

# Assignment 2 - Greedy Regret Heuristics for Selective TSP

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## Problem Description

This is a variant of the Traveling Salesman Problem where:

- Select exactly 50% of nodes (rounded up if odd)
- Form a Hamiltonian cycle through selected nodes
- Minimize: total path length + sum of selected node costs
- Distances are Euclidean distances rounded to integers

## Algorithm Pseudocode

### Greedy 2-Regret

1. Start with given node
2. Add nearest node to form initial 2-node cycle
3. While not enough nodes selected:
  - a. For each unselected node  $i$ :
    - For each edge  $(u,v)$  in cycle:
 
$$\text{Calculate } \delta = \text{dist}[u][i] + \text{dist}[i][v] - \text{dist}[u][v] + \text{cost}[i]$$
    - Find best (minimum  $\delta$ ) and 2nd-best insertion positions
    - Calculate  $\text{regret} = \text{2nd\_best\_delta} - \text{best\_delta}$
  - b. Select node with maximum regret (ties broken by minimum  $\text{best\_delta}$ )
  - c. Insert at its best position
4. Return cycle

### Greedy Weighted (2-Regret + BestDelta)

1. Start with given node
2. Add nearest node to form initial 2-node cycle
3. While not enough nodes selected:
  - a. For each unselected node  $i$ :
    - For each edge  $(u,v)$  in cycle:
 
$$\text{Calculate } \delta = \text{dist}[u][i] + \text{dist}[i][v] - \text{dist}[u][v] + \text{cost}[i]$$
    - Find best (minimum  $\delta$ ) and 2nd-best insertion positions
    - Calculate  $\text{regret} = \text{2nd\_best\_delta} - \text{best\_delta}$
    - Calculate  $\text{score} = w_{\text{Regret}} \times \text{regret} - w_{\text{Best}} \times \text{best\_delta}$
  - b. Select node with maximum score (default weights:  $w_{\text{Regret}}=1.0$ ,  $w_{\text{Best}}=1.0$ )

- c. Insert at its best position
- 4. Return cycle

### Nearest Neighbor Any 2-Regret

1. Start with given node
2. While not enough nodes selected:
  - a. For each unselected node  $i$ :
    - For each position  $pos$  in current path ( $0$  to  $size$ ):
      - If  $pos == 0$ :  $\delta = cost[i] + dist[i][first\_node]$
      - Else if  $pos == size$ :  $\delta = cost[i] + dist[last\_node][i]$
      - Else:  $\delta = cost[i] + dist[path[pos-1]][i] + dist[i][path[pos]] - dist[path[pos-1]][path[pos]]$
    - Find best (minimum  $\delta$ ) and 2nd-best insertion positions
    - Calculate  $regret = 2nd\_best\_delta - best\_delta$
  - b. Select node with maximum regret (ties broken by minimum  $best\_delta$ )
  - c. Insert at its best position
3. Return path

### Nearest Neighbor Any Weighted (2-Regret + BestDelta)

1. Start with given node
2. While not enough nodes selected:
  - a. For each unselected node  $i$ :
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      - Else:  $\delta = cost[i] + dist[path[pos-1]][i] + dist[i][path[pos]] - dist[path[pos-1]][path[pos]]$
    - Find best (minimum  $\delta$ ) and 2nd-best insertion positions
    - Calculate  $regret = 2nd\_best\_delta - best\_delta$
    - Calculate  $score = wRegret \times regret - wBest \times best\_delta$
  - b. Select node with maximum score (default weights:  $wRegret=1.0$ ,  $wBest=1.0$ )
  - c. Insert at its best position
3. Return path

## Key Results

TSPA.csv (200 nodes, select 100)

Method	Min	Max	Avg
Random	242247	288959	265582
Nearest Neighbor (end only)	83182	89433	85108
Nearest Neighbor (any position)	71179	75450	73178

Method	Min	Max	Avg
Greedy Cycle	71488	74410	72646
Greedy 2-Regret	105852	123428	115474
Greedy Weighted (2-Regret + BestDelta)	71108	73395	72129
Nearest Neighbor Any 2-Regret	106373	126570	116659
Nearest Neighbor Any Weighted (2-Regret + BestDelta)	70010	75452	72401

TSPB.csv (200 nodes, select 100)

