

# Supplier Encroachment with a Dual-Purpose Retailer

## 3 Model and Benchmark

### 3.1 Model Setup

Supplier

- sell through retailer

dual-purpose retailer

- choose order quantity
- maximize profit and consumer surplus

Strategies of retailer:

- Consumer cooperatives
- Certified B Corporation
- Commercial nonprofit

$\lambda$ : retailer's weight on profit

$\delta \in [0, 1)$ : retailer's weight on consumer surplus

objective function:

- $v_R = \pi_R + \delta CS$
- $v_S = \pi_S$ 
  - $\pi$ : profit

$c$ : Supplier direct selling cost

$p = a - bQ$ : market clearing price

- $Q$ : total quantity

$$U(Q) = aQ - \frac{bQ^2}{2} \text{ "consumer utility function"}$$

$$cs = U(Q) - pQ = \frac{bQ^2}{2} \text{ : consumer surplus}$$

$$(\text{in 5.1: } cs_R = \frac{q_R \cdot cs}{q_R + q_S})$$

1. Supplier decide encroach ability
2. supplier decide  $w$ (wholesale price)
3. retailer decide  $q_R$ (quantity)
4. supplier decide  $q_S$ (quantity)

## 3.2 Benchmark Analysis

### 3.2.1 Benchmark Game

for-profit retailer, no encroachment:

$$\begin{aligned} w^N &= \frac{a}{2} \\ q_R^N &= \frac{a}{4b} \\ \pi_S^N &= \frac{a^2}{8b} \\ \pi_R^N &= \frac{a^2}{16b} \\ cs^N &= \frac{a^2}{32b} \end{aligned}$$

### 3.2.2 The Peril of Being a Dual-Purpose Firm

dual-purpose retailer, no encroachment

$$\begin{aligned} w^{RN} &= \frac{a}{2} \\ q_R^{RN} &= \frac{a}{4b - 2b\delta} \end{aligned}$$

$$\pi_S^{RN} = \frac{a^2}{4b(2 - \delta)}$$

$$\pi_R^{RN} = \frac{a^2(1 - \delta)}{4b(2 - \delta)^2}$$

$$c_S^{RN} = \frac{a^2}{8b(2 - \delta)^2}$$

## Observation 1

In the absence of supplier encroachment, a dual-purpose retailer earns a lower profit than a for-profit retailer.

## 3.2.3 The Bright Side and Downside of Supplier Encroachment.

for-profit retailer, encroachment

### Observation 2 (The Bright Side of Supplier Encroachment)

In the benchmark with a for-profit retailer,

(i) the supplier is never worse off for having the encroachment ability, and strictly better off for having the option of encroachment when

$$c \in [0, 5a/6);$$

(ii) the retailer can be better off by supplier encroachment when

$$c \in (3a/[4\sqrt{2}], (1 - \sqrt{2}/4)a).$$

### Observation 3 (The Downside of Supplier Encroachment)

In the benchmark with a for-profit retailer,

both the retailer and consumers can be worse off by supplier encroachment when

$$c \in (3a/4, 5a/6).$$

# 4 Results

dual-purpose encroachment

## 4.1 Equilibrium

(1)

$$\pi_S = (a - bq_R - bq_S) q_S - cq_S + wq_R$$

(2)

$$v_R = (a - bq_R - bq_S) q_R - wq_R + \frac{b\delta}{2} (q_R + q_S)^2$$

## 4.2 Encroachment Outcomes under Dual-Purpose Setting

### Proposition 1

With a for-profit supplier and a dualpurpose retailer, there exists a threshold on  $\delta$ , denoted by  $\delta_E = 2\sqrt{2} - 2 < 1$ , such that:

(i) When  $\delta \in [0, \delta_E]$ ,

- (a) the supplier is better off for having the option of encroachment if  $c \in [0, c_2(\delta))$ ,
- (b) the supplier is indifferent if  $c \in [c_2(\delta), a)$ .

(ii) When  $\delta \in (\delta_E, 1)$ ,

- (a) the supplier is better off for having the option of encroachment if  $c \in [0, c_3(\delta))$  or  $c \in (c_4(\delta), c_1(\delta))$  or  $c \in (\max \{c_1(\delta), c_5(\delta)\}, c_2(\delta))$ ,
- (b) the supplier is worse off for having the option of encroachment if  $c \in (c_3(\delta), \min \{c_1(\delta), c_4(\delta)\})$  or  $c \in (c_1(\delta), c_5(\delta))$ , and
- (c) the supplier is indifferent if  $c \in [c_2(\delta), a)$ .

