

Lab 2 - Compare one-point, multi-point, and uniform crossover operators

CSE, SUSTech

Outline of This Lab

- How Does A Crossover Operator Work
- Does The Crossover Type Matter?
- Test Function
- Illustrate The Results!

How Does A Crossover Operator Work

Recombination for **discrete** representation

- ✓ One-point crossover
- ✓ k-point crossover ($k > 1$)
- ✓ Uniform crossover

One-point Crossover

Example: choose a **random** crossover point at 3

Parent 1

0	1	0	1	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Parent 2

0	1	1	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

Offspring 1

0	1	0	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

Offspring 2

0	1	1	1	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

k-point Crossover ($k > 1$)

- Example: $k = 2$, choose **two** random crossover points at 3 and 6

Parent 1

0	1	0	1	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Parent 2

0	1	1	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

Offspring 1

0	1	0	1	0	1	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Offspring 2

0	1	1	1	0	0	1	0	1	1
---	---	---	---	---	---	---	---	---	---

- Example: $k = 3$, choose **three** random crossover points at 3, 6, 8

Parent 1

0	1	0	1	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Parent 2

0	1	1	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

Offspring 1

0	1	0	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

Offspring 2

0	1	1	1	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Uniform Crossover

Example: at every point, generate a random number $\in [0, 1]$ with crossover rate 0.5

Gene Index	1	2	3	4	5	6	7	8	9	10
Random	0.31	0.63	0.58	0.07	0.29	0.42	0.59	0.63	0.13	0.73

Parent 1

0	1	0	1	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Parent 2

0	1	1	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

Offspring 1

0	1	0	1	0	1	1	0	1	0
---	---	---	---	---	---	---	---	---	---

Offspring 2

0	1	1	1	0	0	1	0	0	1
---	---	---	---	---	---	---	---	---	---

Does The Crossover Type Matter?

Modify the simple evolutionary algorithm (EA) in Lab 1 with the following three Crossover Operators

- ✓ One-point crossover
- ✓ Two-point crossover
- ✓ Uniform crossover

and run the EA to solve the Test Function given in the next slide.

Test Function

Sphere Function

$$f(x) = \sum_{i=1}^n x_i^2$$

with different dimension $n = 1, 10, 20$, and 30 , and x_i , ($i = 1, \dots, n$), in the integer interval $[0, 127]$.

Assume each variable x_i is encoded by 8 bits, and all encoded variables are concatenated to form an individual, therefore, each individual is a string of $8n$ bits. Assume the population size is 30.

Illustrate The Results!

Plot 12 figures for each combination of crossover type and dimension

- ✓ x-axis: current evaluation number.
- ✓ y-axis: fitness value of the best individual of current population.