019-01-01	China	60.01	127.80	212.96	12730.0
	19	2020-01-01	China	83.59	215.03	257.26	12341.0
	20	2021-01-01	China	81.02	226.48	279.55	11629.0

21	2022-01-01	China	64.14	181.54	283.04	11497.0
22	2012-01-01	Qatar	0.00	10.39	0.00	42.0
23	2013-01-01	Qatar	76.78	10.35	13.48	42.0
24	2014-01-01	Qatar	90.13	26.54	29.45	43.0
25	2015-01-01	Qatar	88.14	14.93	16.94	43.0
26	2016-01-01	Qatar	102.04	12.49	12.65	44.0
27	2017-01-01	Qatar	81.07	11.38	14.03	45.0
28	2018-01-01	Qatar	88.93	10.35	11.64	46.0
29	2019-01-01	Qatar	90.75	7.56	8.34	47.0
30	2020-01-01	Qatar	114.53	16.05	14.01	0.0
31	2021-01-01	Qatar	103.04	17.28	16.77	0.0
32	2022-01-01	Qatar	70.74	18.72	26.46	0.0
33	2012-01-01	South Africa	208.96	52.22	24.99	338.0
34	2013-01-01	South Africa	235.18	57.93	24.63	322.0
35	2014-01-01	South Africa	245.00	64.45	26.31	322.0
36	2015-01-01	South Africa	212.27	67.49	31.79	316.0
37	2016-01-01	South Africa	293.99	124.37	38.37	303.0
38	2017-01-01	South Africa	322.71	107.41	25.74	294.0
39	2018-01-01	South Africa	213.52	72.80	41.86	289.0
40	2019-01-01	South Africa	271.32	73.16	33.13	274.0
41	2020-01-01	South Africa	310.84	86.86	35.30	264.0
42	2021-01-01	South Africa	272.07	61.41	29.37	252.0
43	2022-01-01	South Africa	289.13	57.76	26.69	237.0
44	2012-01-01	United States	114.85	199.03	173.29	4102.0
45	2013-01-01	United States	142.38	196.95	138.33	4180.0
46	2014-01-01	United States	149.54	221.36	148.03	4369.0
47	2015-01-01	United States	137.02	226.28	165.15	4381.0
48	2016-01-01	United States	145.45	223.73	94.72	4331.0
49	2017-01-01	United States	163.78	202.86	116.08	4336.0
50	2018-01-01	United States	147.34	237.52	0.00	4013.0
51	2019-01-01	United States	158.38	168.87	0.00	3910.0
52	2020-01-01	United States	194.95	192.69	0.00	4104.0

53	2021-01-01	United States	205.77	194.43	0.00	4774.0
54	2022-01-01	United States	156.53	172.14	0.00	4642.0

ANALYSIS

Usually, the first step in the analysis phase is to compute some summary statistics (mean, std, min, max and so on) for all the variables. Let's do that.

In [20]: round(mrkdf.describe(), 2)

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	mrk_cap	mrk_liq	turnover_ratio	listed_comp
count	55.00	55.00	55.00	55.00
mean	138.23	107.47	86.56	2883.04
std	75.42	77.86	97.36	3131.37
min	0.00	7.56	0.00	0.00
25%	82.33	58.42	20.78	269.00
50%	116.04	80.41	54.08	3278.00
75%	163.19	170.50	137.15	3967.50
max	322.71	355.52	480.29	12730.00

Note: The row labeled "50%" represents the median of the series. By comparing it with the mean, we can get a rough understanding of whether the series contains outliers. For instance, the "listed_comp" series may contain outliers. However, since the aim here is not forecasting but data description, we will retain these outliers as they provide valuable information. Therefore, we will not apply any smoothing techniques to address them.

Next, we will build the correlation matrix for the indicators. This will help us understand how each variable moves in relation to the others.

```
In [21]: # create a copy so that the original DF is not affected
# drop the columns year and country
mrkdf_corr = mrkdf.drop(['date', 'state'], axis='columns')
mrkdf_corr.describe()
mrkdf_corr.corr()
```

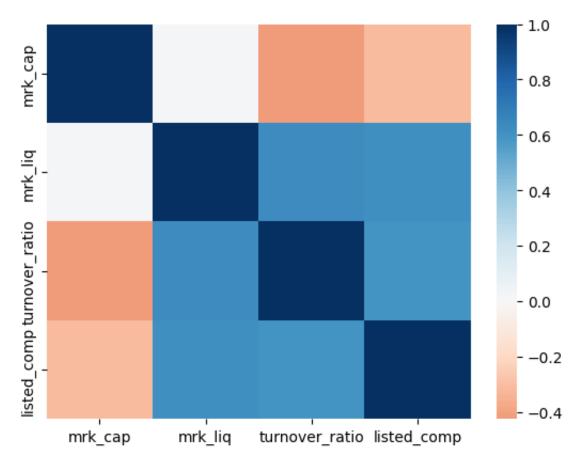
_		$\Gamma \sim$	a .	7
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	тк_сар	mrk_liq	turnover_ratio	listea_comp
mrk_cap	1.000000	0.023733	-0.425372	-0.312310
mrk_liq	0.023733	1.000000	0.631290	0.614742
turnover_ratio	-0.425372	0.631290	1.000000	0.596694
listed_comp	-0.312310	0.614742	0.596694	1.000000

Let's plot that.

In [22]: #plot the correlation matrix
sns.heatmap(mrkdf_corr.corr(), cmap='RdBu', center=0)

Out[22]: <Axes: >



The correlogram gives few insights about the variables:

- Market Capitalization seems to be negatively correlated with other variables, especially turnover ratio and the number of listed companies, implying that larger markets in terms of value might have lower trading activity (turnover) and fewer listed companies.
- Market Liquidity is positively correlated with both turnover ratio and listed companies, suggesting that markets with more listed companies are more liquid, and liquidity is associated with higher trading frequency.

• Turnover Ratio is closely tied to market liquidity and the number of listed companies, meaning that markets with more trading activity tend to be more liquid and have more companies listed

Generally, markets with high liquidity and more listed companies tend to have higher turnover ratios, but market capitalization doesn't seem to have a strong positive relationship with these factors. Instead, larger market capitalizations are somewhat inversely related to trading activity and the number of listed companies.

LISTED COMPANIES

Considering each single indicators one-by-one helps in performing a more detailed analysis. To begin, we consider the listed companies to get an overview of how much companies have been formed or have been gone public for the past years. In details, will compare the number of listed company in 2012 with the ones in 2022 (last available year). The code below performs this task.

```
In [23]: #keep just the year 2012 and 2022
listcomp = mrkdf.loc[(mrkdf["date"] == "2012-01-01") | (mrkdf["date"] == #keep just the column date, state and listed_comp
listcomp = listcomp.loc[:, ['date', "state", "listed_comp"]]
# Assuming your DataFrame is called listcomp
listcomp_pivot = listcomp.pivot(index='state', columns='date', values='li
# Reset the column index so that "date" is removed
listcomp_pivot.columns = listcomp_pivot.columns.get_level_values(0)

# Alternatively, you can also convert the dates to string if they are not
listcomp_pivot.columns = listcomp_pivot.columns.astype(str)

# Display the cleaned pivoted DataFrame
listcomp_pivot
```

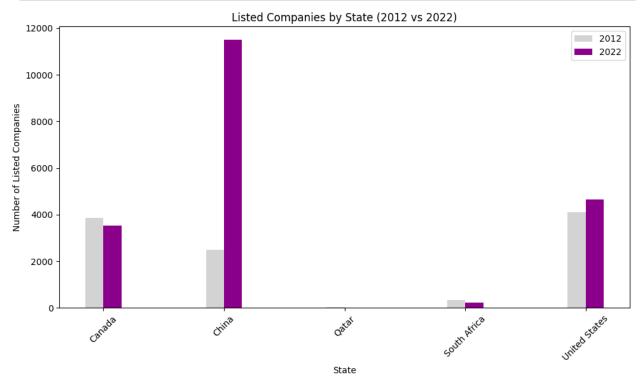
Out[23]:

state		
Canada	3874.0	3534.0
China	2494.0	11497.0
Qatar	42.0	0.0
South Africa	338.0	237.0
United States	4102.0	4642.0

date 2012-01-01 2022-01-01

Although numbers are meaningful, plots provide a quicker way to interpret the data.

```
In [24]:
         # Set the figure size
         plt.figure(figsize=(10, 6))
         # Set the positions for the bars on the x-axis
         states = listcomp_pivot.index
         years = listcomp_pivot.columns
         x = np.arange(len(states)) # The label locations
         width = 0.15 # The width of the bars
         # Create bar plots for both years
         plt.bar(x - width/2, listcomp_pivot['2012-01-01'], width, label='2012', c
         plt.bar(x + width/2, listcomp_pivot['2022-01-01'], width, label='2022', c
         # Add labels, title, and custom x-axis tick labels
         plt.xlabel('State')
         plt.ylabel('Number of Listed Companies')
         plt.title('Listed Companies by State (2012 vs 2022)')
         plt.xticks(x, states, rotation=45) # Rotate state labels for better read
         # Add a legend
         plt.legend()
         # Save the figure to the img directory
         plt.savefig('img/ListCompanies.png', bbox_inches='tight')
         # Display the plot
         plt.tight_layout()
         plt.show()
```



Not surprisingly, China has both the greatest number of public companies and has witnessed the largest growth in this number. This may be due to the large size of its

territory or new policies that have encouraged companies to go public or attracted foreign investments.

