

CH6 習題

2. (1) $t_{0.025}(10) = 2.228$ (b) $F_{0.05}(5, 8) = 3.69$

(2) $t_{0.95}(8) = -1.86$ (c) $F_{0.95}(6, 7)$
 $1 - 0.05$

(3) $\chi^2_{0.05}(12) = 21.026$
 $= \frac{1}{F_{0.05}(7, 6)}$
 $= \frac{1}{4.26} = 0.238$

(4) $\chi^2_{\alpha}(15) = 7.26 \alpha = ?$
 $\alpha = 0.95$ (8) $F_{\alpha}(6, 6) = 4.28$
 $\alpha = 0.05$

(5) $\chi^2_{0.95}(10) = 3.940$

7. (1) $\hat{p} = \frac{45}{80} = 0.56$

(2) $z = \frac{\hat{p} - p}{\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}}$
 $= \frac{0.56 - 0.5}{\sqrt{\frac{0.56 \times 0.44}{80}}} = \frac{0.06}{1.96 \times 0.06} = 0.12$

(3) $\hat{p} \pm z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$
 $= 0.56 \pm z_{0.05} \sqrt{\frac{0.56 \times 0.44}{80}}$
 $= 0.56 \pm 1.645 \times 0.06$
 $= 0.56 \pm 0.1$
 $= (0.46, 0.66)$

8. $\hat{p}_1 = 0.55$ $\hat{p}_2 = 0.6$

$(\hat{p}_1 - \hat{p}_2) \pm z_{\frac{\alpha}{2}} \sqrt{\frac{p_1(1-p_1)}{n_1} + \frac{p_2(1-p_2)}{n_2}}$
 $= (0.55 - 0.6) \pm z_{0.025} \sqrt{\frac{0.55 \times 0.45}{100} + \frac{0.6 \times 0.4}{100}}$
 $= -0.05 \pm 1.96 \times 0.07$
 $= -0.05 \pm 0.14$

$$z_1 \text{ (1)} \hat{p} = \frac{105}{250} = 0.42$$

$$0.42 \pm z_{0.05} \sqrt{\frac{0.42 \times 0.58}{250}}$$

$$= 0.42 \pm 1.645 \times 0.03$$

$$= 0.42 \pm 0.05$$

$$\Rightarrow (0.37, 0.47)$$

$$(2) \text{ (1)} \hat{p} = 0.3, e = 0.03, 1 - \alpha = 0.95$$

$$e = \frac{\alpha}{\sqrt{n}} \times z$$

$$n = \left(\frac{z}{e}\right)^2 \times \hat{p} \times (1 - \hat{p})$$

$$n = \left(\frac{1.96}{0.03}\right)^2 \times 0.3 \times 0.7 = 896.37 \approx 897$$

$$(b) \hat{p} = 0.42$$

$$n = \left(\frac{1.96}{0.03}\right)^2 \times 0.42 \times 0.58 = 1039.11 \approx 1040$$

$$(c) \hat{p} = 0.5$$

$$n = \left(\frac{1.96}{0.03}\right)^2 \times 0.5 \times 0.5 = 1067.11 \approx 1068$$

$$z_1 e = \frac{b}{\sqrt{n}} \times z \frac{\alpha}{2}$$

$$(1) b = 3, e = 0.5, 1 - \alpha = 0.95$$

$$n = \left(\frac{3}{0.5}\right)^2 \times 1.96^2$$

$$= 138.13 \approx 139$$

$$(2) b = 0.2, e = 0.03, 1 - \alpha = 0.9$$

$$n = \left(\frac{0.2}{0.03}\right)^2 \times 1.645^2$$

$$= 120.27 \approx 121$$

$$(3) b = 0.05, e = 0.02, 1 - \alpha = 0.98$$

$$n = \left(\frac{0.05}{0.02}\right)^2 \times 2.326^2 = 33.8 \approx 34$$