Question 1: Evaluate the following postfix expression using stack data structure.

```
Postfix Expression:
2 + ((5 + 4) * 3) + 1
Let's break it down step by step. We'll use a stack to evaluate the
expression.
Push 2 onto the stack:
Stack = [2]
Push 5 onto the stack:
Stack = [2, 5]
Push 4 onto the stack:
Stack = [2, 5, 4]
Encounter "+" (addition):
Pop 4 and 5 from the stack, add them:
5 + 4 = 9
Push the result (9) back onto the stack:
Stack = [2, 9]
Push 3 onto the stack:
Stack = [2, 9, 3]
Encounter "*" (multiplication):
Pop 3 and 9 from the stack, multiply them:
9 * 3 = 27
Push the result (27) back onto the stack:
Stack = [2, 27]
Encounter "+" (addition):
Pop 27 and 2 from the stack, add them:
2 + 27 = 29
Push the result (29) back onto the stack:
Stack = [29]
Push 1 onto the stack:
Stack = [29, 1]
Encounter "+" (addition):
Pop 1 and 29 from the stack, add them:
29 + 1 = 30
Push the result (30) back onto the stack:
Stack = [30]
```

Answer: The result is 30.

## Question 2: Consider a stack A. What will be in the stack A after the following operations?

## Operations:

```
Push(5):
Stack = [5]
Push(10):
Stack = [5, 10]
Pop():
Pop the top element (10):
Stack = [5]
Push(2):
Stack = [5, 2]
Push(5):
Stack = [5, 2, 5]
Push(Pop() + Pop()):
Pop 5 and 2, then add them:
5 + 2 = 7
Push the result (7) back onto the stack:
Stack = [5, 7]
Pop():
Pop the top element (7):
Stack = [5]
Push(9):
Stack = [5, 9]
Push(1):
Stack = [5, 9, 1]
Push(Pop()):
Pop 1 and push it back onto the stack:
Stack = [5, 9, 1]
```

Answer: The final stack is [5, 9, 1].

Question 3: Using stack, check if the following expression is correct or not. Expression:

$$a + (b + 3) - ((c * d) + e$$

To check if this expression has balanced parentheses, we use a stack.

- a: No parentheses, ignore.
- +: No parentheses, ignore.
- (: Push onto stack: Stack = ['(']
- b: No parentheses, ignore.
- +: No parentheses, ignore.
- 3: No parentheses, ignore.
- ): Pop from stack to match the opening parenthesis: Stack = []
- -: No parentheses, ignore.
- (: Push onto stack: Stack = ['(']
- (: Push onto stack: Stack = ['(', '(']
- c: No parentheses, ignore.
- \*: No parentheses, ignore.
- d: No parentheses, ignore.
- ): Pop from stack to match the opening parenthesis: Stack = ['(']
- +: No parentheses, ignore.
- e: No parentheses, ignore.

At the end, there is still one unmatched opening parenthesis in the stack, which means the expression is not balanced.

Answer: The expression is incorrect.

```
Ouestion 4: Convert the following infix expression to postfix expression
using stack.
a. Infix: 8 * 2 - 3
8: Operand, add directly to the postfix expression: Postfix = 8
*: Operator, push onto the stack: Stack = [*]
2: Operand, add directly to the postfix expression: Postfix = 8 2
-: Operator, pop from the stack until encountering an operator with lower
precedence (pop * and add to the postfix expression):
Postfix = 82*
Then push - onto the stack: Stack = [-]
3: Operand, add directly to the postfix expression: Postfix = 8 2 * 3
Pop - from the stack and add to the postfix expression: Postfix = 8 2 * 3 -
Converted Postfix Expression: 8 2 * 3 -
b. Infix: 1 * 3 * 3 + 5 + 1
1: Operand, add directly to the postfix expression: Postfix = 1
*: Operator, push onto the stack: Stack = [*]
3: Operand, add directly to the postfix expression: Postfix = 1 3
*: Operator, pop from the stack (pop * and add to the postfix expression):
Postfix = 1.3 *
Then push * onto the stack: Stack = [*]
3: Operand, add directly to the postfix expression: Postfix = 1 3 * 3
+: Operator, pop from the stack (pop * and add to the postfix expression):
Postfix = 1 3 * 3 *
Then push + onto the stack: Stack = [+]
5: Operand, add directly to the postfix expression: Postfix = 1 3 * 3 * 5
+: Operator, pop from the stack (pop + and add to the postfix expression):
Postfix = 1 \ 3 * 3 * 5 +
Then push + onto the stack: Stack = [+]
1: Operand, add directly to the postfix expression: Postfix = 1 \ 3 \ * \ 5 \ + \ 1
```

Pop + from the stack and add to the postfix expression: Postfix = 1 3 \* 3 \* 5

Converted Postfix Expression: 1 3 \* 3 \* 5 + 1 +