### Proposition 2

With a for-profit supplier and a dualpurpose retailer, there exists a threshold on  $\delta$ , denoted by  $\delta_R = (34 - 16\sqrt{2})/23 < 1$ , such that:

(i) When  $\delta \in [0, \delta_R]$ , the retailer is better off by supplier encroachment if  $c \in (c_6(\delta), c_7(\delta))$ , and worse off by supplier encroachment if  $c \in [0, c_6(\delta))$  or  $c \in (c_7(\delta), a)$ .

(ii) When  $\delta \in (\delta_R, 1)$ , the retailer is always worse off by supplier encroachment.

## 4.3 Implication for Firm Profitability

- Retailer can boost profit from being dual-purpose?

### Proposition 3

In the presence of supplier encroachment, a dual-purpose retailer earns a higher profit than a for-profit retailer when:

- (i)  $c \in (c_3(\delta), \min \{ (3a\sqrt{2-2\delta})/(8-4\delta), c_4(\delta) \})$ ; or
- (ii)  $c \in (\max \{ a - a\sqrt{2-2\delta}/(4-2\delta), c_2(\delta) \}, 5a/6)$ .

## 4.4 Implications for Consumer Surplus

### Proposition 4

Consumer surplus when the retailer is a dual-purpose corporation compared to when he is a purely for-profit firm:

- (i) is lower if  $c \in (c_3(\delta), \min \{ (3a - 3a\delta)/(2 - \delta), c_4(\delta) \})$ ;
- (ii) is indifferent if  $c \in (3a/5, c_2(\delta))$ ;
- (iii) is higher if  $c$  is not within the region specified above.

### Proposition 5

Retailer's interest in consumer surplus

- (i) increases his own profit but reduces consumer surplus if  $c \in (c_3(\delta), \min \{ (3a\sqrt{2-2\delta})/(8-4\delta), (3a - 3a\delta)/(2 - \delta), c_4(\delta) \})$ ;
- (ii) increases both his own profit and consumer surplus if (a)  $c \in (\max \{ c_3(\delta), (3a - 3a\delta)/(2 - \delta) \}, (3a\sqrt{2-2\delta})/(8-4\delta))$ ; or (b)  $c \in (\max \{ a - a\sqrt{2-2\delta}/(4-2\delta), c_2(\delta) \}, 5a/6)$ .

# 5 Extensions

## 5.1 Consumer Surplus Specific to the Retailer's Quantity

retailer only care his consumers' surplus

$$cs_R = \frac{q_R \cdot cs}{q_R + q_S}$$

### Proposition 6

Under the parsimonious dual-purpose retailer setting,

- (i) the supplier is always better off for having the encroachment ability;
- (ii) the retailer is better off by supplier encroachment if  $c \in (\bar{c}_3(\delta), \bar{c}_4(\delta))$ .

### Proposition 7

(i) The retailer earns a higher profit from establishing himself as a parsimonious dual-purpose firm rather than a pure profit maximizer if:

- (a)  $c \in (\bar{c}_5(\delta), \bar{c}_6(\delta))$ ; or \$
- (b)  $c \in \left( \max \left\{ \bar{c}_2(\delta), \bar{c}_7(\delta) \right\}, \bar{c}_8(\delta) \right)$ ,  $5a/6 \leq c \leq 5a/5$ .

(ii) The presence of parsimonious dual-purpose retailer has no effect on consumer surplus if  $c \in (3a/5, \bar{c}_2(\delta))$ ; Otherwise, it always increases consumer surplus.

## 5.2 Extremely High Interests in Consumer Surplus

$$\delta \in [1, 2)$$

### Proposition 8

When  $\delta \in [1, 2)$ ,

- (i) the supplier is worse off for having the option to encroach if  $c \in (0, \tilde{c}_2(\delta))$ ;
- (ii) the retailer's profit is always worse off by supplier encroachment;

(iii) the dual-purpose structure always hurts the retailer's profit but benefits consumer surplus.

## 5.3 Price Competition

$k$ : differentiation

$$q_i = \frac{(1 - k)a - p_i + kp_i}{1 - k^2}$$

- tension between supplier encroachment and the retailer's dual-purpose structure becomes less intense
- the encroachment deterrence effect (i.e., deterring the supplier from selling a positive quantity) is not present with a dual-purpose retailer
- the reduction in wholesale price is less pronounced than under quantity competition
- the supplier will sell a positive quantity through her direct channel in a smaller region of parameter space
- the supplier secures greater retail profit (relies more on reselling) by raising the wholesale price even if her selling cost is relatively small