# Bottom Up Parsing

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# LR(0) Parsing

- Build the derivation tree from the bottom
- First build the children, then connect to the parent
- Can handle left recursion
  - Which is common in real-world grammars

#### LR(0) Item

An LR(0) item is of the form:

•  $N \rightarrow \alpha . \beta$ 

The dot gives us the current location (a local view).

### LR(0) Item

An LR(0) item with the dot at the end is called **reduce** item:

•  $N \rightarrow \alpha \beta$ .

Otherwise, it's a **shift** item:

- $N \rightarrow \alpha \beta$
- $N \rightarrow \alpha . \beta$

#### LR(0) Item Closure Set

The LR(0) closure set of an LR(0) item i is a set S such that:

- $i \in S$
- If  $A \to \alpha . N\beta \in S$  then for each rule  $N \to \gamma$ :
  - $N \rightarrow \gamma \in S$

# LR(0) Item Closure Set

For example, given the following CFG:

- $S \rightarrow E$ \$
- $E \rightarrow ID = X$
- $E \rightarrow \{ID\}$
- $X \rightarrow INT$

the closure set of the  $S \rightarrow E$ \$ contains:

- $S \rightarrow E$ \$
- $E \rightarrow ID = X$
- $E \rightarrow \{ID\}$

# LR(0) Parsing

Consider the following CFG:

- $S \rightarrow E$ \$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$
- $L \rightarrow E$
- $L \rightarrow L; E$

What will be the **transition system** of the LR(0) parser for this CFG?



We start with the initial LR(0) item (that comes from the initial rule):

• 
$$S \rightarrow E$$
\$

The initial state is the  $\epsilon$ -closure of that item, which contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

We start with the initial LR(0) item (that comes from the initial rule):

•  $S \rightarrow E$ \$

The initial state is the  $\epsilon$ -closure of that item, which contains:

- $S \rightarrow E$ \$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

#### $S_0$ : $S \rightarrow E$ $E \rightarrow ID = INT$ $E \rightarrow \{L\}$

From  $s_0$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

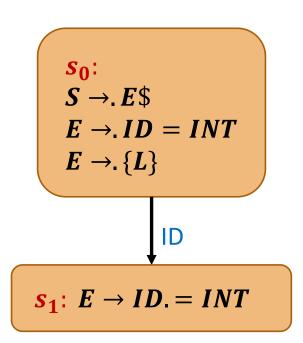
From  $s_0$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_1$ , if we recognized =, then the next state will contain:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

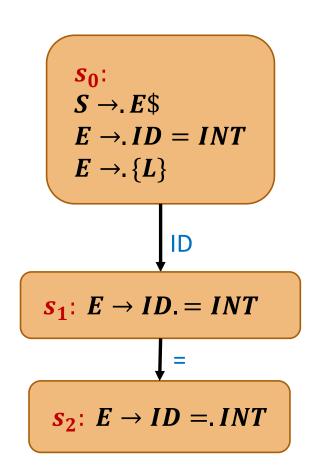
From  $s_1$ , if we recognized =, then the next state will contain:

•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

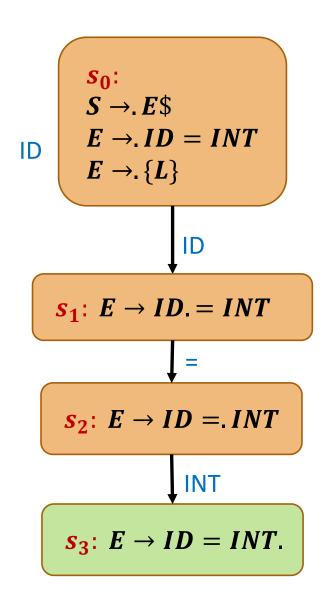


From  $s_2$ , if we recognized INT, then the next state will contain:

•  $E \rightarrow ID = INT$ .

Which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_0$ , if we recognized  $\{$ , then the next state will contain:

• 
$$E \rightarrow \{.L\}$$

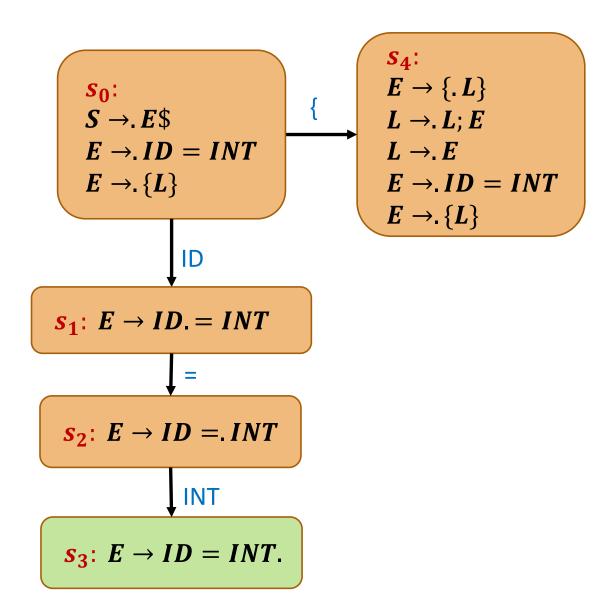
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_0$ , if we recognized  $\{$ , then the next state will contain:

•  $E \rightarrow \{.L\}$ 

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_4$ , if we recognized  $\{$ , then the next state will contain:

• 
$$E \rightarrow \{.L\}$$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_4$ , if we recognized  $\{$ , then the next state will contain:

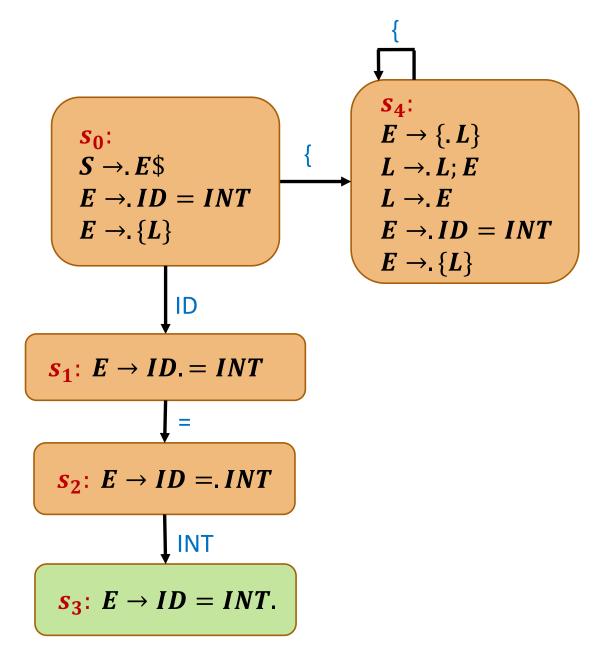
•  $E \rightarrow \{.L\}$ 

So the next state (the  $\epsilon$ -closure) contains:

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

which was already computed:  $s_4$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_4$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_4$ , if we recognized ID, then the next state will contain:

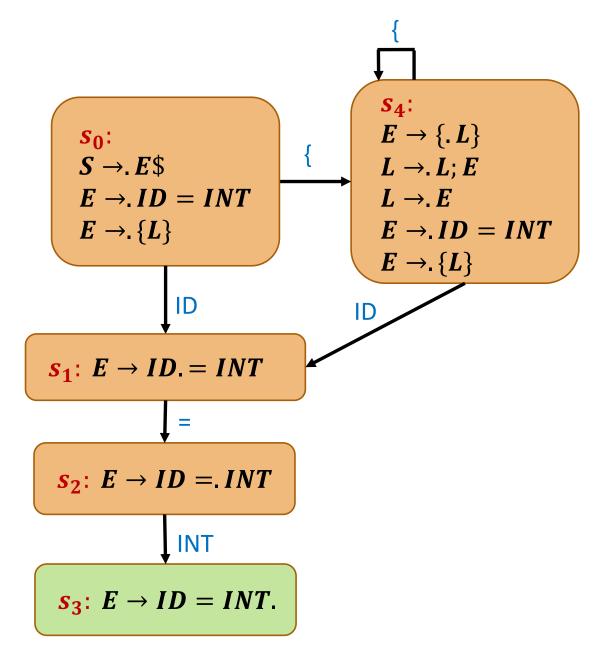
•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

which was already computed:  $s_1$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

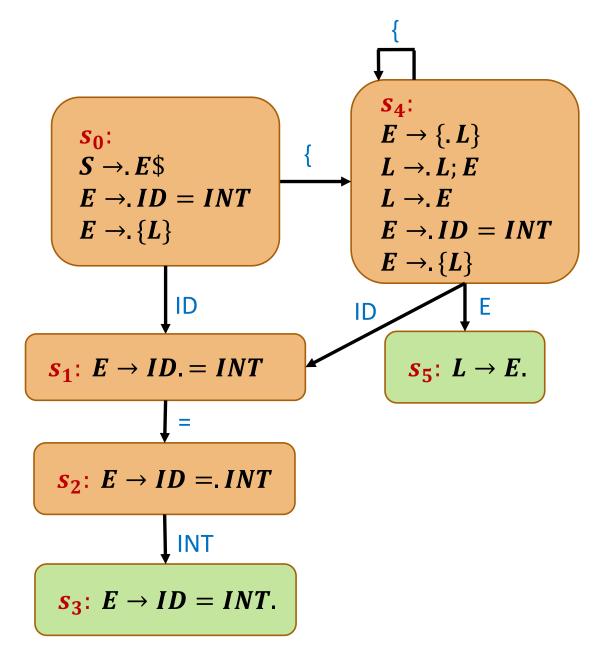


From  $s_4$ , if we recognized E, then the next state will contain:

•  $L \rightarrow E$ .

which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_4$ , if we recognized L, then the next state will contain:

- $E \rightarrow \{L.\}$
- $L \rightarrow L$ ; E

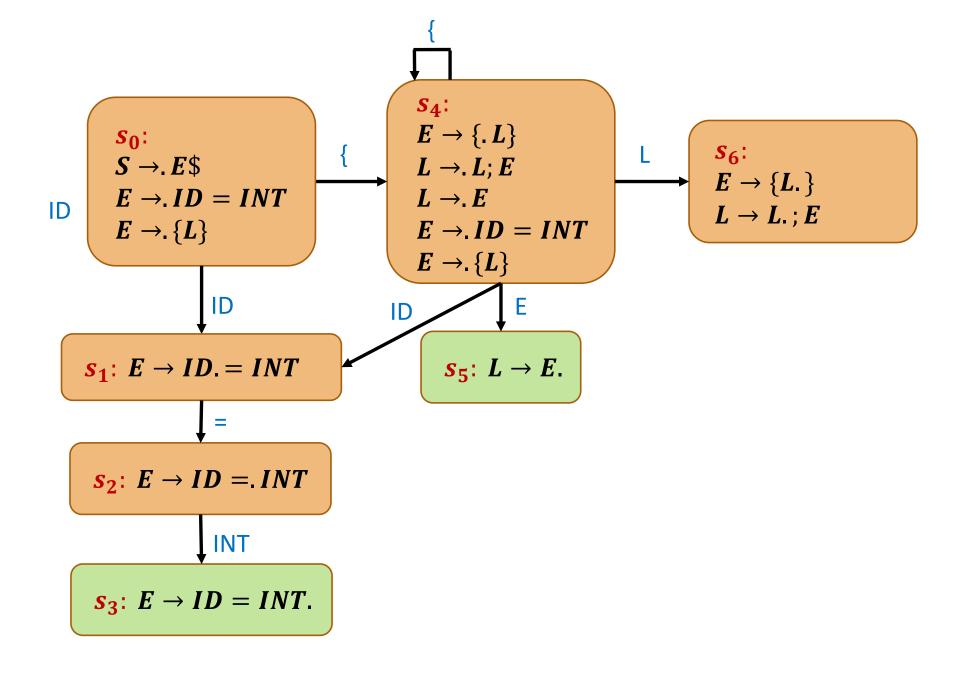
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_4$ , if we recognized L, then the next state will contain:

- $E \rightarrow \{L.\}$
- $L \rightarrow L$ ; E

- $E \rightarrow \{L.\}$
- $L \rightarrow L$ ; E

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

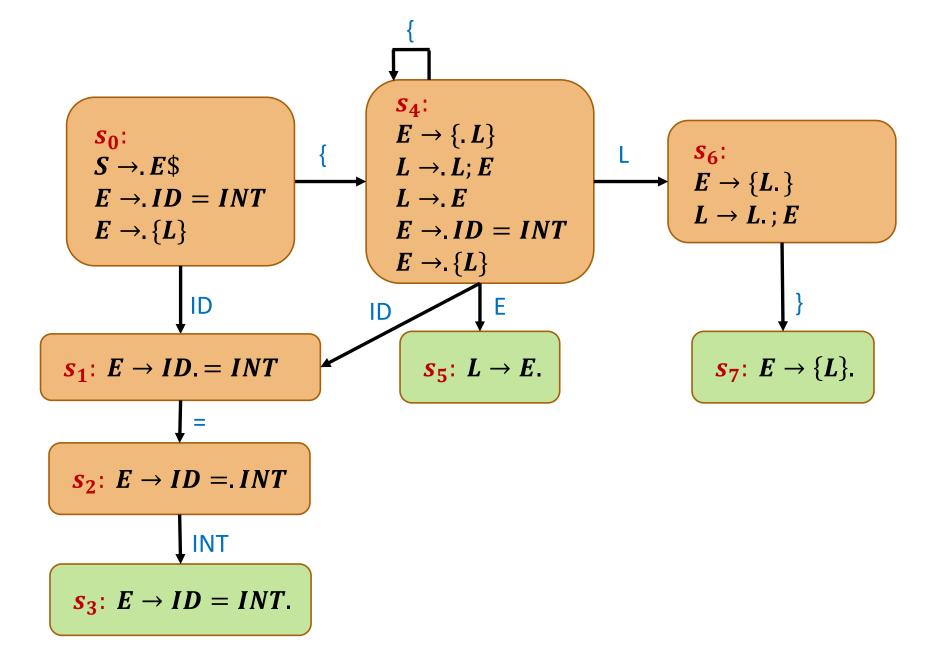


From  $s_6$ , if we recognized }, then the next state will contain:

•  $E \rightarrow \{L\}$ .

Which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_6$ , if we recognized;, then the next state will contain:

•  $L \rightarrow L$ ; E

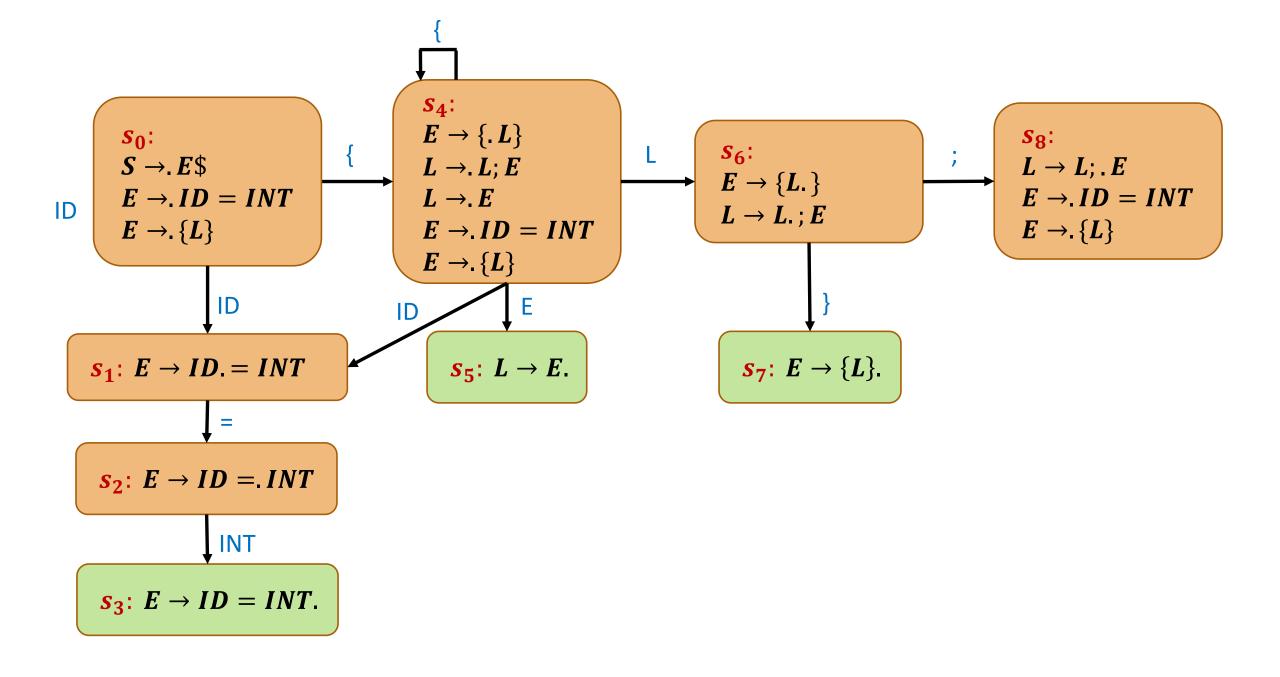
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_6$ , if we recognized;, then the next state will contain:

•  $L \rightarrow L$ ; E

- $L \rightarrow L$ ; E
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

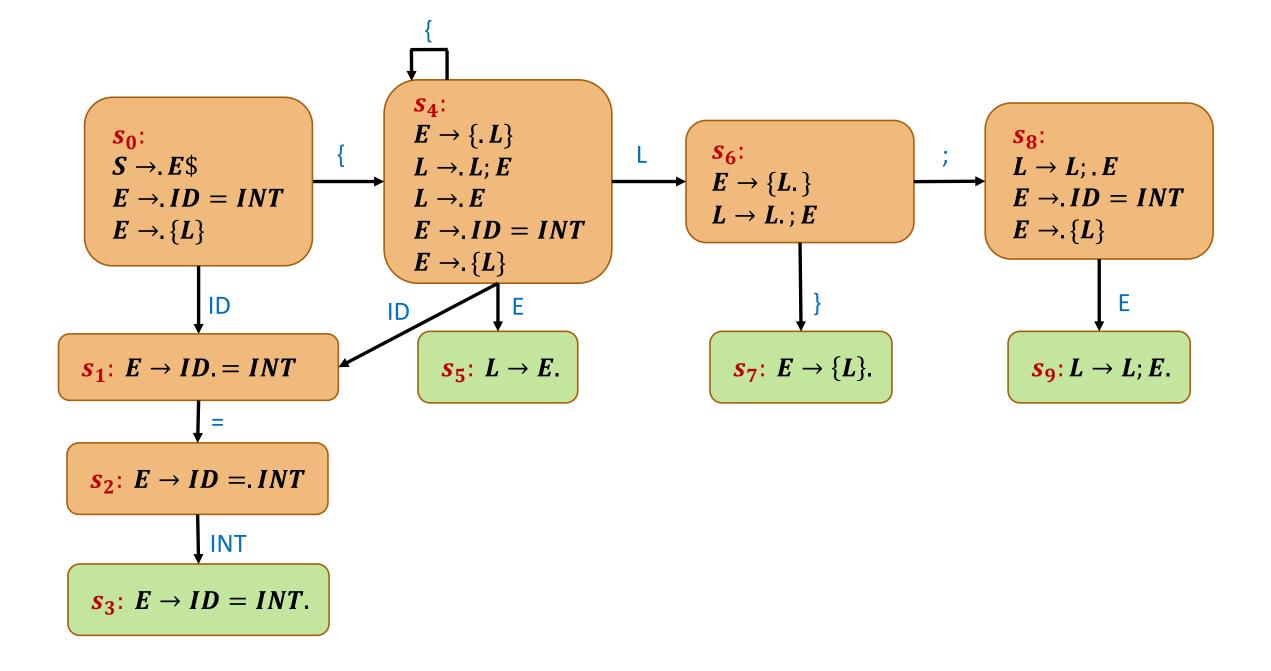


From  $s_8$ , if we recognized E, then the next state will contain:

•  $E \rightarrow L; E$ .

which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_8$ , if we recognized  $\{$ , then the next state will contain:

• 
$$E \rightarrow \{.L\}$$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_8$ , if we recognized  $\{$ , then the next state will contain:

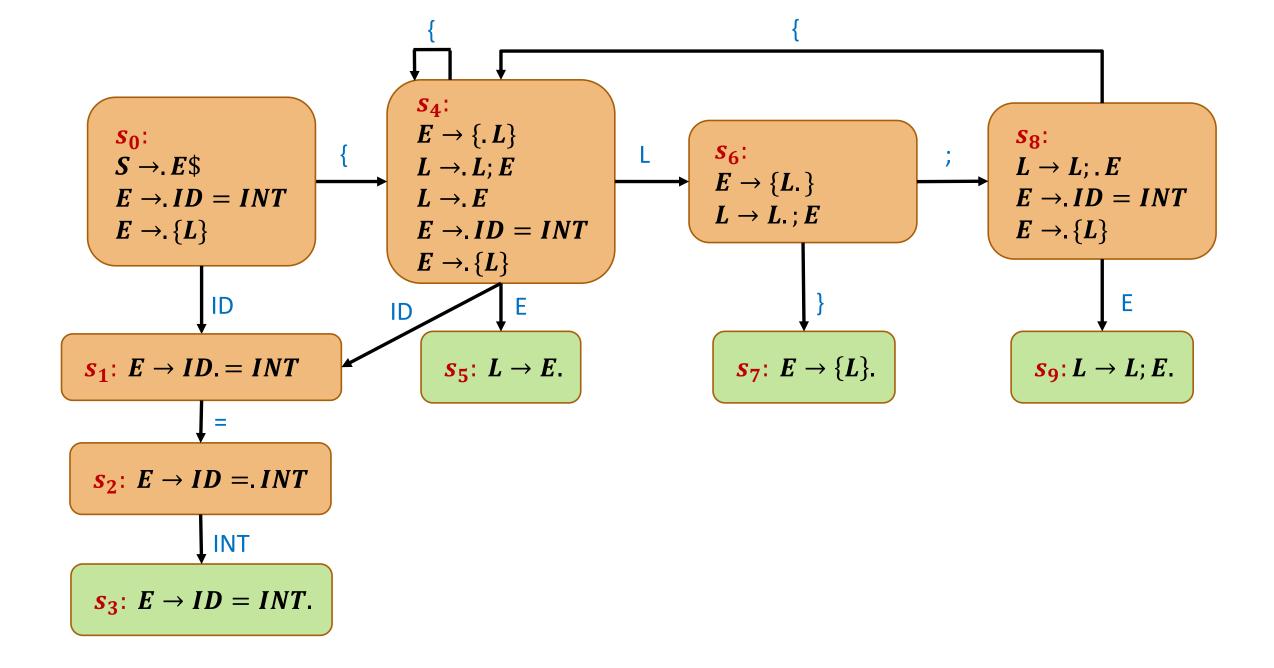
•  $E \rightarrow \{.L\}$ 

So the next state (the  $\epsilon$ -closure) contains:

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

which was already computed:  $s_4$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_8$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_8$ , if we recognized ID, then the next state will contain:

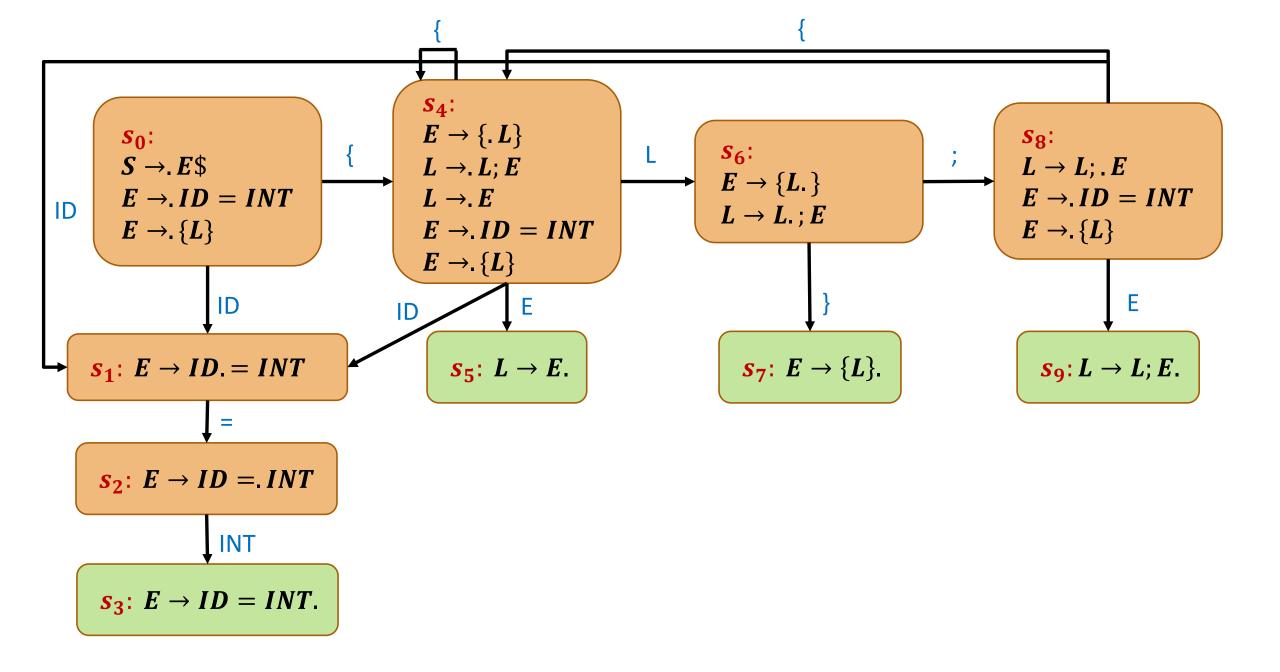
•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

which was already computed:  $s_1$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_0$ , if we recognized E, then the next state will contain:

• 
$$S \rightarrow E.\$$$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

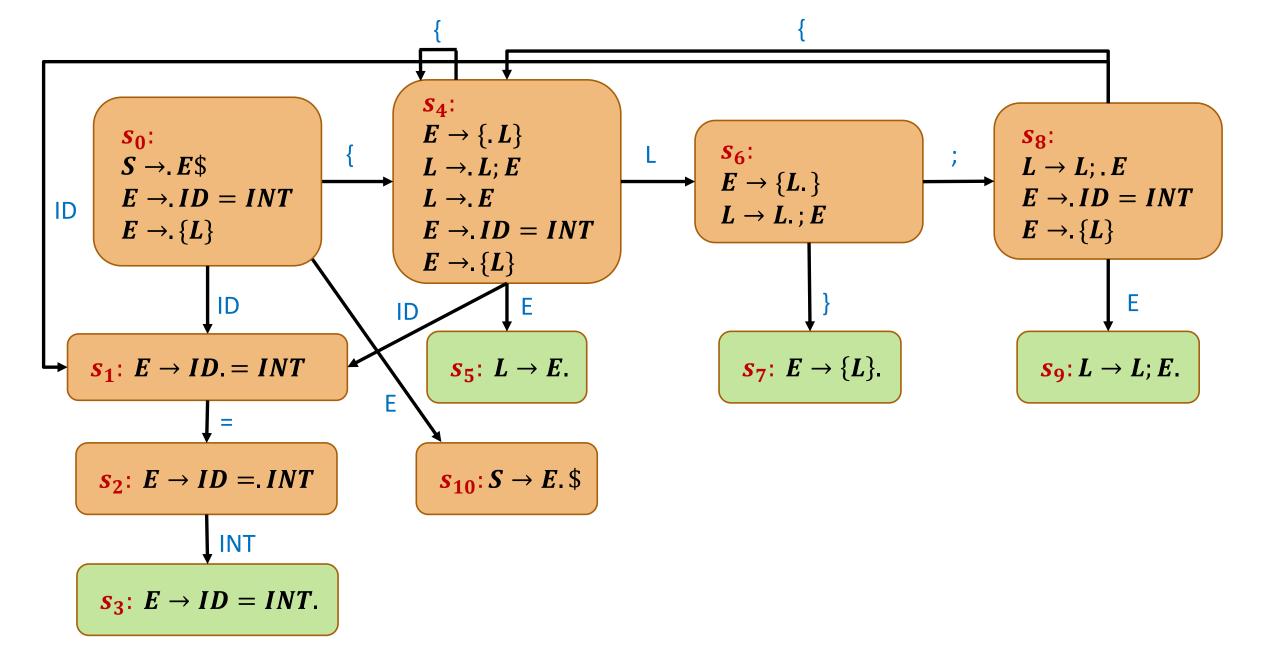
From  $s_0$ , if we recognized E, then the next state will contain:

•  $S \rightarrow E.\$$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $S \rightarrow E.\$$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_{10}$ , if we recognized \$, then the next state will contain:

•  $S \rightarrow E$ \$.

which is a reduce state.

