Stat_computing_1

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2 Length of Ones

Given an integer vector of 0 and 1's, write an R function named len_one that returns the length of its longest subsequence of consecutive 1's, among all possible subsequences of consecutive 1's.

```
# write function
len_one = function(seq){
  s = rle(seq)
  l = s$lengths[s$val == 1]
  if (length(1) > 0)
    max(1)
  else
    0
}
# test
len_one(c(0, 0, 1, 1, 1, 0, 1, 1))
## [1] 3
len_one(c(1, 1, 1, 1))
## [1] 4
len_one(c(0, 0, 0, 0))
## [1] 0
```

3 Hybrid Matrix

- a. create a covariance matrix with 2's on the diagonal and 1's off the diagonal. The dimension of this matrix is 10×10 .
- b. convert this covariance matrix to a correlation matrix.
- c. compute the Cholesky factorization of the correlation matrix.

d. create a hybrid matrix representation of both the correlation matrix and its Cholesky factorization, where its upper triangular part is the upper triangular part of the correlation matrix (excluding the diagonal) and its lower triangular part is the upper triangular part including the diagonal of the Cholesky factorization (by chol).

```
# (a) create cov matrix
cov_matrix = matrix(nrow = 10, ncol = 10)
diag(cov_matrix) = 2
cov_matrix[lower.tri(cov_matrix)]=1
cov_matrix[upper.tri(cov_matrix)]=1
```

```
##
           [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
     [1,]
               2
                            1
                                  1
                                        1
                                               1
                                                                  1
                                                                          1
##
     [2,]
               1
                     2
                            1
                                  1
                                        1
                                               1
                                                     1
                                                            1
                                                                  1
                                                                          1
     [3,]
                            2
##
               1
                     1
                                  1
                                        1
                                               1
                                                     1
                                                                  1
                                                                          1
    [4,]
##
               1
                     1
                            1
                                  2
                                        1
                                               1
                                                     1
                                                            1
                                                                  1
                                                                          1
##
    [5,]
               1
                     1
                            1
                                        2
                                               1
                                                                          1
                                  1
                                                                  1
    [6,]
                                               2
##
                                                     1
               1
                     1
                            1
                                  1
                                        1
                                                            1
                                                                  1
                                                                          1
##
     [7,]
               1
                     1
                            1
                                        1
                                               1
                                                     2
                                                                          1
                                  1
                                                            1
                                                                  1
##
    [8,]
               1
                     1
                            1
                                  1
                                        1
                                               1
                                                     1
                                                            2
                                                                  1
                                                                          1
    [9,]
               1
                                               1
                                                                  2
##
                     1
                            1
                                  1
                                        1
                                                     1
                                                            1
                                                                          1
                                                                          2
## [10,]
               1
                      1
                            1
                                  1
                                        1
                                               1
                                                     1
                                                            1
                                                                  1
```

```
# (b) convert cov matrix to correlation matrix
cor_matrix = cov2cor(cov_matrix); cor_matrix
```

```
[,1] [,2]
##
                    [,3] [,4] [,5] [,6] [,7]
                                                [,8]
                                                     [,9]
##
          1.0
                0.5
                     0.5