Method	Min	Max	Avg
Random	188533	235611	212974
Nearest Neighbor (end only)	52319	59030	54390
Nearest Neighbor (any position)	44417	53438	45870
Greedy Cycle	49001	57324	51400
Greedy 2-Regret	66505	77072	72454
Greedy Weighted (2-Regret + BestDelta)	47144	55700	50950
Nearest Neighbor Any 2-Regret	67121	79013	73646
Nearest Neighbor Any Weighted (2-Regret + BestDelta)	44891	55247	47653

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The solutions were checked using Solution checker.xlsx

Github

<https://github.com/Luncenok/EvolutionaryComputingLab1>

Conclusions

Cycle-based Regret Heuristics

The experimental results reveal critical insights about regret-based greedy heuristics:

**Greedy 2-Regret performs poorly**, producing solutions significantly worse than simpler methods (avg 115k for TSPA vs 72k for Greedy Cycle; 72k for TSPB vs 51k for Greedy Cycle). This counterintuitive result demonstrates that **maximizing regret alone is insufficient** - prioritizing only "picky" nodes without considering insertion cost leads to poor early decisions that constrain later choices.

**Greedy Weighted (2-Regret + BestDelta) achieves excellent performance**, ranking among the best methods tested:

- TSPA: 72.1k average (competitive with Greedy Cycle at 72.6k)

- TSPB: 51k average (between Nearest Neighbor any-position at 45.8k and Greedy Cycle at 51.4k)
- Lower variance than pure 2-Regret (narrower min-max ranges)

The **weighted criterion successfully balances two competing objectives**:

- High regret → prioritize nodes with few good placement options
- Low insertion cost → avoid expensive additions to the current cycle

**Key insight:** The weights (default 1.0, 1.0) allow the algorithm to consider both urgency (regret) and efficiency (cost), avoiding the myopic behavior of pure regret maximization. The weighted approach effectively combines the "look-ahead" benefit of regret with immediate cost optimization.

**Comparison to baseline methods:**

- Outperforms Nearest Neighbor (end-only) by ~15-6%
- Competitive with or slightly better than Greedy Cycle
- Slightly behind Nearest Neighbor (any-position) on TSPB, but more consistent

The weighted regret heuristic demonstrates that **sophisticated selection criteria require balancing multiple factors** rather than optimizing a single metric, making it a robust choice for practical selective TSP instances.

Path-based Regret Heuristics (Nearest Neighbor)

The **Nearest Neighbor Any 2-Regret** and **Nearest Neighbor Any Weighted** variants differ from their greedy cycle counterparts in a fundamental way:

**Key Difference: Path vs Cycle Construction**

- **Greedy Cycle variants:** Treat the solution as a cycle from the start, inserting nodes between existing edges (u,v) and considering the closing edge back to the first node
- **Nearest Neighbor variants:** Build a path sequentially, allowing insertion at beginning, middle, or end positions without forming a cycle until construction is complete

**Experimental Results:**

The results confirm our expectations about path-based vs cycle-based construction:

**Nearest Neighbor Any 2-Regret performs poorly**, mirroring the cycle-based Greedy 2-Regret:

- TSPA: 116.7k average (vs 115.5k for Greedy 2-Regret, vs 72.6k for Greedy Cycle)
- TSPB: 73.6k average (vs 72.5k for Greedy 2-Regret, vs 51.4k for Greedy Cycle)
- This confirms that **pure regret maximization fails regardless of construction strategy** (path or cycle)

**Nearest Neighbor Any Weighted achieves competitive performance:**

- TSPA: 72.4k average (comparable to Greedy Weighted at 72.1k and Greedy Cycle at 72.6k)
- TSPB: 47.7k average (slightly better than Greedy Weighted at 51.0k, approaching Nearest Neighbor any-position at 45.9k)
- **Best minimum on TSPA:** 70,010 (better than Greedy Weighted's 71,108)
- **Excellent performance on TSPB:** Ranks 2nd overall, just behind pure Nearest Neighbor any-position

**Key Finding:** The weighted criterion succeeds with **both path and cycle construction**, demonstrating that:

1. The balance between regret and insertion cost is the critical factor, not the construction strategy
2. Path-based construction can actually perform slightly better on certain instances (TSPB)
3. The flexibility of path insertion at endpoints provides practical advantages without sacrificing solution quality

The path-based weighted approach offers a viable alternative to cycle-based construction with competitive or superior performance.