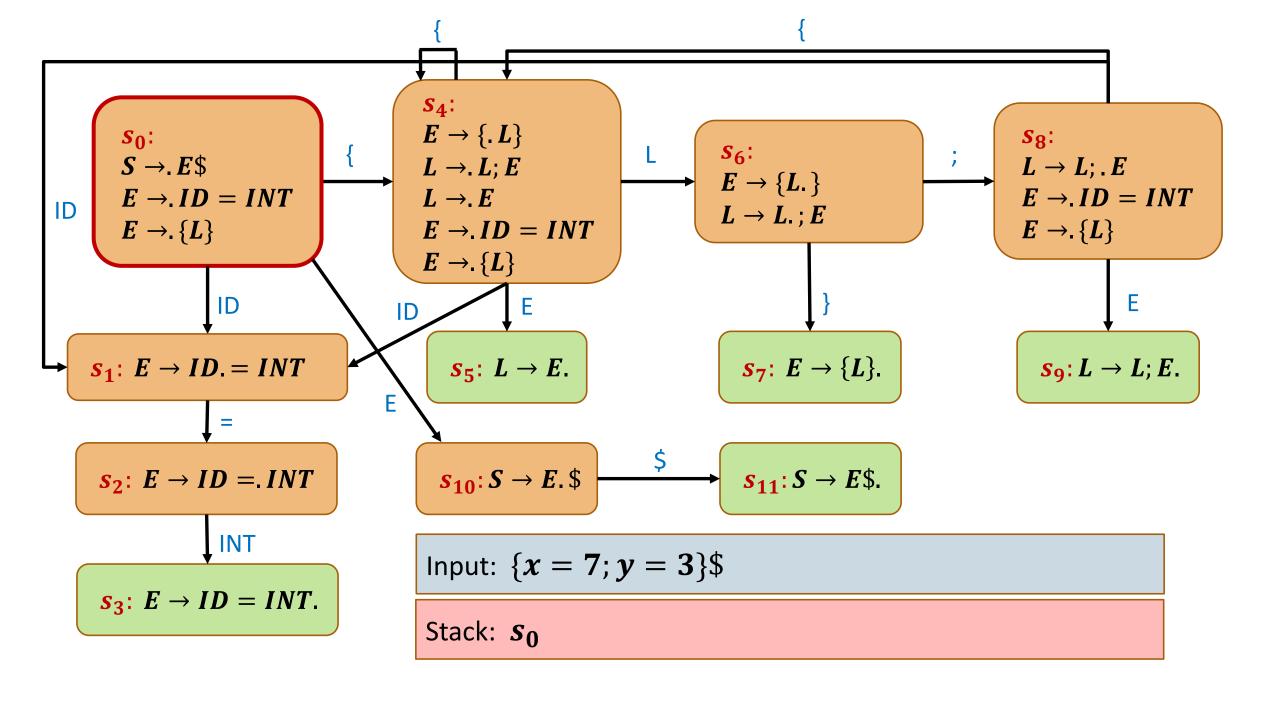
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

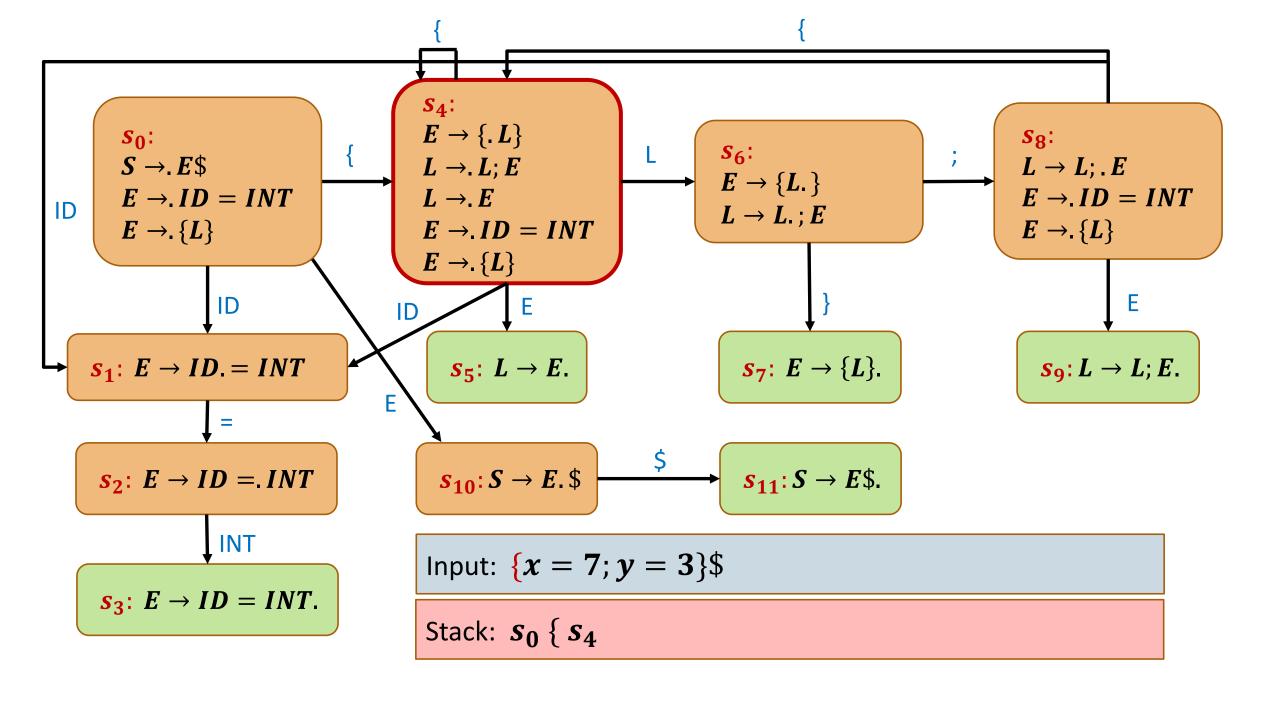


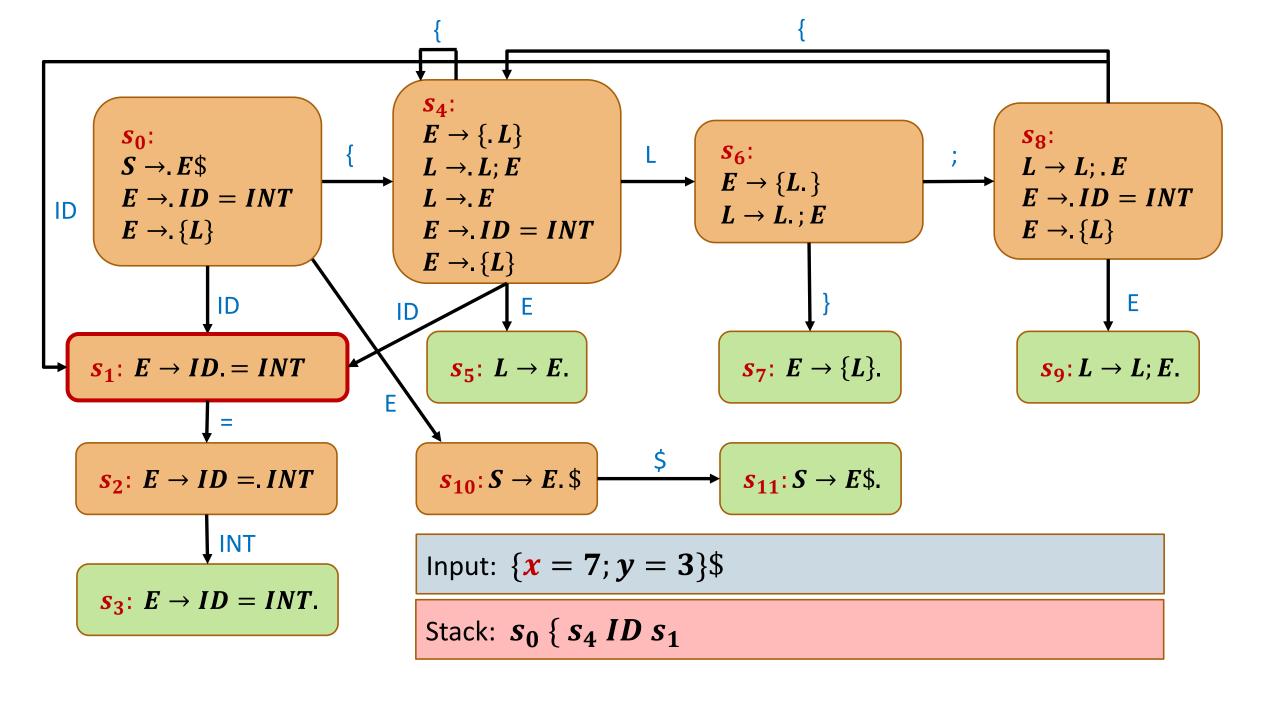
### LR(0) Parser: Running Example

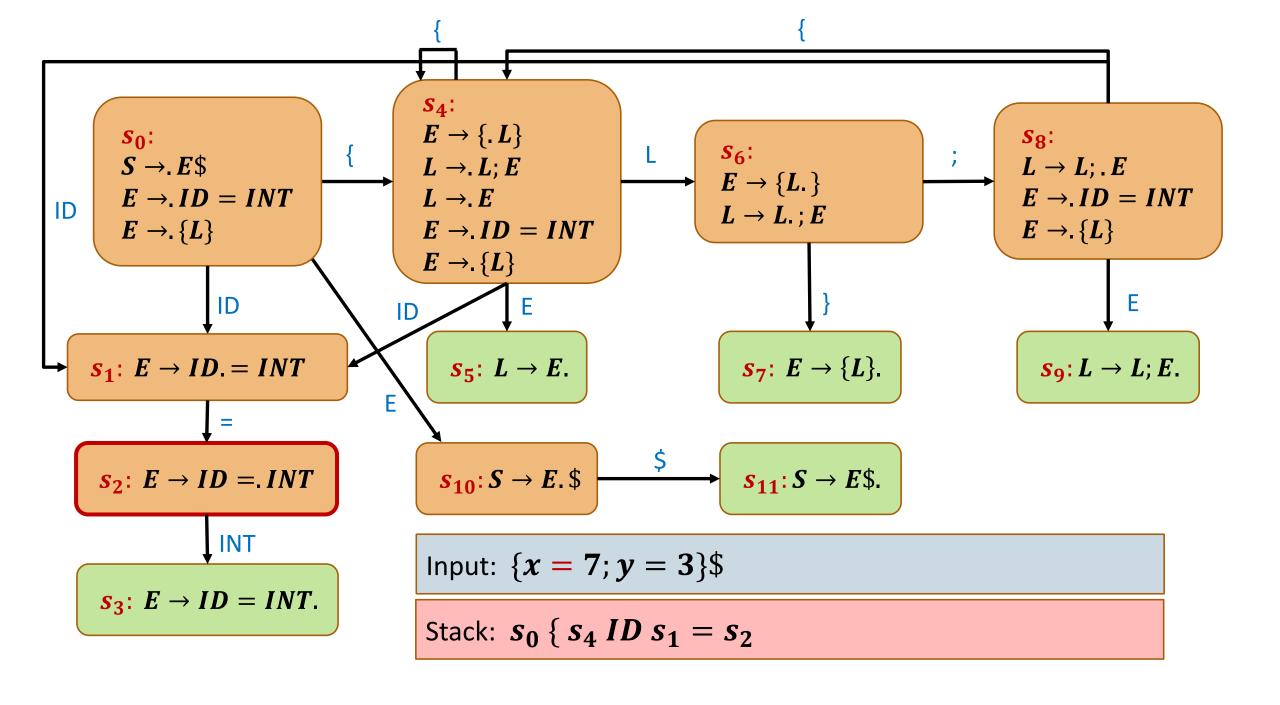
What will happen with the following input:

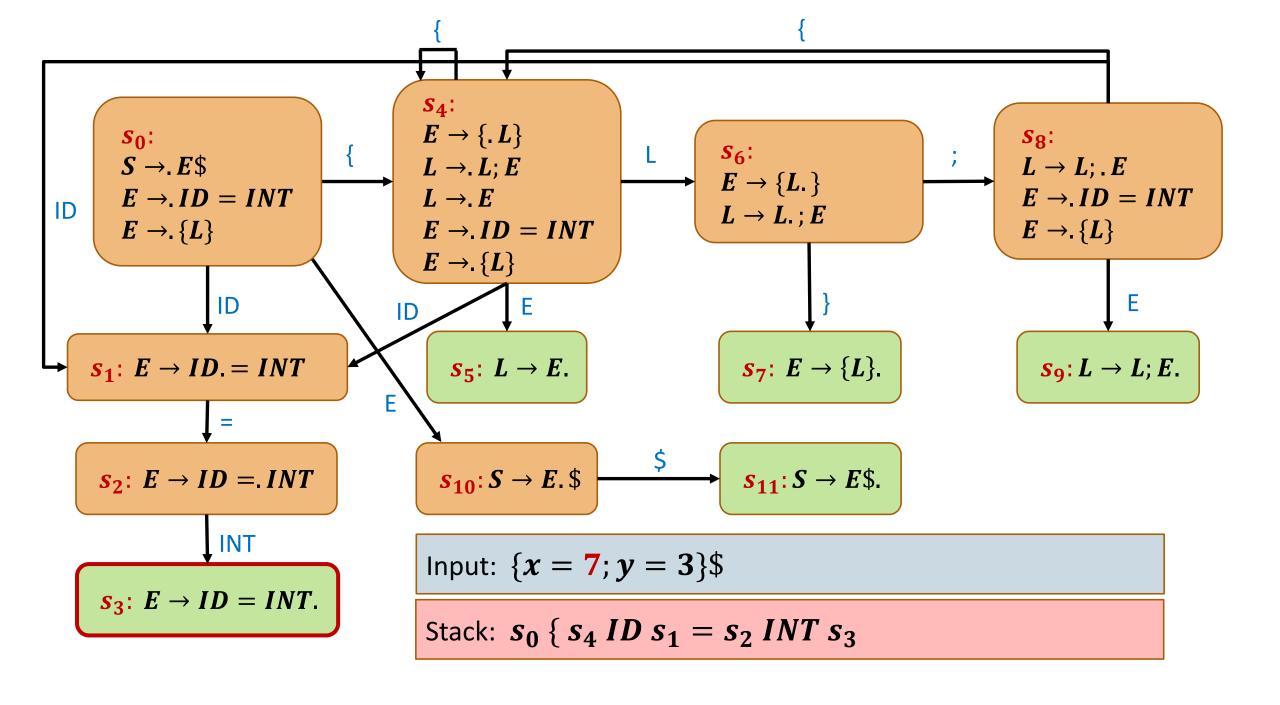
• 
$$\{x = 7; y = 3\}$$
\$

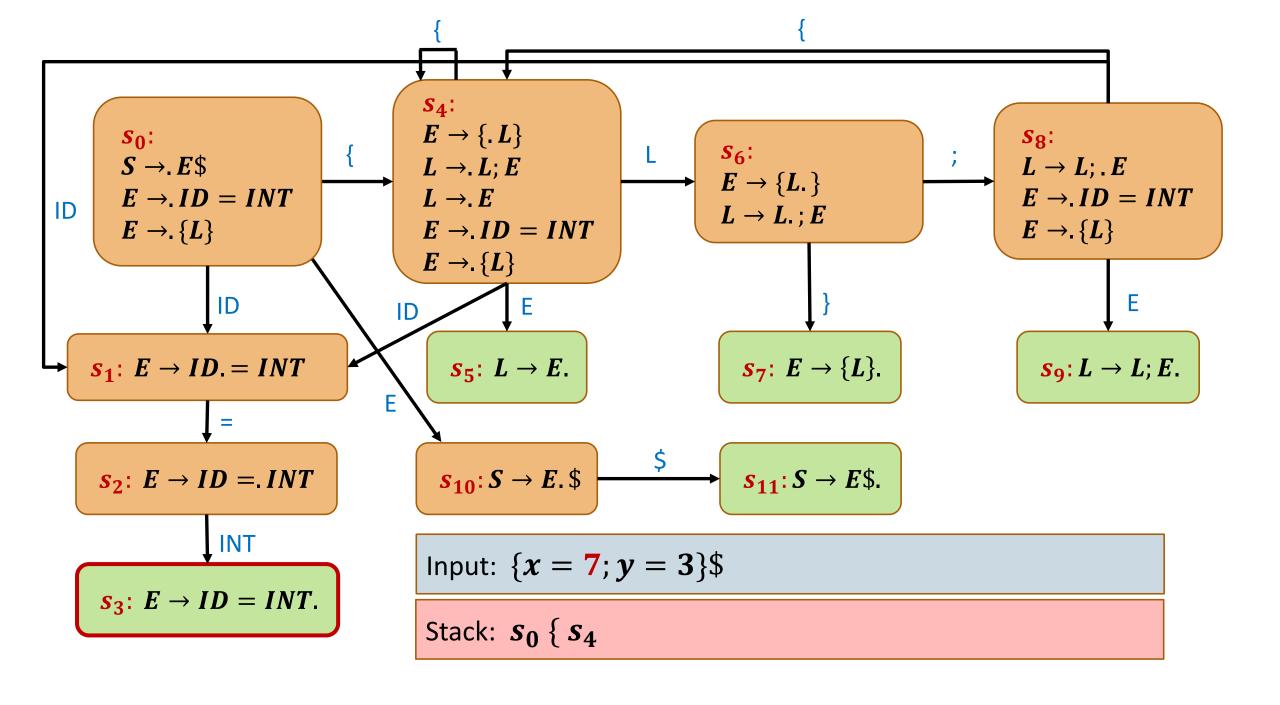


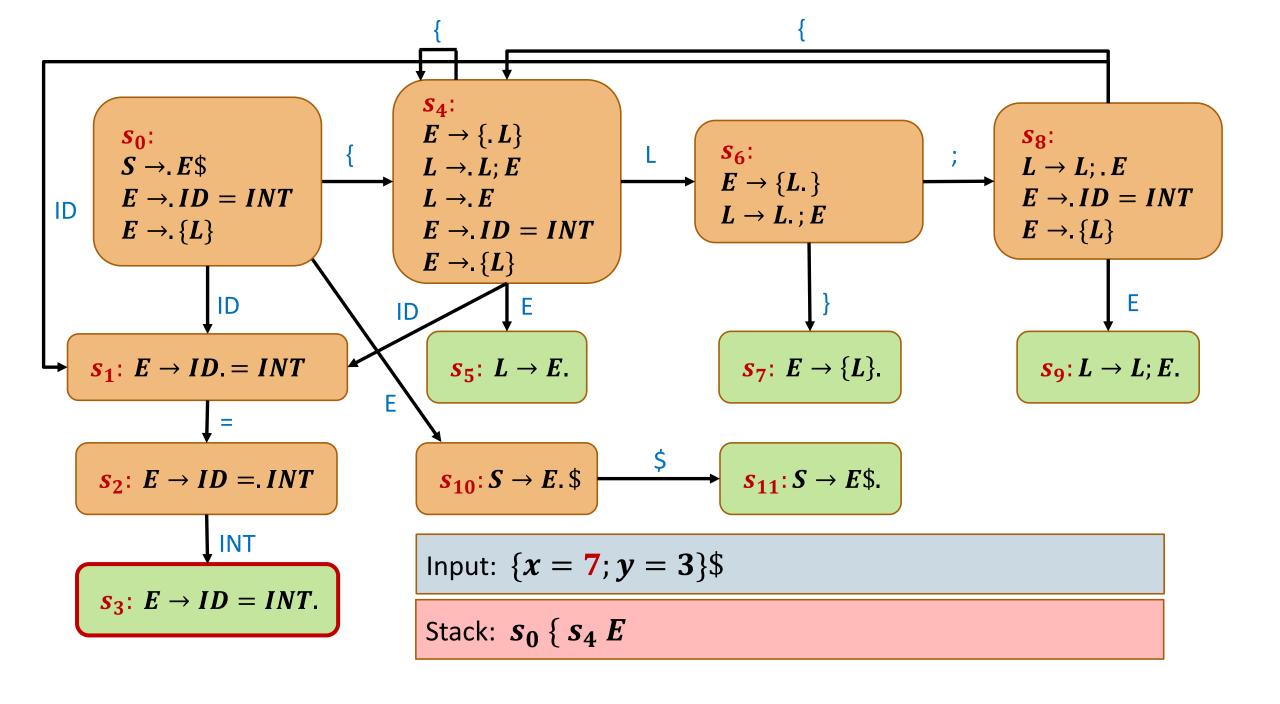


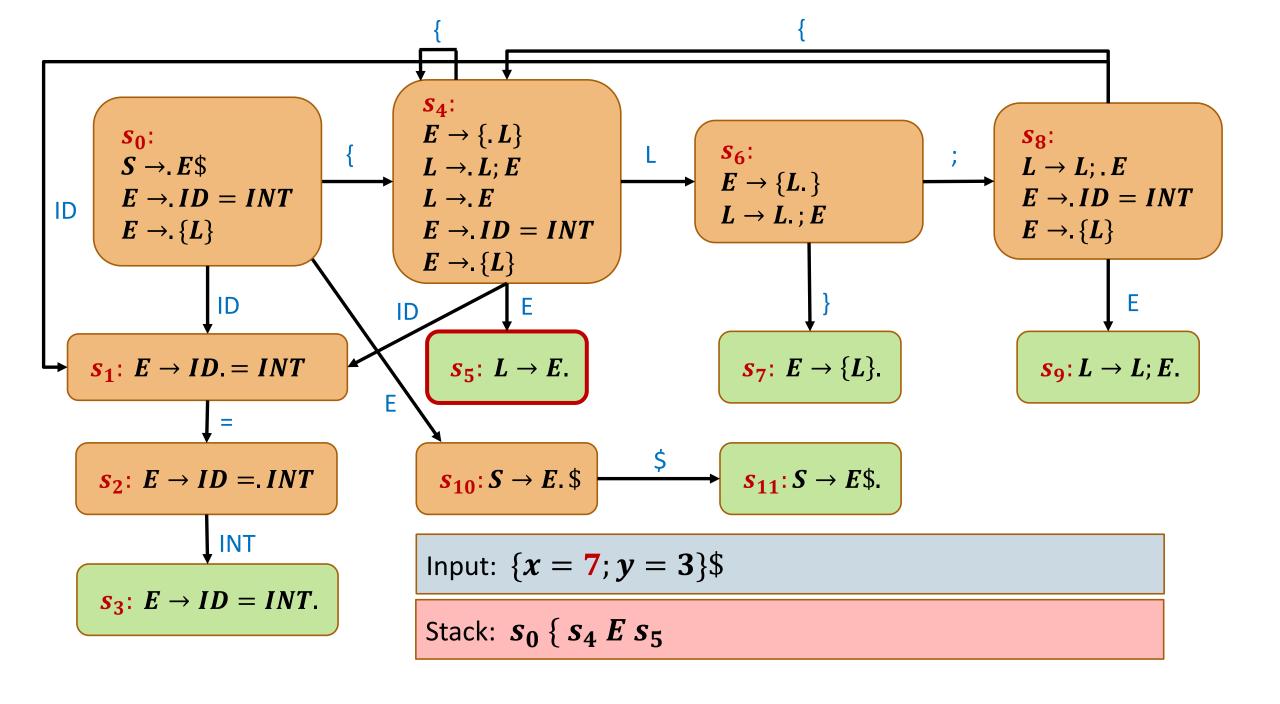


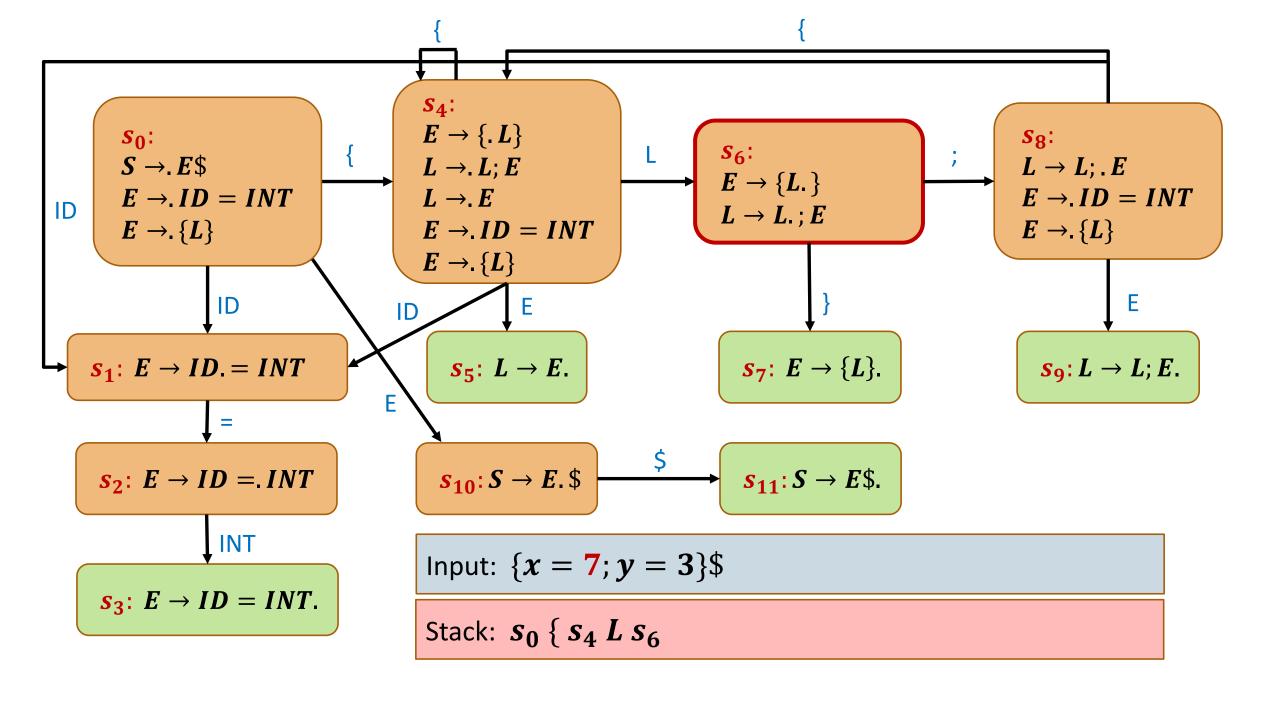


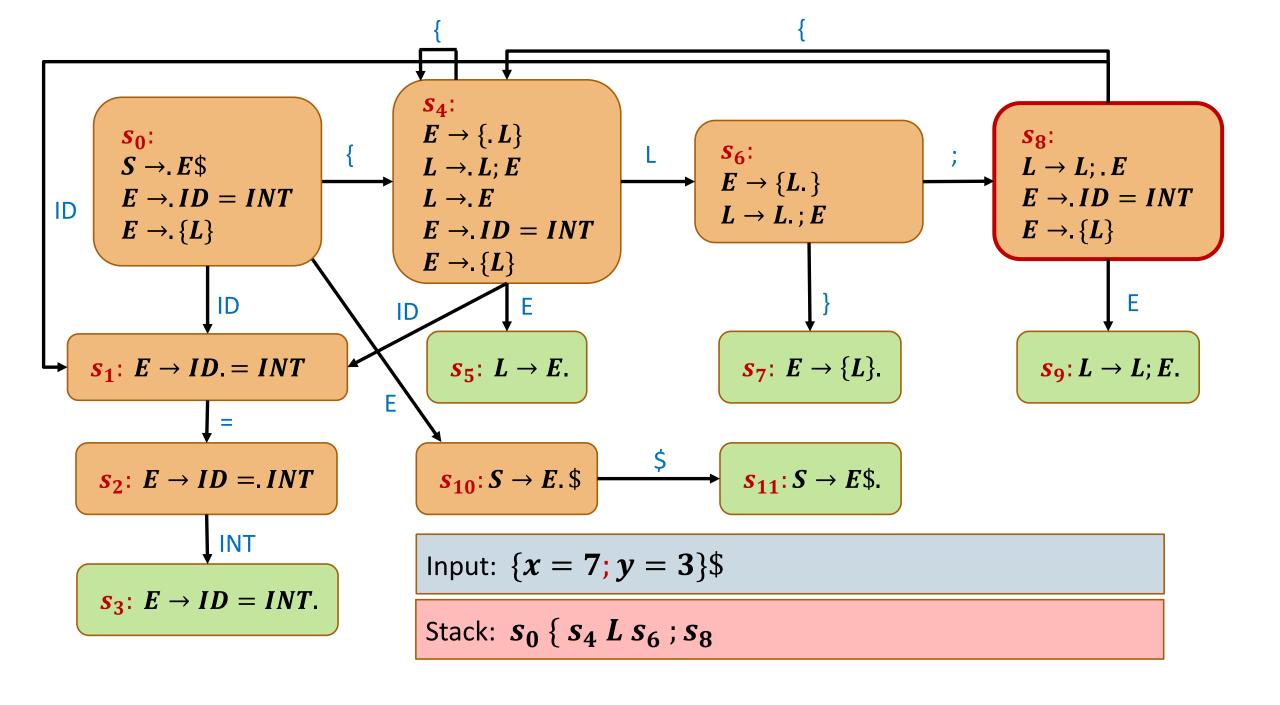


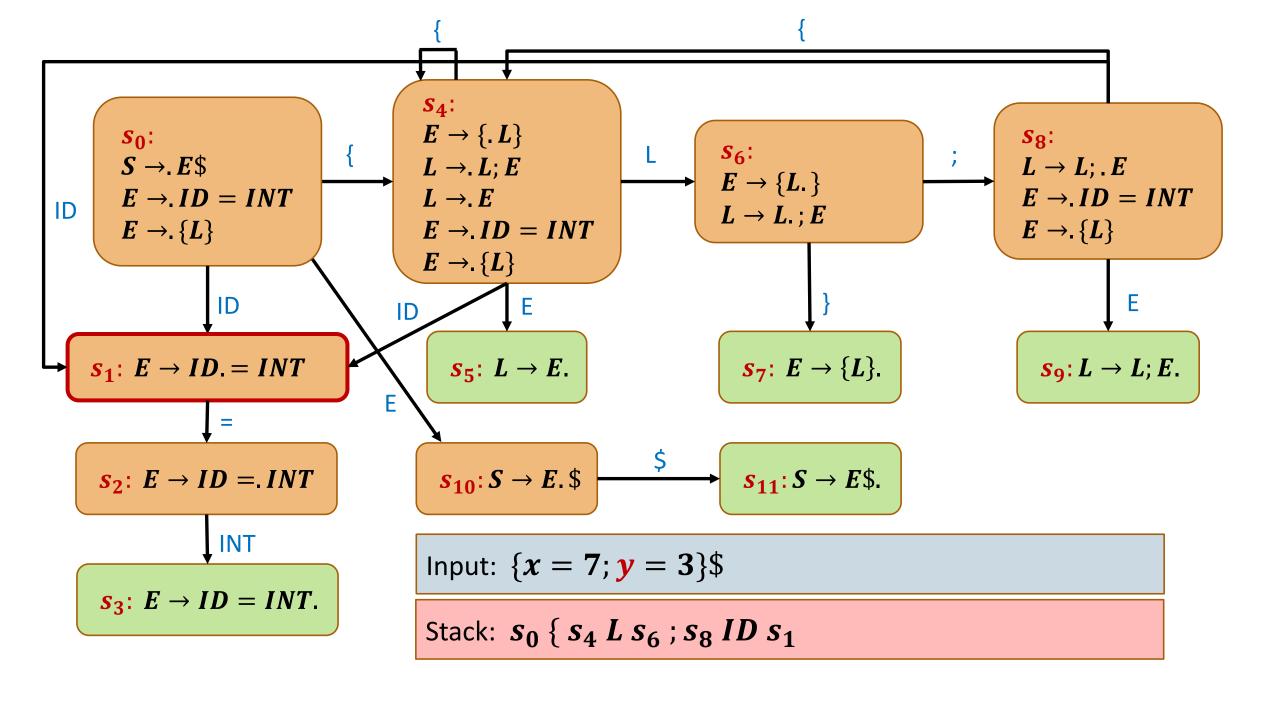


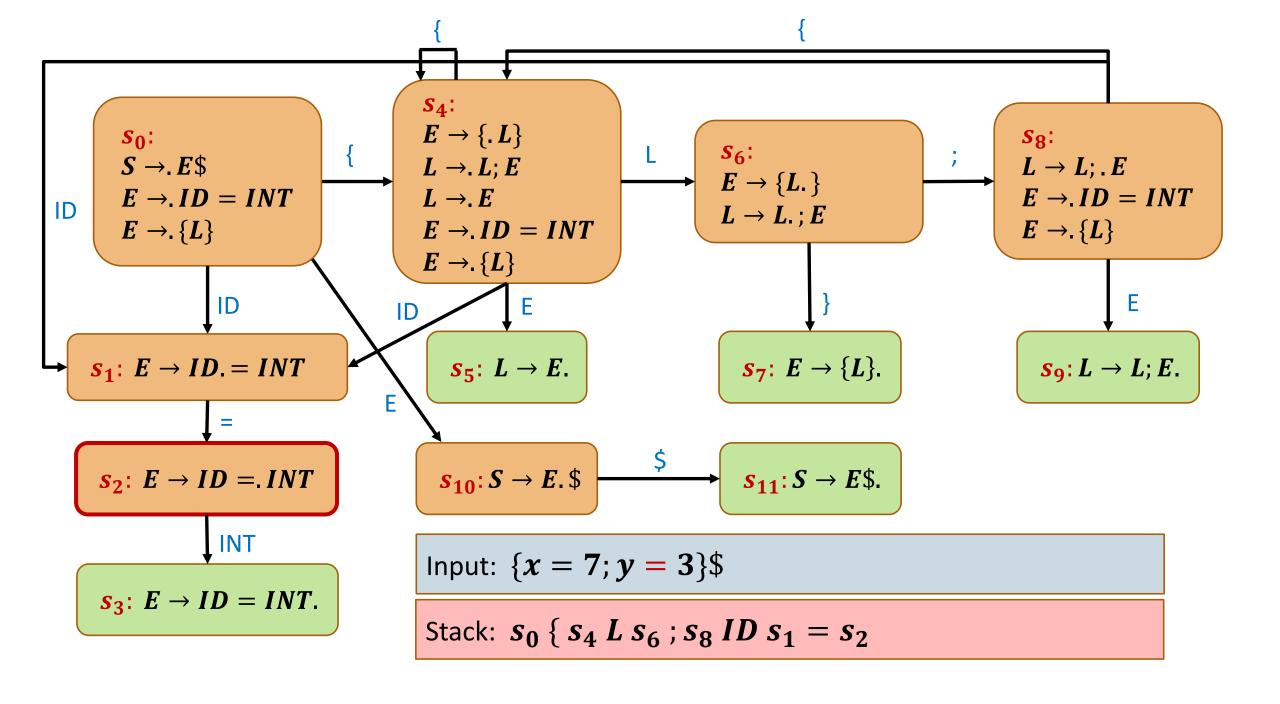


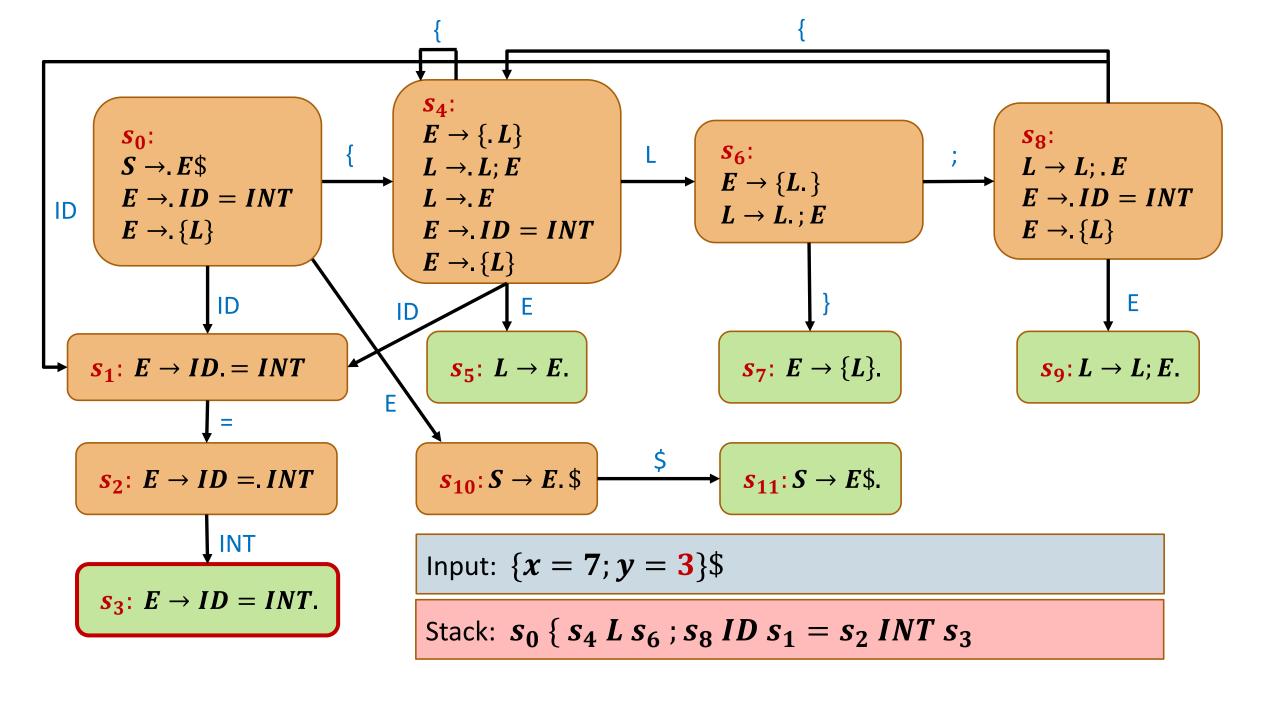


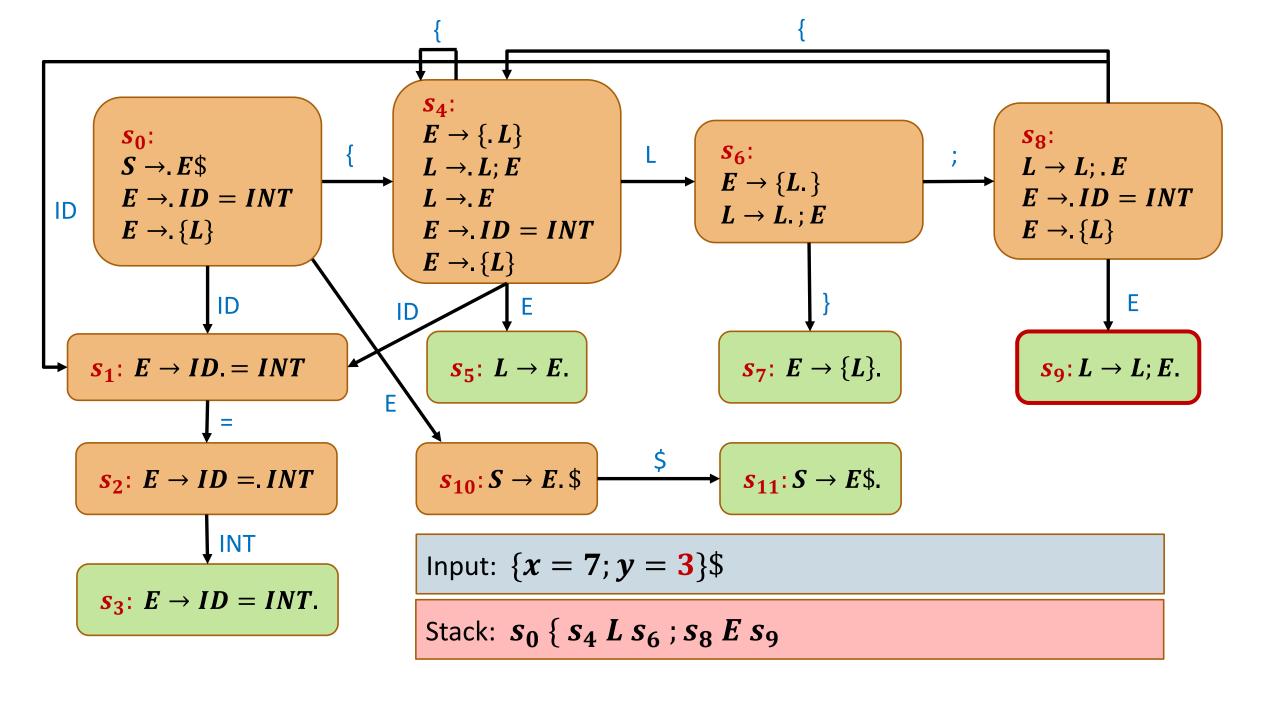


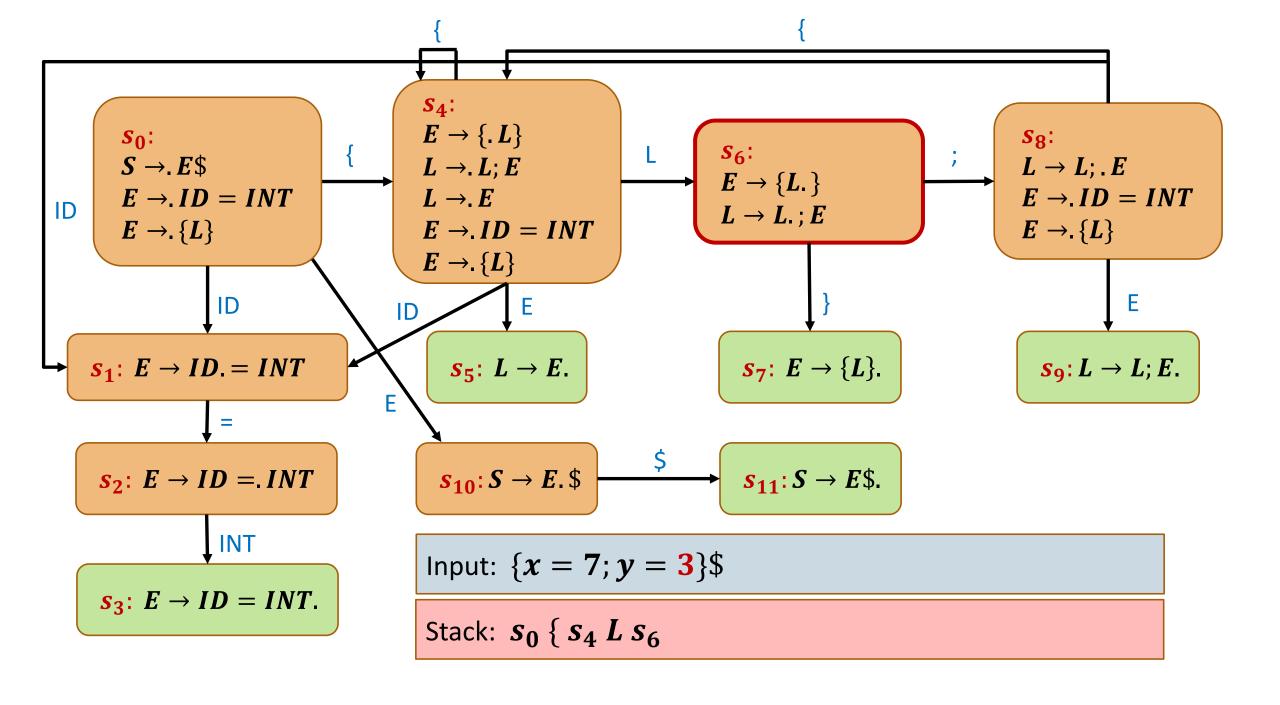


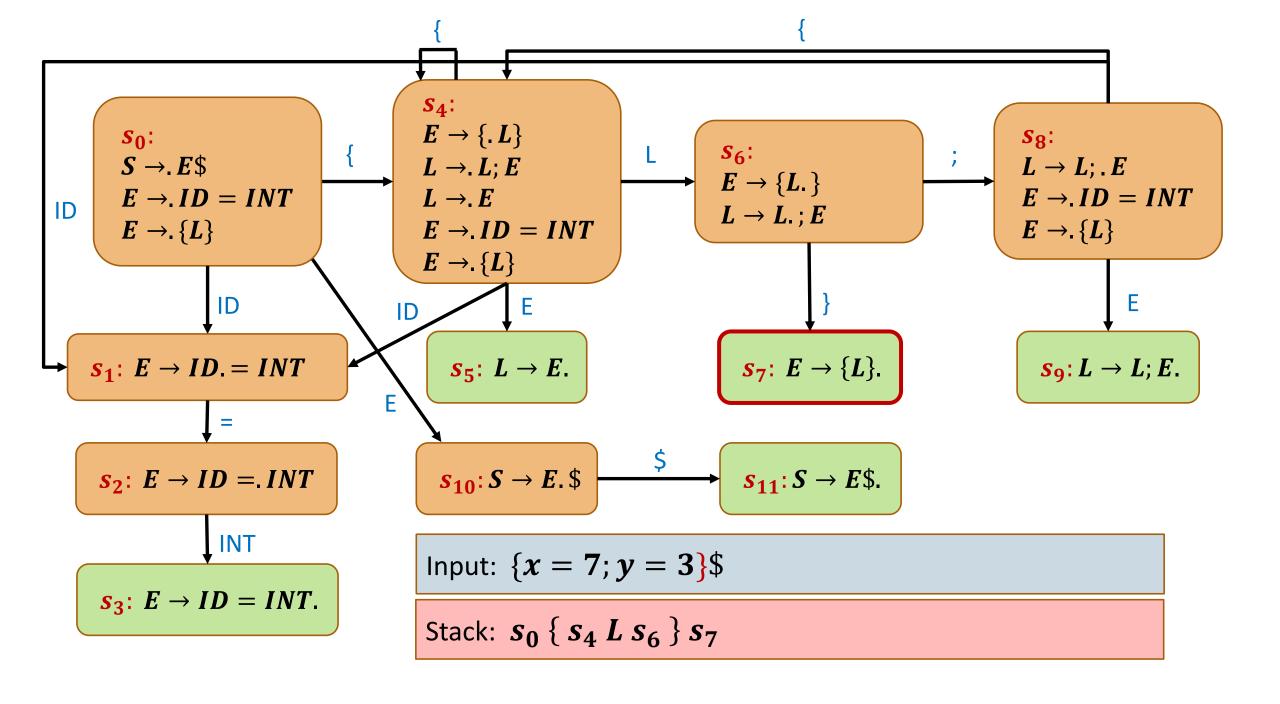


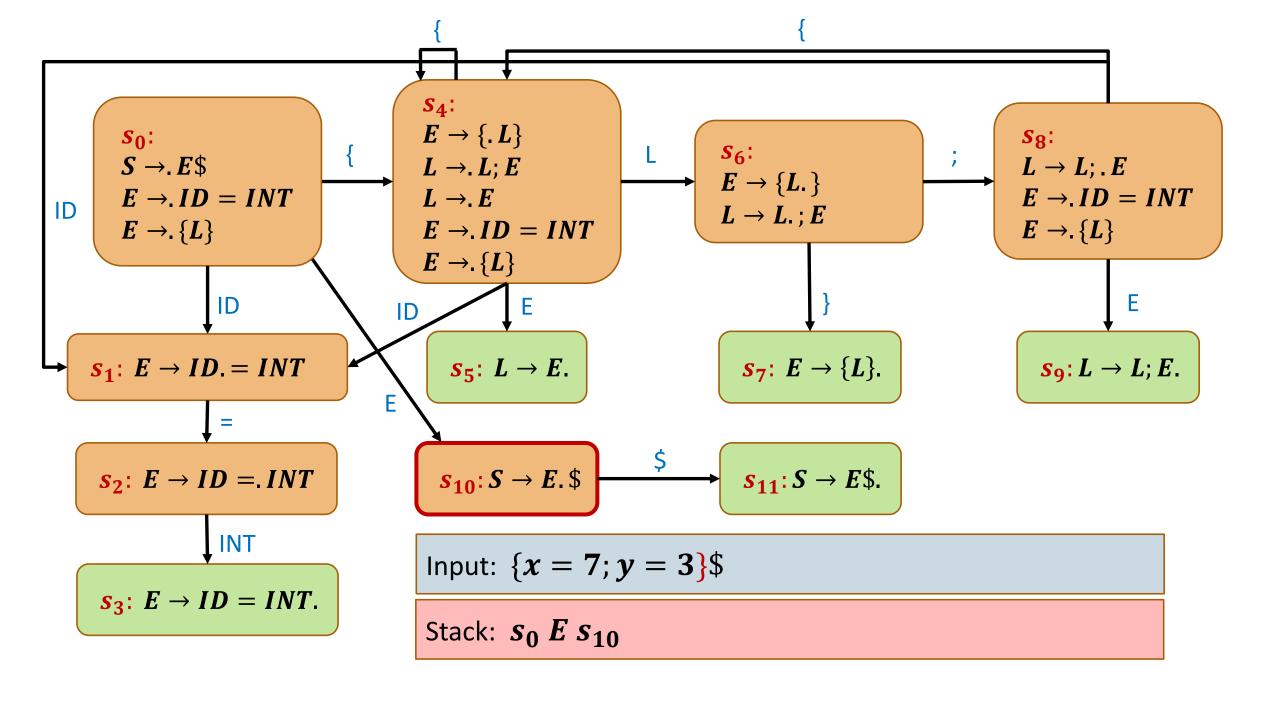


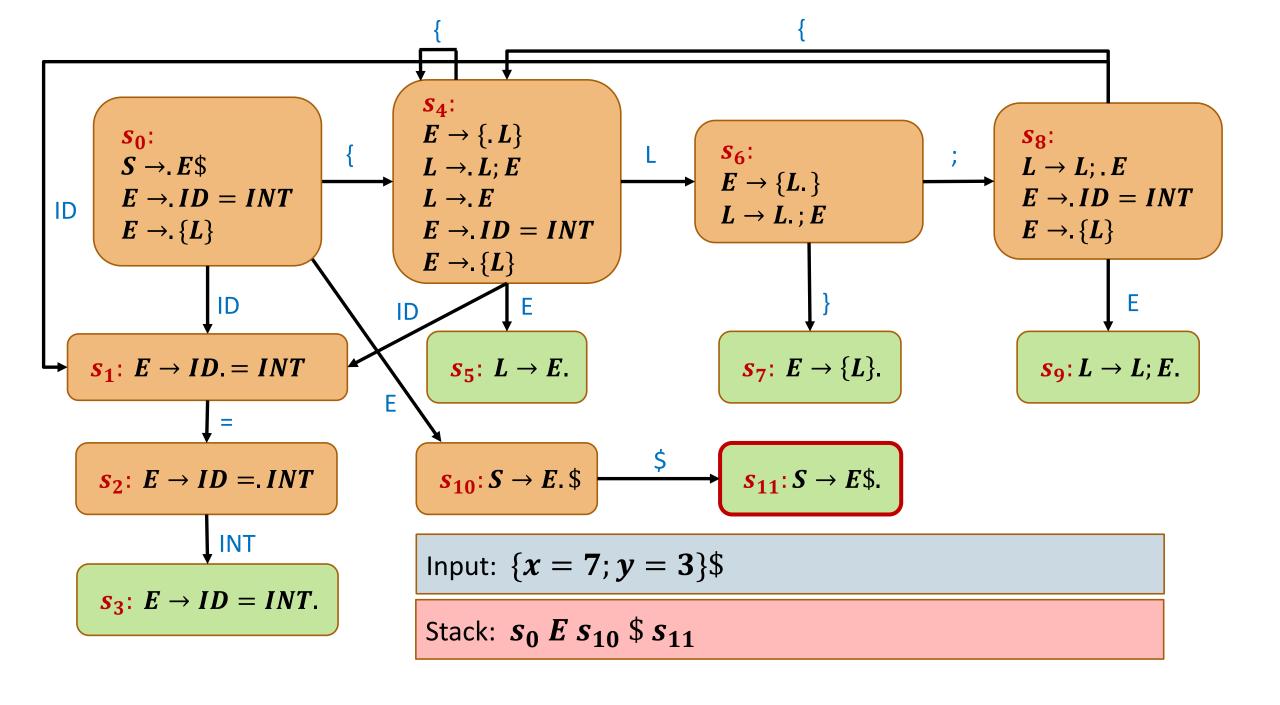


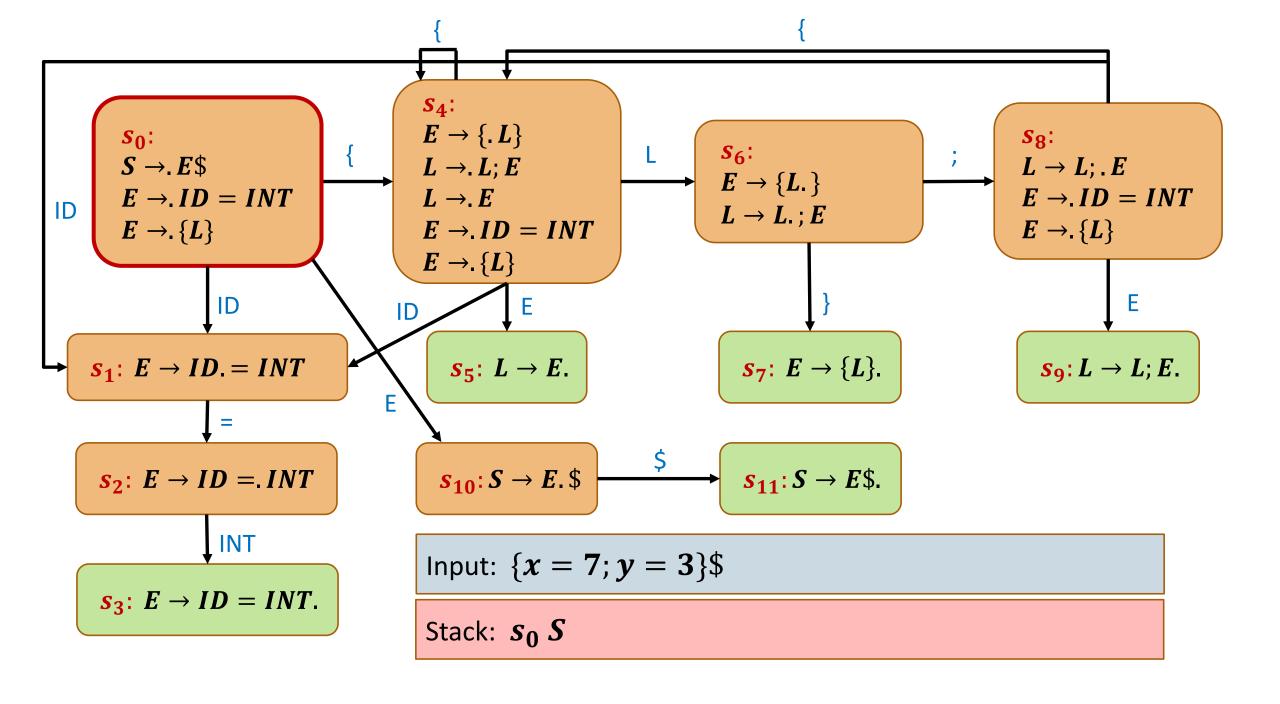










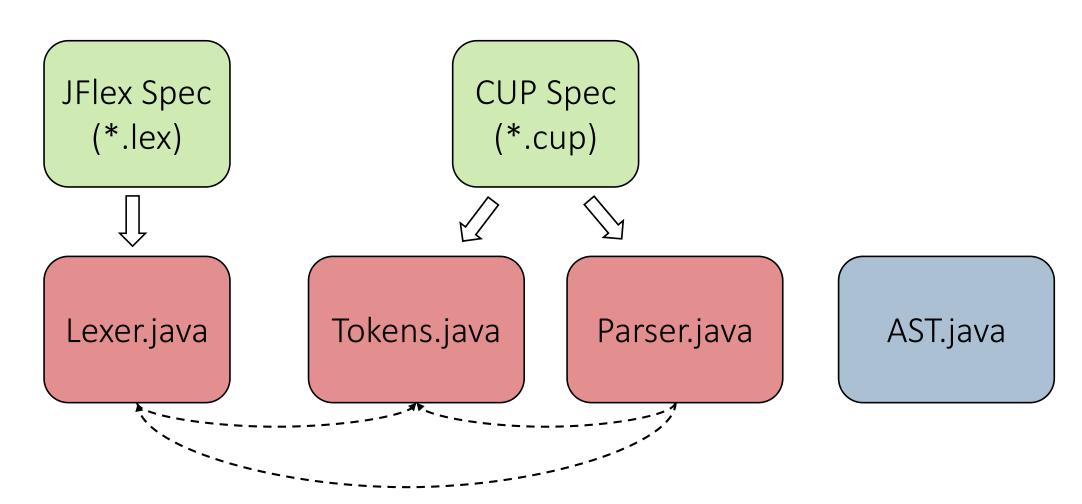


# Parsing with CUP

#### CUP

- Given a user-specified grammar, generates an LALR parser
- Works with JFlex, which provides the parsed tokens
- Other tools:
  - Bison (for C)

# CUP/JFlex Workflow



#### **CUP Format**

```
parser code {:
parser setup
                      scan with {:
 lexer setup -
                      terminal ...
                       non terminal ...
                       start with ...
    grammar
                      <derivation rules...>
```

#### CUP Spec: Parser Setup

```
parser code {:
      public Lexer lexer;
      public Parser(Lexer lexer) {
             super(lexer);
             this.lexer = lexer;
      public void report_error(String message, Object info) {
             System.exit(0);
```

#### CUP Spec: Lexer Setup

```
scan with {:
         Symbol s;
         s = lexer.next_token();
         // print token...
        return s;
:};
```

## **CUP Spec: Terminals**

```
terminal T1;
terminal T2;
terminal T3;
terminal T4;
```

#### CUP Spec: Non-Terminals

```
non terminal AST_NODE_1 E1;
non terminal AST_NODE_2 E2;
non terminal AST_NODE_3 E3;
...
```

#### CUP Spec: Operator Precedence

```
precedence left OP1;
precedence left OP2;
precedence left OP3;
precedence left OP4;
...
```

These are token names...