                           0.5
                                0.5
                                      0.5
                                           0.5
                                                0.5
                                                      0.5
                                                             0.5
    [1,]
##
    [2,]
          0.5
                1.0
                     0.5
                           0.5
                                0.5
                                      0.5
                                           0.5
                                                0.5
                                                      0.5
                                                             0.5
##
    [3,]
          0.5
                0.5
                     1.0
                           0.5
                                0.5
                                      0.5
                                           0.5
                                                 0.5
                                                      0.5
                                                             0.5
##
    [4,]
          0.5
                0.5
                     0.5
                           1.0
                                0.5
                                      0.5
                                           0.5
                                                 0.5
                                                      0.5
                                                             0.5
                           0.5
                0.5
                     0.5
##
    [5,]
          0.5
                                1.0
                                      0.5
                                           0.5
                                                 0.5
                                                      0.5
                                                             0.5
##
    [6,]
          0.5
                0.5
                     0.5
                           0.5
                                0.5
                                      1.0
                                           0.5
                                                 0.5
                                                      0.5
                                                             0.5
    [7,]
                     0.5
                           0.5
                                0.5
##
          0.5
                0.5
                                      0.5
                                           1.0
                                                0.5
                                                      0.5
                                                             0.5
##
    [8,]
          0.5
                0.5
                     0.5
                           0.5
                                0.5
                                      0.5
                                           0.5
                                                 1.0
                                                      0.5
                                                             0.5
          0.5
                     0.5
                           0.5
                                      0.5
                                           0.5
                                                0.5
                                                      1.0
                                                             0.5
##
    [9,]
                0.5
                                0.5
## [10,]
                0.5
                     0.5
                           0.5
                                0.5
                                      0.5
                                           0.5
                                                0.5
                                                             1.0
          0.5
```

```
# (c) compute the Cholesky factorization of the correlation matrix
cor_matrix_chol = chol(cor_matrix); cor_matrix_chol
```

```
##
      [,1]
             [,2]
                    [,3]
                            [,4]
                                   [,5]
                                          [,6]
                                                 [,7]
##
  [1,]
        1 0.5000000 0.5000000 0.5000000 0.5000000 0.5000000 0.5000000
##
  [2,]
        0 0.8660254 0.2886751 0.2886751 0.2886751 0.2886751 0.2886751
##
  [3,]
        0 0.0000000 0.8164966 0.2041241 0.2041241 0.2041241 0.2041241
  [4,]
        0 0.0000000 0.0000000 0.7905694 0.1581139 0.1581139 0.1581139
##
        0 0.0000000 0.0000000 0.0000000 0.7745967 0.1290994 0.1290994
##
  [5,]
  [6,]
        ##
  [7,]
        ##
        [8,]
##
```

```
[9,]
          [10,]
          ##
##
                       [,9]
                                [,10]
   [1,] 0.50000000 0.50000000 0.50000000
##
##
   [2,] 0.28867513 0.28867513 0.28867513
   [3,] 0.20412415 0.20412415 0.20412415
##
   [4,] 0.15811388 0.15811388 0.15811388
##
   [5,] 0.12909944 0.12909944 0.12909944
##
   [6,] 0.10910895 0.10910895 0.10910895
   [7,] 0.09449112 0.09449112 0.09449112
   [8,] 0.75000000 0.08333333 0.08333333
   [9,] 0.00000000 0.74535599 0.07453560
## [10,] 0.00000000 0.00000000 0.74161985
t(cor_matrix_chol)
                          [,3]
                                           [,5]
                                                    [,6]
##
                 [,2]
                                   [,4]
                                                              [,7]
##
        [1,]
        [3,]
        [4,] 0.5 0.2886751 0.2041241 0.7905694 0.0000000 0.0000000 0.00000000
##
##
   [5,] 0.5 0.2886751 0.2041241 0.1581139 0.7745967 0.0000000 0.00000000
   [6,] 0.5 0.2886751 0.2041241 0.1581139 0.1290994 0.7637626 0.00000000
   [7,] 0.5 0.2886751 0.2041241 0.1581139 0.1290994 0.1091089 0.75592895
##
   [8,]
        0.5 0.2886751 0.2041241 0.1581139 0.1290994 0.1091089 0.09449112
   [9,] 0.5 0.2886751 0.2041241 0.1581139 0.1290994 0.1091089 0.09449112
##
  [10,] 0.5 0.2886751 0.2041241 0.1581139 0.1290994 0.1091089 0.09449112