Following China are the United States. Interestingly, in 2012, the U.S. had more listed companies than China, but the tremendous growth China has experienced since then has surpassed U.S. numbers.

In contrast, Canada and South Africa have seen a decline in the number of publicly listed companies.

A special note on Qatar: the number of listed companies in 2022 is a missing value, but it's almost certain that Qatar's number could not compete with the other countries.

MARKET CAPITALIZATION & MARKET LIQUIDITY

Market Capitalization

According to the World Bank, market capitalization (also known as market value) is the share price multiplied by the number of outstanding shares (including all share classes) for listed domestic companies. In a nutshell, market capitalization gives an indication of the size of a country's public market.

Now, let's plot these values for each country.

```
In [25]: #add a column displaying just year
         mrkCapclean["year"] = pd.to_datetime(mrkCapclean["date"])
         mrkCapclean["year"] = mrkCapclean["year"].dt.year
In [26]: #define the plot
         fid, ax = plt.subplots()
         #focus on the mrk Cap (mrkCapclean df) and plot to check the changes in m
         plt.plot(mrkCapclean["year"], mrkCapclean["Canada"], label = "Canada", co
         plt.plot(mrkCapclean["year"] , mrkCapclean["China"], label = "China", col
         plt.plot(mrkCapclean["year"] , mrkCapclean["Qatar"], label = "Qatar", col
         plt.plot(mrkCapclean["year"] , mrkCapclean["United States"], label = "USA
         plt.plot(mrkCapclean["year"] , mrkCapclean["South Africa"], label = "Sout
         #add horizontal grids
         ax.grid(axis = "y")
         #add the legend
         plt.legend(loc='upper left', bbox_to_anchor=(1, 1))
         #add the title
         plt.title("Market Capitalization from 2012 to 2022")
         # Save the figure to the img directory
```

```
plt.savefig('img/MarketCap.png', bbox_inches='tight')
#show the chart
plt.show()
```



Let's make the chart fancier by making it interactive.

```
In [27]: import plotly graph objects as go
         # Create traces for each country
         fig = go.Figure()
         fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean["Canada"],
                                   mode='lines+markers', name='Canada',
                                   line = dict(color = "mediumorchid")))
         fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean["China"],
                                   mode='lines+markers', name='China',
                                   line = dict(color = "darkred")))
         fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean["Qatar"],
                                   mode='lines+markers', name='Qatar',
                                   line = dict(color = "darkgreen")))
         fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean["United Sta
                                   mode='lines+markers', name='USA',
                                   line = dict(color = "mediumblue")))
         fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean["South Afri
                                   mode='lines+markers', name='South Africa',
                                   line = dict(color = "darkorange")))
         # Add a grid using plotly's layout settings
         fig.update_layout(
             title='Market Capitalization from 2012 to 2022 ',
```

```
xaxis_title='Year',
  yaxis_title='Market Capitalization (millions USD)',
  xaxis=dict(showgrid=False),
  yaxis=dict(showgrid=True),
)

# Save the figure to the img directory
save_plotly_figure(fig, 'img/marketCapInt', format='png')

# Show interactive chart
fig.show()
```

Figure saved as img/marketCapInt.png

Interestingly, the country with the highest market capitalization (in millions of USD) is South Africa. Moreover, it has the most volatility. This may be due to its abundant resources and favorable demographics, which continue to attract both domestic and foreign investments in this fast-growing, promising market.

The U.S. and Canada are very close in terms of market capitalization. Not only do they have similar values, but they also tend to follow the same trends, moving up or down simultaneously.

China, on the other hand, has the lowest overall market capitalization, with a value that is nearly one-sixth of South Africa's.

Market Liquidity

Turning to market liquidity, the WB defines it as the value of shares traded, i.e the total number of shares traded, both domestic and foreign, multiplied by their respective matching prices. Briefly, it is the main measure to understand how fast market's assets can be converted into cash without affecting its market price.

Let's analyze this indicator.

```
line = dict(color = "darkgreen")))
fig.add_trace(go.Scatter(x=mrkLiqclean["year"], y=mrkLiqclean["United Sta
                         mode='lines+markers', name='USA',
                         line = dict(color = "mediumblue")))
fig.add_trace(go.Scatter(x=mrkLiqclean["year"], y=mrkLiqclean["South Afri
                         mode='lines+markers', name='South Africa',
                         line = dict(color = "darkorange")))
# Add a grid using plotly's layout settings
fig.update_layout(
    title='Market Liquidity from 2012 to 2022',
   xaxis_title='Year',
   yaxis_title='Market Liquidity (% of GDP)',
   xaxis=dict(showqrid=False),
   yaxis=dict(showgrid=True),
# Save the figure to the img directory
save_plotly_figure(fig, 'img/marketLiqInt', format='png')
# Show interactive chart
fig.show()
```

Figure saved as img/marketLiqInt.png

Few trend stands out while speaking about market liquidity. Firstly, volatility in China has an extraordinary peak (that's also the highest value) in 2015 followed by a sharp decline. This is the opposite to the relatively stable trends regarding the US and Canada. Speaking of US and Canada, the close values along similar trends between these two countires suggest a strong correlation in their market activities. Note also that the US has the highest and most consistent market liquidity. Secondly, South Africa grow in liqudity until 2016. However, the subsequent decline raises questions about underlying economic or market factors. Finally there is Qatar, with a relative small trading activity related to other countries.

Market Capitalization and Market Liquidity

Market capitalization and market liquidity describe different aspects of public market. By taking them into account altogether, it is possible to have a 360-degree view of a country financial market.

Let's plot these indicators in the same chart to visualize their relationship. We will start with data about Canada.

```
line = dict(color = "lightgrey")))
fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean["Canada"],
                         mode='lines+markers', name='market_cap',
                         line = dict(color = "purple")))
# Add a grid using plotly's layout settings
fig.update layout(
    title='Canada Market Liquidity vs market Capitalization',
   xaxis_title='Year',
   yaxis_title='Value',
   xaxis=dict(showgrid=False,
               zeroline=True,
               zerolinecolor='black'),
   yaxis=dict(showgrid=True,
               gridcolor = "black",
               zeroline=True,
               zerolinecolor='black'),
   hovermode="x",
   plot_bgcolor='white', # Background of the plot area
   paper_bgcolor='white' # Background of the outside area
)
# Show interactive chart
fig.show()
```

It will be time and space consuming plotting a chart for each single country. To avoid that, we will organize the various plots into a 2x3 grid of subplots.

```
In [30]: # Define subplot grid (3 rows x 2 columns)
         fig = make_subplots(
             rows=3, cols=2,
             subplot_titles=('Canada', 'China', 'Qatar', 'United States', 'South A
             vertical_spacing=0.2, horizontal_spacing=0.2,
             specs=[[{"secondary_y": True}, {"secondary_y": True}], # Enable seco
                    [{"secondary_y": True}, {"secondary_y": True}],
                    [{"secondary_y": True}, {"secondary_y": True}]]
         )
         # List of countries
         countries = ['Canada', 'China', 'Qatar', 'United States', 'South Africa']
         # Add traces for each country without legend
         for i, country in enumerate(countries):
             row = i // 2 + 1
             col = i % 2 + 1
             # Add market_lig trace (percentage of GDP) on the primary y-axis (lef
             fig.add_trace(go.Scatter(x=mrkLiqclean["year"], y=mrkLiqclean[country
                                       mode='lines+markers', line=dict(color="light
                                       name='Market Liquidity (% of GDP)',
                                       showlegend=False),
```

```
row=row, col=col, secondary y=False) # False means lef
   # Add market_cap trace (USD) on the secondary y-axis (right)
   fig.add_trace(go.Scatter(x=mrkCapclean["year"], y=mrkCapclean[country
                             mode='lines+markers', line=dict(color="darkm
                             name='Market Capitalization (USD)',
                             showlegend=False),
                  row=row, col=col, secondary_y=True) # True means right
# Add legend traces for the entire figure
fig.add_trace(go.Scatter(
   x=[None], y=[None],
   mode='lines',
    line=dict(color="lightgrey"),
   name='Market Liquidity (% of GDP)',
   showlegend=True
))
fig.add_trace(go.Scatter(
   x=[None], y=[None],
   mode='lines',
    line=dict(color="purple"),
   name='Market Capitalization (USD)',
   showlegend=True
))
# Update layout for the entire figure
fig.update_layout(
   title_text='Market Liquidity (% of GDP) vs Market Capitalization (USD
   title x=0.5,
   title_y=0.95,
   xaxis_title='Year',
    showlegend=True, # Enable legend
    leaend=dict(
       x=0.6, # Position the legend outside of the plot area
       y=0.05,
       traceorder='normal',
        orientation='v'
    ),
   plot_bgcolor='white',
   paper_bgcolor='white',
   margin=dict(l=40, r=150, t=70, b=40), # Adjust right margin to fit t
    font=dict(size=12) # Set global font size
# Reduce font size for subplot titles
fig.update_layout(annotations=[dict(font=dict(size=13)) for annotation in
# Update x and y axis titles for each subplot
for i in range(1, 4): # For rows 1, 2, 3
    for j in range(1, 3): # For columns 1, 2
        fig.update_xaxes(title_text="Year", title_font=dict(size=9), row=
        # Update left y-axis (Market Liquidity)
       fig.update_yaxes(title_text="Mrk Liq (% of GDP)", title_font=dict
```