#### CUP Spec: Grammar

#### CUP Spec: AST Nodes

- We need to decide which node types we have in our AST
- We need to **define** the classes for these AST nodes

## CUP Example

Consider the following CFG:

- $E \rightarrow INT$
- $E \rightarrow V$
- $E \rightarrow E + E$
- $E \rightarrow E E$
- $V \rightarrow ID$
- $V \rightarrow V . ID$

#### CUP Example: Terminals

```
terminal Integer INT;
terminal String ID;
terminal PLUS;
terminal MINUS;
terminal DOT;
```

## CUP Example: Non-Terminals

```
non terminal AST_EXP EXP;
non terminal AST_VAR VAR;
```

#### CUP Example: Operator Precedence

```
precedence left PLUS;
precedence left MINUS;
```

#### CUP Example: Grammar

```
start with EXP;
EXP ::=
  INT:i {: RESULT = new AST EXP INT(i); :} |
  VAR: \lor \{: RESULT = new AST_EXP_VAR(\lor); :\} 
  EXP:e1 PLUS EXP:e2 {: RESULT = new AST EXP BINOP(e1, e2, 0); :} |
  EXP:e1 MINUS EXP:e2 {: RESULT = new AST EXP BINOP(e1, e2, 1); :};
VAR ::=
  ID:name {: RESULT = new AST VAR SIMPLE(name); :} |
  VAR:v DOT ID:fieldName {: RESULT = new AST VAR FIELD(v, fieldName); :};
```

For the non-terminal *VAR*:

```
public abstract class AST_VAR extends AST_Node {
}
```

For the rule *VAR* ::= *ID*:name:

```
public class AST_VAR_SIMPLE extends AST_VAR {
    public String name;
    public AST_VAR_SIMPLE(String name) {
        this.name = name;
    }
}
```

For the rule *VAR* ::= *VAR:v DOT ID:fieldName* :

```
public class AST_VAR_FIELD extends AST_VAR {
    public AST_VAR var;
    public String fieldName;
    public AST_VAR_FIELD(AST_VAR var, String fieldName) {
        this.var = var;
        this.fieldName = fieldName;
    }
}
```

For the non-terminal *EXP*:

```
public abstract class AST_EXP extends AST_Node {
}
```

For the rule **EXP** ::= **INT**:**i**:

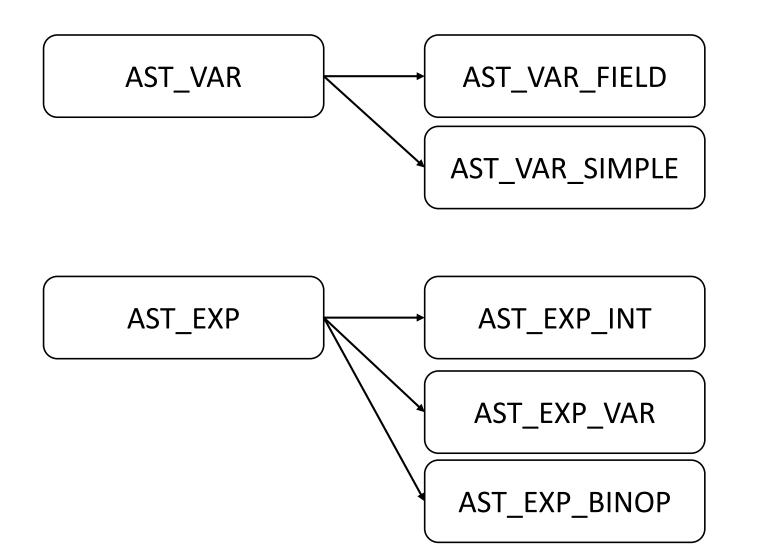
```
public class AST_EXP_INT extends AST_EXP {
    public int value;
    public AST_EXP_INT(int value) {
        this.value = value;
    }
}
```

For the rule *EXP* ::= *VAR:v*:

```
public class AST_EXP_VAR extends AST_EXP {
    public AST_VAR var;
    public AST_EXP_VAR(AST_VAR var) {
        this.var = var;
    }
}
```

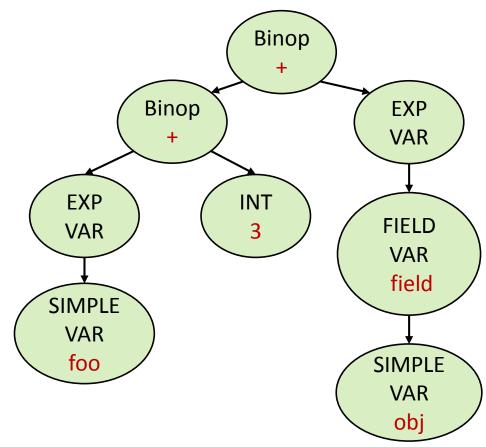
```
For the rule EXP ::= EXP:e1 <OP> EXP:e2 :
public class AST EXP BINOP extends AST EXP {
      int OP;
      public AST EXP left;
      public AST EXP right;
      public AST_EXP_BINOP(AST_EXP left, AST_EXP right, int OP) {
            this.left = left;
             this.right = right;
            this.OP = OP;
```

## Class Hierarchy (Inheritance)



## CUP Example: Debugging

We can generate an image of the AST (using the exercise template) For the input foo + 3 + obj.field we have:



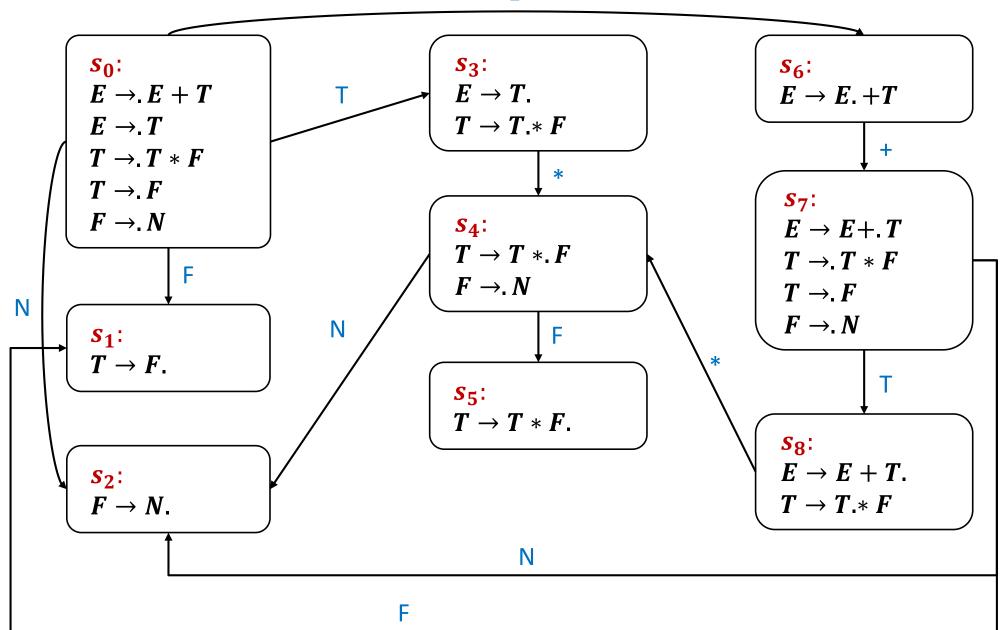
# SLR(1), LR(1)

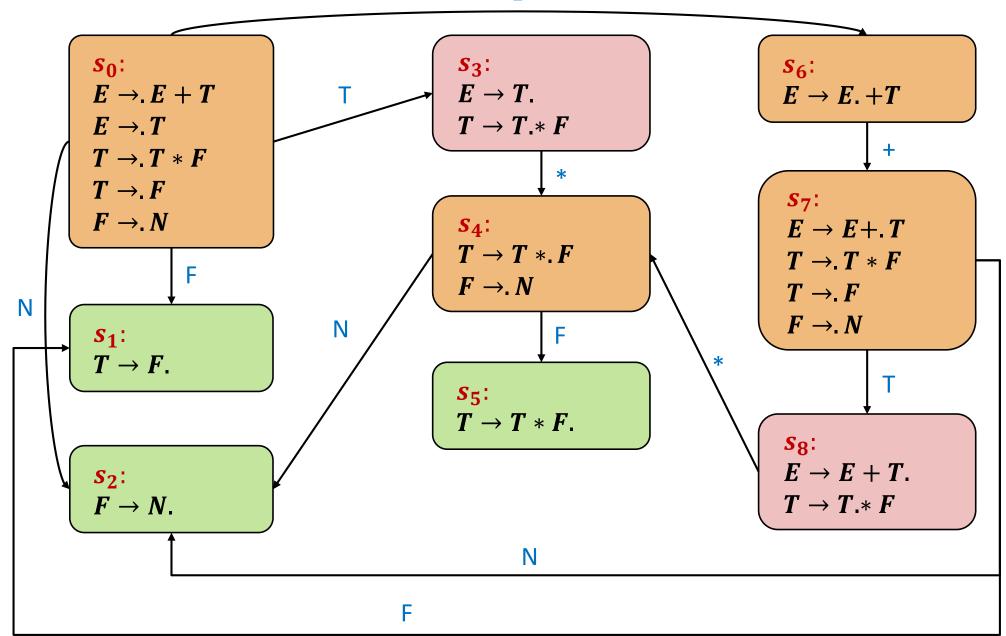
## LR(0) Parsing

Consider the following CFG:

- $E \rightarrow E + T$
- $E \rightarrow T$
- $T \rightarrow T * F$
- $T \rightarrow F$
- $F \rightarrow N$

What will be the **transition system** of the LR(0) parser for this CFG?





## LR(0) Conflict

• The conflict occurs when the next token is: \*

- $E \rightarrow E + T$
- $E \rightarrow T$
- $T \rightarrow T * F$
- $T \rightarrow F$
- $F \rightarrow N$

**S**<sub>3</sub>:

 $E \rightarrow T$ .

T o T.\*F

## LR(0) Conflict

- E can be followed only by: +\$
- Taking into account the next token can help...

• 
$$E \rightarrow E + T$$

- $E \rightarrow T$
- $T \rightarrow T * F$
- $T \rightarrow F$
- $F \rightarrow N$

**S**<sub>3</sub>:

$$E \rightarrow T$$
.

$$m{E} 
ightarrow m{T}$$
 .\*  $m{F}$ 

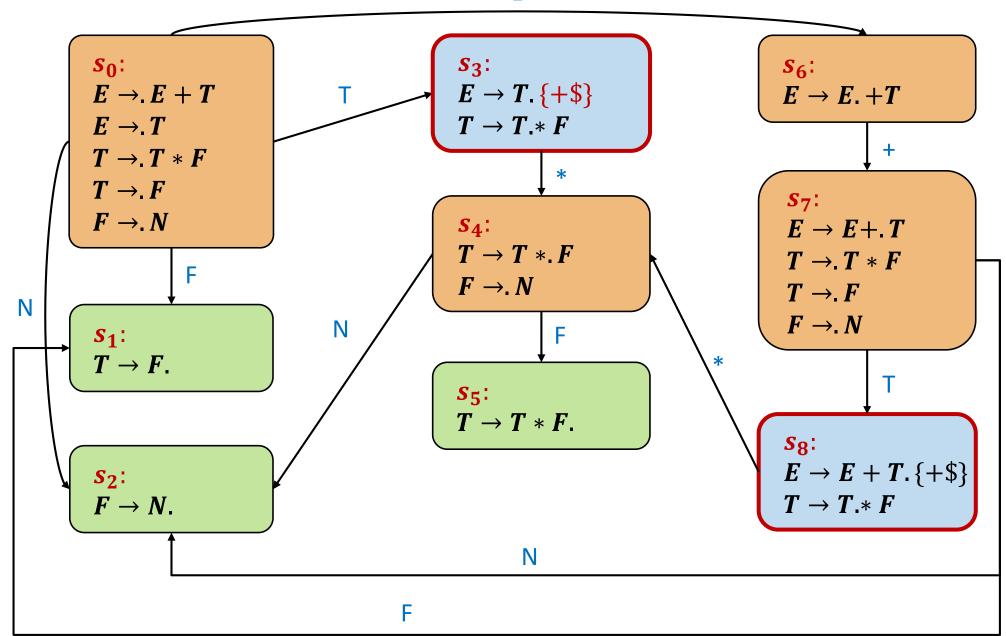
## **SLR(1)**

- Same push-down automaton as in LR(0)
- But reduce items has a look-ahead set
  - $A \to \alpha.\{t_1, t_2, ...\}$
  - where  $Follow(A) = \{t_1, t_2, ...\}$

## **SLR(1)**

- ullet Solve shift-reduce conflicts using the look-ahead token t
- If  $Follow(Y) \cap First(\beta) = \emptyset$ 
  - If  $t \in Follow(Y)$ , apply the reduce
  - Otherwise, apply the shift

$$Y \rightarrow \gamma. \{...\}$$
  
 $X \rightarrow \alpha. \beta$ 

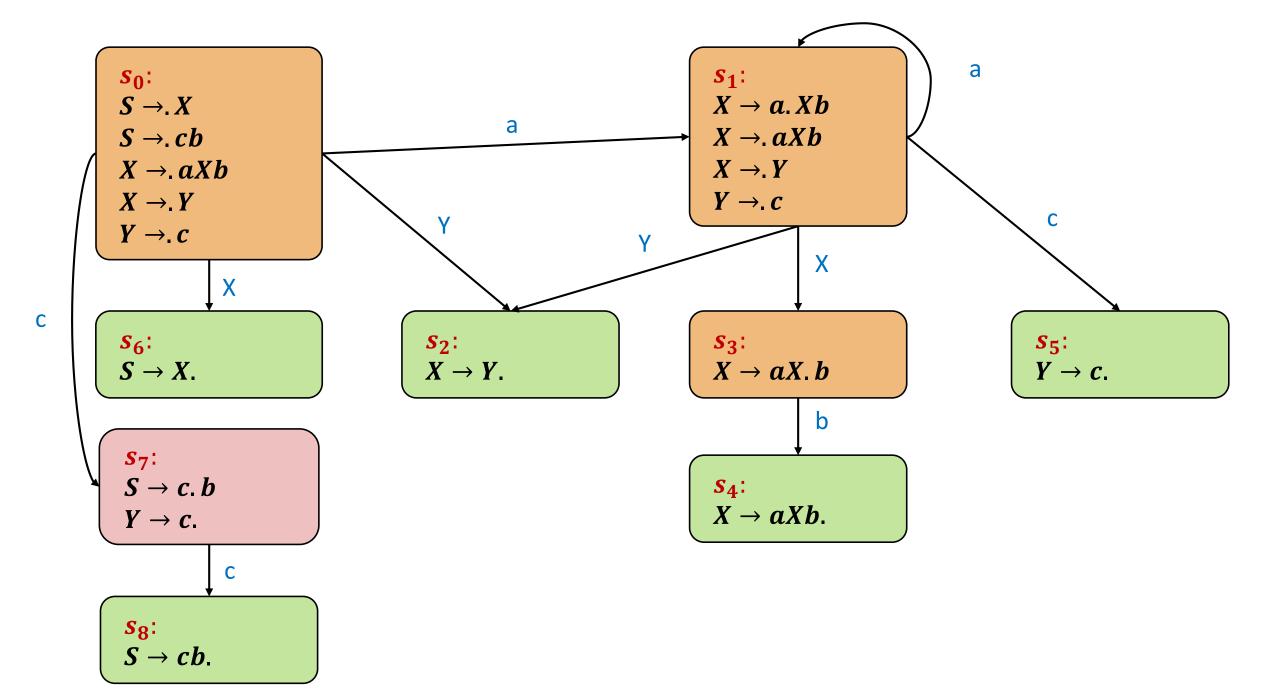


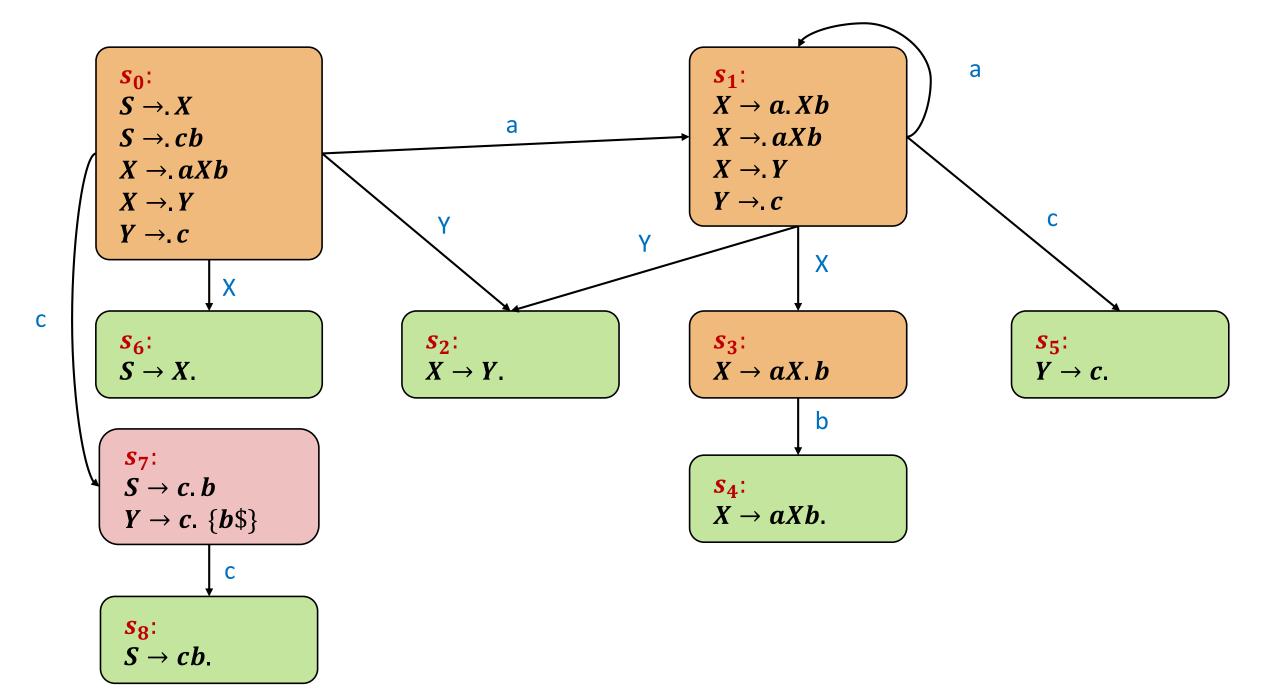
## SLR(1) Parsing

Consider the following CFG:

- $S \rightarrow X$
- $S \rightarrow cb$
- $X \rightarrow aXb$
- $X \to Y$
- $Y \rightarrow c$

What will be the **transition system** of the SLR(1) parser for this CFG?





### SLR(1) Conflict

- The conflict occurs when the next token is: b
- Relying on Follow(Y)
  - Considers all the occurrences of Y in all the states / grammar

- $S \rightarrow X$
- $S \rightarrow cb$
- $X \rightarrow aXb$
- $X \to Y$
- $Y \rightarrow c$

```
S_7:
S \to c.b {$}
Y \to c. \{b$}
```

# LR(1)

Maintain items with more precise look-ahead sets

An LR(1) item is of the form:

- $N \to \alpha . \beta \{\sigma\}$
- where  $\sigma = t_1, t_2, \dots$  (terminals)

### LR(1) Item Closure Set

The LR(1) closure set of an LR(1) item i is a set S such that:

- $i \in S$
- If  $A \to \alpha . N\beta \{\sigma\} \in S$  then for each rule  $N \to \gamma$ :
  - $N \rightarrow \gamma\{\tau\} \in S$ , where  $\tau = First(\beta, \{\sigma\})$

Definition for  $First(\beta, \{\sigma\})$ :

- If  $\beta$  is not nullable:
  - $First(\beta)$
- Otherwise:
  - $(First(\beta) \cup {\sigma}) \setminus {\epsilon}$

## LR(1) Parsing

Consider the following CFG:

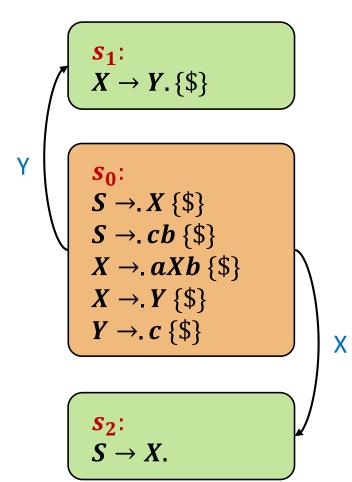
- $S \rightarrow X$
- $S \rightarrow cb$
- $X \rightarrow aXb$
- $X \to Y$
- $Y \rightarrow c$

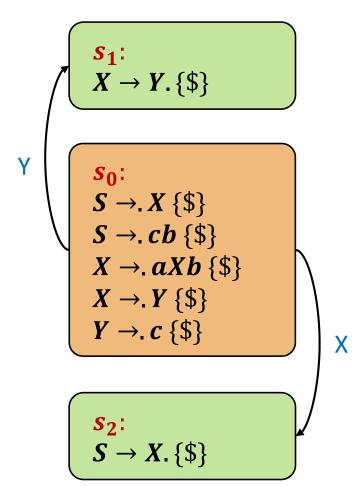
What will be the **transition system** of the LR(1) parser for this CFG?

 $S_0$ :  $S \rightarrow X \{\$\}$   $S \rightarrow cb \{\$\}$ 

 $S_0$ :  $S \to X \{\$\}$   $S \to cb \{\$\}$   $X \to aXb \{\$\}$   $X \to Y \{\$\}$  $Y \to c \{\$\}$ 

```
S_{1}: X \to Y. \{\$\}
S_{0}: S \to X \{\$\}
S \to cb \{\$\}
X \to aXb \{\$\}
X \to Y \{\$\}
Y \to C \{\$\}
```





```
s<sub>1</sub>:
            X \to Y.\{\$\}
            s_0:
            S \rightarrow X \{\$\}
            S \rightarrow cb \{\$\}
           X \rightarrow aXb \{\$\}
            X \rightarrow Y \{\$\}
            Y \rightarrow c \{\$\}
                                                     X
C
             s<sub>2</sub>:
            S \rightarrow X.\{\$\}
            S \rightarrow c.b
            Y \rightarrow c.
```

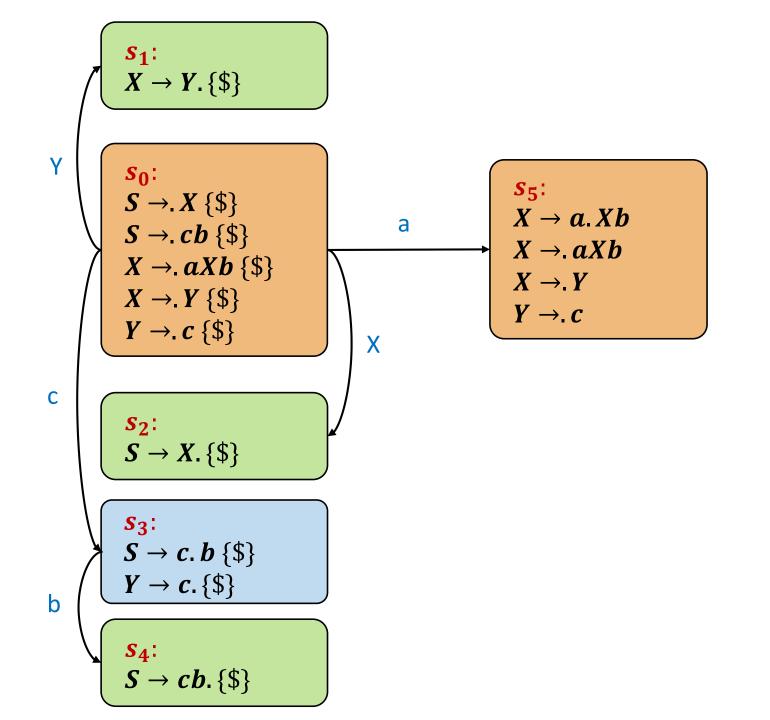
```
s<sub>1</sub>:
             X \rightarrow Y.\{\$\}
               s<sub>0</sub>:
              S \rightarrow X \{\$\}
              S \rightarrow cb \{\$\}
             X \rightarrow aXb \{\$\}
             X \rightarrow Y \{\$\}
             Y \rightarrow c \{\$\}
                                                            X
C
              s<sub>2</sub>:
              S \rightarrow X.\{\$\}
              s<sub>3</sub>:
              S \rightarrow c.b \{\$\}
             Y \rightarrow c. \{\$\}
```

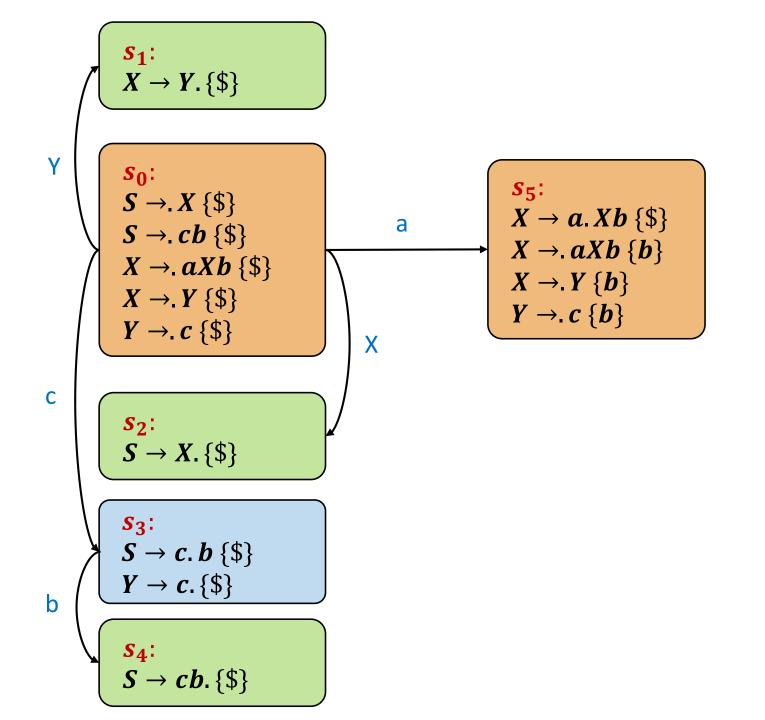
```
X \rightarrow Y.\{\$\}
               s<sub>0</sub>:
               S \rightarrow X \{\$\}
               S \rightarrow cb \{\$\}
              X \rightarrow aXb \{\$\}
              X \rightarrow Y \{\$\}
              Y \rightarrow c \{\$\}
                                                             X
C
               s<sub>2</sub>:
              S \rightarrow X.\{\$\}
              S<sub>3</sub>:
              S \rightarrow c.b \{\$\}
             Y \rightarrow c.\{\$\}
```