##
             [,8]
                      [,9]
                              [,10]
   [1,] 0.00000000 0.0000000 0.0000000
##
##
   [2,] 0.00000000 0.0000000 0.0000000
   [3,] 0.00000000 0.0000000 0.0000000
   [4,] 0.00000000 0.0000000 0.0000000
##
   [5,] 0.00000000 0.0000000 0.0000000
   [6,] 0.00000000 0.0000000 0.0000000
   [7,] 0.00000000 0.0000000 0.0000000
   [8,] 0.75000000 0.0000000 0.0000000
   [9,] 0.08333333 0.7453560 0.0000000
  [10,] 0.08333333 0.0745356 0.7416198
# check result
t(cor_matrix_chol) %*% cor_matrix_chol
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
   [1,]
        1.0
             0.5
                 0.5
                      0.5
                          0.5
                               0.5
                                   0.5
                                       0.5
                                            0.5
                                                 0.5
                      0.5
   [2,]
        0.5
             1.0
                 0.5
                          0.5
                               0.5
                                   0.5
                                       0.5
                                            0.5
                                                 0.5
   [3,]
        0.5
                      0.5
                          0.5
                               0.5
                                   0.5
                                            0.5
                                                 0.5
             0.5
                 1.0
                                       0.5
             0.5
   [4,]
                                   0.5
                                       0.5
                                            0.5
                                                 0.5
##
        0.5
                 0.5
                      1.0
                          0.5
                               0.5
   [5,]
        0.5
             0.5
                 0.5
                      0.5
                          1.0
                               0.5
                                   0.5
                                       0.5
                      0.5
##
   [6,]
        0.5
             0.5
                 0.5
                          0.5
                               1.0
                                   0.5
                                       0.5
                                            0.5
                                                 0.5
   [7,]
                      0.5
##
        0.5
             0.5
                 0.5
                          0.5
                               0.5
                                   1.0
                                       0.5
                                            0.5
                                                 0.5
##
   [8,]
        0.5
             0.5
                 0.5
                      0.5
                          0.5
                               0.5
                                   0.5
                                       1.0
                                            0.5
                                                 0.5
   [9,]
        0.5
             0.5
                 0.5
                      0.5
                          0.5
                               0.5
                                   0.5
                                       0.5
                                            1.0
                                                 0.5
                                       0.5
                      0.5 0.5
                              0.5 0.5
## [10,]
        0.5
             0.5
                 0.5
                                                 1.0
```

```
# (d) create a hybrid matrix representation
hybrid_matrix = matrix(nrow = 10, ncol = 10)
hybrid_matrix[upper.tri(hybrid_matrix)] = cor_matrix[upper.tri(cor_matrix)]
hybrid_matrix[lower.tri(hybrid_matrix)] = cor_matrix_chol[upper.tri(cor_matrix_chol)]
diag(hybrid_matrix) = diag(cor_matrix_chol)
hybrid_matrix
```

```
[,3]
##
              [,1]
                        [,2]
                                             [,4]
                                                        [,5]
                                                                    [,6]
                                                                              [,7]
##
    [1,] 1.0000000 0.5000000 0.5000000 0.50000000 0.50000000 0.50000000 0.50000000
   [2.] 0.5000000 0.8660254 0.5000000 0.50000000 0.50000000 0.50000000 0.5000000
##
  [3,] 0.5000000 0.1581139 0.8164966 0.50000000 0.50000000 0.50000000 0.50000000
##
  [4,] 0.2886751 0.5000000 0.2041241 0.79056942 0.50000000 0.50000000 0.50000000
   [5,] 0.5000000 0.2886751 0.1581139 0.15811388 0.77459667 0.50000000 0.5000000
##
   [6,] 0.2886751 0.2041241 0.1290994 0.12909944 0.20412415 0.76376262 0.5000000
  [7,] 0.2041241 0.1581139 0.1091089 0.10910895 0.15811388 0.08333333 0.7559289
##
   [8,] 0.5000000 0.1290994 0.5000000 0.09449112 0.12909944 0.50000000 0.1581139
   [9,] 0.2886751 0.5000000 0.2886751 0.50000000 0.10910895 0.28867513 0.1290994
## [10,] 0.2041241 0.2886751 0.2041241 0.28867513 0.09449112 0.20412415 0.1091089
##
               [,8]
                         [,9]
                                  [,10]
  [1,] 0.50000000 0.5000000 0.5000000
##
    [2,] 0.50000000 0.5000000 0.5000000
  [3,] 0.50000000 0.5000000 0.5000000
  [4,] 0.50000000 0.5000000 0.5000000
  [5,] 0.50000000 0.5000000 0.5000000
##
   [6,] 0.50000000 0.5000000 0.5000000
## [7,] 0.50000000 0.5000000 0.5000000
## [8,] 0.75000000 0.5000000 0.5000000
## [9,] 0.09449112 0.7453560 0.5000000
## [10,] 0.08333333 0.0745356 0.7416198
```

4 Translation

Roman numerals are represented by seven different symbols: I, V, X, L, C, D and M, shown by the following table: Symbol Value I 1 V 5 X 10 L 50 C 100 D 500 M 1000 Write an R function named roman_trans using appropriate data structures that returns the value of an input roman symbol listed above.

[1] 5

roman_trans("I")

[1] 1

roman_trans("D")

[1] 500

roman_trans("M")

[1] 1000