Figure saved as img/mrkCapMrkLiqInt.png

Even though this charts may appears as overwelming, they provide some important insights.

The first one is that it is not possible to state that one is always higher than the other. Some countries have a bigger market liquidity, while others have a greater market capitalization. The second one is that the 0.2 correlation we computed above is confirmed by this charts. Indeed, market capitalization and market liquidity do not appear to influence each other that much.

The final test to check their relation is to plot a scatterplot of market capitalization vs market liquidity.

```
In [31]: from plotly.subplots import make_subplots
         import plotly.graph objects as go
         # Define subplot grid (3 rows x 2 columns)
         fig = make_subplots(rows=3, cols=2,
                             subplot_titles=('Canada', 'China', 'Qatar', 'United S
                             vertical_spacing=0.2, horizontal_spacing=0.2)
         # List of countries
         countries = ['Canada', 'China', 'Qatar', 'United States', 'South Africa']
         # Add scatter traces for each country (Market Liquidity vs Market Capital
         for i, country in enumerate(countries):
             row = i // 2 + 1
             col = i % 2 + 1
             # Scatter plot: x = market_cap, y = market_liq
             fig.add_trace(go.Scatter(x=mrkCapclean[country], y=mrkLiqclean[countr
                                      mode='markers', marker=dict(color="darkmagen
                                       name=country, showlegend=False),
                            row=row, col=col)
```

```
# Update layout for the entire figure
fig.update_layout(
    title_text='Market Liquidity vs Market Capitalization (Scatter Plot)'
    title_x=0.5,
   title_y=0.95,
   xaxis_title='Market Capitalization',
   yaxis_title='Market Liquidity',
   plot_bgcolor='white',
   paper_bgcolor='white',
   margin=dict(l=40, r=150, t=70, b=40), # Adjust right margin to fit t
    font=dict(size=10) # Set global font size
# Reduce font size for subplot titles
fig.update_layout(annotations=[dict(font=dict(size=13)) for annotation in
# Update x and y axis titles for each subplot
for i in range(1, 4): # For rows 1, 2, 3
    for j in range(1, 3): # For columns 1, 2
        fig.update xaxes(title text="Market Capitalization", title font=d
        fig.update_yaxes(title_text="Market Liquidity", title_font=dict(s
# Update x and y axes for each subplot
for axis in fig.select xaxes():
    axis.update(showgrid=True, zeroline=False, gridcolor='lightgrey')
for axis in fig.select_yaxes():
    axis.update(showgrid=True, zeroline=False, gridcolor='lightgrey')
# Save the figure to the img directory
save_plotly_figure(fig, 'img/CapLiqScatterInt', format='png')
# Show the interactive scatter plot
fig.show()
```

Figure saved as img/CapLiqScatterInt.png

Scatterplots provide a comprehensive view of market dynamics in different countries.

In China and Canada, these two indicators (market capitalization and market liquidity) show the most linear relationship. In both countries, market liquidity tends to increase as market capitalization grows. South Africa exhibits a slightly linear relationship as well, though less pronounced.

On the other hand, Qatar shows the most clustered data: market capitalization remains consistently within the range of 70-120, while market liquidity varies slightly between 5% and 30%.

In the United States, no clear trend can be identified between market liquidity and market capitalization.

TURNOVER RATIO

To conclude, we will analyze turnover ratio. Turnover ratio is the value of domestic shares traded divided by their market capitalization. By considering the mean, we will get an idea about where shares are traded the most.

Out[32]:

Country Average Turnover Ratio 0 Canada 66.00 1 China 245.22 2 Qatar 14.89 3 South Africa 30.74 4 United States 75.96

```
In [33]: # Create the interactive bar chart with different colors for each country
         fig = go.Figure(data=[
             go.Bar(name='Average Turnover Ratio', x=turnRatiomean['Country'],
                    y=turnRatiomean['Average Turnover Ratio'],
                    marker_color=['mediumorchid', 'darkred', 'darkgreen', "darkora
                    width=[0.5, 0.5, 0.5, 0.5, 0.5]
         1)
         fig.update layout(
             title="Average Turnover Ratio by Country",
             xaxis_title="Country",
             yaxis_title="Average Turnover Ratio",
             plot_bgcolor='white', # Background color of the plot area
             paper_bgcolor='white',  # Background color outside the plot
             hovermode='x',
             # Add gridlines for x and y axes
             xaxis=dict(
```

```
showgrid=True, # Show gridlines for x-axis
    gridcolor='lightgrey' # Gridline color for x-axis
),
yaxis=dict(
    showgrid=True, # Show gridlines for y-axis
    gridcolor='lightgrey' # Gridline color for y-axis
)
)

# Save the figure to the img directory
save_plotly_figure(fig, 'img/TurnoverRatio', format='png')

# Show the interactive plot
fig.show()
```

Figure saved as img/TurnoverRatio.png

The turnover ratio data reveals significant differences in market activity across countries. China stands out with the highest turnover ratio (245.22), indicating a very active and liquid market.

The United States (75.96) and Canada (66.00) show moderate levels of activity, reflecting stable and mature markets. South Africa (30.74) has lower activity, while Qatar (14.89) has the least trading activity, suggesting a less liquid market.

S&P Global Equity Indices

According to the World Bank, the S&P Global Equity Indices measure the U.S. dollar price changes in stock markets covered by the S&P/IFCI and S&P/Frontier BMI country indices.

As mentioned earlier, this data is available annually for each country, and there are no missing values.

Since the goal of the analysis is to compare different countries, we will conduct a detailed analysis of this indicator. Additionally, we will reintroduce the data for both Italy and France.

```
In [34]: SP500Indexclean["year"] = pd.to_datetime(SP500Indexclean["date"])
    SP500Indexclean["year"] = SP500Indexclean["year"].dt.year
    SP500Indexclean
```

Out[34]:

	date	Canada	China	France	Italy	Qatar	South Africa	United States	year
0	2012-01- 01	5.99	17.17	15.23	11.03	-1.86	15.75	13.41	2012
1	2013-01- 01	2.98	7.26	17.99	23.06	23.97	-7.45	29.60	2013
2	2014-01- 01	-2.14	3.03	-0.54	-12.02	23.00	3.86	11.39	2014
3	2015-01- 01	-26.17	-6.01	8.53	3.20	-18.65	-26.62	-0.73	2015
4	2016-01- 01	22.56	-2.02	4.86	-13.00	2.19	17.62	9.54	2016
5	2017-01- 01	13.75	46.03	9.26	29.77	-16.77	30.62	19.42	2017
6	2018-01- 01	-19.38	-20.52	-10.95	-20.95	22.22	-25.89	-6.24	2018
7	2019-01- 01	25.32	19.26	26.37	24.54	-1.90	8.55	28.88	2019
8	2020- 01-01	4.48	27.87	-7.14	2.68	-4.04	-7.02	16.26	2020
9	2021-01- 01	22.68	-20.65	28.85	14.87	12.23	5.44	26.89	2021
10	2022- 01-01	-14.80	-23.62	-9.50	-19.40	-11.26	-7.15	-19.44	2022

Let's compute some summary statistics.