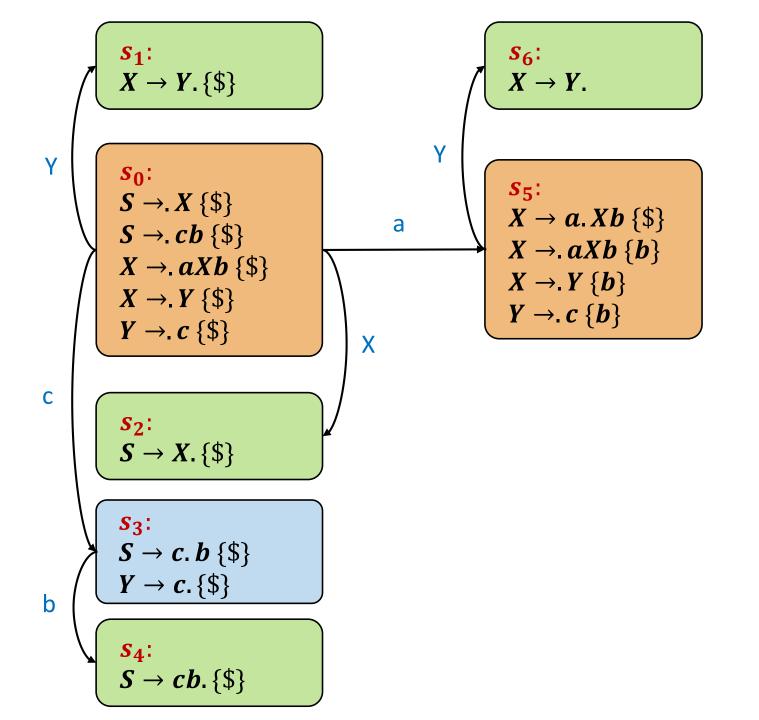
In SLR(1) we had: {b\$}

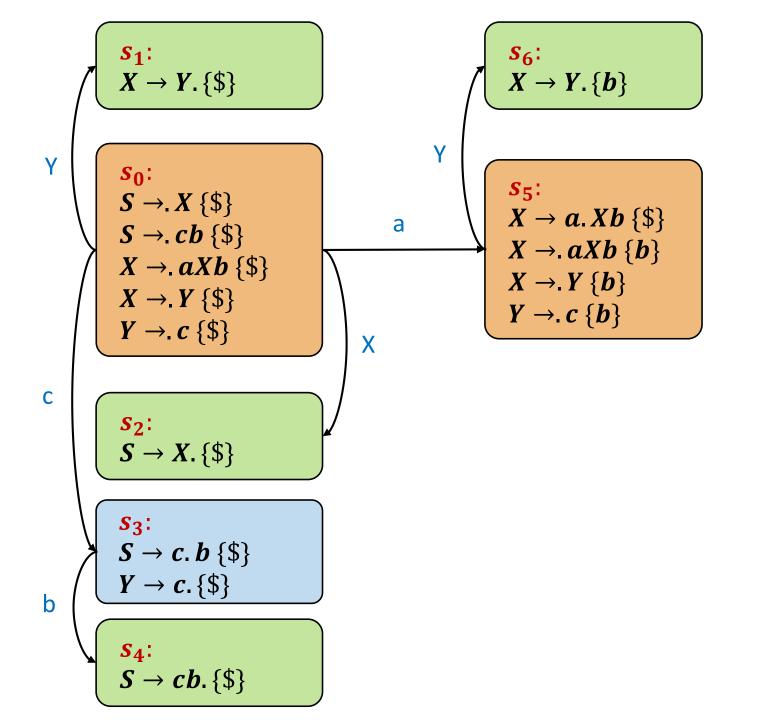
```
s<sub>1</sub>:
             X \rightarrow Y.\{\$\}
               s<sub>0</sub>:
              S \rightarrow X \{\$\}
              S \rightarrow cb \{\$\}
             X \rightarrow aXb \{\$\}
              X \rightarrow Y \{\$\}
              Y \rightarrow c \{\$\}
                                                            X
C
               s<sub>2</sub>:
              S \rightarrow X.\{\$\}
              S<sub>3</sub>:
              S \rightarrow c.b \{\$\}
             Y \rightarrow c.\{\$\}
b
              S<sub>4</sub>:
              S \rightarrow cb.
```

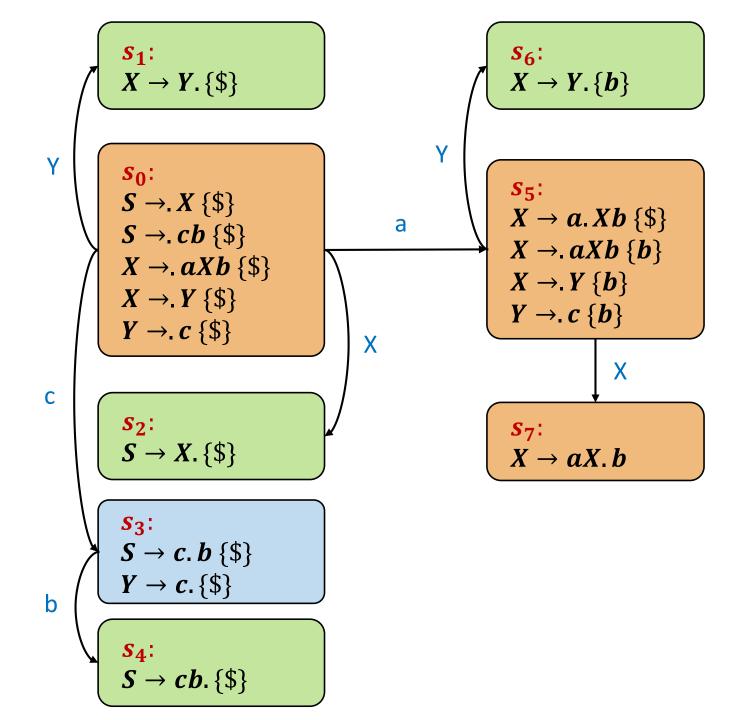
```
s<sub>1</sub>:
              X \rightarrow Y.\{\$\}
               s<sub>0</sub>:
              S \rightarrow X \{\$\}
              S \rightarrow cb \{\$\}
             X \rightarrow aXb \{\$\}
              X \rightarrow Y \{\$\}
              Y \rightarrow c \{\$\}
                                                             X
C
               s<sub>2</sub>:
              S \rightarrow X.\{\$\}
              S<sub>3</sub>:
              S \rightarrow c.b \{\$\}
             Y \rightarrow c.\{\$\}
b
               S<sub>4</sub>:
               S \rightarrow cb. \{\$\}
```