In [35]: round(SP500Indexclean.iloc[:, 1:7].describe(), 3)

Out[35]:

	Canada	China	France	Italy	Qatar	South Africa
count	11.000	11.000	11.000	11.000	11.000	11.000
mean	3.206	4.345	7.542	3.980	2.648	0.701
std	17.576	22.048	13.788	18.262	15.664	17.729
min	-26.170	-23.620	-10.950	-20.950	-18.650	-26.620
25%	-8.470	-13.265	-3.840	-12.510	-7.650	-7.300
50%	4.480	3.030	8.530	3.200	-1.860	3.860
75%	18.155	18.215	16.610	18.965	17.225	12.150
max	25.320	46.030	28.850	29.770	23.970	30.620

And plot the data to visualize how SP500 Index moved in each country.

```
In [36]:
         # Create traces for each country
         fig = go.Figure()
         fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["Ca
                                   mode='lines+markers', name='Canada',
                                   line = dict(color = "mediumorchid")))
         fig.add trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["Ch
                                   mode='lines+markers', name='China',
                                   line = dict(color = "darkred")))
         fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["Qa
                                   mode='lines+markers', name='Qatar',
                                   line = dict(color = "darkgreen")))
         fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["Un
                                   mode='lines+markers', name='USA',
                                   line = dict(color = "mediumblue")))
         fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["So
                                  mode='lines+markers', name='South Africa',
                                   line = dict(color = "darkorange")))
         fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["It
                                  mode='lines+markers', name='Italy',
                                   line = dict(color = "red"))) # Set marker color
         fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean["Fr
                                   mode='lines+markers', name='France',
                                   line = dict(color = "dimgrey")))
         # Add a grid using plotly's layout settings
         fig.update_layout(
             title='S&P500 Index over the years',
             xaxis_title='Year',
             yaxis_title='S&P500 Index % change',
             xaxis=dict(showgrid=False),
             yaxis=dict(showqrid=True),
         # Save the figure to the img directory
         save_plotly_figure(fig, 'img/SP500', format='png')
         # Show interactive chart
         fig.show()
```

Figure saved as img/SP500.png

Plotted altogether, it is quite challenging to spot any kind of trend. To ease up this process, we will split the chart into subplots.

```
# List of countries
countries = ['Canada', 'China', 'Qatar', 'United States', 'South Africa',
# List of colors
colors = ['mediumorchid', 'darkred', 'darkgreen', "mediumblue", "darkoran
# Add traces for each country without legend
for i, country in enumerate(countries):
    row = i // 2 + 1
    col = i % 2 + 1
    # Add market_lig trace
    fig.add_trace(go.Scatter(x=SP500Indexclean["year"], y=SP500Indexclean
                             mode='lines+markers', line=dict(color=colors
                             showlegend=False),
                  row=row, col=col)
# Update layout for the entire figure
fig.update layout(
    title_text='SP500 Index over the years',
    title x=0.5,
    title_y=0.95,
    showlegend=True, # Enable legend
    legend=dict(
        x=0.6, # Position the legend outside of the plot area
        y=0.05,
        traceorder='normal',
        orientation='v'
    ),
    plot_bgcolor='white',
    paper bgcolor='white',
    margin=dict(l=40, r=150, t=70, b=40), # Adjust right margin to fit t
    font=dict(size=12) # Set global font size
# Reduce font size for subplot titles
fig.update_layout(annotations=[dict(font=dict(size=13)) for annotation in
# Update x and y axis titles for each subplot
for i in range(1, 5): # For rows 1, 2, 3, 4
    for j in range(1, 3): # For columns 1, 2
        fig.update_xaxes(title_text="Year", title_font=dict(size=9), tick
        fig.update_yaxes(title_text="% change", title_font=dict(size=9),
# Update x and y axes for each subplot
for axis in fig.select_xaxes():
    axis.update(showgrid=True, zeroline=False, gridcolor='lightgrey')
for axis in fig.select_yaxes():
    axis.update(showgrid=True, zeroline=False, gridcolor='lightgrey')
# Save the figure to the img directory
save_plotly_figure(fig, 'img/SP500Subplot', format='png')
# Show the interactive chart
```

```
fig.show()
```

Figure saved as img/SP500Subplot.png

China and South Africa display high volatility, with large swings in performance. For example, China's 46% increase in 2017 is followed by a -20% drop in 2018. The United States generally shows positive growth, with notable highs like 29% in 2013 and a few downturns, such as -19% in 2022. Canada, France, and Italy show a mix of positive and negative trends, indicating fluctuating market conditions. Finally, Qatar experiences erratic performance, with significant growth in some years (23.97% in 2013) and downturns in others (-18.65% in 2015).

While general insights are certainly valuable, what if we want to dig deeper? For instance, can we predict the future values of the S&P 500 Index based on this data?

We will explore this by forecasting future values for the U.S. market.

S&P 500 Index Forecasting

As aforementioned, here we will focus just on US. Furthermore, we will stretch the time range. Indeed, we will load data from 1990 (first available data) to 2022 (last available data).

Let's build a new df (US_SP) with these features.

```
In [38]: #load the data from WB API just for US and from 1990 (first available) to
    #set ut just SP500 Global index as indicator and give it a clear name
    SP = {"CM.MKT.INDX.ZG": "US_SP500"}
    #create a tuples for the dates we are interested into
    dateSP = ("1990-01-01", "2022-01-01")

#grab indicators above for countires above and load into data frame
    US_SP = wbdata.get_dataframe(SP, country="US", parse_dates=True, date = d

#transform it into a pandas df
    US_SP = pd.DataFrame(US_SP)
    #reset the index
    US_SP = US_SP.reset_index()
    #display the df
    US_SP
```

```
        Out [38]:
        date
        US_SP500

        0
        2022-01-01
        -19.442824

        1
        2021-01-01
        26.892736

        2
        2020-01-01
        16.258922
```

3	2019-01-01	28.878069
4	2018-01-01	-6.237260
5	2017-01-01	19.419965
6	2016-01-01	9.535016
7	2015-01-01	-0.726602
8	2014-01-01	11.390638
9	2013-01-01	29.601250
10	2012-01-01	13.405690
11	2011-01-01	-0.002480
12	2010-01-01	12.782079
13	2009-01-01	23.453817
14	2008-01-01	-38.485256
15	2007-01-01	3.529202
16	2006-01-01	13.619200
17	2005-01-01	3.001582
18	2004-01-01	8.993540
19	2003-01-01	26.380037
20	2002-01-01	-23.366249
21	2001-01-01	-13.042456
22	2000-01-01	-10.139187
23	1999-01-01	19.526045
24	1998-01-01	26.668590
25	1997-01-01	31.008181
26	1996-01-01	20.263666
27	1995-01-01	34.110654
28	1994-01-01	-1.539286
29	1993-01-01	7.055151
30	1992-01-01	4.464264
31	1991-01-01	26.306705
32	1990-01-01	-6.559140

Let's perform to routine check-ups: there should not be NaN and we will transform

"date" column into datetime type.

```
In [39]: #count if there are missing values
    print(US_SP.isnull().sum())
    #transform the date into datetime format
    US_SP["date"] = pd.to_datetime(US_SP["date"])
    #add the year column
    US_SP["year"] = US_SP["date"].dt.year

date    0
    US_SP500    0
    dtype: int64
```

Let's briefly plot it along with computing summary statistics to have an idea of how the index behaved.

```
In [40]: # Create traces for each country
         fig = go.Figure()
         fig.add_trace(go.Scatter(x=US_SP["year"], y=US_SP["US_SP500"],
                                   mode='lines+markers', name='US_SP500',
                                   line=dict(color="mediumblue")))
         # Add a grid using plotly's layout settings
         fig.update_layout(
             title='US S&P500 Index over the years (1990-2022)',
             xaxis_title='Year',
             yaxis_title='SP500 Index (% Change)',
             xaxis=dict(showgrid=False),
             yaxis=dict(showgrid=True),
         # Save the figure to the img directory
         save_plotly_figure(fig, 'img/USSP500', format='png')
         # Show interactive chart
         fig.show()
         #compute statistics for the df
         print("summary statistics for the US SP500:")
         US_SP["US_SP500"].describe()
```

Figure saved as img/USSP500.png summary statistics for the US SP500:

```
Out[40]: count
                  33.000000
                   9.000129
         mean
                  17.367465
         std
                 -38,485256
         min
         25%
                  -0.726602
         50%
                  11.390638
         75%
                  23.453817
                  34.110654
         Name: US_SP500, dtype: float64
```

The chart shows a continuos up and down. It is worth to note the lowest point in 2008, as a consequence of the global financial crisis, and the downfall in 2021, the COVID year. Overall, the % change has been positive for the most of the time. On average, the % changes was around 9% yearly.

Now that we have a general idea, we can begin the forecasting phase. Prior to setting a model up, it is good practice to split the data into training and testing. In this specific case, we will follow the standard 80% (training) - 20% (testing) rule.

```
In [41]: # Sort the dataframe by date in reverse order (latest year first)
US_SP = US_SP.sort_values(by="date").reset_index(drop=True)

# Total number of observations
total_observations = len(US_SP)

# Split index for 80% training data
split_index = int(total_observations * 0.8)

# Split the dataframe into training (80%) and test (20%) based on date
training = US_SP.iloc[:split_index]
test = US_SP.iloc[split_index:]

# Display the training and test dataframes
print("Training Data:\n", training)
print("\nTest Data:\n", test)
```

```
Training Data:
          date
                 US SP500
                           year
   1990-01-01 -6.559140
                          1990
   1991-01-01 26.306705
1
                          1991
2
  1992-01-01
                4.464264
                          1992
3
   1993-01-01
                7.055151
                          1993
4
   1994-01-01 -1.539286
                          1994
5
   1995-01-01 34.110654
                          1995
6
  1996-01-01 20.263666
                          1996
7
  1997-01-01
               31.008181
                          1997
8
   1998-01-01
               26.668590
                          1998
  1999-01-01 19.526045
                          1999
10 2000-01-01 -10.139187
                          2000
11 2001-01-01 -13.042456
                          2001
12 2002-01-01 -23.366249
                          2002
13 2003-01-01
               26.380037
                          2003
14 2004-01-01
                8.993540
                          2004
15 2005-01-01
                3.001582
                          2005
16 2006-01-01
              13.619200
                          2006
17 2007-01-01
                3.529202
                          2007
18 2008-01-01 -38.485256
                          2008
19 2009-01-01 23.453817
                          2009
20 2010-01-01 12.782079
                          2010
21 2011-01-01 -0.002480
                          2011
22 2012-01-01
               13.405690
                          2012
23 2013-01-01 29.601250
                          2013
24 2014-01-01
               11.390638
                          2014
25 2015-01-01 -0.726602
                          2015
Test Data:
                 US_SP500
          date
                           year
26 2016-01-01
                9.535016
                          2016
27 2017-01-01 19.419965
                          2017
28 2018-01-01 -6.237260
                          2018
29 2019-01-01
               28.878069
                          2019
30 2020-01-01
               16.258922
                          2020
31 2021-01-01
               26.892736
                          2021
32 2022-01-01 -19.442824
                          2022
```

Then, we must perform a stationarity test to understand whether or not our data is stationary. More in details, we will employ an ADF test.

We will first set up a function, then perform the ADF both with BIC and AIC as parameters.

```
In [42]: # Set a function to perform and interpret the ADF

def adf_test(series, lag):
    result = adfuller(series, autolag=lag) #lag can be chosen by the use
    print(f"Lag selection by: {lag}")
    print('ADF Statistic:', result[0])
    print('p-value:', result[1])
    print('Critical Values:')
    for key, value in result[4].items():
```

```
print(f' {key}, {value}')
     # Check for stationarity
     if result[1] <= 0.05:
         print("The series is stationary.")
     else:
         print("The series is non-stationary.")
 # Run ADF test on US_SP500 series with BIC
 adf_test(US_SP["US_SP500"], "BIC")
 # Run ADF test on US_SP500 series with AIC
 adf_test(US_SP["US_SP500"], "AIC")
Lag selection by: BIC
ADF Statistic: -5.424589596816409
p-value: 3.0068321206431566e-06
Critical Values:
   1%, -3.653519805908203
   5%, -2.9572185644531253
   10%, -2.6175881640625
The series is stationary.
Lag selection by: AIC
ADF Statistic: -5.424589596816409
p-value: 3.0068321206431566e-06
Critical Values:
   1%, -3.653519805908203
   5%, -2.9572185644531253
   10%, -2.6175881640625
The series is stationary.
```

The series is stationary. This mean there is not the necessity to differentiate since many models require stationarity.

Moreover, we will set up also a function to compute accuracy measures of different models. It will be useful later on.

```
In [43]: #set up a function to compute accuracy measures
def accuracy_measures(testing, prediction):
    # Calculate Mean Absolute Error (MAE)
    mae = mean_absolute_error(testing, prediction)

# Calculate Mean Squared Error (MSE)
    mse = mean_squared_error(testing, prediction)

# Calculate Root Mean Squared Error (RMSE)
    rmse = np.sqrt(mse)

# Calculate Mean Absolute Percentage Error (MAPE)
    mape = np.mean(np.abs((testing - prediction) / testing)) * 100

# Calculate R-squared (R²)
    r2 = r2_score(testing, prediction)
```

HOLT-WINTER ESTIMATION

The first model we will try is the Holt-Winter Estimation is composed by three different smoothing methods. Its peculiarity is that it succeeds in taking into consideration both the trend and seasonality.

However, our data does not appear to have neither a trend nor a seasonality. As a consequence, the HW may not be the best model.

Out[44]:		Actual	Forecast
	26	9.535016	8.526969
	27	19.419965	8.526969
	28	-6.237260	8.526969
	29	28.878069	8.526969
	30	16.258922	8.526969
	31	26.892736	8.526969
	32	-19.442824	8.526969

As predictable, the model display the same value for all the future years. This is one more things against the use of this model.

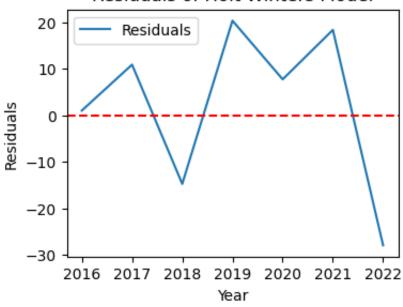
Residuals diagnostics and accuracy measures helps in evaluating the model. The code below computes them.

```
In [45]: from statsmodels.stats.diagnostic import acorr_ljungbox
         import scipy.stats as stats
         # Calculate residuals (Actual - Forecast)
         residuals = test['US_SP500'] - hw_forecast
         # Plot the residuals over time
         plt.figure(figsize=(4,3))
         plt.plot(test['year'], residuals, label='Residuals')
         plt.axhline(y=0, color='r', linestyle='--')
         plt.title('Residuals of Holt-Winters Model')
         plt.xlabel('Year')
         plt.ylabel('Residuals')
         plt.legend()
         plt.show()
         # Plot the distribution of residuals (Histogram and KDE)
         plt.figure(figsize=(4.12,3))
         sns.histplot(residuals, kde=True, color='blue', bins=15)
         plt.title('Residuals Distribution')
         plt.show()
         # Q-Q plot to check normality of residuals
         plt.figure(figsize=(4,3))
         stats.probplot(residuals, dist="norm", plot=plt)
         plt.title('Q-Q Plot of Residuals')
         plt.show()
         # Plot ACF (Autocorrelation Function) of residuals
         plot_acf(residuals, lags=6)
         plt.title('Autocorrelation of Residuals')
```

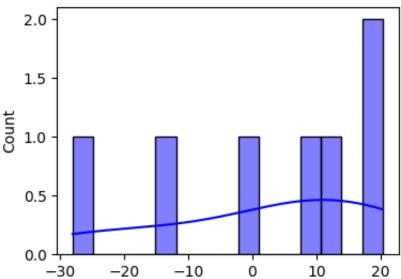
```
plt.show()

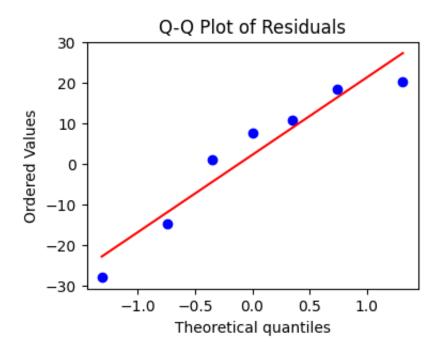
# Ljung-Box Test to check for autocorrelation in residuals
ljung_box_test = acorr_ljungbox(residuals, lags=[6], return_df=True)
print("Ljung-Box Test Results:")
print(ljung_box_test)
```

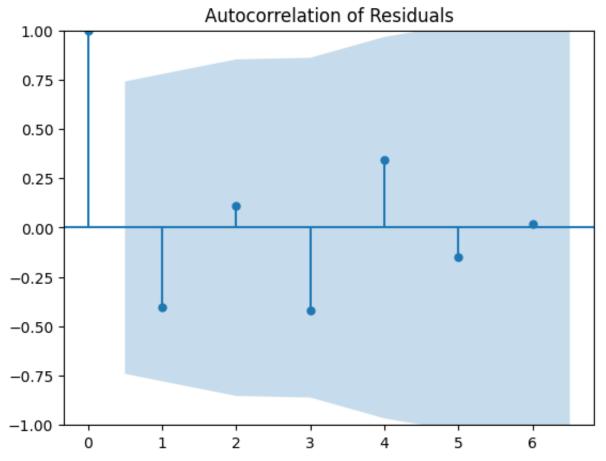
Residuals of Holt-Winters Model



Residuals Distribution







Ljung-Box Test Results: lb_stat lb_pvalue 6 7.793112 0.253656

Check the accuracy measures.

```
In [46]: #compute accuracy measures:
    accuracy_measures(test["US_SP500"], hw_forecast)
```

fundamental metrics are:

Mean Absolute Error (MAE): 14.44055495255945

Mean Squared Error (MSE): 275.88815410202955

Root Mean Squared Error (RMSE): 16.609881218781474

Mean Absolute Percentage Error (MAPE): 90.50727454144003%

R-squared (R²): -0.018369914567093026

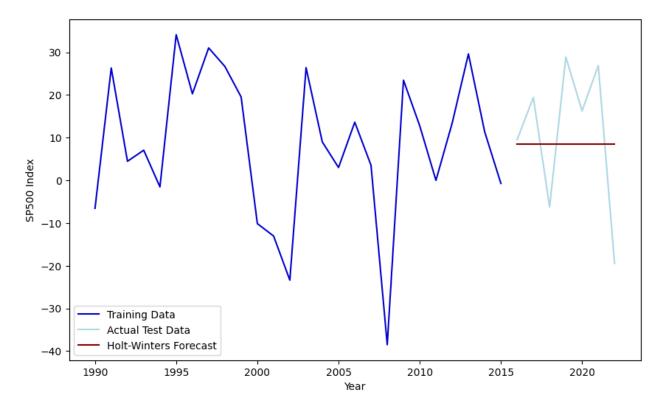
Standard Error of Regression (SER): 19.653076495623818

Neither the residuals nor the accuracy measures look good. The latter indicate poor performance. The high MAPE (90.51%) shows large percentage errors in predictions, while the negative R-squared (-0.018) suggests the model fails to explain the variance in the data. The MAE and RMSE are also relatively high, pointing to significant deviations between predicted and actual values.

Overall, the model needs improvement to enhance predictive accuracy. To double check this conclusion, we will plot the estimated values against the actual ones.

```
In [47]: #plot the results
    plt.figure(figsize=(10,6))
    plt.plot(training['year'], training['US_SP500'], label='Training Data', c
    plt.plot(test['year'], test['US_SP500'], label='Actual Test Data', color=
    plt.plot(test['year'], hw_forecast, label='Holt-Winters Forecast', color=
    plt.xlabel('Year')
    plt.ylabel('SP500 Index')
    plt.legend(loc='best')

#save the plot
    plt.savefig('img/HWtest.png', bbox_inches='tight')
#show it
    plt.show()
```



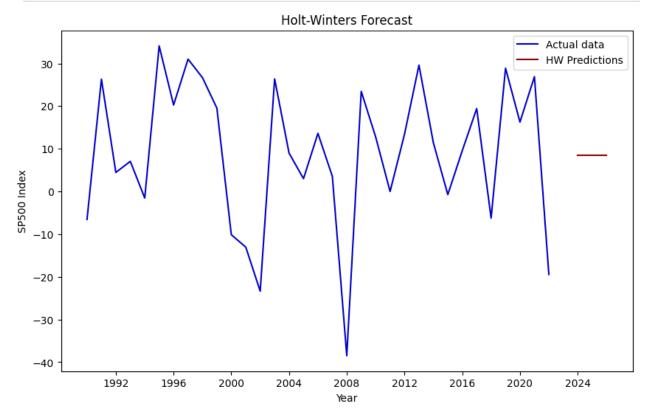
As discussed above, these are poor predictions.

For the sake of completness, we will employ the HW model on the entire series too.

```
In [48]:
         # Chose alpha and beta
         alpha = 0.2 # Adjust this value for level smoothing
         beta = 0.2
                      # Adjust this value for trend smoothing
         #Fit Holt-Winters Exponential Smoothing model for entire data
         HW_US = ExponentialSmoothing(US_SP['US_SP500'],
                                       trend = None, # no trend component
                                       seasonal=None, # No seasonality in this cas
                                       initialization method="estimated").fit(smoot
         # Forecast the test data length
         # Create a date range for the next 3 years
         last_date = US_SP['date'].iloc[-1]
         HWUS_forecast = HW_US.forecast(steps = 3)
         # Combine forecast and actual values
         HWUS df = pd.DataFrame({
             'Actual': US_SP['US_SP500'],
             'Forecast': HWUS_forecast
         })
         print(HWUS_forecast)
        33
              8.487483
        34
              8.487483
        35
              8.487483
        dtype: float64
```

Plot the estimates.

```
# Display the actual values and future forecasts
In [49]:
         plt.figure(figsize=(10, 6))
         # Plot actual data
         plt.plot(US_SP["date"], US_SP["US_SP500"], label='Actual data', color = "
         # Create future dates for the forecast
         last date = US SP["date"].iloc[-1]
         future_dates = pd.date_range(start=last_date + pd.DateOffset(years=1), pe
         # Plot the forecasted values
         plt.plot(future_dates, HWUS_forecast, label='HW Predictions', color='dark
         plt.title('Holt-Winters Forecast')
         plt.xlabel('Year')
         plt.ylabel('SP500 Index')
         plt.legend()
         #save the plot
         plt.savefig('img/HW.png', bbox_inches='tight')
         #show it
         plt.show()
```



It is crystal-clear that estimates are not looking good. The question is: why? That may be a consequene of data that does not vary significantly or has low volatility. In this case, the smoothing estimation results in similar predictions (i.e the red stright line).

That is, there is the necessity to opt for a different model. Seeing the fluctuations displayed by the series, an ARIMA model could be the best choice.

ARIMA MODEL

Based on the series' feature, an Auto-Regressive Integrated Moving Average model would be the fittest choice to guess US SP500's future value. Note that there is an ARIMA variation, the SARIMA, that accounts also for seasonality in the series. However, our series does not has this feature. As a result, we will focus just on ARIMA.

To begin with, it is necessary to choose ARIMA paramaters (p,d,q). We know that the series is stationary, thus d = 0. For p and q, instead, the autoregressive and the partial-autoregressive plot come in handy.

Let's plot both by defining a function.

```
In [50]: #Define a function to display acf and pacf values
         def display_acf_pacf(series, nlags):
             Display ACF and PACF values for a given time series.
             Parameters:
             - series: The time series data as a pandas Series.

    nlags: Number of lags to consider for ACF and PACF.

             # Ensure the series is stationary
             result = adfuller(series)
             print(f"ADF Statistic: {result[0]}")
             print(f"p-value: {result[1]}")
             if result[1] < 0.05:
                 print("The series is stationary.")
             else:
                 print("The series is non-stationary. Consider differencing the da
             # Calculate ACF and PACF values
             acf_values = acf(series, nlags=nlags)
             pacf_values = pacf(series, nlags=nlags)
             # Create a DataFrame to display the results
              results_df = pd.DataFrame({
                  'Lag': range(nlags + 1),
                  'ACF': acf_values,
                  'PACF': pacf_values
             })
             plot acf(series)
             plot_pacf(series)
```