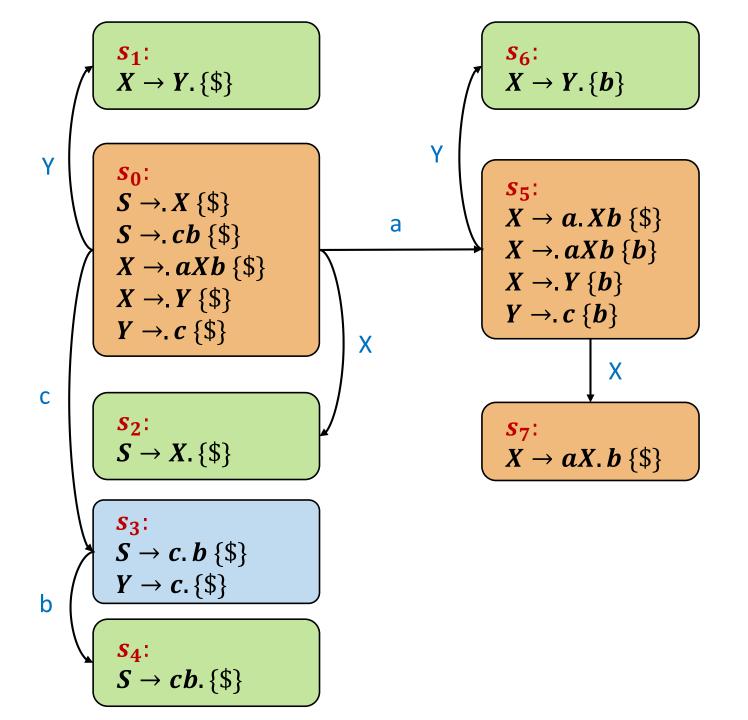


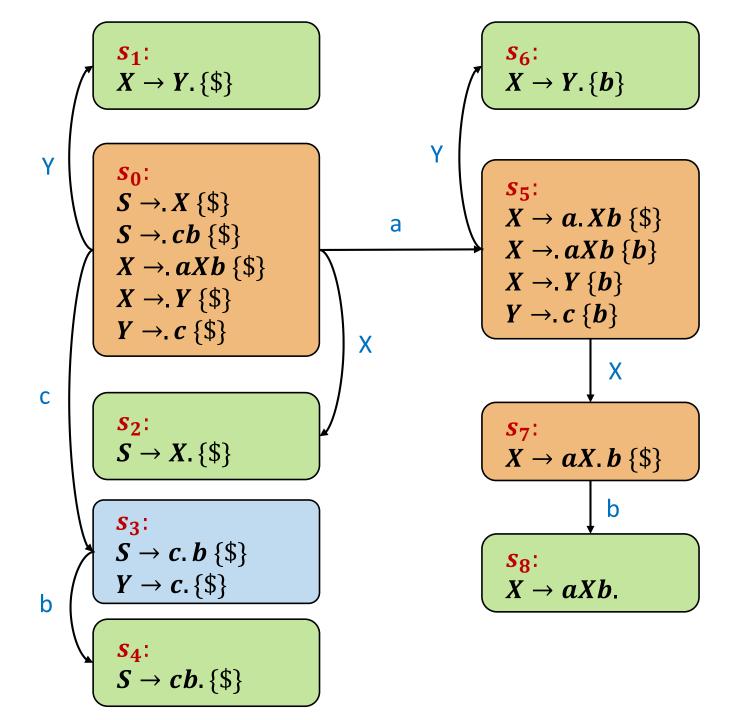


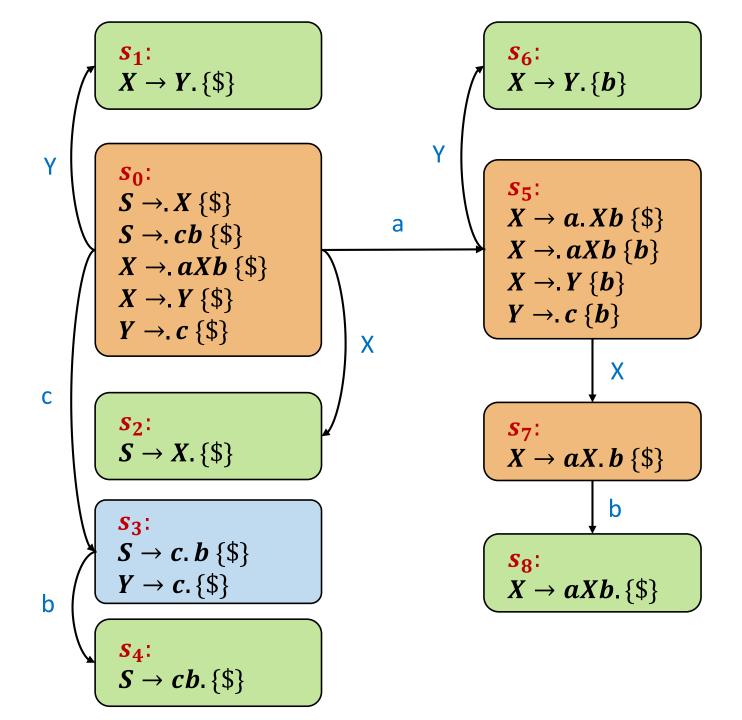


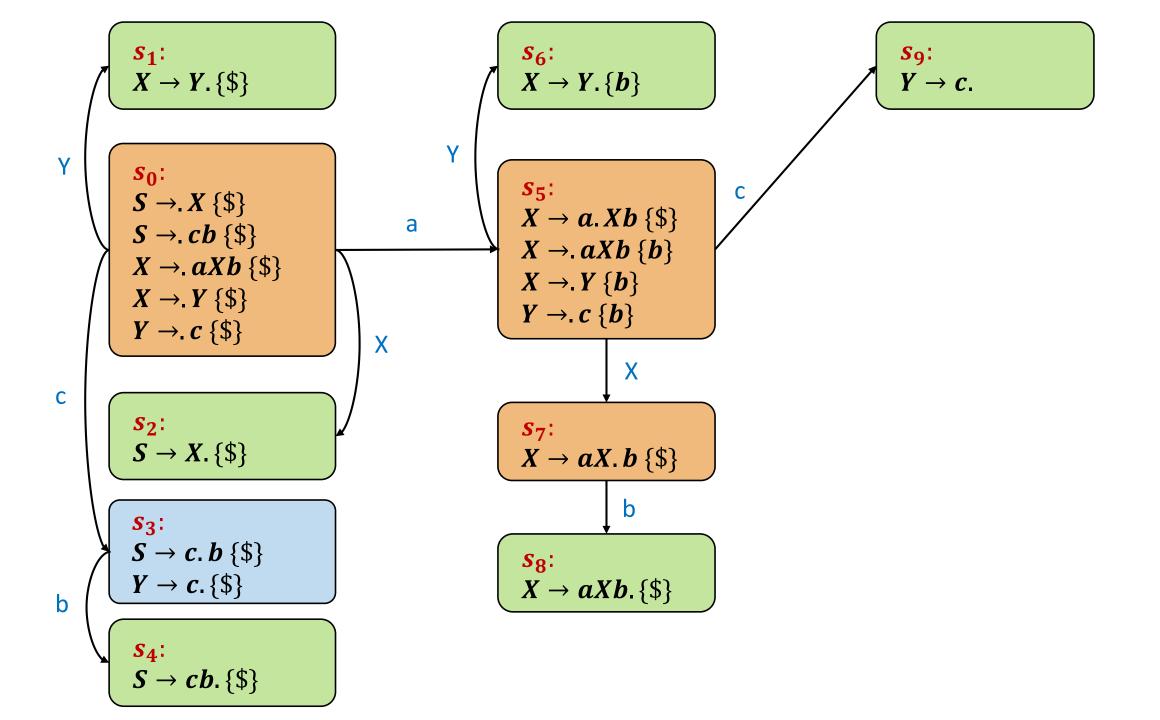


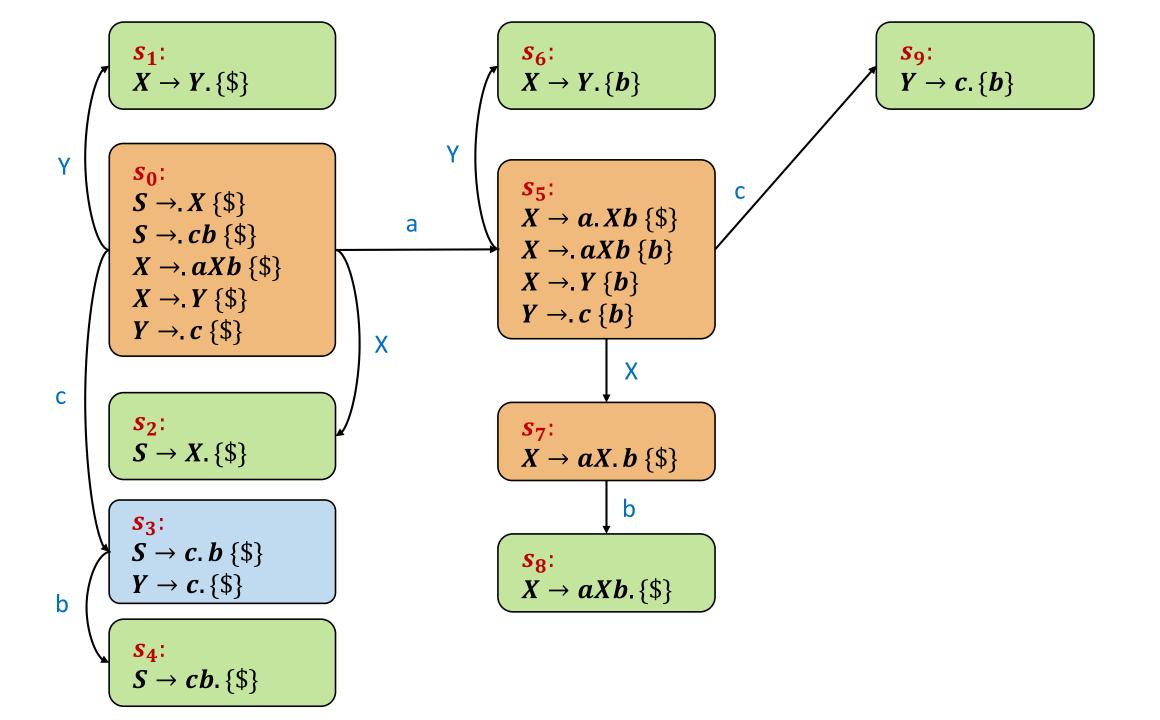


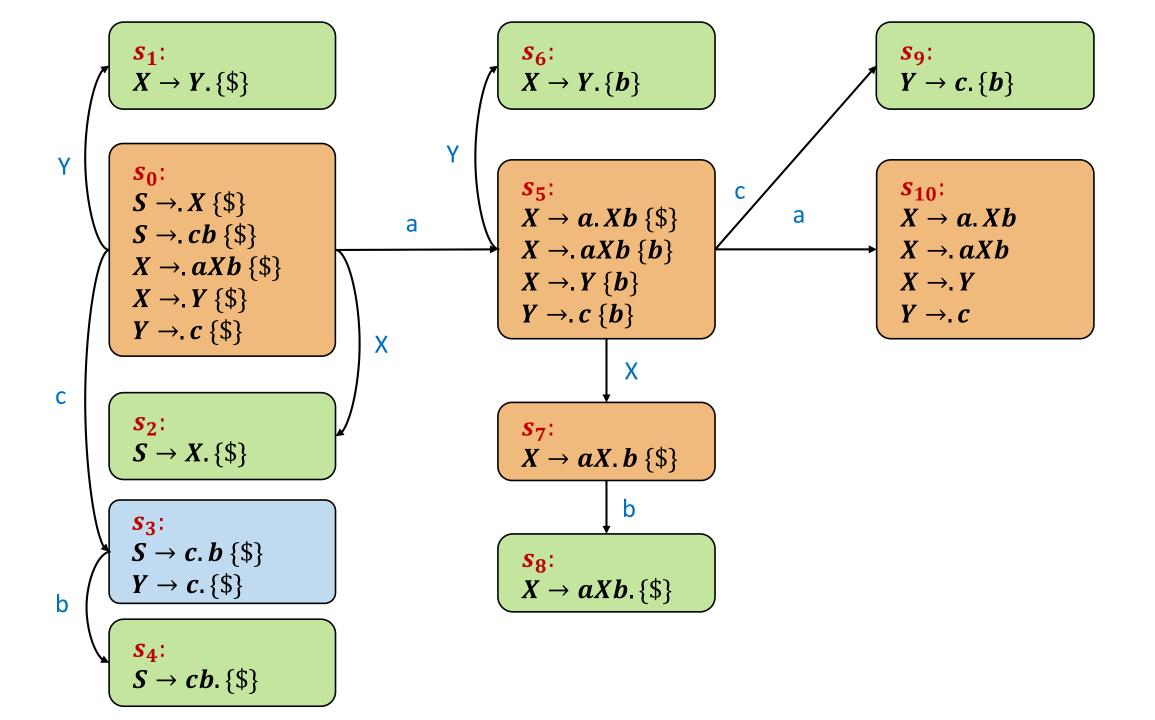


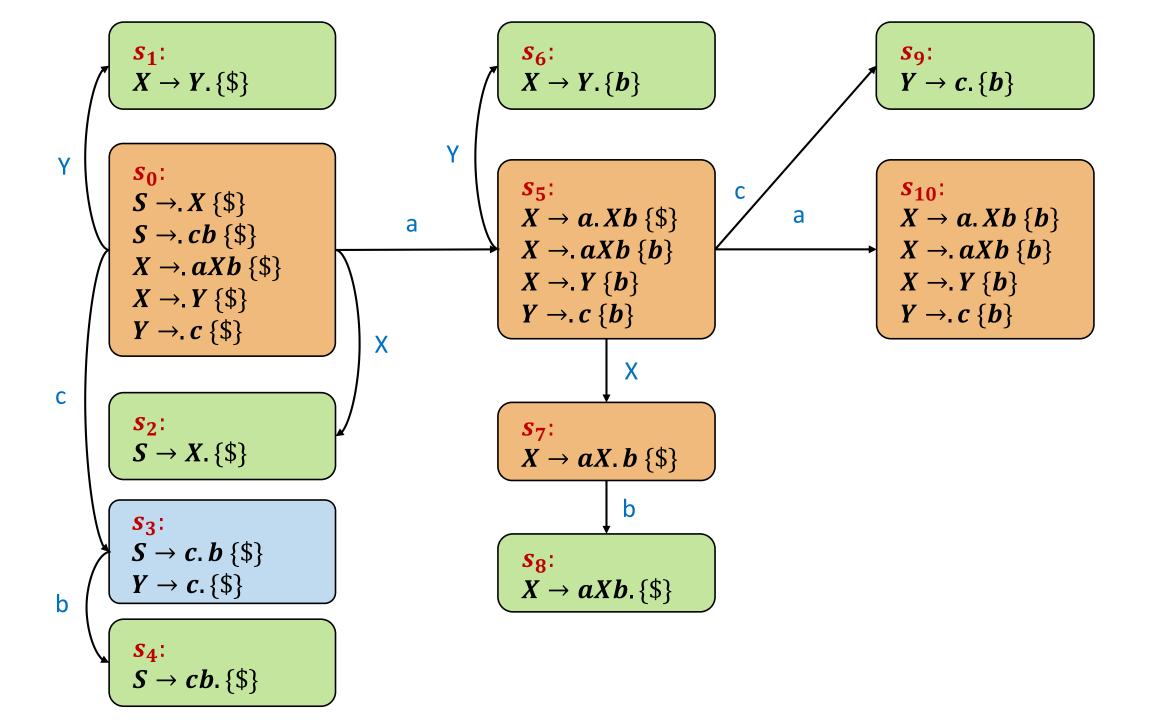


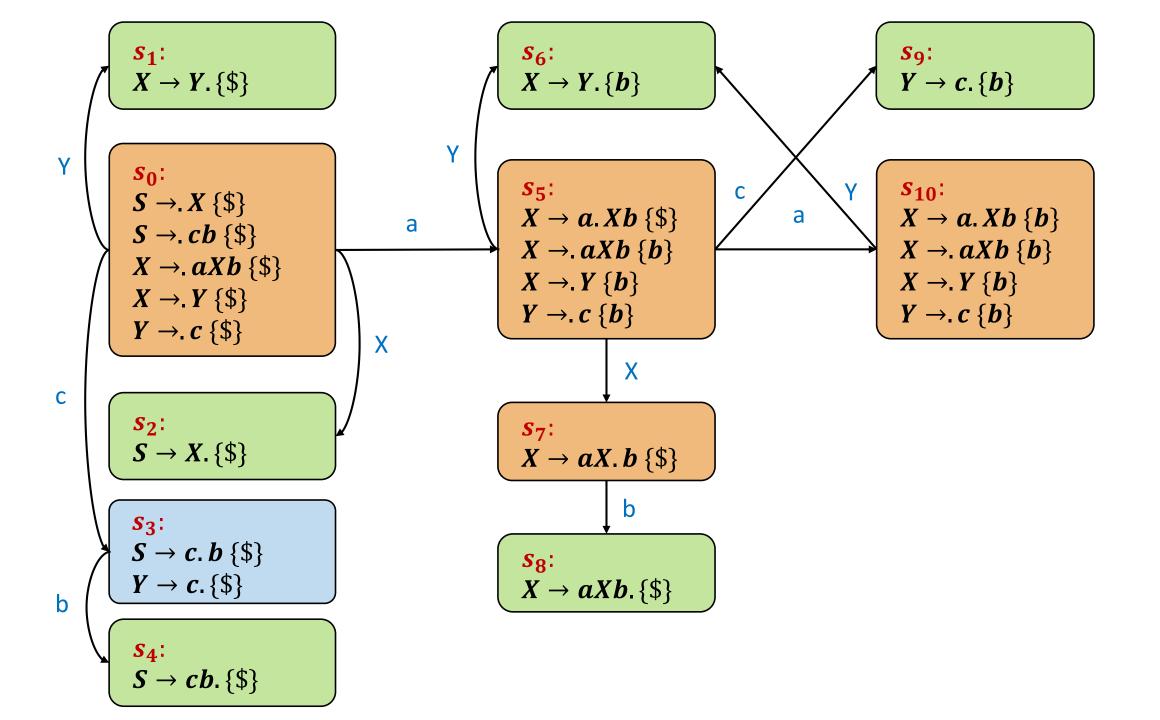


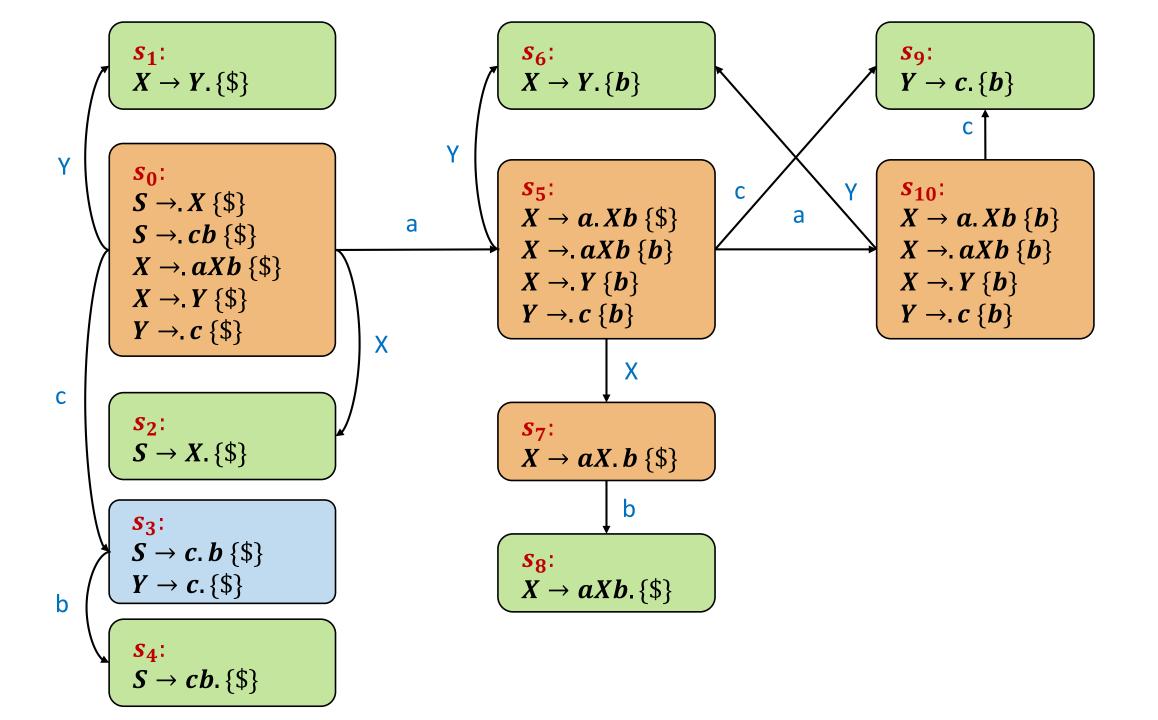


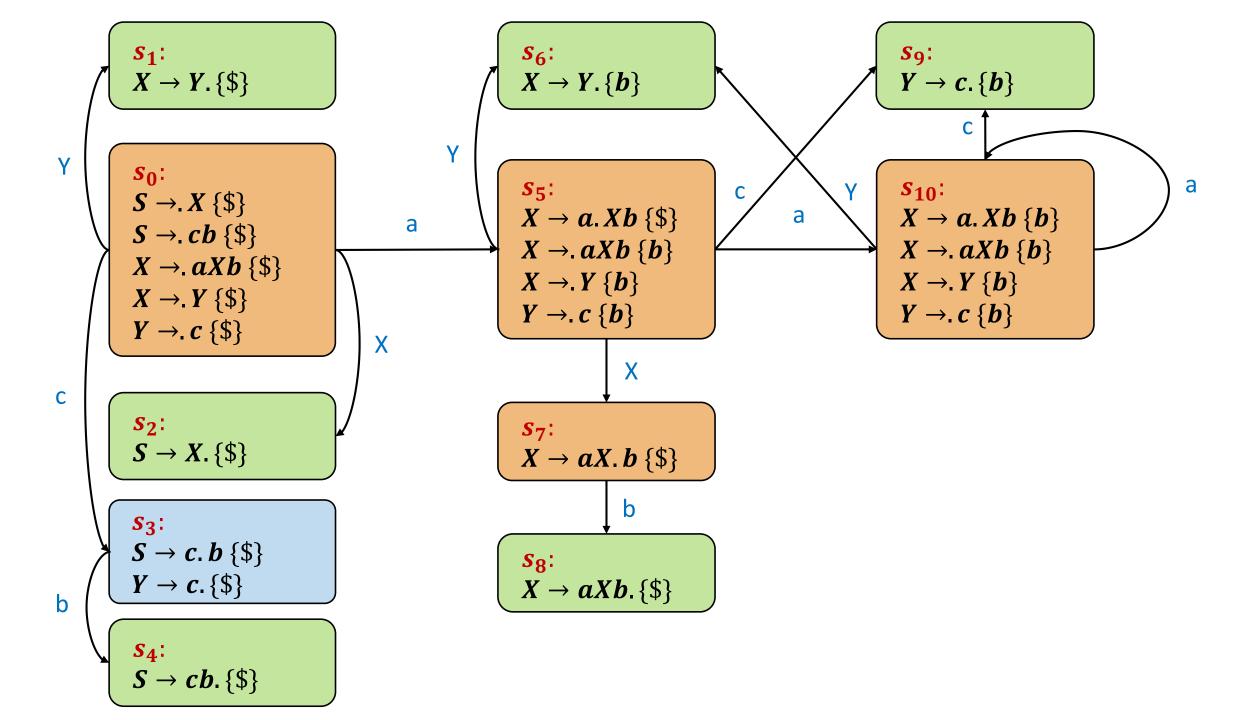


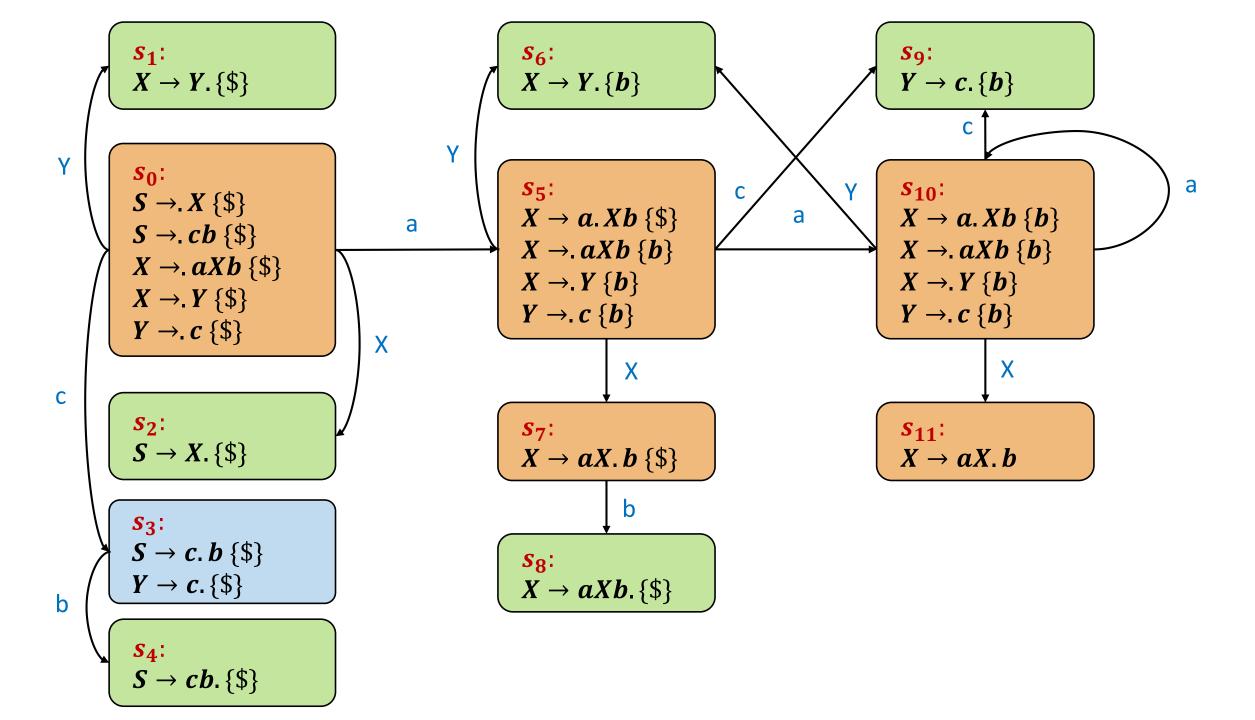


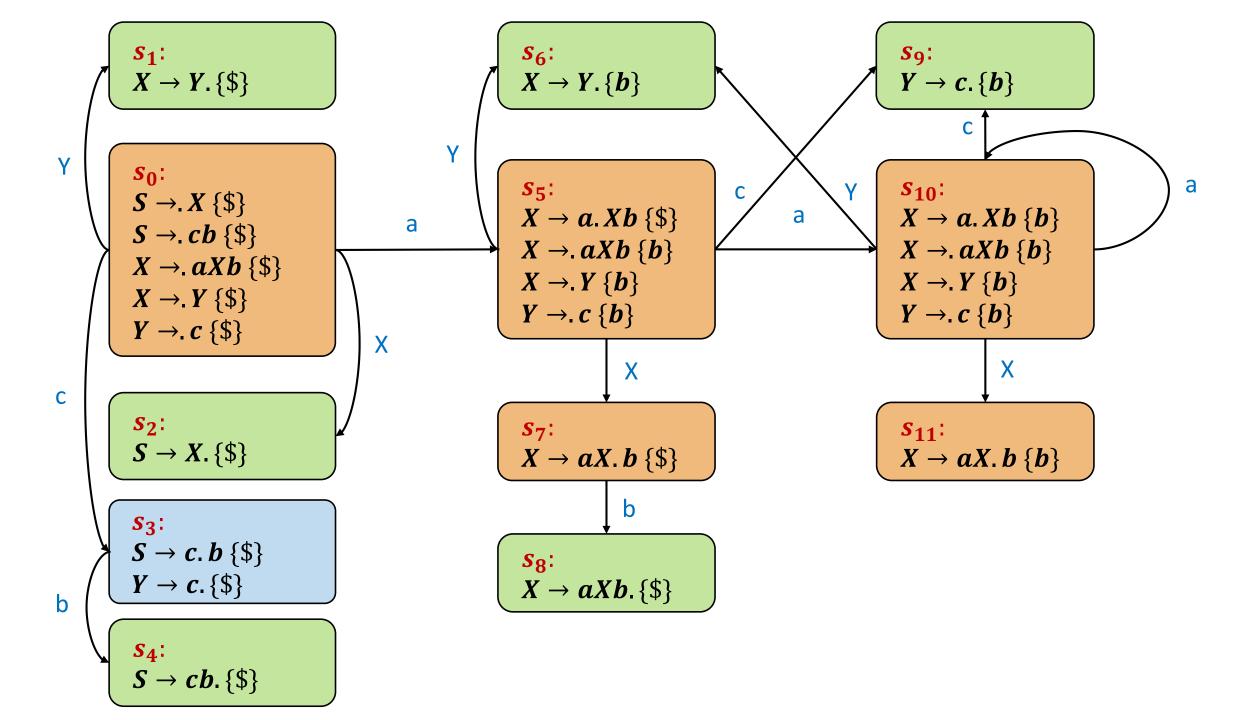


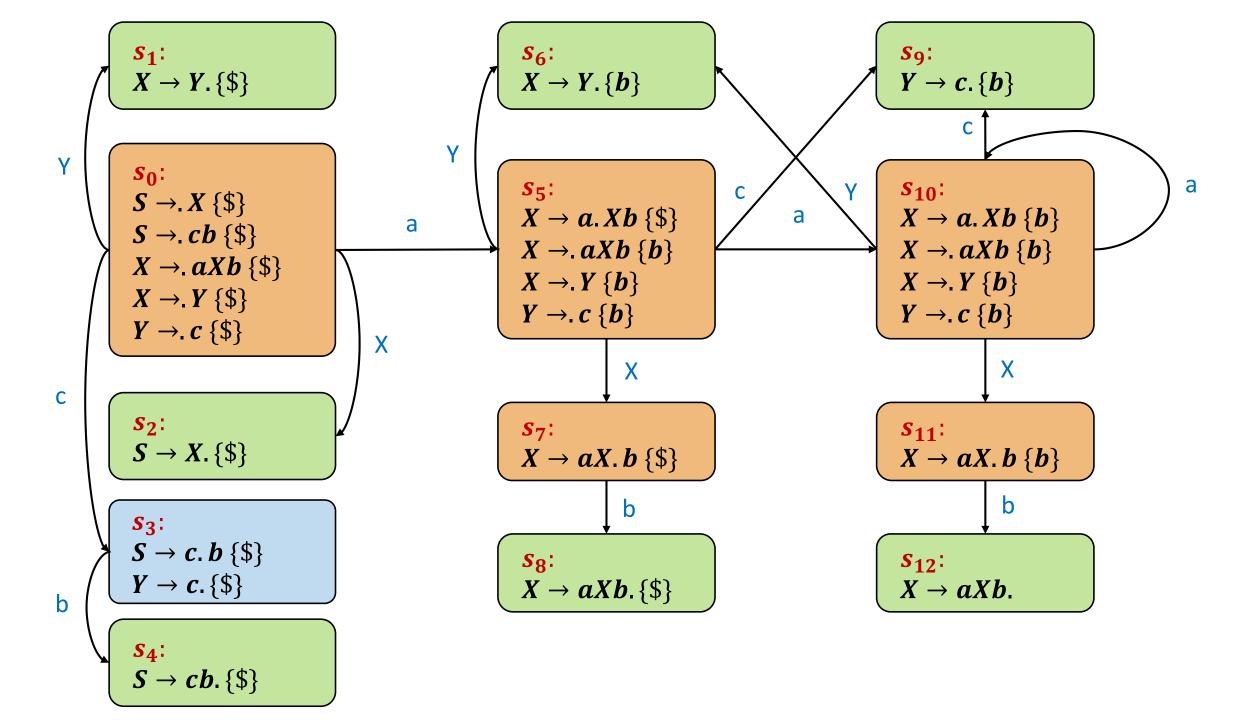


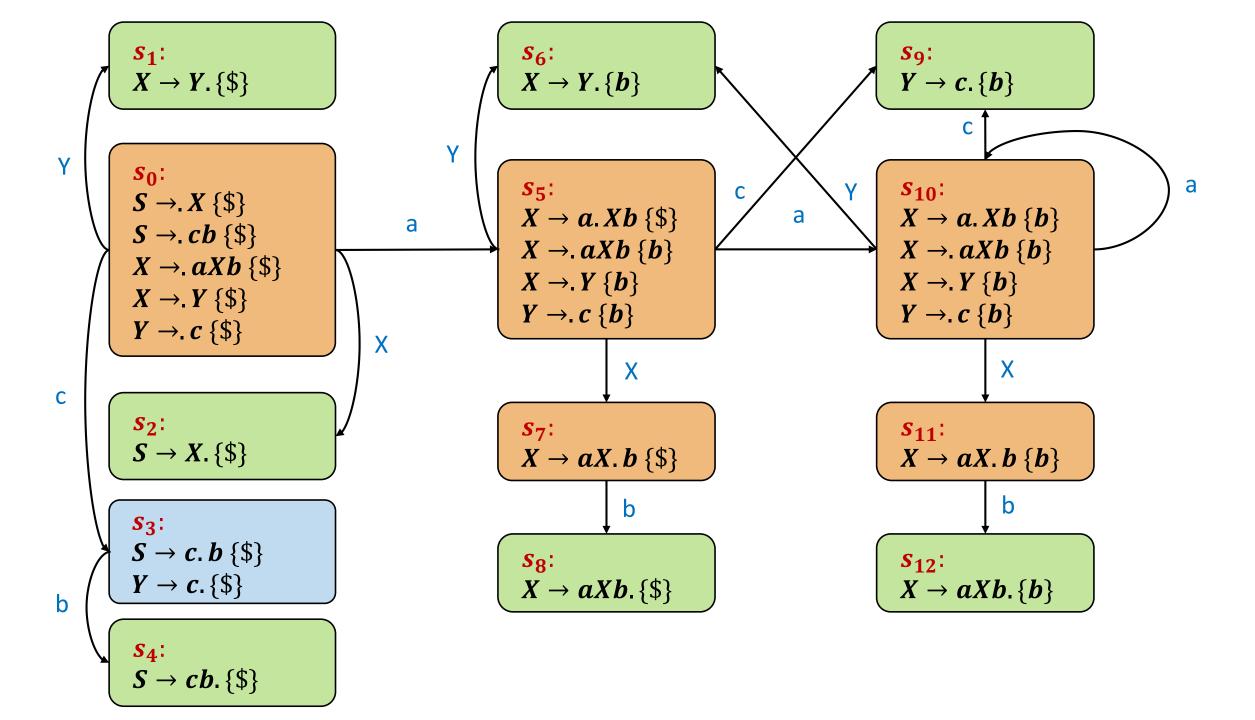










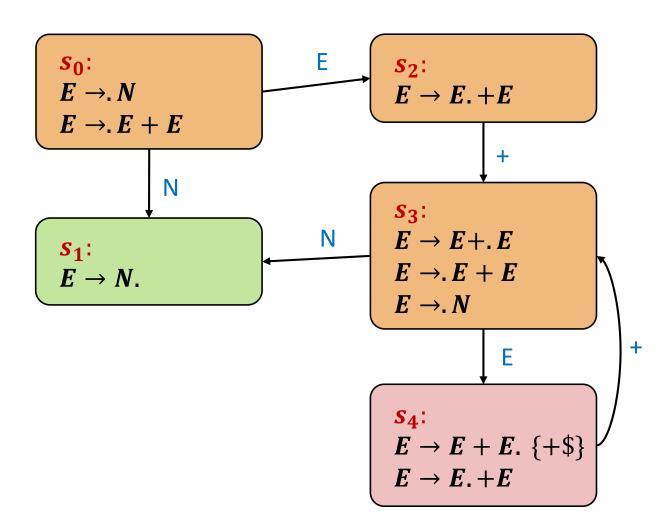


## Resolving Conflicts

Consider the following CFG:

- $E \rightarrow N$
- $E \rightarrow E + E$

What will be the transition system of the SLR(1) parser for this CFG?



### Resolving Conflicts

How will affect associativity?

$$S_4$$
:
 $E \rightarrow E + E$ .  $\{+\$\}$ 
 $E \rightarrow E$ .  $+E$ 

How will affect associativity?

#### Shift:

Right associative

#### Reduce:

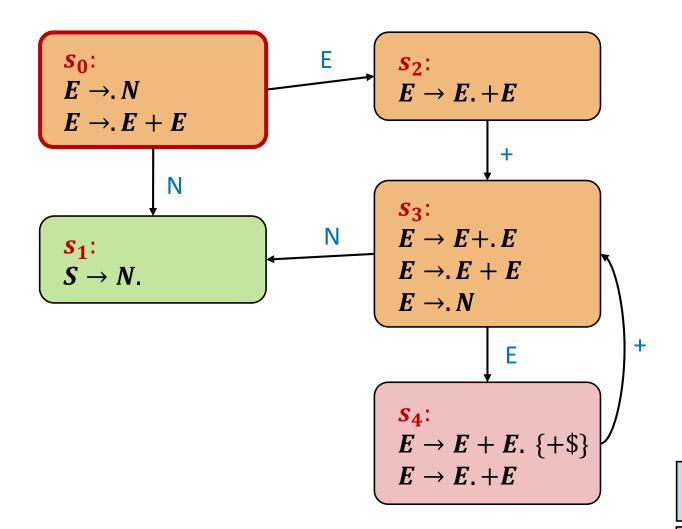
Left associative

S<sub>4</sub>:
$$E \rightarrow E + E. \{+\$\}$$

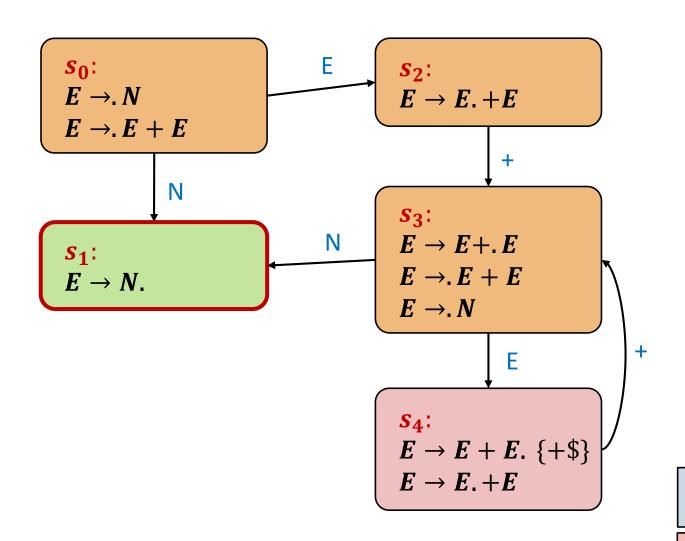
$$E \rightarrow E. + E$$

When resolving using the **reduce** item:

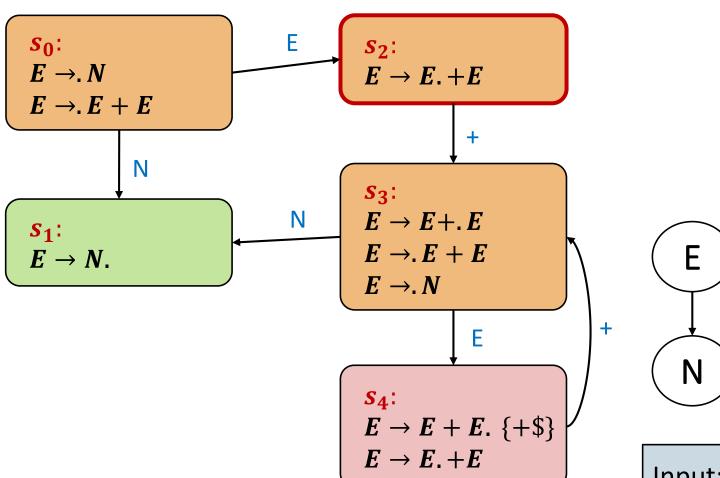
Left associative

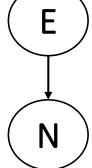


Stack:  $s_0$ 

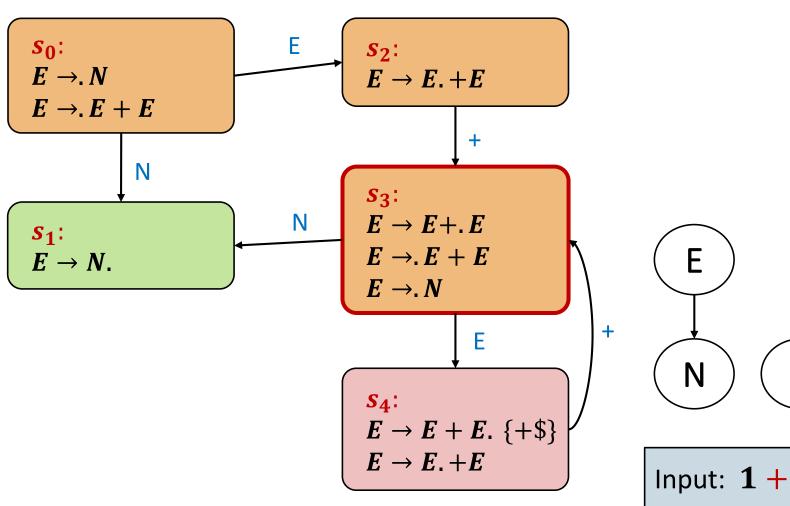


Stack:  $s_0 N s_1$ 

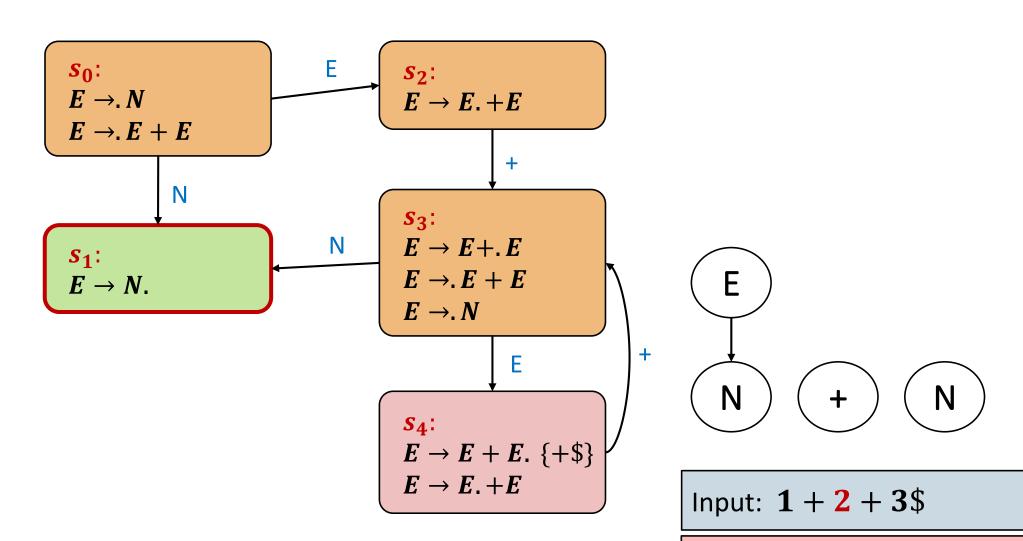




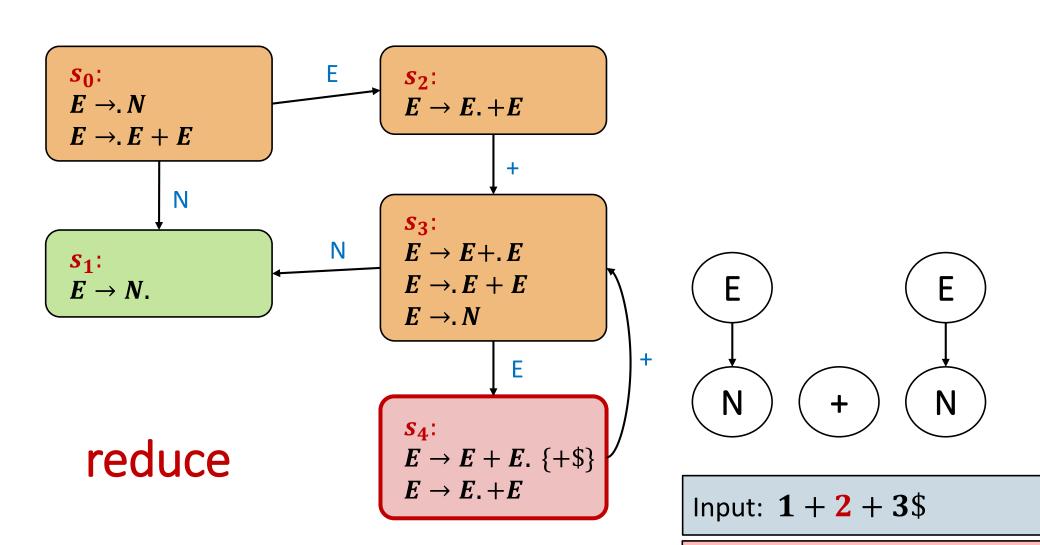
Stack:  $s_0 E s_2$ 



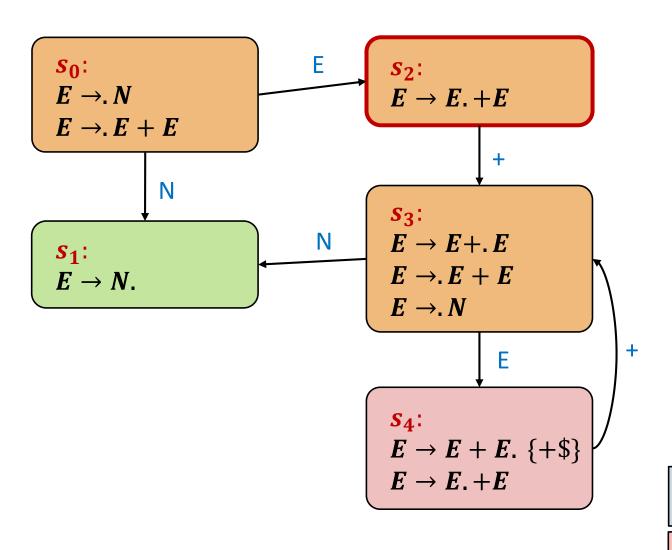
Stack:  $s_0 E s_2 + s_3$ 

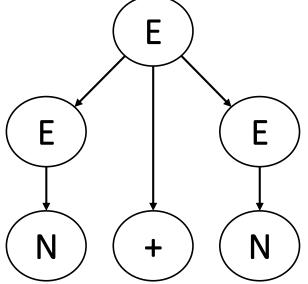


Stack:  $s_0 E s_2 + s_3 N s_1$ 

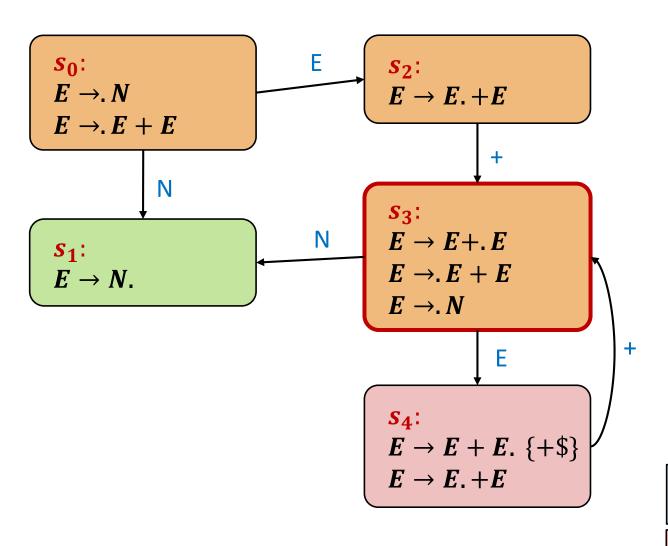


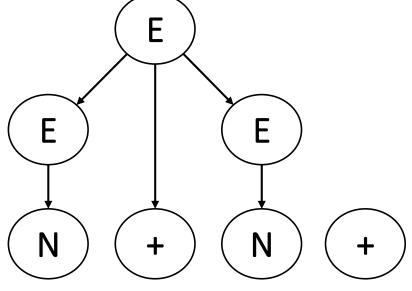
Stack:  $s_0Es_2 + s_3Es_4$ 



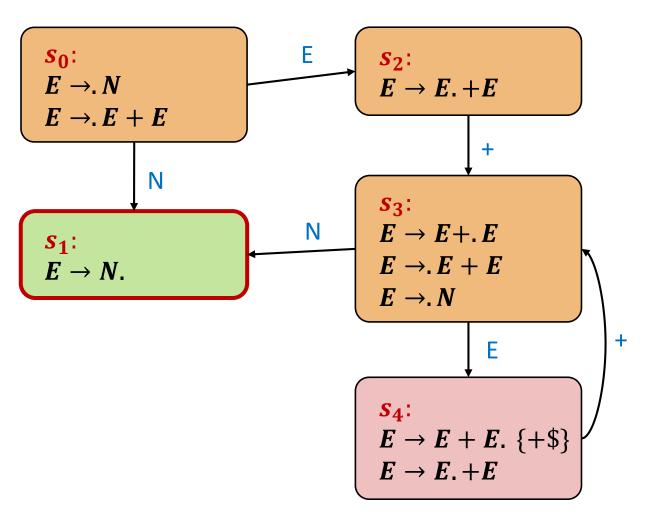


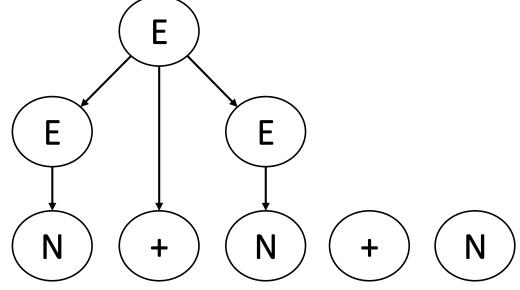
Stack:  $s_0 E s_2$ 



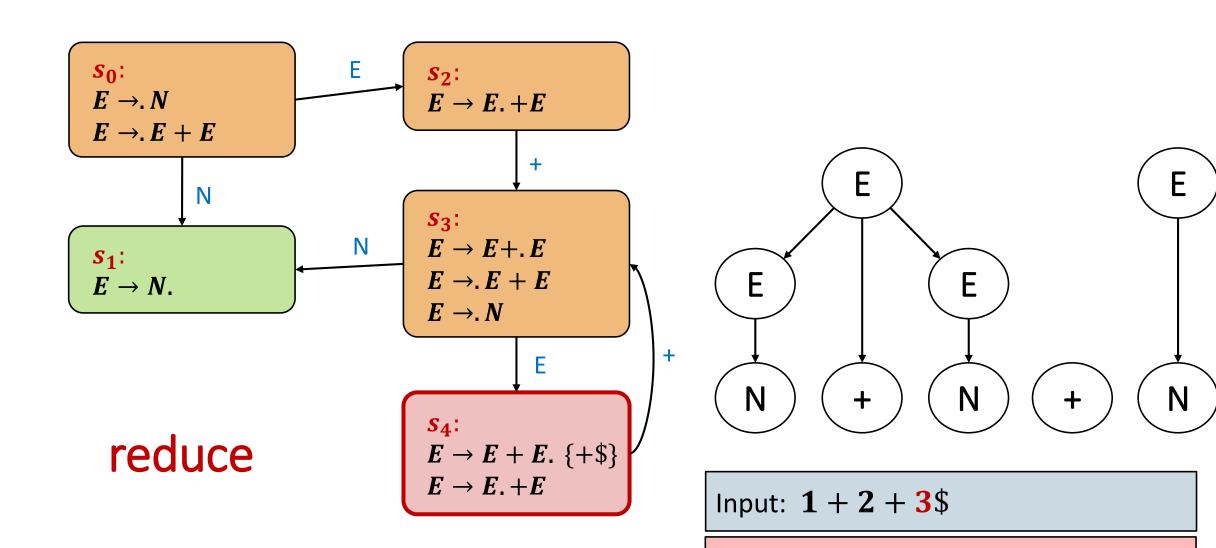


Stack:  $s_0 E s_2 + s_3$ 

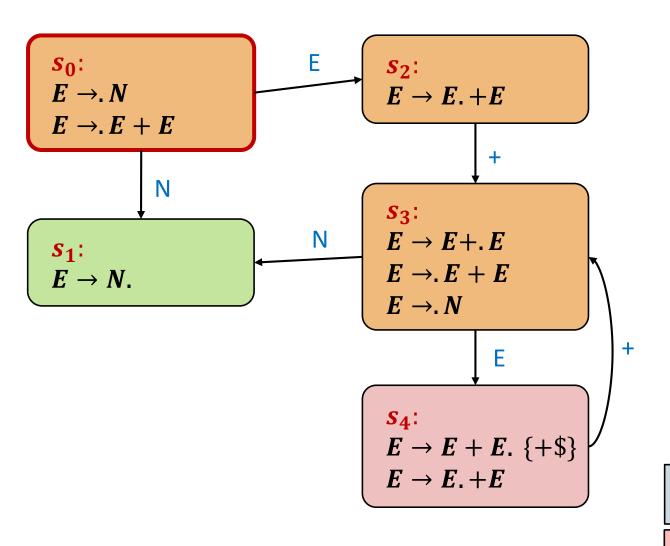


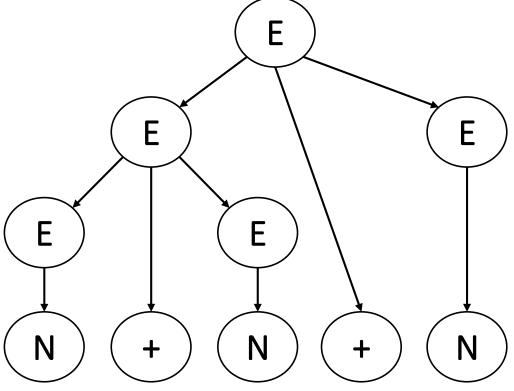


Stack:  $s_0 E s_2 + s_3 N s_1$ 

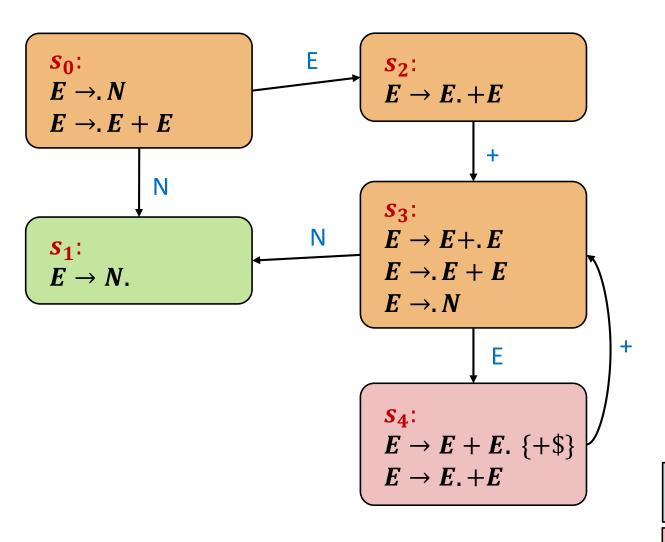


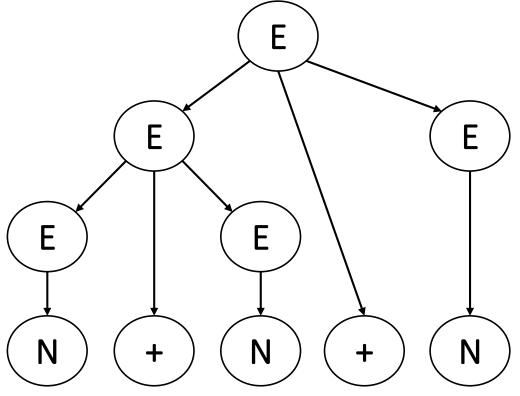
Stack:  $s_0 E s_2 + s_3 E s_4$ 





Stack:  $s_0 E$ 

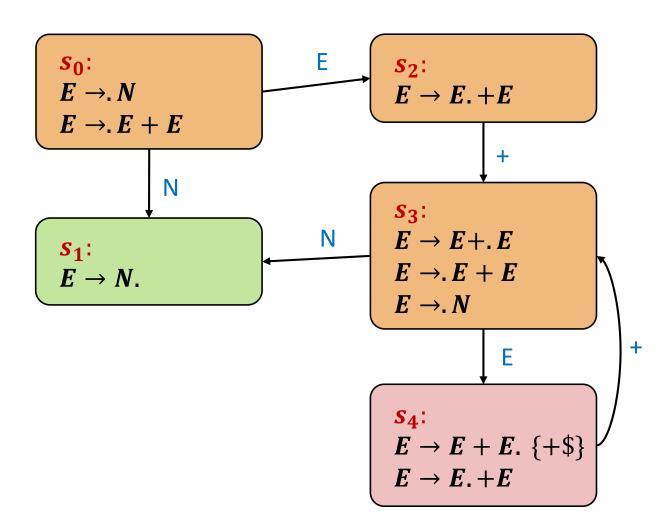


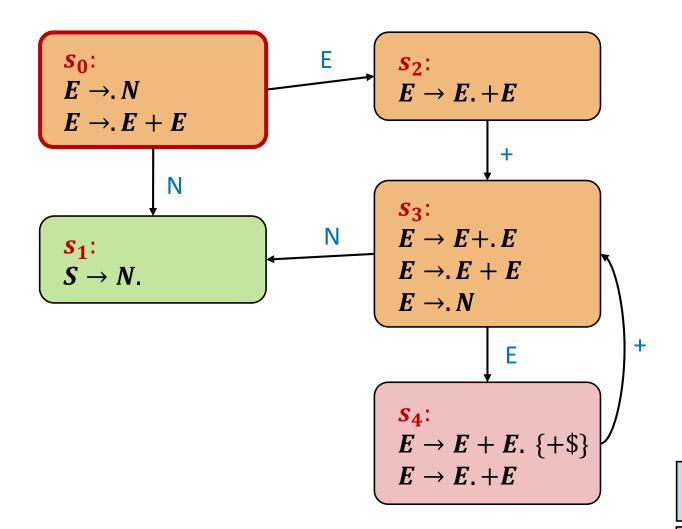


Stack:  $s_0E$ 

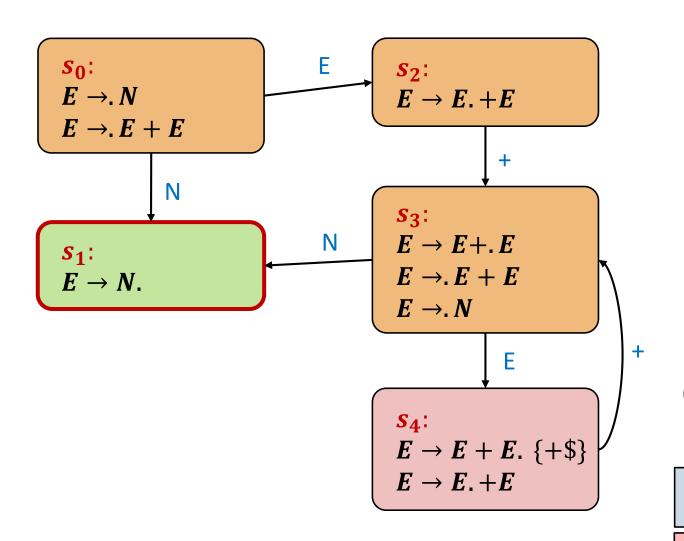
When resolving using the **shift** item:

Right associative

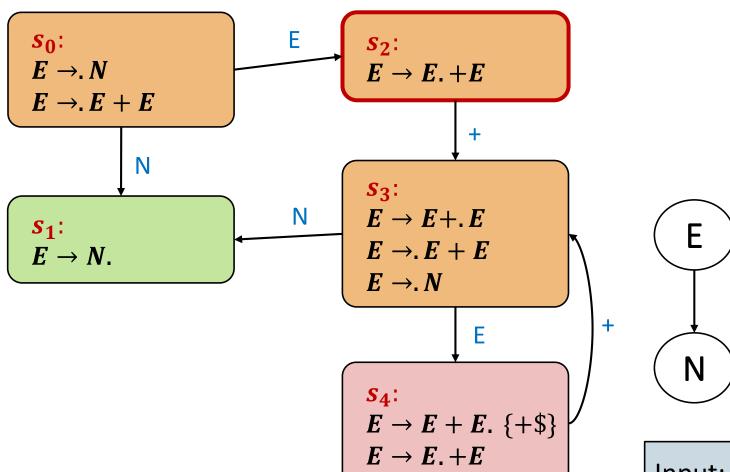




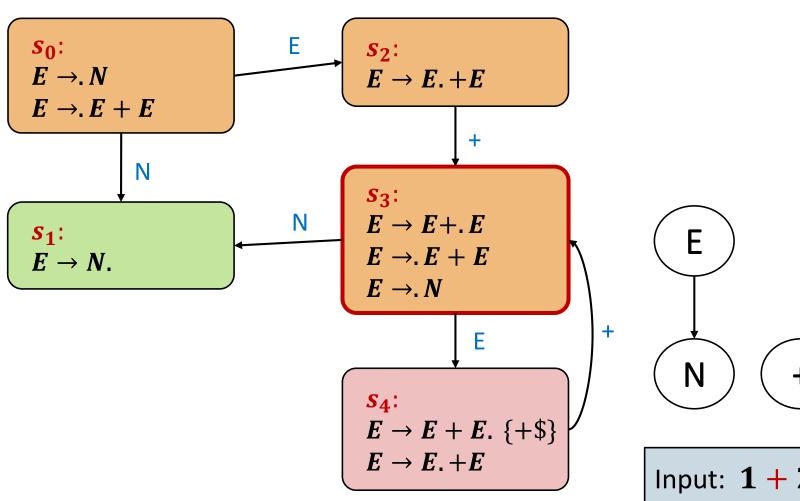
Stack:  $s_0$ 

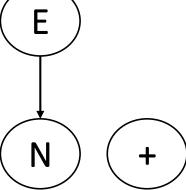


Stack:  $s_0 N s_1$ 

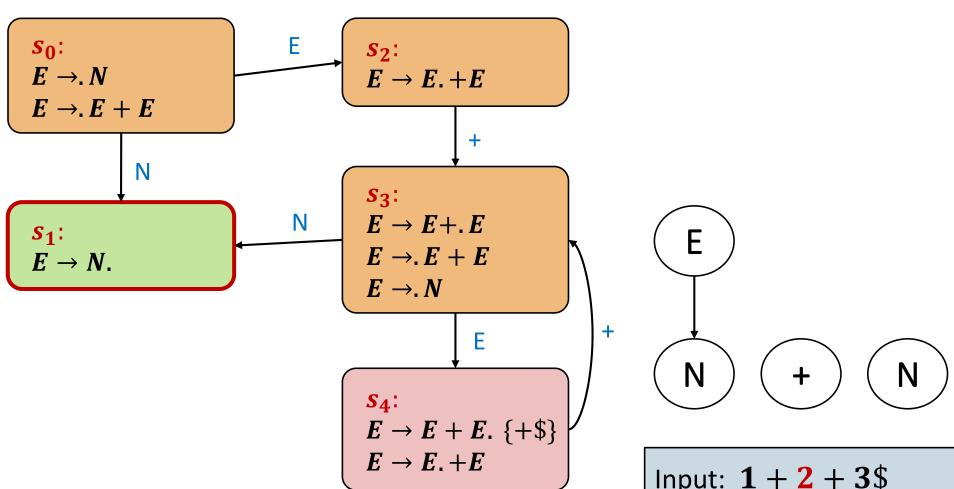


Stack:  $s_0 E s_2$ 

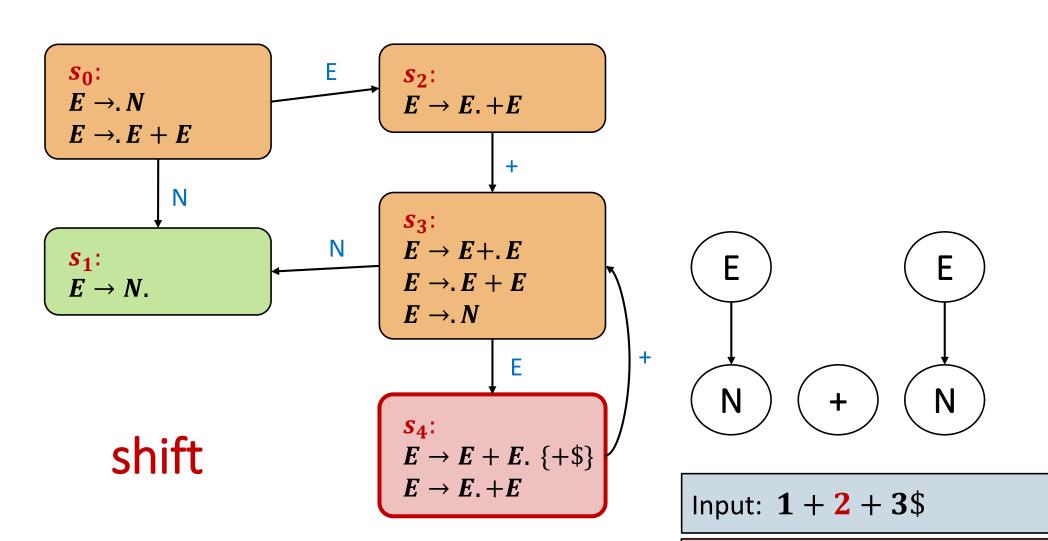




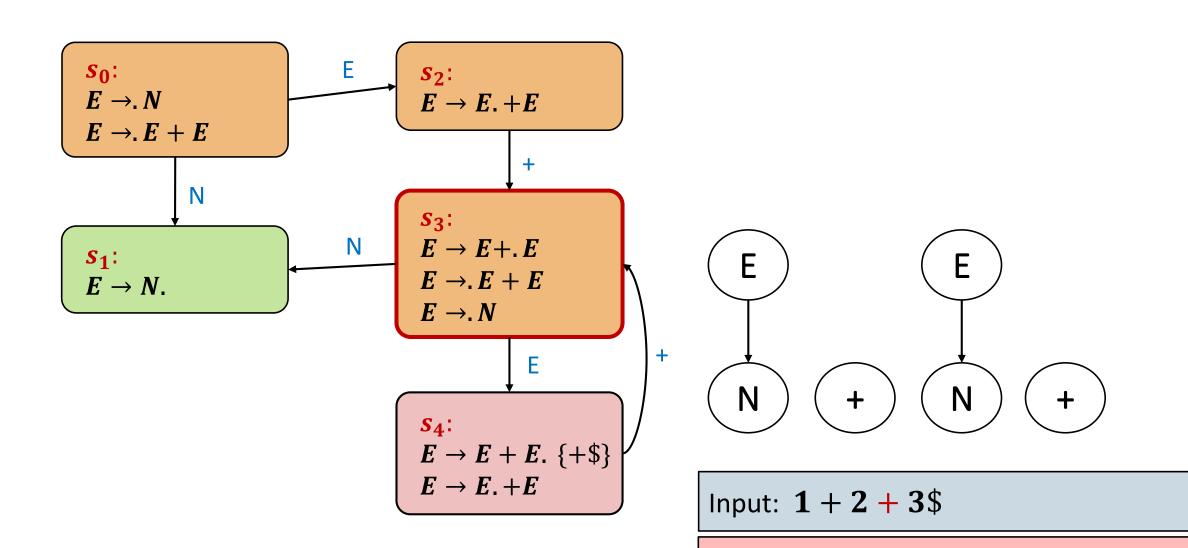
Stack:  $s_0 E s_2 + s_3$ 



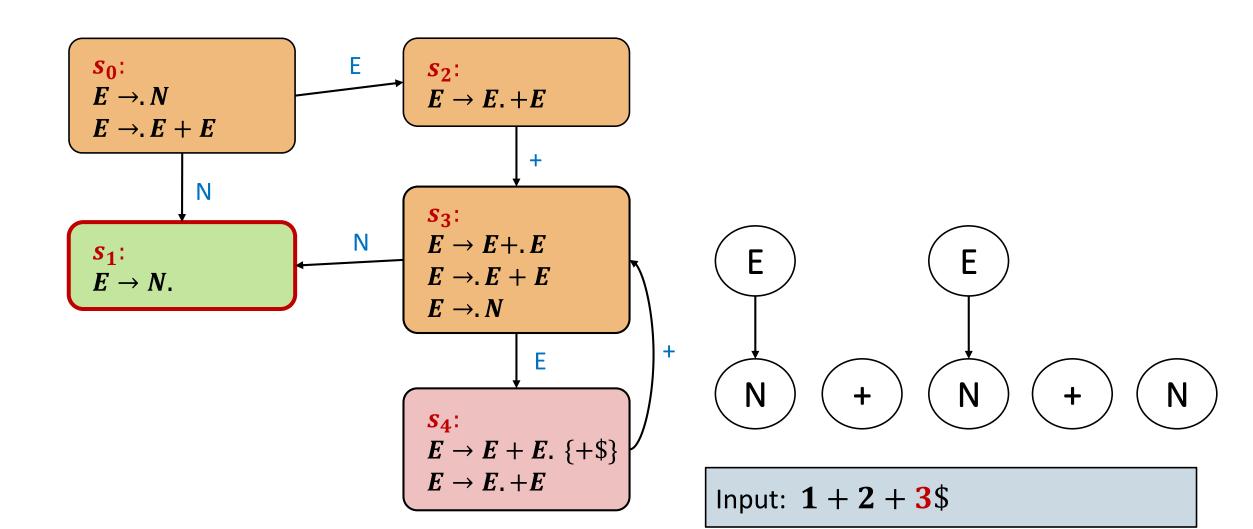
Stack:  $s_0 E s_2 + s_3 N s_1$ 



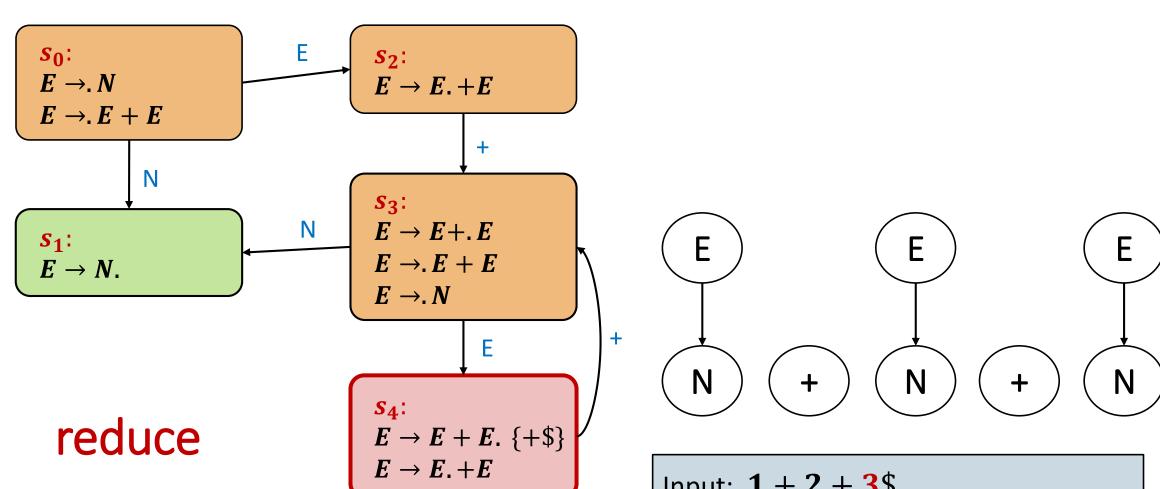
Stack:  $s_0 E s_2 + s_3 E s_4$ 



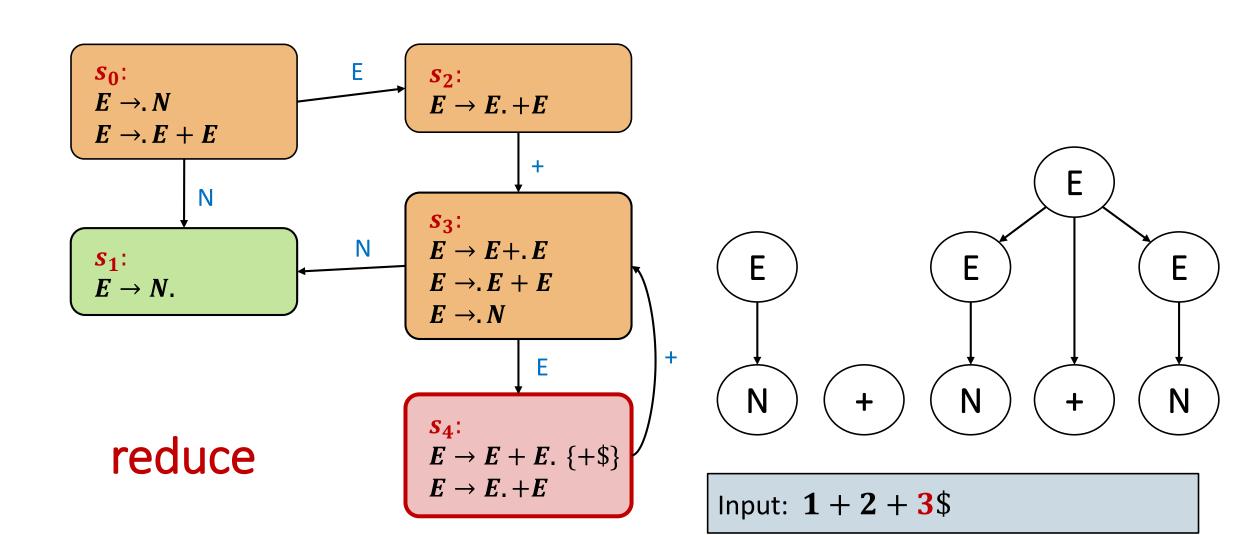
Stack:  $s_0 E s_2 + s_3 E s_4 + s_3$ 



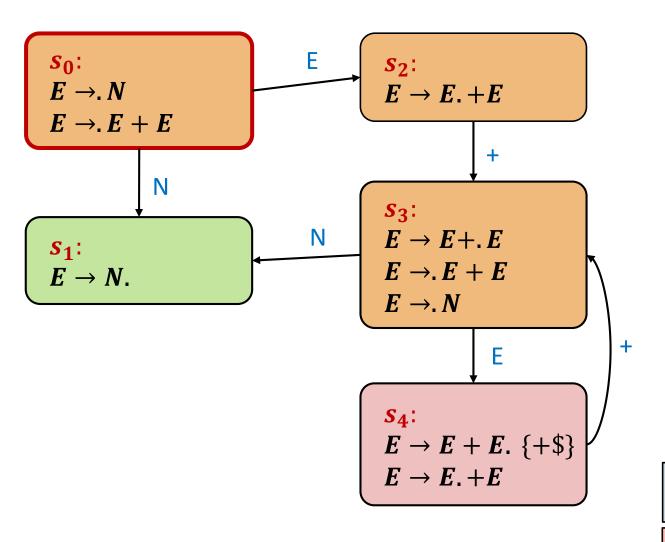
Stack:  $s_0 E s_2 + s_3 E s_4 + s_3 N s_1$ 

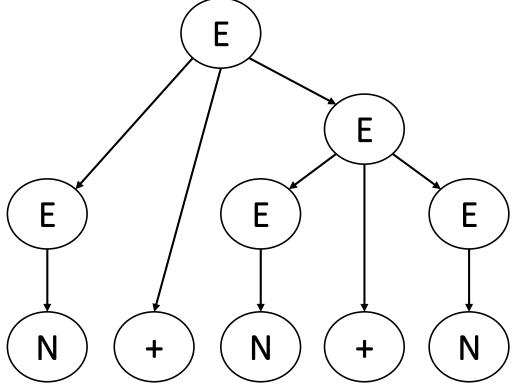


Stack:  $s_0 E s_2 + s_3 E s_4 + s_3 E s_4$ 

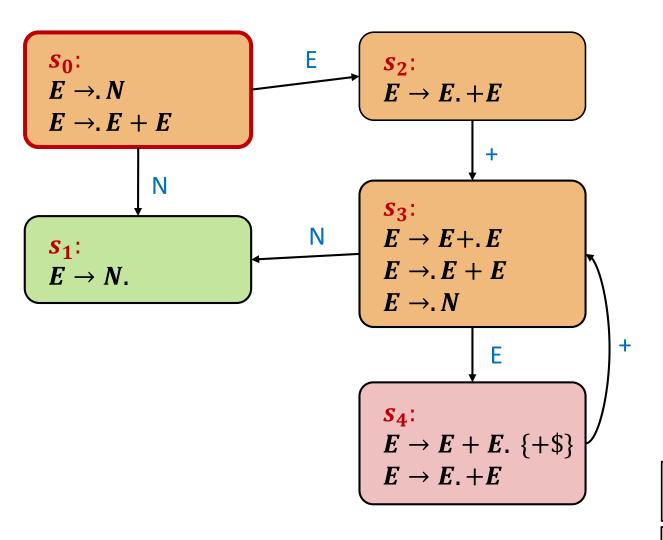


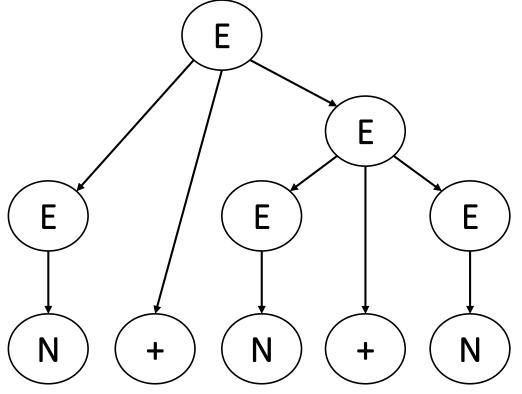
Stack:  $s_0 E s_2 + s_3 E s_4$ 





Stack:  $s_0 E$ 



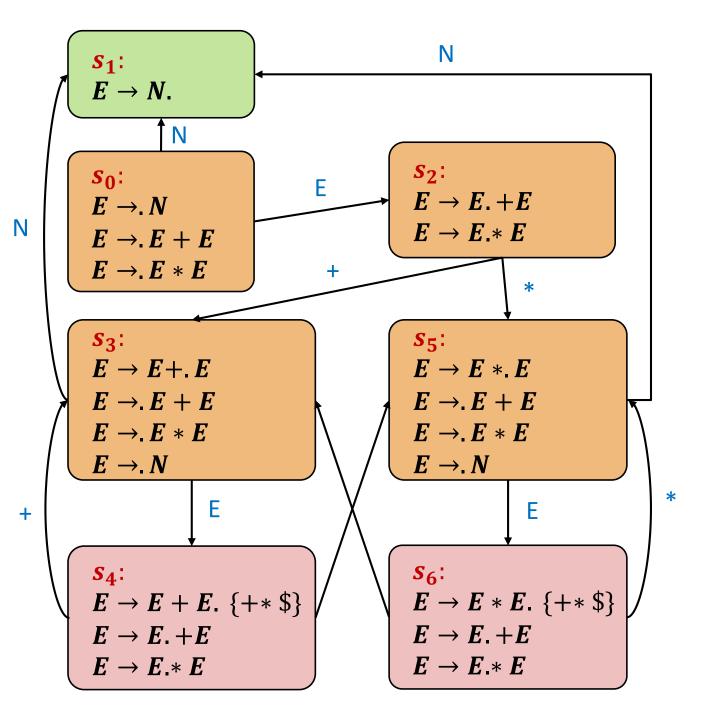


Stack:  $s_0 E$ 

Consider the following CFG:

- $E \rightarrow N$
- $E \rightarrow E + E$
- $E \rightarrow E * E$

What will be the **transition system** of the SLR(1) parser for this CFG?