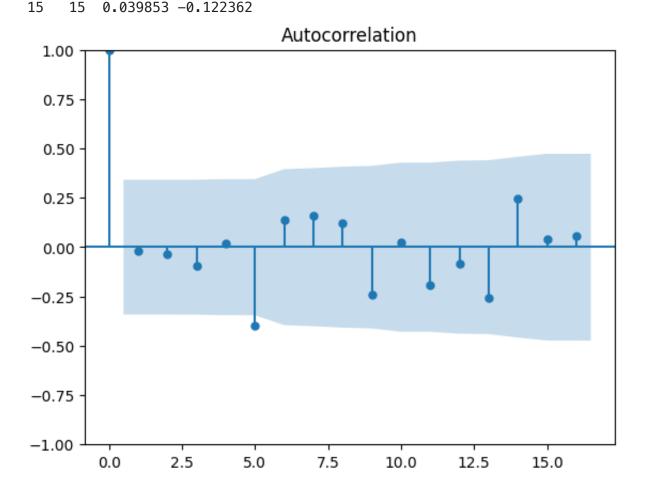
```
print(results_df)
```

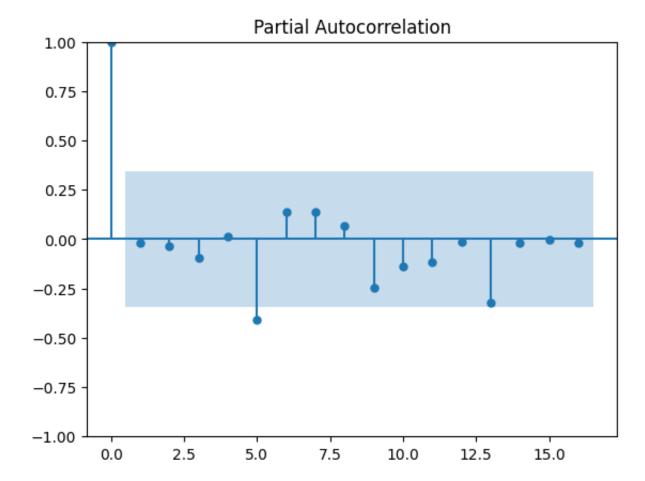
Compute the acf and pacf.

```
In [51]: display_acf_pacf(US_SP["US_SP500"], 15)
```

```
p-value: 3.0068321206431566e-06
The series is stationary.
    Lag
              ACF
                        PACF
0
         1.000000
                   1.000000
      0
1
      1 -0.019079 -0.019676
2
      2 -0.034590 -0.037223
3
      3 -0.093146 -0.104129
        0.016305
                   0.012728
5
      5 -0.400116 -0.484877
6
      6
         0.136183
                   0.182927
7
      7
         0.157316
                   0.185046
         0.122218
                   0.094342
9
      9 -0.242902 -0.392479
10
     10 0.022872 -0.222213
11
     11 -0.193248 -0.202772
12
     12 -0.086489 0.002133
     13 -0.258374 -0.692127
13
14
        0.247417 -0.069371
```

ADF Statistic: -5.424589596816409





According to the acf and pacf, the possible values for p and q are:

- p: 1 or 5
- q: 1 or 5

A model 5,0,5 is going to be too expensive for the little amount of data we have. The same is for the ARIMA(1,0,5). Thus, we will not consider that. The model left are:

- ARIMA(1,0,1)
- ARIMA(5,0,1)

For the sake of clarity, we are going to show only the ARIMA(5,0,1) (i.e the chosen) model. Yet, it is important to note that we tested even the ARIMA(1,0,1) model.

Let's fit our model.

```
In [52]: # Fit ARIMA model (p,d,q parameters need tuning based on ACF/PACF or a gr
arima = ARIMA(training["US_SP500"], order=(5,0,1)) # Adjust (p,d,q) as n
arima_fit = arima.fit()
```

And show the ARIMA (5,0,1) model summary.

```
In [53]: print(arima_fit.summary())
```

SARIMAX Results

========		JAN =========	========	========		
====	_					
Dep. Variab 26	le:	US_SP	500 No.	Observations:		
Model:		ARIMA(5, 0,	1) Log	Likelihood		-10
6.394						
Date: 8.788	Fr	i, 27 Sep 2	024 AIC			22
Time:		18:24	:34 BIC			23
8.853						
Sample:			0 HQIC			23
1.686		_	26			
Covariance ¹	Type:		opg			
=======================================		=======	=======	========	=======	======
	coef	std err	Z	P> z	[0.025	0.
975]						
const	8.1686	3.030	2.696	0.007	2.231	1
4.106	0 5000		4 000	0 070	4 000	
ar.L1 0.046	-0.5220	0.290	-1.800	0.072	-1.090	
ar.L2	-0.0351	0.265	-0.132	0.895	-0.555	
0.485						
ar.L3 0.441	-0.1263	0.289	-0.437	0.662	-0.693	
ar.L4	-0.0376	0.277	-0.136	0.892	-0.580	
0.505			4 000			
ar.L5 0.212	-0.4153	0.320	-1.298	0.194	-1.042	
ma.L1	0.8992	0.381	2.359	0.018	0.152	
1.646	100 0722	06 277	2 467	0.020	47.070	25
sigma2 6.072	186.9722	86.2//	2.167	0.030	17.872	35
========		========	=======		=======	======
======================================	11) (0)-		0.00	James Lama	(ID) .	
Ljung-Box (L1) (Q):		0.00	Jarque-Bera	(JR):	
Prob(Q):			1.00	Prob(JB):		
0.52	-11-11- (11)		1 10	Classics		
Heteroskedasticity (H): -0.11		1.19	Skew:			
Prob(H) (tw	o-sided):		0.80	Kurtosis:		
1.92						
========			=======			======

=======

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

Residuals Diagnostic plays a fundamental role in assessing a model goodness of fit. Let's assess those.

```
In [54]:
             SARIMAX(training["US_SP500"], order=(5,0,1))
                 ).plot_diagnostics(figsize=(10,10))
         plt.show()
        RUNNING THE L-BFGS-B CODE
                   * * *
        Machine precision = 2.220D-16
        N =
                        7
                              M =
                                            10
                      0 variables are exactly at the bounds
        At X0
        At iterate
                           f= 4.28914D+00
                                              |proj g| = 5.69701D-02
        At iterate
                      5
                           f= 4.22807D+00
                                              |proj g| = 2.91968D-02
        At iterate
                     10
                          f= 4.21294D+00
                                              |proj g| = 9.09456D-02
        At iterate
                                              |proj g| = 9.03100D - 03
                     15
                           f= 4.19672D+00
```

This problem is unconstrained.

```
At iterate
            20
                  f= 4.19637D+00
                                     |proj g| = 1.33236D-03
                                     |proj g| = 3.71160D-03
At iterate
            25
                  f= 4.19614D+00
                  f= 4.19606D+00
                                     |proj g| = 5.39559D-04
At iterate
            30
At iterate
            35
                  f= 4.19605D+00
                                     |proj g| = 2.65728D-04
At iterate
            40
                  f= 4.19605D+00
                                     |proj g| = 2.09114D-05
```

* * *

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

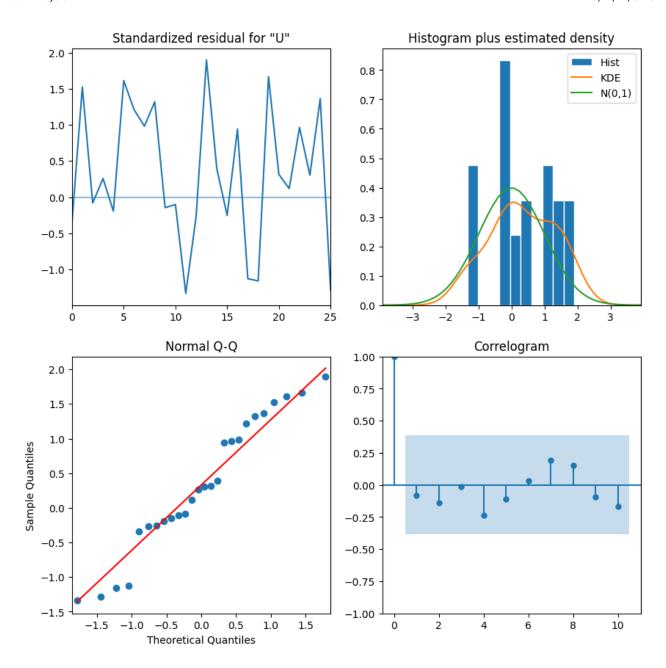
Projg = norm of the final projected gradient

F = final function value

* * *

N Tit Tnf Tnint Skip Nact Projg F 7 40 44 1 0 0 2.091D-05 4.196D+00 F = 4.1960469220713374

CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH



Residuals are not autocorrelated and overall they seem normally distributed. As such, the model appears to be good.

We can now make predictions.

```
In [55]: # Make predictions
    start = len(training["US_SP500"])
    end = len(training["US_SP500"]) + len(test["US_SP500"]) - 1
    predictions = arima_fit.predict(start=start, end=end)
#print predictions
print(predictions)
```

```
26 -5.734900

27 12.351909

28 -1.424520

29 13.781553

30 9.263326

31 14.228458

32 2.881107

Name: predicted_mean, dtype: float64
```

Luckily, prediction values are not on straight line. Plotting them along with the actual values (i.e the test dataset) will help us in assessing our model's performance.

```
In [56]: import pandas as pd
         import plotly.graph_objects as go
         # Append the last point of training to the start of test and predictions
         last_training_point = training.iloc[-1] # Get the last row of training d
         # Create new dataframes for test and predictions with an additional first
         test_with_last_training = pd.concat([last_training_point.to_frame().T, te
         predictions_with_last_training = pd.Series([last_training_point["US_SP500"])
         # Create an interactive figure
         fig = go.Figure()
         # Add training data as a line plot
         fig.add_trace(go.Scatter(
             x=training["date"],
             y=training["US_SP500"],
             mode='lines',
             name='Training Data',
             line=dict(color='mediumblue')
         ))
         # Add test data as a line plot with smooth transition from training data
         fig.add trace(go.Scatter(
             x=test with last training["date"],
             y=test_with_last_training["US_SP500"],
             mode='lines',
             name='Test Data',
             line=dict(color='lightblue')
         ))
         # Add ARIMA predictions as a line plot with smooth transition from traini
         fig.add trace(go.Scatter(
             x=predictions_with_last_training.index,
             y=predictions_with_last_training,
             mode='lines',
             name='Predictions'.
             line=dict(color='darkred')
         ))
         # Update layout for the interactive plot
```

```
fig.update_layout(
    title='ARIMA Forecast vs Actual (US)',
    xaxis_title='Year',
    yaxis_title='SP500 Index (% change)',
    legend_title='Data',
    template='plotly_white',
    hovermode='x unified' # Show hover information for all traces at the
)

# Save the figure to the img directory
save_plotly_figure(fig, 'img/ARIMAtest', format='png')

# Display the interactive plot
fig.show()
```

/Users/lucaalbertini/Personal/CaseStudies/WB-caseStudy/WBvenv/lib/python3. 12/site-packages/pandas/core/indexes/base.py:7631: FutureWarning:

Dtype inference on a pandas object (Series, Index, ExtensionArray) is deprecated. The Index constructor will keep the original dtype in the future. Call `infer_objects` on the result to get the old behavior.

Figure saved as img/ARIMAtest.png

The ARIMA model does not a bad job in predicting the movements' direction of the SP500 Index in the US. However, it underestimates their magnitude. Note that year with the biggest spread actual value -predicted value is, not surpisingly, 2022. This is a consequence of COVID19, an extreme event that our model fails to take into account. Overall, this estimation shows some room for improvement, since it succeeds in forecasting whether the SP500 index will go up and down but does not get its magnitude.

Now let's use the same ARIMA model to predict the future US_SP500 value for the next 3 years (2023-2024-2025).

```
In [57]: #set up the Arima for the entire series
arima_for = ARIMA(US_SP["US_SP500"], order=(5,0,1)) # p,d,q are as befor
arimafor_fit = arima.fit()
#print a summary for the model
print(arimafor_fit.summary())
```

SARIMAX Results

		JAN.	=========			
====						
Dep. Varia	ble:	US_SP	500 No.	Observations:		
26 Model:		ARIMA(5, 0,	1) Loa	Likelihood		-10
6.394		,	_,g			
Date:	Fr	i, 27 Sep 2	024 AIC			22
8.788 Time:		18:24	:37 BIC			23
8.853		10124	.57 DIC			23
Sample:			0 HQIC			23
1.686			26			
Covariance	Type:		20 opg 			
====						
975]	coef	std err	Z	P> z	[0.025	0.
const	8.1686	3.030	2.696	0.007	2.231	1
4.106	0 5330	0.200	1 000	2 272	4 000	
ar.L1 0.046	-0.5220	0.290	-1.800	0.072	-1.090	
ar.L2	-0.0351	0.265	-0.132	0.895	-0.555	
0.485	0.4000		0 407			
ar.L3 0.441	-0.1263	0.289	-0.437	0.662	-0.693	
ar.L4	-0.0376	0.277	-0.136	0.892	-0.580	
0.505	0 4450	0.220	4 200	0.101	1 0 4 2	
ar.L5 0.212	-0.4153	0.320	-1.298	0.194	-1.042	
ma.L1	0.8992	0.381	2.359	0.018	0.152	
1.646	106 0722	06 277	2 167	0.020	17 070	25
sigma2 6.072	186.9722	80.2//	2.167	0.030	17.872	35
=========	========	========	=======	=========	-=======	=====
Ljung-Box	(L1) (Q):		0.00	Jarque-Bera	(JB):	
1.31 Prob(Q):			1.00	Prob(JB):		
<pre>0.52 Heteroskedasticity (H):</pre>		1.19	Skew:			
-0.11		1117	J.C.W.I			
Prob(H) (two-sided): 1.92		0.80	Kurtosis:			
========		========				=====

=======

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

Compute predictions for future values.

```
In [58]: #display predictions
         startUS = len(US_SP) #start after the first data of US_SP
         endUS = startUS + 3 #forecast for 3 periods
         predictions_US = arimafor_fit.predict(start=startUS, end=endUS)
         print(predictions_US)
        33
              14.350583
        34
               1.989961
        35
              11.162476
        36
               3.724112
        Name: predicted_mean, dtype: float64
         and visualize them.
In [59]: # Filter to keep only the last 5 years of actual data
         last_5_years = US_SP[US_SP["date"] >= (US_SP["date"].max() - pd.DateOffse
         # Get the last actual value to ensure continuity
         last_actual_value = last_5_years["US_SP500"].iloc[-1]
         # Extend the date index by adding future dates (3 years in this case)
         future dates = pd.date range(start=last 5 years["date"].iloc[-1], periods
         # Create a new predictions array that includes the last actual value
         extended_predictions = np.concatenate(([last_actual_value], predictions_U
         # Create a figure with Plotly
         fig = make subplots()
         # Add actual data trace
         fig.add_trace(go.Scatter(x=US_SP["date"], y=US_SP["US_SP500"], mode='line
         # Add predictions trace
         fig.add_trace(go.Scatter(x=future_dates, y=extended_predictions, mode='li
         # Update layout
         fig.update_layout(
             title='US SP500 Forecasting for the next 3 years',
             xaxis_title='Year',
             yaxis_title='SP500 Index (% change)',
             legend_title='Legend'
         # Save the figure to the img directory
         save_plotly_figure(fig, 'img/ARIMA', format='png')
         # Show the interactive plot
         fig.show()
```

Figure saved as img/ARIMA.png

According to our model, in the next 3 years (2023-24-25) the US SP500 is going to recover from the downturn it experienced immediately after covid. Moreover, even though it will face some high and lows, it should be going under 0. This means that the it's value is expected to raise year-after-year.

In conclusion, we consider accuracy measures to evaluate our model performances. To avoid miscalculation, we will exclude the COVID's year. (Note that these measures are computed on the testing data).

```
In [60]: # Exclude the last point from both the test data and predictions
   test_excl_last = test["US_SP500"][:-1]
   predictions_excl_last = predictions[:-1]

# Compute accuracy measures without the last point
   print(accuracy_measures(test_excl_last, predictions_excl_last))
```

fundamental metrics are:

Mean Absolute Error (MAE): 10.317850331370643 Mean Squared Error (MSE): 123.91955225253692

Root Mean Squared Error (RMSE): 11.131915929099398

Mean Absolute Percentage Error (MAPE): 69.34956467623995%

R-squared (R²): 0.10666058253601107

Standard Error of Regression (SER): 13.633756942926825

None

The Mean Absolute Error (MAE) and Root Mean Squared Error (RMSE) suggest that, on average, predictions are off by around 12-13 points from actual SP500 values. However, the high Mean Absolute Percentage Error (MAPE) of 75.85% indicates large relative errors, meaning the model struggles to accurately capture the index's movements in percentage terms.

The R-squared (R²) value of 0.345 shows that the model explains only 34.5% of the variance in the SP500 index, leaving much of the variability unaccounted for. The Standard Error of Regression (SER) of 15.76 further highlights the typical prediction error magnitude.

In a nutshell, while the model has some predictive power, it may benefit from trying different configurations or including additional explanatory variables.

CONCLUSION 6 FINAL THOUGHTS

This analysis offers several valuable insights:

Firstly, the two European countries considered in the study have significant portions of missing data. Understanding the reasons behind this could add meaningful context

to the analysis.

Secondly, no single country overwhelmingly dominates the others in financial terms. A country that performs well in one indicator may lag in another. For example, South Africa has the highest market capitalization, yet it has relatively few listed companies and low market liquidity.

This highlights the main recommendation of this study: financial indicators should always be analyzed together. While individual measures can be informative, a comprehensive understanding of a country's financial landscape requires considering all relevant indicators. Take China as an example: it has rapidly increased the number of listed companies, but did its market capitalization grow at the same pace? Apparently not. This discrepancy may suggest that newly listed companies have lower market values or that the Yen/USD exchange rate affected the results or that there may be additional forces at play.

Lastly, estimation techniques could (and should) be improved. Neither the HW nor the ARIMA models provided satisfactory results. While not reported in detail, a GARCH model was also tested but failed due to insufficient data. To enhance estimation, two key improvements are recommended:

- Waiting for more data: Additional data would help fine-tune the ARIMA model and potentially make the GARCH model viable.
- Incorporating additional explanatory variables: The future values of the S&P 500 are likely influenced by factors beyond their past values alone. An ARDL or VAR model might be more appropriate in this case.

Overall, this analysis achieved its goal of providing a general overview of the financial situation in various countries. Repeating it periodically would help refine the insights and provide more accurate, data-driven recommendations.