When having a shift/reduce conflict:

- $E_1 \rightarrow \alpha_1 t_1 \beta_1$ .
- $E_2 \rightarrow \alpha_2 \cdot t_2 \beta_2$

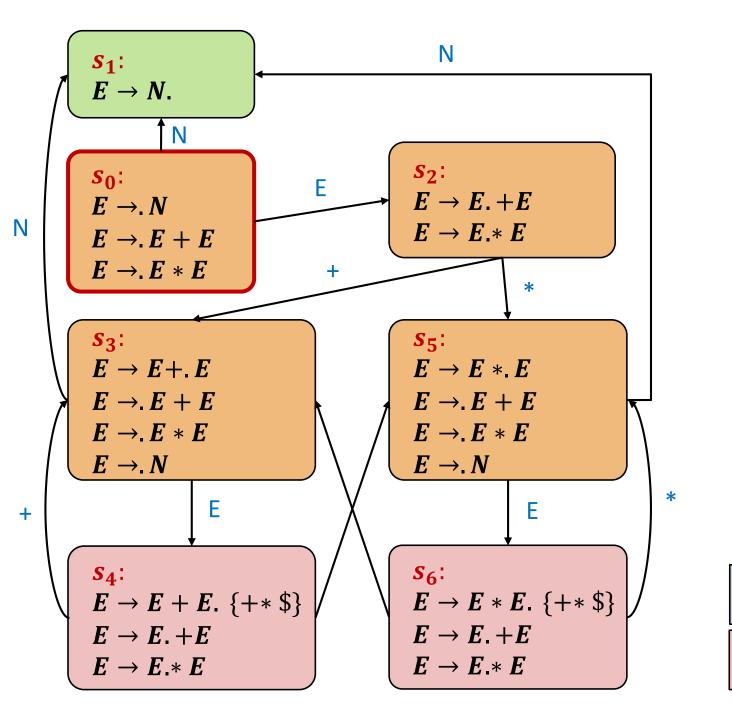
If  $t_1$  has higher precedence, reduce If  $t_2$  has higher precedence, shift

In our case:

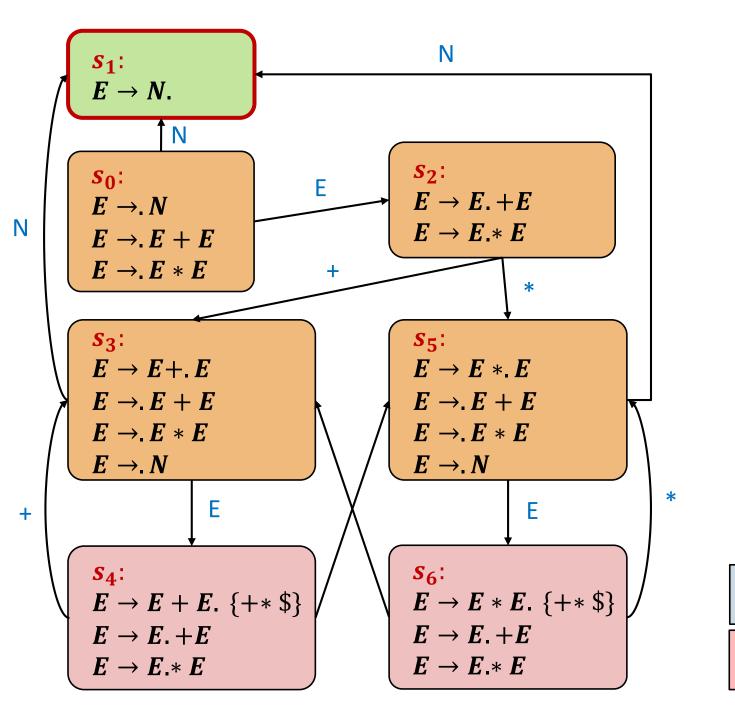
- $E \rightarrow E + E$ .
- $E \rightarrow E \cdot * E$

Assuming that multiplication has higher precedence:

Resolve by Shift



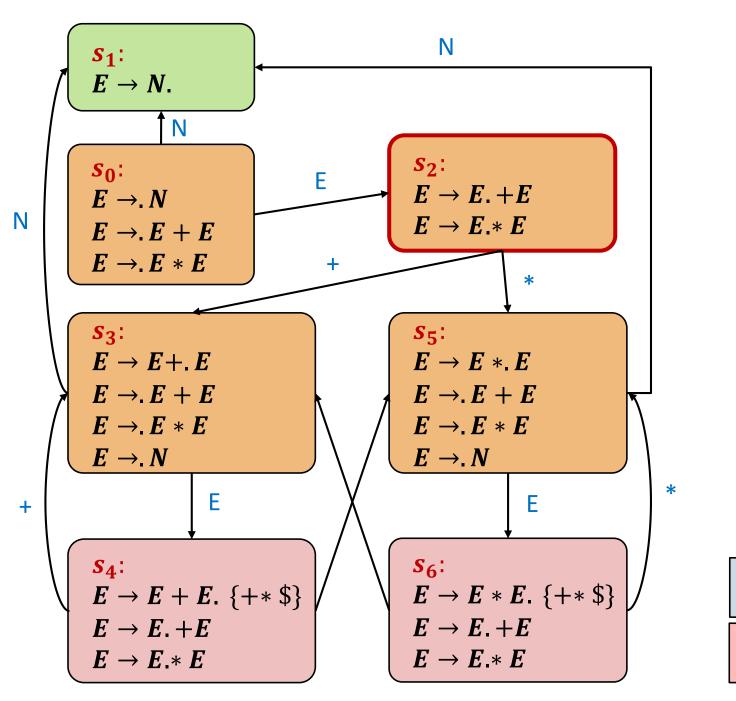
Stack:  $s_0$ 

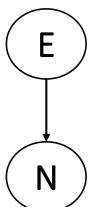


 $\left[ \mathsf{N} \right]$ 

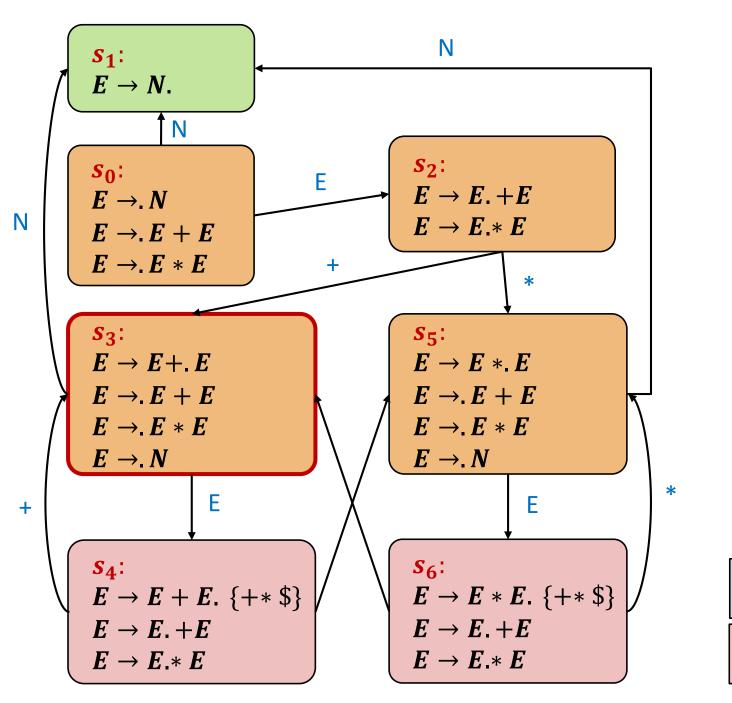
Input: 3 + 4 \* 8\$

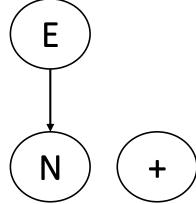
Stack:  $s_0 N s_1$ 



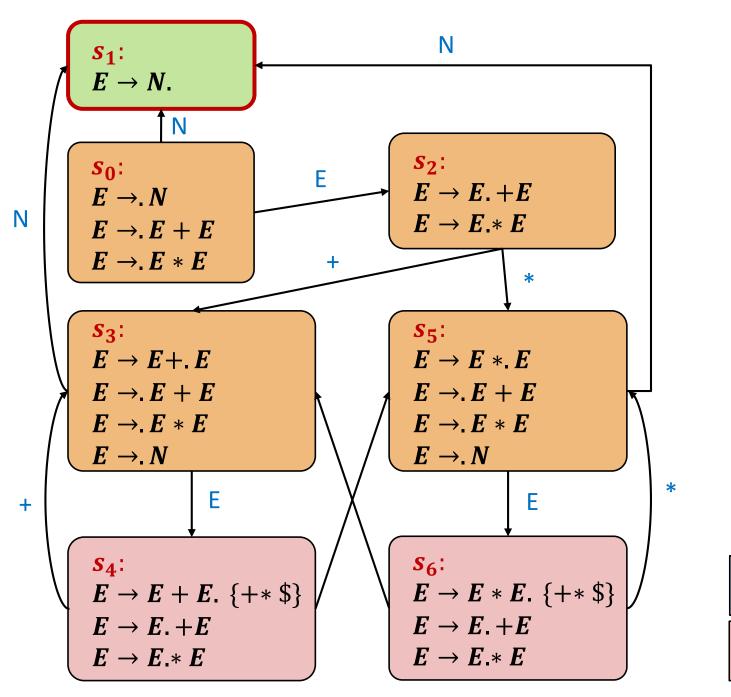


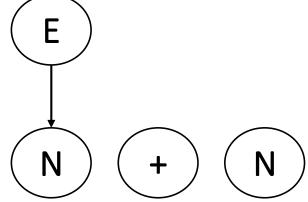
Stack:  $s_0 E s_2$ 



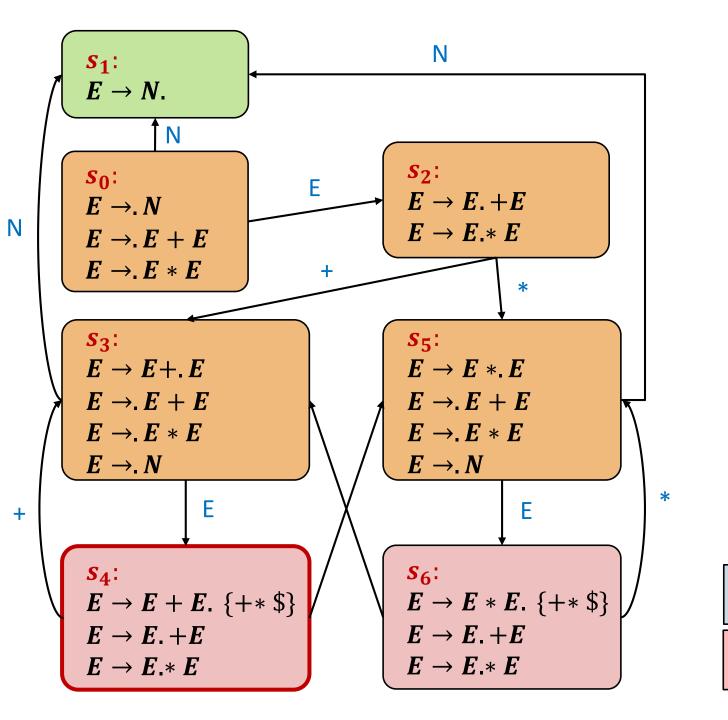


Stack:  $s_0 E s_2 + s_3$ 

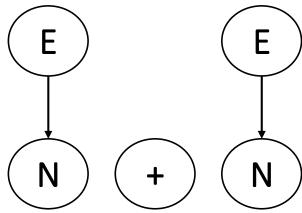




Stack:  $s_0 E s_2 + s_3 N s_1$ 

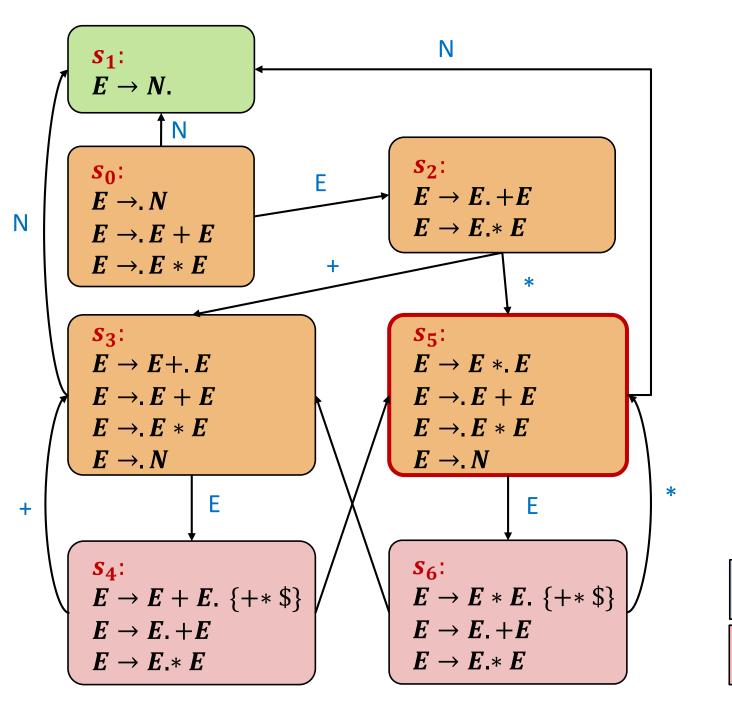


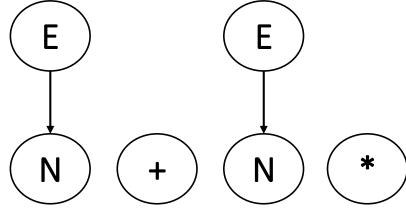
## shift



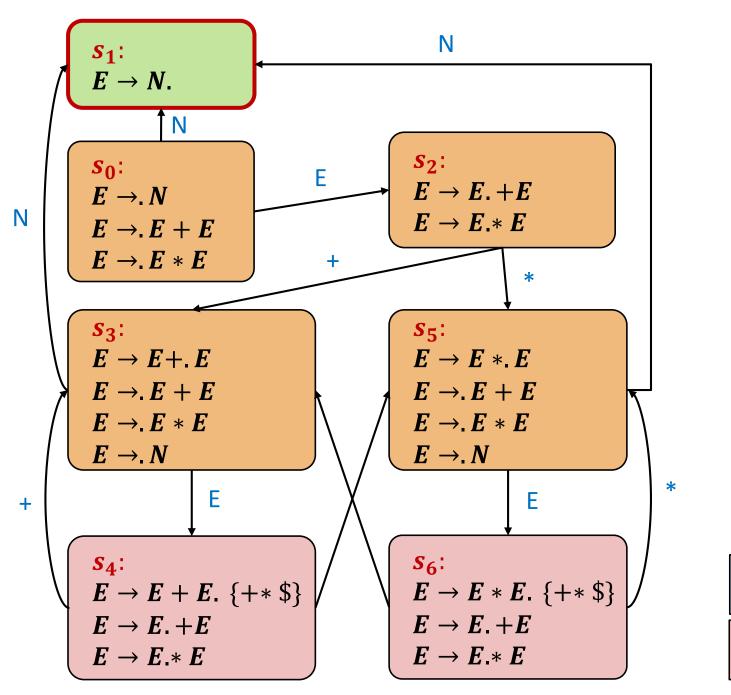
Input: 3 + 4 \* 8\$

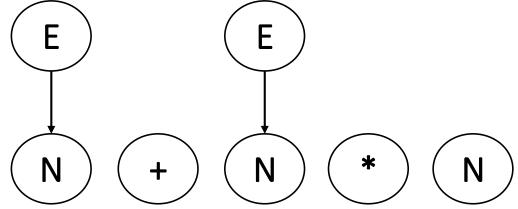
Stack:  $s_0Es_2 + s_3Es_4$ 



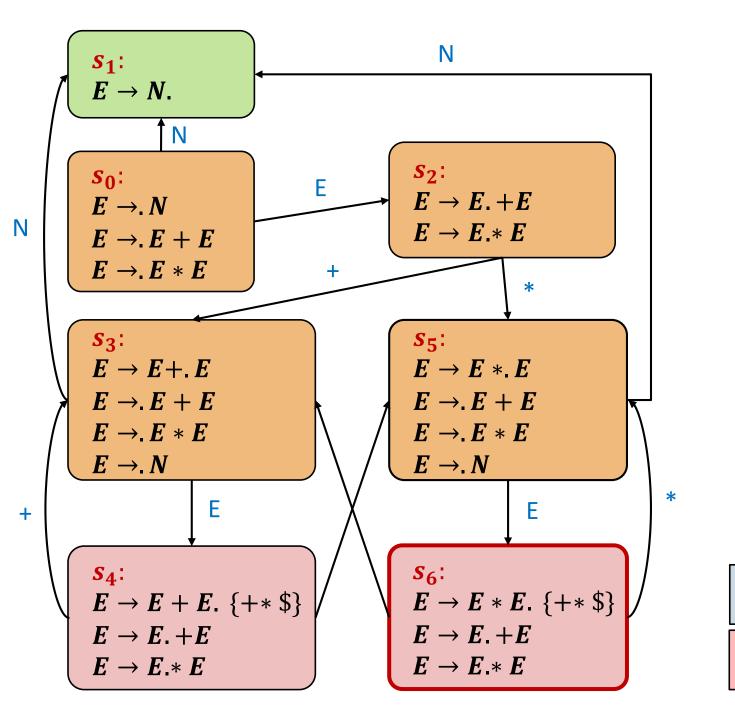


Stack:  $s_0 E s_2 + s_3 E s_4 * s_5$ 

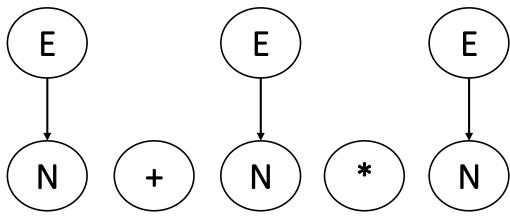




Stack:  $s_0 E s_2 + s_3 E s_4 * s_5 N s_1$ 

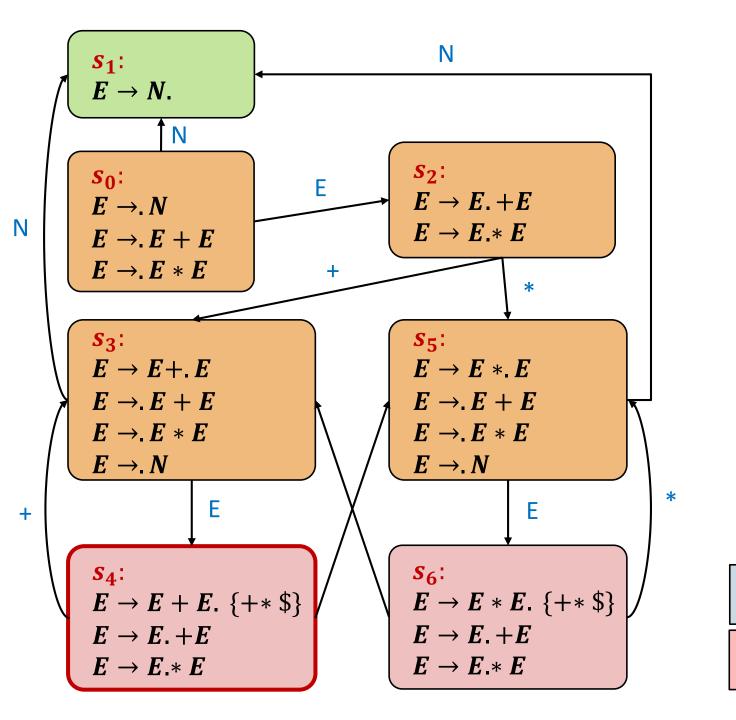


### reduce

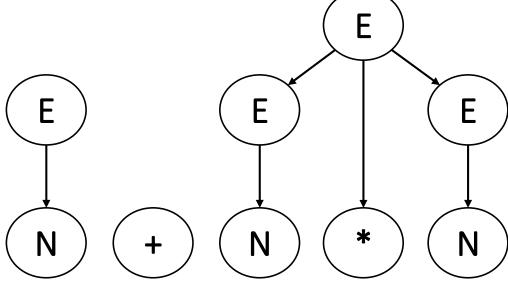


Input: 3 + 4 \* 8\$

Stack:  $s_0 E s_2 + s_3 E s_4 * s_5 E s_6$ 

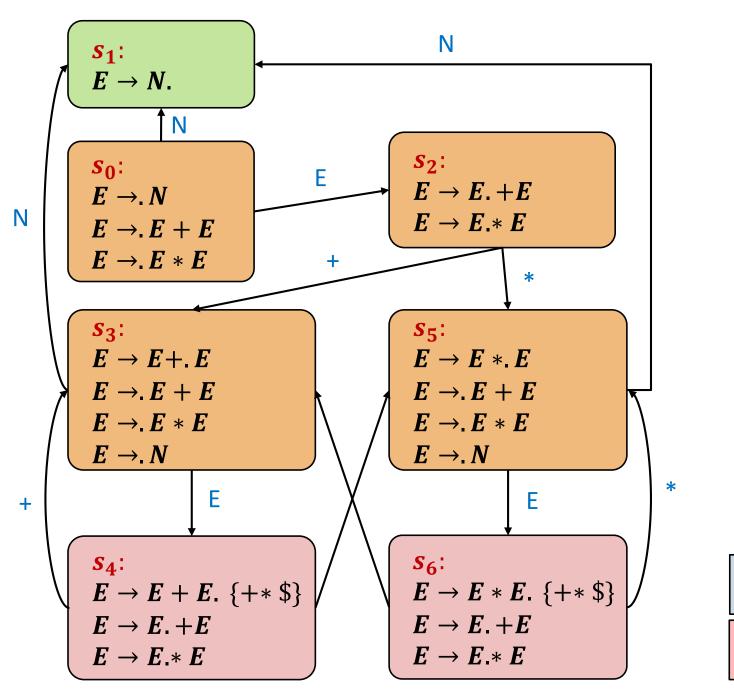


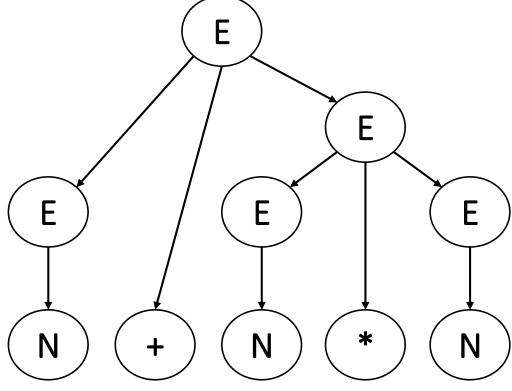
### reduce



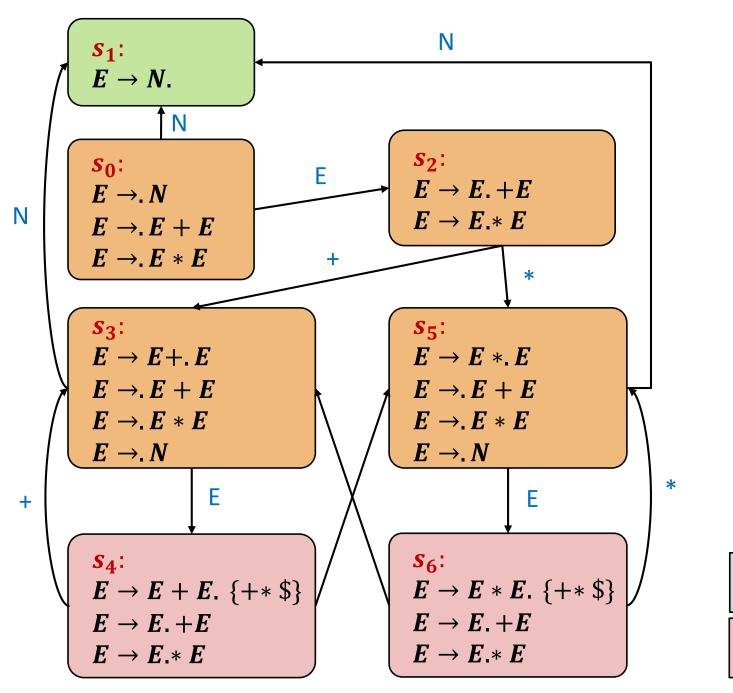
Input: 3 + 4 \* 8\$

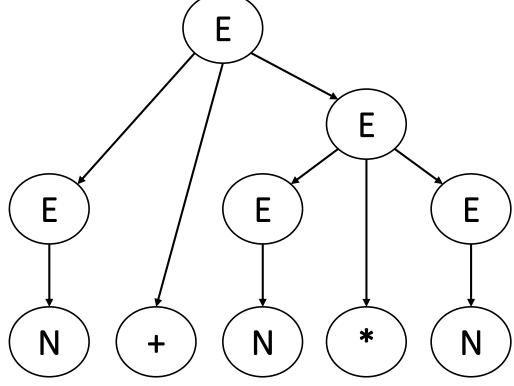
Stack:  $s_0Es_2 + s_3Es_4$ 





Stack:  $s_0E$ 





Stack:  $s_0E$